



**University Institute of Engineering**  
**Department of Computer Science & Engineering**

**EXPERIMENT:4**

NAME : Ankush  
BRANCH : BE-CSE  
SEMESTER : 5TH  
SUBJECT NAME : ADBMS

UID : 23BCS12742  
SECTION : KRG\_3B  
SUBJECT : 23CSP-339

**1. AIM:-**

Solve the Problem related to Normalisation and give its closure, candidate key along with prime attribute and non-prime attribute and in which type of normal form it exists

**Problem 1**

Consider a relation R having attributes as R(ABCD), functional dependencies are given below:

$AB \rightarrow C$ ,

$C \rightarrow D$ ,

$D \rightarrow A$

Identify the set of candidate keys possible in relation R. List all the set of prime and non-prime attributes.

**Solution**

Closures to find candidate keys

**(AB)<sup>+</sup>**

- Start: {A, B}
- From  $AB \rightarrow C \Rightarrow \{A, B, C\}$
- From  $C \rightarrow D \Rightarrow \{A, B, C, D\}$
- From  $D \rightarrow A$  already there.

$AB^+ = \{A, B, C, D\} \Rightarrow AB$  is a candidate key.

**(BC)<sup>+</sup>**

- Start: {B, C}
- From  $C \rightarrow D \Rightarrow \{B, C, D\}$
- From  $D \rightarrow A \Rightarrow \{A, B, C, D\}$

$BC^+ = \{A, B, C, D\} \Rightarrow BC$  is a candidate key

(BD)+

- Start: {B, D}
- From  $D \rightarrow A \Rightarrow \{A, B, D\}$
- From  $AB \rightarrow C \Rightarrow \{A, B, C, D\}$
- $BD^+ = \{A, B, C, D\} \Rightarrow BD$  is a candidate key
- 

(CD)+

- Start: {C,D}
- From  $C \rightarrow D \Rightarrow \{C, D\}$  (no change)
- From  $D \rightarrow A \Rightarrow \{A, C, D\}$
- From  $AB \rightarrow C$  (needs B, but not present)  $\rightarrow$  stop.
- CD is not a key.

Candidate Keys = {AB, BC, BD}

Prime and Non-prime Attributes

- Prime attributes = appear in at least one candidate key.
  - Candidate keys: {AB}, {BC}, {BD}
  - Prime attributes = {A, B, C, D} (since all appear across candidate keys).
- Non-prime attributes = none (all are prime).

Given Relation is in 3rd normal Form

Problem 2 Relation R(ABCDE) having functional dependencies as :  $A \rightarrow D$ ,  $B \rightarrow A$ ,

$BC \rightarrow D$ ,

$AC \rightarrow BE$

Identify the set of candidate keys possible in relation R. List all the set of prime and non prime attributes.

Solution

Step 1: closures to find candidate keys

(B, C)+

- Start: {B,C}
- From  $B \rightarrow A \Rightarrow \{A, B, C\}$
- From  $A \rightarrow D \Rightarrow \{A, B, C, D\}$
- From  $AC \rightarrow BE$  (since A and C present)  $\Rightarrow \{A, B, C, D, E\}$
- BC is a candidate key.

$(A, C)^+$

- Start:  $\{A, C\}$
- From  $A \rightarrow D \Rightarrow \{A, C, D\}$
- From  $AC \rightarrow BE \Rightarrow \{A, B, C, D, E\}$   
AC is a candidate key.

$(B, E)^+$

- Start:  $\{B, E\}$
- From  $B \rightarrow A \Rightarrow \{A, B, E\}$
- From  $A \rightarrow D \Rightarrow \{A, B, D, E\}$
- From  $AC \rightarrow BE$  (need C)
- From  $BC \rightarrow D$  (need C)  
So  $\{B, E, A, D\}$  (missing C) not a key.

$(B, C, E)^+$

- Start:  $\{B, C, E\}$
- $B \rightarrow A \Rightarrow \{A, B, C, E\}$
- $A \rightarrow D \Rightarrow \{A, B, C, D, E\}$  .
- But BC alone is already a key  $\rightarrow$  So BCE is superkey, not minimal.

So, Candidate Keys =  $\{BC, AC\}$

- Prime attributes = those that appear in at least one candidate key.
  - Candidate keys =  $\{BC, AC\}$
  - Prime attributes =  $\{A, B, C\}$ .
- Non-prime attributes = the rest.
  - Non-prime =  $\{D, E\}$ .

Normal Form

Given Relation is in 1 Normal Form

Problem 3. Consider a relation R having attributes as R(ABCDE), functional dependencies are given below:

$B \rightarrow A,$   
 $A \rightarrow C,$   
 $BC \rightarrow D,$   
 $AC \rightarrow BE$

Identify the set of candidate keys possible in relation R. List all the set of prime and non prime

attributes.

Solution

Compute Closures

$(B, C)^+$

- Start:  $\{B, C\}$  From  $B \rightarrow A \Rightarrow \{A, B, C\}$
- From  $A \rightarrow C$  (C already present) From  $AC \rightarrow BE \Rightarrow \{A, B, C, E\}$
- From  $BC \rightarrow D \Rightarrow \{A, B, C, D, E\}$ .

BC is a candidatekey.

$(A, C)^+$

- Start:  $\{A, C\}$
- From  $A \rightarrow C$  (no change)
- From  $AC \rightarrow BE \Rightarrow \{A, B, C, E\}$
- From  $B \rightarrow A$  (already have A)
- From  $BC \rightarrow D \Rightarrow \{A, B, C, D, E\}$ .

AC is a candidatekey.

$(B, A)^+$  (same as AB)

- Start:  $\{A, B\}$
- From  $B \rightarrow A$  (already there)
- From  $A \rightarrow C \Rightarrow \{A, B, C\}$
- From  $AC \rightarrow BE \Rightarrow \{A, B, C, E\}$
- From  $BC \rightarrow D \Rightarrow \{A, B, C, D, E\}$

AB is a candidate key.

$(B)^+$

- • • Start:  $\{B\}$
- From  $B \rightarrow A \Rightarrow \{A, B\}$
- From  $A \rightarrow C \Rightarrow \{A, B, C\}$
- From  $AC \rightarrow BE \Rightarrow \{A, B, C, E\}$
- From  $BC \rightarrow D \Rightarrow \{A, B, C, D, E\}$

B alone is a candidatekey.

$(A)^+$

- • • Start:  $\{A\}$
- From  $A \rightarrow C \Rightarrow \{A, C\}$
- From  $AC \rightarrow BE \Rightarrow \{A, B, C, E\}$
- From  $B \rightarrow A$  (already have A)
- From  $BC \rightarrow D \Rightarrow \{A, B, C, D, E\}$

A alone is a candidatekey.

Minimal candidate keys = {A, B}

Prime vs Non-prime Attributes

- Prime attributes = attributes in any candidate key.
  - Candidate keys = {A, B}
  - Prime attributes = {A, B}
- Non-prime attributes = others.
  - Non-prime = {C, D, E}

Normal Form

Given Relation is in BCNF

Problem 4 Consider a relation R having attributes as R(ABCDEF), functional dependencies are given below:

$A \rightarrow BCD$ ,

$BC \rightarrow DE$ ,

$B \rightarrow D$ ,

$D \rightarrow A$

Identify the set of candidate keys possible in relation R. List all the set of prime and non prime attributes.

Solution

To check Attribute Closures

(A)+

- Start: {A}  $A \rightarrow BCD \Rightarrow \{A, B, C,$
- $D\}$  From  $B \rightarrow D$  (already have D)
- From  $D \rightarrow A$  (already have A)
- From  $BC \rightarrow DE$  ( $BC \subseteq \{A, B, C, D\}$ )  $\Rightarrow$  add E
- $\rightarrow \{A, B, C, D, E\}$   
Missing F. Not a key.

(B)+

- Start: {B}
- From  $B \rightarrow D \Rightarrow \{B, D\}$
- From  $D \rightarrow A \Rightarrow \{A, B, D\}$
- From  $A \rightarrow BCD \Rightarrow \{A, B, C, D\}$
- From  $BC \rightarrow DE$  (need C, now present)  $\Rightarrow \{A, B, C, D, E\}$
- Still missing F. Not a key.

(C)+

- Start: {C}
- No FD fires  $\Rightarrow$  {C} Not a key.

(D)+

- • • Start: {D}
- From  $D \rightarrow A \Rightarrow \{A, D\}$   
From  $A \rightarrow BCD \Rightarrow \{A, B, C, D\}$   
From  $BC \rightarrow DE$  (have B,C)  $\Rightarrow$  add E  
 $\Rightarrow \{A, B, C, D, E\}$   
Missing F. Not a key.

(E)+

- Start: {E}
- No FD fires  $\Rightarrow$  {E} Not a key.
- 

(F)+

- Start: {F}, no FDs apply. Not a key.

(A,F)+

- Start: {A, F}
- From  $A \rightarrow BCD \Rightarrow \{A, B, C, D, F\}$
- From  $BC \rightarrow DE \Rightarrow$  add E  
 ~~$\{A, B, C, D, E, F\}$~~  .  
{A, F} is a key.

(B,F)+

- Start: {B, F}
- From  $B \rightarrow D \Rightarrow \{B, D, F\}$
- From  $D \rightarrow A \Rightarrow \{A, B, D, F\}$
- From  $A \rightarrow BCD \Rightarrow \{A, B, C, D, F\}$
- From  $BC \rightarrow DE \Rightarrow \{A, B, C, D, E, F\}$ .  
{B, F} is a key.

(C,F)+

- Start: {C,F}
- No FDs fire (need A, B, D) Not a key.

(D,F)+

- Start: {D, F}
- From  $D \rightarrow A \Rightarrow \{A, D, F\}$
- From  $A \rightarrow BCD \Rightarrow \{A, B, C, D, F\}$
- From  $BC \rightarrow DE \Rightarrow$  add E

$\Rightarrow \{A, B, C, D, E, F\}$ .  
 $\{D, F\}$  is a key.

$(E, F)^+$

- Start:  $\{E, F\}$ , no FDs apply. Not a key.

Check minimality

- $\{A, F\}$  minimal
- $\{B, F\}$  minimal
- $\{D, F\}$

Candidate keys

$\{AF, BF, DF\}$

Prime vs Non-prime Attributes

- Prime attributes = those that appear in at least one candidate key.
  - Candidate keys =  $\{A, F\}$ ,  $\{B, F\}$ ,  $\{D, F\}$
  - Prime attributes =  $\{A, B, D, F\}$
- Non-prime attributes = the rest.
  - Non-prime =  $\{E, C\}$

Normal Form

Given relation is 1st Normal Form

Problem 5.

Designing a student database involves certain dependencies which are listed below:

$X \rightarrow Y$   
 $WZ \rightarrow X$   
 $WZ \rightarrow Y$   
 $Y \rightarrow W$   
 $Y \rightarrow XY$   
 $\rightarrow Z$

The task here is to remove all the redundant FDs for efficient working of the student database management system.

Solution

Closure are

$X^+ \rightarrow \{X, Y, W, Z\}$   
 $Y^+ \rightarrow \{X, Y, W, Z\}$   
 $WZ^+ \rightarrow \{X, Y, W, Z\}$

Candidate Keys Are

$\{X, Y, WZ\}$

### Prime vs Non-prime Attributes

- Prime attributes = those that appear in at least one candidate key.
  - Candidate keys = {X}, {Y}, {WZ}
  - Prime attributes = {X, Y, W, Z}
- Non-prime attributes = null;

### Normal Form

Given relation is in BCNF

### Problem 6

Debit Pvt Ltd needs to maintain database having dependent attributes ABCDEF. These attributes are functionally dependent on each other for which functional dependency set F given as:

$A \rightarrow BC$ ,

$D \rightarrow E$ ,

$BC \rightarrow D$ ,

$A \rightarrow D$

Consider a universal relation  $R_1(A, B, C, D, E, F)$  with functional dependency set F, also all attributes are simple and take atomic values only. Find the highest normal form along with the candidate keys with prime and non-prime attribute.

### Solution

Find Candidate Keys

- $AF^+$ :
  - Start with {A, F}.
  - From  $A \rightarrow B, C, D, E$ , we get {A, B, C, D, E, F}
  - So AF is a candidate key.

$A^+ = \{A, B, C, D, E\} \neq R_1$  (F missing).

$F^+ = \{F\} \neq R_1$  (F missing).

$FD^+ = \{F, D, E\} \neq R_1$  (F missing).

$FBC^+ = \{F, B, C, D\} \neq R_1$  (F missing).

Thus, the only candidate key = {A F}.

### Prime vs Non-prime Attributes

- Prime attributes = those that appear in at least one candidate key.
  - Candidate keys = {AF}
  - Prime attributes = {A, F}
- Non-prime attributes = {B, C, D, E}

### Normal Form

Given relation is in 1st normal form