

Answer 1)

Assumptions –

`A[0] = x27`

`B[0] = x30`

`C[0] = x31`

`f = x5`

`g = x6`

`h = x7`

`I = x28`

`j = x29`

In order to fetch the address, we multiply the position with 4 to generate the offset address w.r.t the address of Array[0]

Temporary registers for storing the temp values are x3 and x4

The machine is a 32bit machine hence, we are considering sw and lw instead of ld and sd.

a)

4 address spaces (pointers) allocated per integer makes $A[10] = 4 * 10$ spaces

= 40 bytes as offset

Read memory and update register

lw x5, 40(x27)

b)

Similarly, $A[17] = 4 * 17 = 68$ bytes as offset

Writing register value to memory (Store)

sw x5, 68(x27)

c)

add x7, x5, x6

d) $C[g] = A[i+j+31]$ (given)

$A[31] = 4 * 31 = 124$ bytes as offset

add x3, x28, x29	- adding I and J
addi x3, x3, 31	- incrementing pointer by 31 places
slli x3, x3, 2	- fetch offset form by shift left of 2 places
add x3, x27, x3	- add the base address of A [0]
lw x3, 0(x3)	- load x3 register with value of x3
slli x4, x6, 2	- fetch value (g) in offset by shift left by 2 places
add x4, x31, x4	- add the base address of C [0]
sw x3, 0(x4)	- store x4 with the value stored in register x3

e)

i) $f = g - A[B[9]]$

$B[9] = 9 * 4 = 36$ offset

lw x3, 36(x30)	- load x3 with address of B9
slli x3, x3, 2	- Fetch the value in offset by shifting left by 2
add x3, x3, x27	- Add base value of A[0] to this offset value
lw x3, 0(x3)	- load register x3 with value at this position
sub x5, x6, x3	- fetching f by subtracting value of x3 from g

(ii) $f = g - A[C[8] + B[4]]$

$C[8] = 8 * 4 = 32$ offset and $B[4] = 4 * 4 = 16$ offset

lw x3, 32(x31)	- load x3 with address of C8
lw x4, 16(x30)	- load x4 with address of B4
add x3, x3, x4	- add these values in x3

Repeat the last 4 steps from i)

slli x3, x3, 2	- Fetch the value in offset by shifting left by 2
add x3, x3, x27	- Add base value of A[0] to this offset value
lw x3, 0(x3)	- load register x3 with value at this position

sub x5, x6, x3 - fetching f by subtracting value of x3 from g

(iii) $A[i] = B[2i+1]$, $C[i] = B[2i]$

$B[2i] = 2 * 4 * i = 8i$ offset and $C[i] = i * 4 = 4i$ offset (where i is x28)

slli x3, x28, 3	- Fetch the value 8i in offset by shifting left by 3
add x3, x3, x30	- Add base value of B [0] to this offset value
slli x4, x28, 2	- Fetch the value 4i in offset by shifting left by 2
add x4, x4, x31	- Add base value of C [0] to this offset value
sw x3, 0(x4)	- load register x4 with value at register x3

Similarly, follow the above steps for A instead of C

slli x3, x28, 3	- Fetch the value 8i in offset by shifting left by 3
add x3, x3, 4	- Adding 4 from B[2i+1] offset bytes
add x3, x3, x30	- Add base value of B [0] to this offset value
slli x4, x28, 2	- Fetch the value 4i in offset by shifting left by 2
add x4, x4, x27	- Add base value of A [0] to this offset value
sw x3, 0(x4)	- load register x4 with value at register x3

(iv) $A[i] = 4B[i-1] + 4C[i+1]$

$4B[i] = 4 * 4 * i = 16i$ offset and $4C[i] = 4 * 4 * i = 16i$ offset

addi x3, x28, -1	- decrementing pointer by 1 place
slli x3, x3, 4	- Fetch the value 16i in offset by shifting left by 4
add x3, x3, x30	- Add base value of B [0] to this offset value
addi x4, x28, 1	- incrementing pointer by 1 place
slli x4, x4, 4	- Fetch the value 16i in offset by shifting left by 4
add x4, x4, x31	- Add base value of C [0] to this offset value
slli x4, x28, 2	- Fetch the value 4i in offset by shifting left by 2

add x3, x3, x4	- adding B and C related value to register x3
lw x3, 0(x3)	- load register x3 with value at register x3

add x4, x4, x27	- Add base value of A [0] to this offset value
sw x3, 0(x4)	- load register x4 with value at register x3

(v) $f = g - A[C[4] + B[12]]$

$C[4] = 4 * 4 = 16$ offset and $B[12] = 12 * 4 = 48$ offset

lw x3, 16(x31)	- load x3 with address of C4
lw x4, 48(x30)	- load x4 with address of B12
add x3, x3, x4	- add these values in x3
slli x3, x3, 2	- Fetch the value in offset by shifting left by 2
add x3, x3, x27	- Add base value of A[0] to this offset value
lw x3, 0(x3)	- load register x3 with value at this position
sub x5, x6, x3	- fetching f by subtracting value of x3 from g

Answer 2)

Given

$x5 = 0x00000000AAAAAA = 10101010101010101010101010101010$

$x6 = 0x1234567812345678 = 00010010001101000101011001111000$
 $00010010001101000101011001111000$

a)

`srli x7, x5, 16`

shift right with 0 = $(1010101010101010)_2 = (000000000000AAAA)_{16}$

`addi x7, x7, -128`

$(128)_{10} = (10000000)_2$

$(-128)_{10} = (11111111111111111111101111111)_2 + (1)_2$

$= (11111111111111111111110000000)_2$

Addition immediate = $x7 + (-128)_2$

$= (00000000000000001010101010101010)_2$

$+ (1111111111111111111111110000000)_2$

$= (00000000000000001010101000101010)_2$

$= (000000000000AA2A)_{16}$

`srai x7, x7, 2`

shift right with sign bit = $(000000000000000010101010001010)_2$

$= (0000000000002A8A)_{16}$

`and x7, x7, x6`

$= (000000000000000010101010001010)_2 \text{ AND}$

$(00010010001101000101011001111000)_2$

$= (000000000000000000000100001000)_2$

$= (0000000000000208)_{16}$

Instruction	func7 or immediate (imm)	source register (rs2)	source register (rs1)	func3	destination register (rd) or immediate (imm)	opcode (op)
	7	5	5	3	5	7
add x5, x6, x7	0000 000	0 0110	0011 1	000	0010 1	011 0011
addi x8, x5, 512	0010 0000 0000		0010 1	000	0100 0	001 0011
ld x3, 128(x27)	0000 1000 0000		1101 1	011	0001 1	000 0011
sd x3, 256(x28)	0001 000	0 0011	1110 0	011	0000 0	010 0011
beq x5, x6 ELSE	---	0 0110	0010 1	000	1000 0	110 0011
add x3, x0, x0	0000 000	00000	00000	000	0001 1	011 0011
auipc x3, FFEFA	1111 1111 1110 1111 1010				0001 1	001 0111
jal x3 ELSE	0000 0001 0000 0000 0000				0001 1	110 1111

Instruction	Format	8 hex char instruction	32-bit instruction
<code>add x5, x6, x7</code>	R	007382B3	0000 0000 0111 0011 1000 0010 1011 0011
<code>addi x8, x5, 512</code>	I	20028413	0010 0000 0000 0010 1000 0100 0001 0011
<code>ld x3, 128(x27)</code>	I	080DB183	0000 1000 0000 1101 1011 0001 1000 0011
<code>sd x3, 256(x28)</code>	S	103E3023	0001 0000 0011 1110 0011 0000 0010 0011
<code>beq x5, x6 ELSE</code>	SB	00628863	0000 0000 0110 0010 1000 1000 0110 0011
<code>add x3, x0, x0</code>	R	000001B3	0000 0000 0000 0000 0000 0001 1011 0011
<code>auipc x3, FFEFA</code>	U	FFEFA197	1111 1111 1110 1111 1010 0001 1001 0111
<code>jal x3 ELSE</code>	UJ	010001EF	0000 0001 0000 0000 0000 0001 1110 1111

Answer 4)

a) Value of A = x5

Base address of C = x11

lw x5, 0(x11)

- assign x5 the value stored at C [0]

slli x5, x5, 16

- shifting the bits to left by 16 places

b) x3=0 and x4 = 0xFFFFFFFFFFFFFFFF (given)

i) Load 6 bits from 12th to 7th from x3

`addi x10, x0, 0x3F`

i.e., 0011 1111 (required for masking the bits)

`slli x10, x10, 7`

- shift the bits by 7 places i.e., 12th to 7th

`and x11, x10, x3`

- fetch only desired bits in x11

We need to shift it for (28-12) i.e., 16 places.

ii) Store 6 bits from 28th to 23rd in x4

`slli x11, x11, 16`

- shift by 16 places

`slli x10, x10, 16`

- shifting masking bits by 16 places

`xori x10, x10, -1`

- inverting the masked bits

(Gives 1 when both bits are same)

and x4, x4, x10

- empty the 28th to 23rd place in register to 0

or x4, x4, x11

- anything OR with 0 is the number itself

c) xori x5, x6, -1 //invert the bits at x5 and x6 & store them in x5

Answer 5)

PC = 0x60000000_{hex}

We can start storing values from PC + 1 position i.e., 0x60000004_{hex}

a)

The immediate value for jal instruction can be 20bits long i.e., between $(-2)^{19}$ to $(2)^{19} - 1$

Hence, the range of possible values of offset lies between $(-2)^{20}$ to $(2)^{20} - 2$

$$= (100000)_{16} \text{ to } (FFFFC)_{16}$$

Therefore, the range of PC after jump and link is

From $(60000004)_{16} - (100000)_{16}$ to $(60000000)_{16} - (FFFFC)_{16}$

Final range = $(5FF00004)_{16}$ to $(600FFFFE)_{16}$

b)

The immediate value for beq instruction can be 12bits long i.e., between $(-2)^{11}$ to $(2)^{11} - 1$

Hence, the range of possible values of offset lies between $(-2)^{12}$ to $(2)^{12} - 2$

$$= (1000)_{16} \text{ to } (FFE)_{16}$$

Therefore, the range of PC after branch if equal is

From $(60000004)_{16} - (1000)_{16}$ to $(60000000)_{16} - (FFE)_{16}$

Final range = $(5FFFF004)_{16}$ to $(60001002)_{16}$

Answer 6)

Assumptions –

```
LOOP:      beq x6, x0, DONE
           addi x6, x6, -1
           addi x5, x5, 2
           jal x0, LOOP
```

DONE:

x6 Register = 10 = i

x5 Register = 0 = acc

a)

```
#include <stdio.h>
```

```
int main()
```

```
{
```

```
int i=10, acc=0;
```

```
LOOP:
```

```
{
```

```
if(i==0)          //beq x6, x0, DONE
```

```
goto DONE;
```

```
else
```

```
{
```

```
i=i-1; //addi x6, x6, -1
```

```
acc=acc+2; //addi x5, x5, 2
```

```
goto LOOP; //jal x0, LOOP
```

```
}
```

```
}
```

```
DONE:
```

```
{return 0;}
```

```
}
```

b)

No. of instructions in loop : 4

No. of times loop would run : $N + 1$ // ($N=10, N \geq 0, N--$)

No. of time “Done” instruction run: 1

Total = $(4 * N + 1) + 1 = 4N + 2$ RISK instructions will be executed.

c)

```
#include <stdio.h>
int main()
{
    int i=10, acc=0;
LOOP:
{
    if(i<0)          //blt x6, x0, DONE
    goto DONE;
    else
    {
        i--; //addi x6, x6, -1
        acc=acc+2; //addi x5, x5, 2
        goto LOOP; //jal x0, LOOP
    }
}
DONE:
{return 0;}
}
```

Answer 7)

Assumptions –

A[0] = x5

B[0] = x6

&D[0] = x10

I = x7

j = x29

Temporary registers for storing the temp values are x3 and x4

First initialize counter registers to store iterations values (x7 (i) and x29 (j))

The comments/explanation are now written in this color beyond this point.

a)

```
addi x7, x0, 0 - i=0
```

Outer_Loop:

```
bge x7, x5, Outer_Loop_End // - i<a
```

```
addi x29, x0, 0 - j=0
```

Inner_Loop:

```
bge x29, x6, Inner_Loop_End - j<b
```

```
add x3, x7, x29 - i + j;
```

```
slli x4, x29, 4 - 4*j
```

```
add x4, x4, x10 - D[4*j]
```

```
sw x3, 0(x4) - D[4*j] = i + j
```

(i.e., storing the value of x3 directly to the address of x4 which is D[4*j])

```
addi x29, x29, 1 - j++
```

```
jal x0, Inner_Loop - Jump and return to Inner Loop
```

Inner_Loop_End:

```
addi x7, x7, 1 - i++
```

```
jal x0, Outer_Loop - Jump and return to Outer Loop
```

Outer_Loop_End: - End the program

b)

```
A[0] = x5 register = 10
```

```
B[0] = x6 register = 1
```

```
&D[0] = x10 = 0
```

Command	Times Executed
addi x7, x0, 0	1
Outer_Loop:	
bge x7, x5, Outer_Loop_End	11 (I (0 to 9) - 10 times + I = 10 th value) Outer loop
addi x29, x0, 0	10 (1 time for each i)
Inner_Loop:	
bge x29, x6, Inner_Loop_End	20 [j = 1 (10 times) and j = 0 (10)]
add x3, x7, x29	10 (10 (I times) * 1 (j times))
slli x4, x29, 4	10 (10 (I times) * 1 (j times))
add x4, x4, x10	10 (10 (I times) * 1 (j times))
sw x3, 0(x4)	10 (10 (I times) * 1 (j times))
addi x29, x29, 1	10 (10 (I times) * 1 (j times))
jal x0, Inner_Loop	10 (10 (I times) * 1 (j times))
Inner_Loop_End:	
addi x7, x7, 1	10 (No of iterations of I)
jal x0, Outer_Loop	10 (No of iterations of I)
Outer_Loop_End:	

Total = 1+11+10+20+(6*10) + (2*10) = 122

Answer 8)

Considering the base address 0x10000000. It is 8 bits machine and could store 0x1122334455667788 as

a) Big Endian (MSB is stored last)

Digit	Address
11	0x10000000
22	0x10000001
33	0x10000002
44	0x10000003
55	0x10000004
66	0x10000005
77	0x10000006
88	0x10000007

b) Little Endian (MSB is stored first)

Digit	Address
88	0x10000000
77	0x10000001
66	0x10000002
55	0x10000003
44	0x10000004
33	0x10000005
22	0x10000006
11	0x10000007

Answer 9)

$(1234567812345678)_{16} = (0001001000110100010101100111100000010010001101000101011001111000)_2$ i.e., 64 digits. Hence, we cannot do using a single register x10. The temp register considered here will be x3.

Code –

lui x3, 0x12345 //load 32 bits using this //20 bits (5digits from hex) in x3 temp register

addi x10, 0x678, x3 //r2 being value, add immediate value of 678 to x10 register

slli x10, x10, 32 //shift left by 32 places as the whole word is 64 digits/bits

addi x3, 0x678, x3 //r2 being value, add immediate value of 678 to x3 temp register

//x10 is needed to store the final value so, not touched

add x10, x3, x10 //finally add 1234567800000000 to 12345678 in hex

Answer 10)

Given:

$$x5 = (128)_{10}$$

a)

For overflow, the range should exceed $(FFFFFFFF)_{16}$ for overflow to occur

$$(00000080)_{16} = (128)_{10}$$

Hence,

Minimum value of x6 should = $(FFFFFFFF)_{16} - (00000080)_{16} + 1 = (FFFFFF86)_{16}$ for an overflow to occur.

b)

$x5 - x6$ should not be greater than 0. Hence, $x6 > (128)_{10}$ for an overflow to occur.

c)

$x6 - x5$ should not be greater than 0. Hence, $x6 < (128)_{10}$ for an overflow to occur.