

EX2.R

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```
library(e1071)
library(pracma)
```

```
##
## Attaching package: 'pracma'

## The following object is masked from 'package:e1071':
##
##      sigmoid
```

```
library(dplyr)
```

```
##
## Attaching package: 'dplyr'

## The following objects are masked from 'package:stats':
##
##      filter, lag

## The following objects are masked from 'package:base':
##
##      intersect, setdiff, setequal, union
```

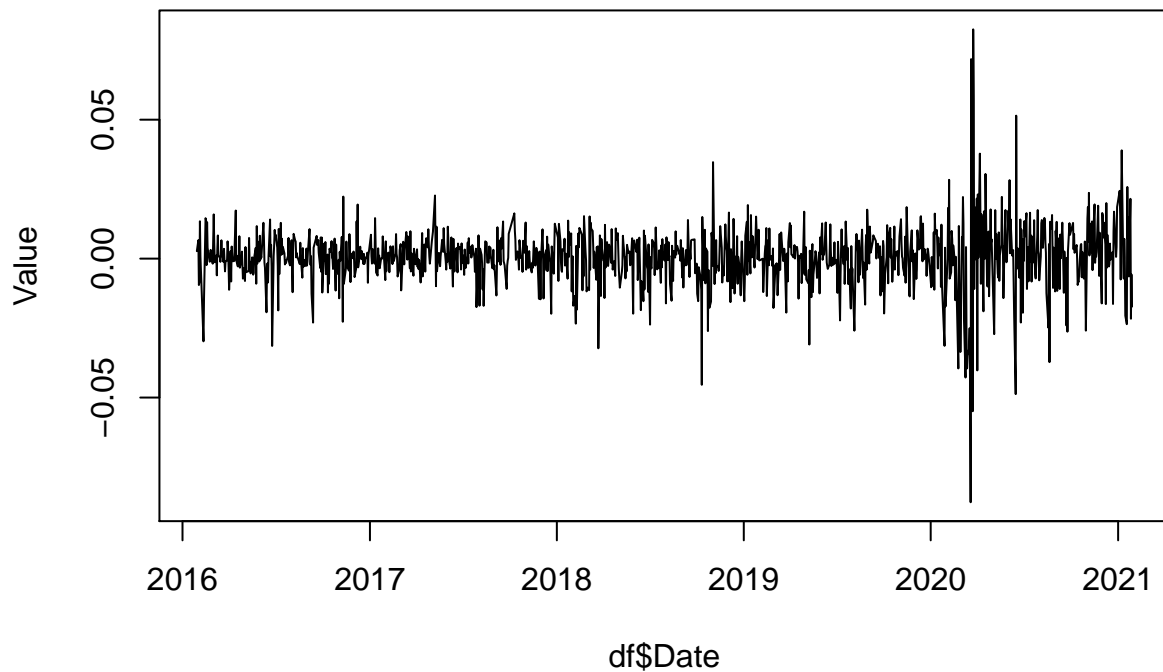
```
df = read.csv("https://raw.githubusercontent.com/Anko-Jipsa/statistics/master/ST436/EX2/%5EKS11.csv")

# Data pre-processing
df = df %>% replace(=="null", NA)
df = na.omit(df)
df$Date = as.Date(df$Date)
df$Adj.Close = as.numeric(df$Adj.Close)

# Log-return
df$log_ret = c(NA, diff(log(df$Adj.Close), lag=1))
df = na.omit(df)

## Stylised facts:
# (a) The returns oscillate around zero
plot(x=df$Date, y=df$log_ret,
     type="l", main="Log Return", ylab = "Value")
```

Log Return

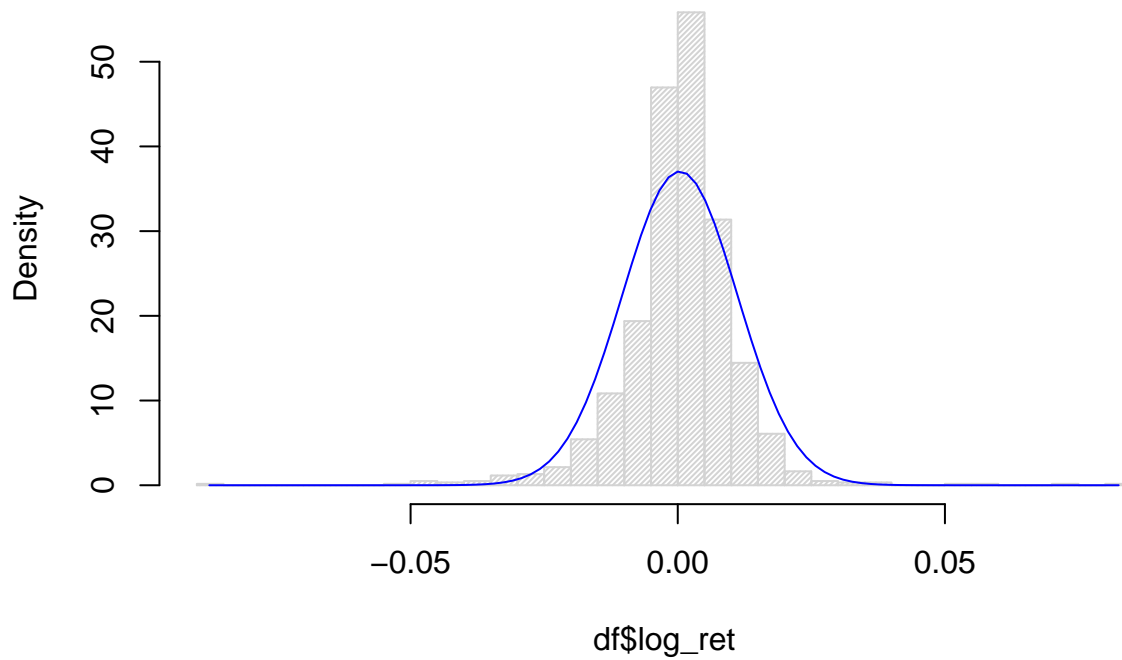


```
mean(df$log_ret) # Almost 0.
```

```
## [1] 0.0003906964
```

```
# (b) The returns are heavy-tailed.
xseq = linspace(min(df$log_ret), max(df$log_ret), n = 100)
x<-seq(min(df$log_ret), max(df$log_ret),by=0.02)
hist(df$log_ret, prob=TRUE, freq=F,density=50, breaks=50)
lines(xseq, dnorm(xseq, mean(df$log_ret), sd(df$log_ret)), col="blue")
```

Histogram of df\$log_ret



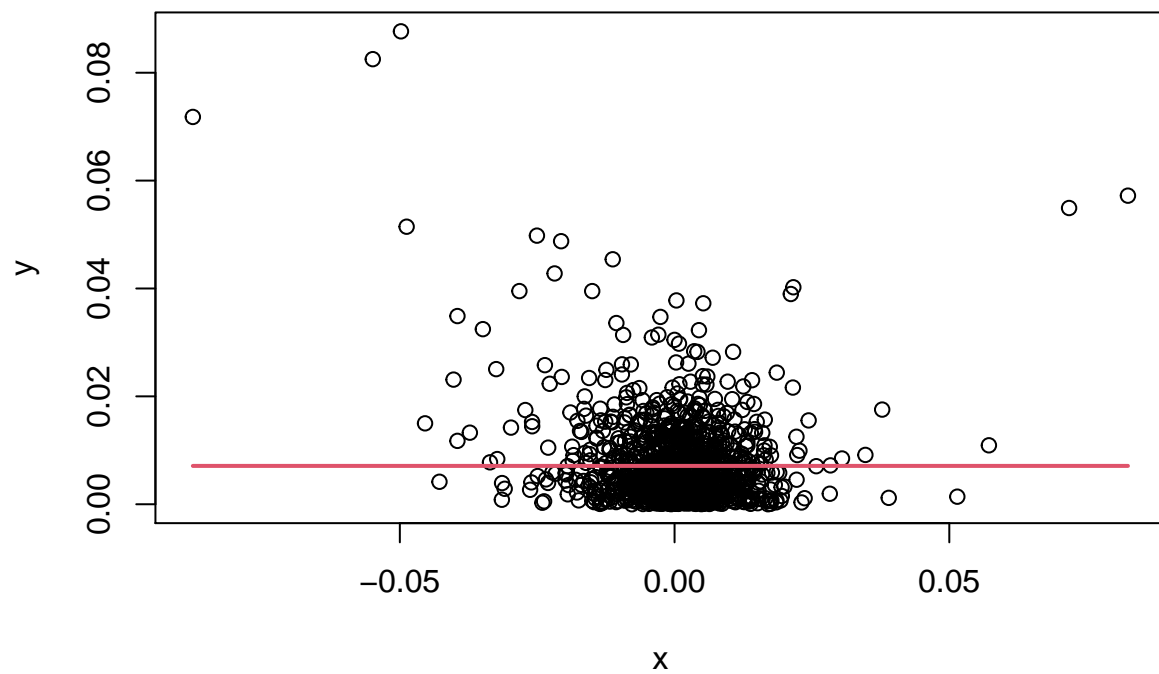
```
kurtosis(df$log_ret) #10.81811, heavy tail
```

```
## [1] 10.81811
```

```
# (c) The returns display a downward skew.  
skewness(df$log_ret) # Negative skewness
```

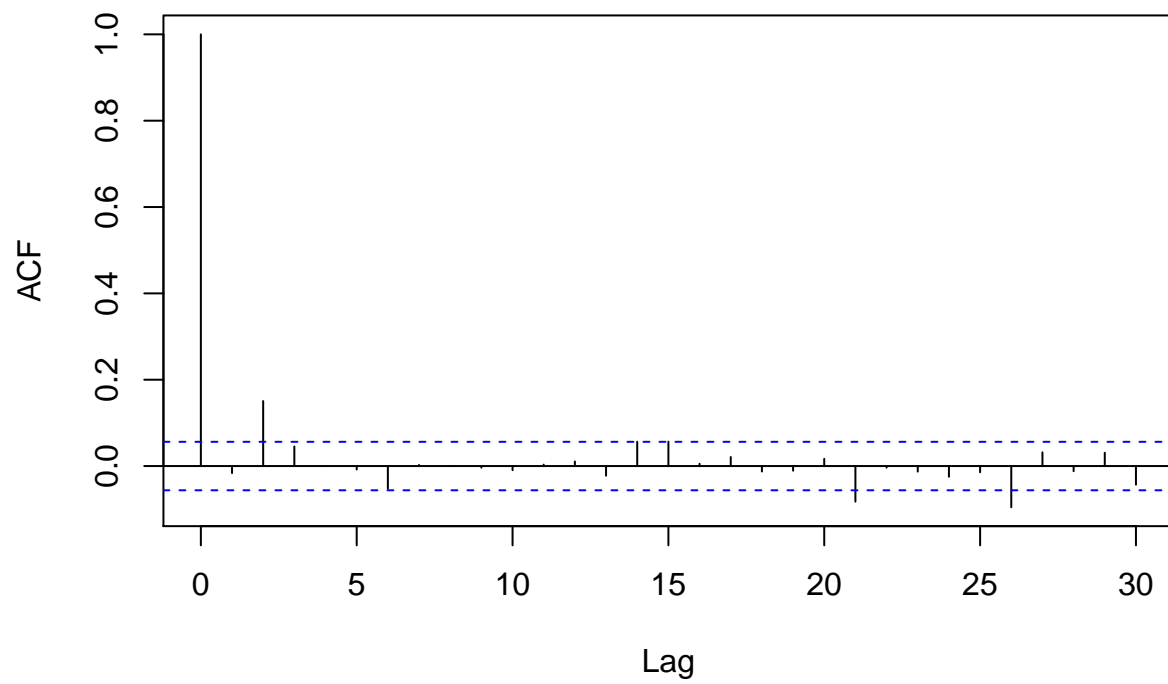
```
## [1] -0.3289955
```

```
# (d) There is a leverage effect in the returns.  
y=abs(df$log_ret[2:length(df$log_ret)])  
x=df$log_ret[1:length(df$log_ret)-1]  
s = ksmooth(x, y)  
plot(x,y)  
lines(s, lwd = 2, col = 2)
```



(e) The sample autocorrelation of the returns is close to zero for almost all lags.
`acf(df$log_ret)`

Series df\$log_ret



(f) The sample autocorrelation of the squared returns is large and positive for many lags
`acf((df$log_ret)^2)`

