

# Advanced Algorithmic Problem Solving (R1UC601B)

### **Assignment for MTE**

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## Advanced Algorithmic Problem Solving (R1UC601B) Assignment for MTE

#### 1. Explain the concept of a prefix sum array and its applications.

A prefix sum array stores cumulative sums of elements from the start. It allows constant-time range sum queries.

**Applications:** Range sum queries, subarray problems, frequency count.

2. Write a program to find the sum of elements in a given range [L, R] using a prefix sum array.

#### Algorithm:

- Build prefix sum array.
- Range sum = prefix[R] prefix[L-1]

#### **Program:**

```
#include <iostream>
using namespace std;

int main() {
    int arr[] = {2, 4, 1, 3, 6}, n = 5;
    int prefix[n];
    prefix[0] = arr[0];
    for (int i = 1; i < n; i++) prefix[i] = prefix[i-1] + arr[i];
    int L = 1, R = 3;
    int rangeSum = prefix[R] - (L > 0 ? prefix[L-1] : 0);
    cout << "Sum = " << rangeSum;
}

Time: O(n) pre-processing, O(1) query
Space: O(n)</pre>
```

3. Solve the problem of finding the equilibrium index in an array.

#### Algorithm:

Total sum of array

**Example:** Range  $[1,3] \rightarrow 4+1+3 = 8$ 

Iterate and check if leftSum == total - leftSum - arr[i]

#### **Program:**

#include <iostream>
using namespace std;

```
int main() {
    int arr[] = {1, 3, 5, 2, 2}, n = 5;
    int total = 0, leftSum = 0;
    for (int i = 0; i < n; i++) total += arr[i];
    for (int i = 0; i < n; i++) {
        if (leftSum == total - leftSum - arr[i]) {
            cout << "Equilibrium Index: " << i;
            break;
        }
        leftSum += arr[i];
    }
}
Time: O(n)
Space: O(1)
Example: Index 2 → 1+3 == 2+2</pre>
```

4. Check if an array can be split into two parts such that the sum of prefix equals suffix.

#### Algorithm:

- Calculate total sum
- Traverse and track prefix sum
- Check if prefix sum == total prefix

#### **Program:**

```
#include <iostream>
using namespace std;
int main() {
  int arr[] = \{1, 2, 3, 3\}, n = 4;
  int total = 0, preSum = 0;
  for (int i = 0; i < n; i++) total += arr[i];
  for (int i = 0; i < n; i++) {
     preSum += arr[i];
     if (preSum == total - preSum) {
        cout << "Can be split at index " << i;
        break;
     }
  }
}
Time: O(n)
Space: O(1)
Example: Split at index 2 \rightarrow 1+2 = 3
```

5. Find the maximum sum of any subarray of size K in a given array.

#### Algorithm:

- Use sliding window of size k
- Update window sum by adding next and removing previous

#### **Program:**

```
#include <iostream>
using namespace std;

int main() {
    int arr[] = {1, 4, 2, 10, 2, 3}, n = 6, k = 3;
    int sum = 0, maxSum = 0;
    for (int i = 0; i < k; i++) sum += arr[i];
    maxSum = sum;
    for (int i = k; i < n; i++) {
        sum += arr[i] - arr[i-k];
        maxSum = max(maxSum, sum);
    }
    cout << "Max sum = " << maxSum;
}

Time: O(n)
Space: O(1)
Example: Max sum of size 3 → 10+2+3 = 15</pre>
```

#### 6. Find the length of the longest substring without repeating characters.

#### Algorithm:

Use sliding window with a set to track characters

```
#include <iostream>
#include <unordered_set>
using namespace std;
int main() {
  string s = "abcabcbb";
  unordered_set<char> seen;
  int left = 0, maxLen = 0;
  for (int right = 0; right < s.size(); right++) {
     while (seen.count(s[right])) seen.erase(s[left++]);
     seen.insert(s[right]);
     maxLen = max(maxLen, right - left + 1);
  cout << "Max Length = " << maxLen;</pre>
}
Time: O(n)
Space: O(n)
Example: "abc" → length 3
```

#### 7. Explain the sliding window technique and its use in string problems.

Sliding window is a method for reducing time complexity by maintaining a subrange (window) that slides over data.

**Use:** Optimal for substring, subarray problems like longest unique substring, max sum of size K, etc.

#### 8. Find the longest palindromic substring in a given string.

#### Algorithm:

Expand around center

#### Program:

```
#include <iostream>
using namespace std;
string expand(string s, int l, int r) {
  while (l \ge 0 \&\& r < s.size() \&\& s[l] == s[r]) l--, r++;
  return s.substr(l+1, r-l-1);
}
int main() {
  string s = "babad", res = "";
  for (int i = 0; i < s.size(); i++) {
     string odd = expand(s, i, i);
     string even = expand(s, i, i+1);
     if (odd.size() > res.size()) res = odd;
     if (even.size() > res.size()) res = even;
  cout << "Longest Palindrome = " << res;</pre>
}
Time: O(n<sup>2</sup>)
Space: O(1)
```

#### 9. Find the longest common prefix among a list of strings.

#### Algorithm:

Compare characters of all strings

Example: "aba" from "babad"

```
#include <iostream>
#include <vector>
using namespace std;

int main() {
    vector<string> strs = {"flower", "flow", "flight"};
```

```
string res = "";
for (int i = 0; i < strs[0].size(); i++) {
    char c = strs[0][i];
    for (auto s : strs)
        if (i >= s.size() || s[i] != c) {
            cout << "LCP = " << res;
            return 0;
        }
        res += c;
    }
    cout << "LCP = " << res;
}
Time: O(n * m)
Space: O(1)
Example: "fl"</pre>
```

#### 10. Generate all permutations of a given string.

#### Algorithm:

Backtracking with swap

#### Program:

```
#include <iostream>
#include <algorithm>
using namespace std;
void permute(string s, int I, int r) {
  if (I == r) cout << s << " ";
  else {
     for (int i = I; i <= r; i++) {
        swap(s[l], s[i]);
        permute(s, l+1, r);
        swap(s[l], s[i]);
     }
  }
}
int main() {
  string s = "abc";
  permute(s, 0, s.size()-1);
}
Time: O(n * n!)
Space: O(n)
Example: "abc" → abc, acb, bac, bca, cab, cba
```

#### 11. Find two numbers in a sorted array that add up to a target.

#### Algorithm:

Use two pointers from start and end.

#### Program:

```
#include <iostream>
using namespace std;
int main() {
  int arr[] = \{1, 2, 4, 6, 10\}, n = 5, target = 8;
  int I = 0, r = n - 1;
  while (l < r) {
     int sum = arr[l] + arr[r];
     if (sum == target) {
        cout << arr[l] << " " << arr[r];
        break;
     } else if (sum < target) l++;
     else r--;
  }
}
Time: O(n)
Space: O(1)
Example: 2 + 6 = 8
```

#### 12. Rearrange numbers into the lexicographically next greater permutation.

#### Algorithm:

Find pivot, swap with successor, reverse suffix.

```
#include <iostream>
#include <vector>
#include <algorithm>
using namespace std;
int main() {
  vector<int> nums = \{1, 2, 3\};
  int i = nums.size() - 2;
  while (i \ge 0 \&\& nums[i] \ge nums[i+1]) i--;
  if (i >= 0) {
     int j = nums.size() - 1;
     while (nums[j] <= nums[i]) j--;
     swap(nums[i], nums[j]);
  }
  reverse(nums.begin() + i + 1, nums.end());
  for (int n : nums) cout << n << " ";
}
Time: O(n)
Space: O(1)
Example: 1 \ 2 \ 3 \to 1 \ 3 \ 2
```

#### 13. How to merge two sorted linked lists into one sorted list.

#### Algorithm:

Use dummy node and compare nodes one by one.

#### Program:

```
#include <iostream>
using namespace std;
struct Node {
  int val;
  Node* next:
  Node(int x) : val(x), next(NULL) {}
};
Node* merge(Node* I1, Node* I2) {
  Node dummy(0), *tail = &dummy;
  while (I1 && I2) {
     if (11-val < 12-val) tail->next = 11, 11 = 11->next;
     else tail->next = I2, I2 = I2->next;
     tail = tail->next;
  tail->next = 11 ? 11 : 12;
  return dummy.next;
}
Time: O(n + m)
Space: O(1)
Example: [1,3] + [2,4] \rightarrow [1,2,3,4]
```

#### 14. Find the median of two sorted arrays using binary search.

#### Algorithm:

Binary search on smaller array to find partition.

```
#include <iostream>
#include <vector>
using namespace std;

double findMedian(vector<int>& A, vector<int>& B) {
    if (A.size() > B.size()) return findMedian(B, A);
    int m = A.size(), n = B.size();
    int I = 0, r = m;
    while (I <= r) {
        int i = (I + r) / 2;
        int j = (m + n + 1) / 2 - i;
        int Aleft = (i == 0) ? INT_MIN : A[i - 1];
        int Aright = (i == m) ? INT_MAX : A[i];
        int Bleft = (j == 0) ? INT_MIN : B[j - 1];
        int Bright = (j == n) ? INT_MAX : B[j];</pre>
```

```
if (Aleft <= Bright && Bleft <= Aright) {
        if ((m + n) % 2 == 0) return (max(Aleft, Bleft) + min(Aright, Bright)) / 2.0;
        else return max(Aleft, Bleft);
        } else if (Aleft > Bright) r = i - 1;
        else I = i + 1;
    }
    return 0.0;
}

int main() {
    vector<int> a = {1, 3}, b = {2};
    cout << findMedian(a, b);
}

Time: O(log(min(m,n)))

Space: O(1)

Example: [1,3] + [2] → median = 2</pre>
```

#### 15. Find the k-th smallest element in a sorted matrix.

#### Algorithm:

Use min-heap or binary search on value range.

```
#include <iostream>
#include <vector>
using namespace std;
int countLE(vector<vector<int>>& mat, int mid) {
  int count = 0, n = mat.size(), j = n - 1;
  for (int i = 0; i < n; i++) {
     while (j \ge 0 \&\& mat[i][j] > mid) j--;
     count += (j + 1);
  }
  return count;
}
int kthSmallest(vector<vector<int>>& mat, int k) {
  int n = \text{mat.size}(), I = \text{mat}[0][0], r = \text{mat}[n-1][n-1];
  while (l < r) {
     int mid = (I + r) / 2;
     if (countLE(mat, mid) < k) I = mid + 1;
     else r = mid;
  }
  return I;
}
int main() {
  vector<vector<int>> mat = {{1, 5, 9}, {10, 11, 13}, {12, 13, 15}};
  cout << kthSmallest(mat, 8);
}
```

Time: O(n log(max-min))

Space: O(1)

**Example:** 8th smallest  $\rightarrow$  13

#### 16. Find the majority element in an array that appears more than n/2 times.

#### Algorithm:

Use Boyer-Moore Voting Algorithm

#### **Program:**

```
#include <iostream>
using namespace std;

int main() {
    int arr[] = {2, 2, 1, 1, 2}, n = 5, count = 0, candidate;
    for (int i = 0; i < n; i++) {
        if (count == 0) candidate = arr[i];
        count += (arr[i] == candidate) ? 1 : -1;
    }
    cout << "Majority = " << candidate;
}

Time: O(n)
Space: O(1)</pre>
```

**Example:** 2 appears 3 times

#### 17. Calculate how much water can be trapped between the bars of a histogram.

#### Algorithm:

Use two-pointer approach tracking leftMax and rightMax.

```
#include <iostream>
using namespace std;

int main() {
    int arr[] = {0, 1, 0, 2, 1, 0, 1, 3}, n = 8;
    int I = 0, r = n - 1, leftMax = 0, rightMax = 0, water = 0;
    while (I < r) {
        if (arr[I] < arr[r]) {
            leftMax = max(leftMax, arr[I]);
            water += leftMax - arr[I++];
        } else {
            rightMax = max(rightMax, arr[r]);
            water += rightMax - arr[r--];
        }
    }
    cout << "Water = " << water;
}</pre>
```

Time: O(n) Space: O(1)

**Example:** Water trapped = 6

#### 18. Find the maximum XOR of two numbers in an array.

#### Algorithm:

Use trie or greedy method with set.

#### **Program:**

```
#include <iostream>
#include <vector>
#include <unordered set>
using namespace std;
int main() {
  vector<int> nums = \{3, 10, 5, 25, 2, 8\}, maxXor = 0, mask = 0;
  for (int i = 31; i >= 0; i--) {
     mask = (1 << i);
     unordered_set<int> s;
     for (int num: nums) s.insert(num & mask);
     int temp = \max Xor \mid (1 << i);
     for (int prefix : s)
       if (s.count(temp ^ prefix)) {
          maxXor = temp;
          break;
       }
  cout << "Max XOR = " << maxXor;
}
```

**Time:** O(n \* 32) **Space:** O(n)

Example: Max XOR = 28

#### 19. How to find the maximum product subarray.

#### Algorithm:

Track maxProd and minProd due to sign flip.

```
#include <iostream>
using namespace std;

int main() {
   int arr[] = {2, 3, -2, 4}, n = 4;
   int maxP = arr[0], minP = arr[0], res = arr[0];
   for (int i = 1; i < n; i++) {
      if (arr[i] < 0) swap(maxP, minP);
   }
}</pre>
```

```
maxP = max(arr[i], maxP * arr[i]);
  minP = min(arr[i], minP * arr[i]);
  res = max(res, maxP);
}
cout << "Max Product = " << res;
}

Time: O(n)
Space: O(1)
Example: 2x3 = 6</pre>
```

20. Count all numbers with unique digits for a given number of digits.

#### Algorithm:

Use combinatorics:  $9 \times 9 \times 8 \times ...$ 

#### **Program:**

```
#include <iostream>
using namespace std;

int countNumbers(int n) {
    if (n == 0) return 1;
    int res = 10, prod = 9, available = 9;
    for (int i = 2; i <= n && available; i++) {
        prod *= available--;
        res += prod;
    }
    return res;
}

int main() {
    cout << countNumbers(2);
}

Time: O(n)
Space: O(1)</pre>
```

21. How to count the number of 1s in the binary representation of numbers from 0 to n.

#### Algorithm:

**Example:**  $n = 2 \rightarrow 91$ 

Use dynamic programming where bits[i] = bits[i >> 1] + (i & 1). □

```
#include <vector>
#include <iostream>
using namespace std;

vector<int> countBits(int n) {
   vector<int> bits(n + 1);
```

```
for (int i = 1; i <= n; ++i)
    bits[i] = bits[i >> 1] + (i & 1);
    return bits;
}

int main() {
    int n = 5;
    vector<int> result = countBits(n);
    for (int i = 0; i <= n; ++i)
        cout << "Number of 1s in " << i << " = " << result[i] << endl;
}

Time Complexity: O(n)
Space Complexity: O(n)
Example: For n = 5, output is [0, 1, 1, 2, 1, 2].□
```

#### 22. How to check if a number is a power of two using bit manipulation.

#### **Algorithm:**

A number is a power of two if n > 0 and n & (n - 1) == 0.□

#### Program:

```
#include <iostream>
using namespace std;

bool isPowerOfTwo(int n) {
    return n > 0 && (n & (n - 1)) == 0;
}

int main() {
    int num = 16;
    cout << num << " is power of two: " << boolalpha << isPowerOfTwo(num) << endl;
}</pre>
```

**Time Complexity:** O(1) **Space Complexity:** O(1)

**Example:** 16 is a power of two.

#### 23. How to find the maximum XOR of two numbers in an array.

#### Algorithm:

Iterate over each pair and calculate XOR to find the maximum.

```
#include <vector>
#include <iostream>
using namespace std;

int findMaximumXOR(vector<int>& nums) {
    int maxXOR = 0;
    for (int i = 0; i < nums.size(); ++i)
        for (int j = i + 1; j < nums.size(); ++j)
            maxXOR = max(maxXOR, nums[i] ^ nums[j]);
    return maxXOR;
}

int main() {
    vector<int> nums = {3, 10, 5, 25, 2, 8};
    cout << "Maximum XOR: " << findMaximumXOR(nums) << endl;
}</pre>
```

**Time Complexity:** O(n^2) **Space Complexity:** O(1)

**Example:** Maximum XOR is 28. □

#### 24. Explain the concept of bit manipulation and its advantages in algorithm design.

#### **Explanation:**

- Bit manipulation involves direct operations on bits using operators like AND, OR, XOR, NOT, shifts, etc. □
- Advantages:
  - Efficient computation.
  - o Memory optimization. □
  - Useful in low-level programming. □

#### 25. Solve the problem of finding the next greater element for each element in an array.

#### Algorithm:

 Use a stack to keep track of elements for which the next greater element hasn't been found.□

```
#include <vector>
#include <stack>
#include <iostream>
using namespace std;

vector<int> nextGreaterElements(vector<int>& nums) {
   vector<int> nge(nums.size(), -1);
   stack<int> s;
```

```
for (int i = 0; i < nums.size(); ++i) {
     while (!s.empty() \&\& nums[s.top()] < nums[i]) {
       nge[s.top()] = nums[i];
       s.pop();
     }
     s.push(i);
  return nge;
}
int main() {
  vector<int> nums = \{2, 1, 2, 4, 3\};
  vector<int> result = nextGreaterElements(nums);
  for (int i = 0; i < nums.size(); ++i)
     cout << "Next greater for " << nums[i] << " is " << result[i] << endl;
}
Time Complexity: O(n)
Space Complexity: O(n)
Example: For [2, 1, 2, 4, 3], output is [4, 2, 4, -1, -1].
```

#### 26. Remove the n-th node from the end of a singly linked list.

#### Algorithm:

 Use two pointers; move one ahead by n steps, then move both until the first reaches the end.□

```
#include <iostream>
using namespace std;
struct ListNode {
  int val:
  ListNode* next;
  ListNode(int x) : val(x), next(NULL) {}
};
ListNode* removeNthFromEnd(ListNode* head, int n) {
  ListNode dummy(0);
  dummy.next = head;
  ListNode* first = &dummy;
  ListNode* second = &dummy;
  for (int i = 0; i <= n; ++i)
     first = first->next;
  while (first) {
     first = first->next;
     second = second->next;
  }
  second->next = second->next->next;
```

```
return dummy.next;
}

Time Complexity: O(L)
Space Complexity: O(1)
Example: Removing 2nd from end in [1,2,3,4,5] results in [1,2,3,5].
```

#### 27. Find the node where two singly linked lists intersect.

#### Algorithm:

- Traverse both lists to determine their lengths.
- Align the start of the longer list with the shorter by advancing the pointer of the longer list by the difference in lengths. □
- Traverse both lists simultaneously until a common node is found or the end is reached. □

```
#include <iostream>
using namespace std;
struct ListNode {
  int val:
  ListNode* next:
  ListNode(int x) : val(x), next(NULL) {}
};
int getLength(ListNode* head) {
  int length = 0;
  while (head) {
     ++length;
     head = head->next;
  return length;
}
ListNode* getIntersectionNode(ListNode* headA, ListNode* headB) {
  int lenA = getLength(headA);
  int lenB = getLength(headB);
  while (lenA > lenB) {
     headA = headA->next;
     --lenA;
  }
  while (lenB > lenA) {
     headB = headB->next;
     --lenB:
  while (headA && headB) {
    if (headA == headB)
       return headA;
     headA = headA->next;
     headB = headB->next;
  }
```

```
return NULL;
```

**Time Complexity:**  $O(m + n) \square$  **Space Complexity:**  $O(1) \square$  **Example:** For lists A: [1, 2, 3, 4, 5] and B: [9, 4, 5], the intersection is at node with value 4.  $\square$ 

#### 28. Implement two stacks in a single array.

#### Algorithm:

- Use a single array with two pointers: one starting from the beginning (top1) for the first stack and one from the end (top2) for the second stack. □
- Ensure that top1 and top2 do not cross each other to prevent overflow.

```
#include <iostream>
using namespace std;
class TwoStacks {
  int* arr;
  int size:
  int top1, top2;
public:
  TwoStacks(int n) {
     size = n;
     arr = new int[n];
     top1 = -1;
     top2 = size;
  void push1(int x) {
     if (top1 < top2 - 1) {
        arr[++top1] = x;
     } else {
        cout << "Stack Overflow\n";</pre>
  void push2(int x) {
     if (top1 < top2 - 1) {
        arr[--top2] = x;
     } else {
        cout << "Stack Overflow\n";</pre>
  int pop1() {
     if (top1 >= 0) {
        return arr[top1--];
     } else {
        cout << "Stack Underflow\n";</pre>
        return -1;
     }
```

```
int pop2() {
     if (top2 < size) {
       return arr[top2++];
     } else {
       cout << "Stack Underflow\n";</pre>
       return -1;
  }
};
Time Complexity: O(1) for push and pop operations. \square Space Complexity: O(n) Example:
Pushing elements 1, 2, 3 to stack1 and 9, 8, 7 to stack2 in an array of size 6. □
29. Write a program to check if an integer is a palindrome without converting it to a string.
Algorithm:
      Handle negative numbers by returning false. □
      Reverse the second half of the number and compare it with the first half.
Program:
#include <iostream>
using namespace std;
bool isPalindrome(int x) {
  if (x < 0 || (x \% 10 == 0 \&\& x != 0)) return false;
  int reversed = 0;
  while (x > reversed) {
     reversed = reversed * 10 + x \% 10;
     x /= 10:
  }
  return x == reversed || x == reversed / 10;
}
```

Time Complexity:  $O(log_{10}(n)) \square$  Space Complexity:  $O(1) \square$  Example: 121 is a palindrome.  $\square$ 

30. Explain the concept of linked lists and their applications in algorithm design.

cout << num << " is palindrome: " << boolalpha << isPalindrome(num) << endl;</pre>

#### **Explanation:**

int main() {

}

int num = 121;

- A linked list is a linear data structure where each element (node) contains a data part and a reference (or link) to the next node in the sequence.
  - Applications:
    - Dynamic memory allocation.
    - o Implementation of stacks, queues, and other abstract data types. □
    - Efficient insertions and deletions.□
- 31. Find the longest consecutive sequence in an unsorted array.

```
#include <unordered set>
int longestConsecutive(vector<int>& nums) {
  unordered set<int> s(nums.begin(), nums.end());
  int longest = 0;
  for (int num : nums) {
     if (!s.count(num - 1)) {
        int length = 0;
        while (s.count(num++)) length++;
        longest = max(longest, length);
     }
  }
  return longest;
}
Time: O(n), Space: O(n)
Example: nums = [100, 4, 200, 1, 3, 2] => Output: 4 (sequence: 1,2,3,4)
32. Count the number of islands in a 2D grid.
void dfs(vector<vector<char>>& grid, int i, int j) {
  if (i < 0 || i >= grid.size() || j < 0 || j >= grid[0].size() || grid[i][j] == '0') return;
  grid[i][j] = '0';
  dfs(grid, i+1, j); dfs(grid, i-1, j); dfs(grid, i, j+1); dfs(grid, i, j-1);
}
```

```
int numlslands(vector<vector<char>>& grid) {
   int count = 0;
  for (int i = 0; i < grid.size(); i++) {
      for (int j = 0; j < grid[0].size(); j++) {
        if (grid[i][j] == '1') {
           dfs(grid, i, j);
           count++;
        }
      }
  }
   return count;
}
Time: O(m*n), Space: O(m*n)
Example: grid = \{\{'1','1','0','0','0'\},\{'1','1','0','0','0'\},\{'0','0','1','0','0'\},\{'0','0','1','1'\}\} => Output: 3
 33. Rotate an n x n matrix 90 degrees clockwise in-place.
void rotate(vector<vector<int>>& matrix) {
   int n = matrix.size();
   for (int i = 0; i < n; i++) {
      for (int j = i; j < n; j++) {
        swap(matrix[i][j], matrix[j][i]);
     }
  }
  for (int i = 0; i < n; i++) {
      reverse(matrix[i].begin(), matrix[i].end());
  }
}
Time: O(n^2), Space: O(1)
 Example: Input = [[1,2,3],[4,5,6],[7,8,9]] \Rightarrow Output = [[7,4,1],[8,5,2],[9,6,3]]
```

```
34. Implement a LRU (Least Recently Used) Cache.
```

```
#include <list>
#include <unordered_map>
class LRUCache {
  int cap;
  list<pair<int, int>> lru;
   unordered_map<int, list<pair<int, int>>::iterator> m;
public:
   LRUCache(int capacity) { cap = capacity; }
  int get(int key) {
     if (m.find(key) == m.end()) return -1;
     Iru.splice(Iru.begin(), Iru, m[key]);
     return m[key]->second;
  }
  void put(int key, int value) {
     if (m.find(key) != m.end()) {
        lru.splice(lru.begin(), lru, m[key]);
        m[key]->second = value;
     } else {
        if (lru.size() == cap) {
          m.erase(lru.back().first);
          lru.pop_back();
        }
        lru.emplace_front(key, value);
        m[key] = lru.begin();
     }
  }
};
```

```
Time: O(1), Space: O(capacity)
Example: put(1,1), put(2,2), get(1), put(3,3), get(2) => Output: 1, -1
35. Find the minimum window substring containing all characters of another string.
#include <climits>
string minWindow(string s, string t) {
  vector<int> freq(128, 0);
  for (char c : t) freq[c]++;
  int left = 0, minLen = INT_MAX, minStart = 0, count = t.size();
  for (int right = 0; right < s.size(); right++) {
     if (freq[s[right]]-- > 0) count--;
     while (count == 0) {
       if (right - left + 1 < minLen) {
          minLen = right - left + 1;
          minStart = left;
       }
       if (++freq[s[left++]] > 0) count++;
     }
  }
  return minLen == INT_MAX ? "" : s.substr(minStart, minLen);
}
Time: O(n), Space: O(1)
Example: s = "ADOBECODEBANC", t = "ABC" => Output: "BANC"
36. Merge two sorted arrays without using extra space.
void merge(vector<int>& nums1, int m, vector<int>& nums2, int n) {
```

int i = m - 1, j = n - 1, k = m + n - 1;

```
while (i \ge 0 \&\& j \ge 0) {
     nums1[k--] = nums1[i] > nums2[j] ? nums1[i--] : nums2[j--];
  }
  while (j \ge 0) nums1[k--] = nums2[j--];
}
Time: O(m + n), Space: O(1)
Example: nums1 = [1,2,3,0,0,0], m = 3, nums2 = [2,5,6], n = 3 => Output: [1,2,2,3,5,6]
37. Implement binary search recursively.
int binarySearch(vector<int>& arr, int low, int high, int target) {
  if (low > high) return -1;
  int mid = low + (high - low) / 2;
  if (arr[mid] == target) return mid;
  else if (arr[mid] > target) return binarySearch(arr, low, mid - 1, target);
  else return binarySearch(arr, mid + 1, high, target);
}
Time: O(log n), Space: O(log n) (due to recursion)
 Example: arr = [1,2,3,4,5], target = 3 => Output: 2
38. Implement BFS traversal for a graph.
#include <queue>
vector<int> bfsOfGraph(int V, vector<int> adj[]) {
  vector<int> visited(V, 0), res;
  queue<int> q;
  q.push(0);
  visited[0] = 1;
  while (!q.empty()) {
```

```
int node = q.front(); q.pop();
     res.push_back(node);
     for (int neighbor : adj[node]) {
        if (!visited[neighbor]) {
          visited[neighbor] = 1;
          q.push(neighbor);
       }
     }
  }
  return res;
}
Time: O(V + E), Space: O(V)
Example: V = 5, edges = \{0-1, 0-2, 1-3, 1-4\} = 0 Output: [0,1,2,3,4]
39. Implement DFS traversal for a graph.
void dfs(int node, vector<int> adj[], vector<int>& visited, vector<int>& res) {
  visited[node] = 1;
  res.push_back(node);
  for (int neighbor : adj[node]) {
     if (!visited[neighbor]) dfs(neighbor, adj, visited, res);
  }
}
vector<int> dfsOfGraph(int V, vector<int> adj[]) {
  vector<int> visited(V, 0), res;
  dfs(0, adj, visited, res);
  return res;
}
Time: O(V + E), Space: O(V)
Example: V = 5, edges = \{0-1, 0-2, 1-3, 1-4\} = 0
```

40. Find the shortest path in an unweighted graph using BFS.

```
vector<int> shortestPath(int V, vector<int> adj[], int src) {
  vector<int> dist(V, -1);
  queue<int> q;
  q.push(src);
  dist[src] = 0;
  while (!q.empty()) {
     int node = q.front(); q.pop();
     for (int neighbor : adj[node]) {
        if (dist[neighbor] == -1) {
           dist[neighbor] = dist[node] + 1;
           q.push(neighbor);
        }
     }
  }
  return dist;
}
Time: O(V + E), Space: O(V)
Example: V = 5, edges = \{0-1, 0-2, 1-3, 1-4\}, src = 0 \Rightarrow 0 Output: [0,1,1,2,2]
```

41. Write a program to find the maximum subarray sum using Kadane's algorithm.

#### Algorithm:

```
    Initialize max_so_far = arr[0] and current_max = arr[0].
    Traverse the array from index 1:

            current_max = max(arr[i], current_max + arr[i])
            max_so_far = max(max_so_far, current_max)

    Return max so far.
```

```
#include <iostream>
#include <vector>
using namespace std;
```

```
int maxSubArraySum(vector<int>& nums) {
    int current_max = nums[0], max_so_far = nums[0];
    for (int i = 1; i < nums.size(); i++) {
        current_max = max(nums[i], current_max + nums[i]);
        max_so_far = max(max_so_far, current_max);
    }
    return max_so_far;
}

Time: O(n) | Space: O(1)

Example:
Input: [-2,1,-3,4,-1,2,1,-5,4]
Output: 6 → Subarray [4,-1,2,1]</pre>
```

42. Explain the concept of dynamic programming and its use in solving the maximum subarray problem.

#### Answer:

**Dynamic Programming (DP)** is a method to solve problems by breaking them into smaller overlapping subproblems and storing their results.

In Kadane's Algorithm, DP helps track:

- The maximum sum ending at index i.
- Using the recurrence: dp[i] = max(arr[i], dp[i-1] + arr[i])

This avoids recalculating subarray sums, making it efficient (O(n) time).

43. Solve the problem of finding the top K frequent elements in an array.

#### Algorithm:

- 1. Count frequency using a hash map.
- 2. Use a min-heap (priority queue) to store top K elements.
- 3. Pop and return the top K frequent.

```
#include <iostream>
#include <vector>
#include <unordered_map>
#include <queue>
using namespace std;

vector<int> topKFrequent(vector<int>& nums, int k) {
    unordered_map<int, int> freq;
    for (int num : nums) freq[num]++;
```

```
priority_queue<pair<int, int>, vector<pair<int, int>>, greater<>> minHeap;
  for (auto& [num, count] : freq) {
     minHeap.push({count, num});
     if (minHeap.size() > k) minHeap.pop();
  }
  vector<int> result:
  while (!minHeap.empty()) {
     result.push_back(minHeap.top().second);
     minHeap.pop();
  }
  return result;
}
Time: O(n log k) | Space: O(n)
Example:
Input: [1,1,1,2,2,3], k = 2
Output: [1,2]
```

#### 44. How to find two numbers in an array that add up to a target using hashing.

#### Algorithm:

- 1. Initialize an empty hash map.
- 2. For each element, check if target current exists in map.
- 3. If yes, return the pair. Else insert current element.

```
#include <iostream>
#include <unordered_map>
#include <vector>
using namespace std;

vector<int> twoSum(vector<int>& nums, int target) {
    unordered_map<int, int> mp;
    for (int i = 0; i < nums.size(); i++) {
        int complement = target - nums[i];
        if (mp.count(complement))
            return {mp[complement], i};
        mp[nums[i]] = i;
    }
    return {};
}</pre>
```

Time: O(n) | Space: O(n)

#### **Example:**

```
Input: [2, 7, 11, 15], target = 9
Output: [0,1] \rightarrow 2 + 7 = 9
```

#### 45. Explain the concept of priority queues and their applications in algorithm design.

#### Answer:

**Priority Queue** is an abstract data structure where each element has a priority. Elements with higher priority are served before others.

C++ STL: priority\_queue<int> pq; (max-heap by default)

#### **Applications:**

- · Dijkstra's algorithm
- Huffman coding
- A\* search
- Task scheduling

#### 46. Write a program to find the longest palindromic substring in a given string.

#### **Algorithm (Expand Around Center):**

- For each character, expand around center (odd and even lengths).
- Track the longest palindrome.

```
#include <iostream>
using namespace std;
string longestPalindrome(string s) {
  int start = 0, maxLen = 0;
  for (int i = 0; i < s.length(); i++) {
     int I = i, r = i;
     while (I \ge 0 \&\& r < s.length() \&\& s[I] == s[r]) {
        if (r - l + 1 > maxLen) {
           maxLen = r - l + 1;
           start = I;
        I--; r++;
     I = i; r = i+1;
     while (I \ge 0 \&\& r < s.length() \&\& s[I] == s[r]) {
        if (r - l + 1 > maxLen) {
           maxLen = r - l + 1;
           start = I;
        I--; r++;
     }
  }
```

```
return s.substr(start, maxLen);
}

Time: O(n^2) | Space: O(1)

Example:

Input: "babad" → Output: "bab" or "aba"
```

47. Explain the concept of histogram problems and their applications in algorithm design.

#### Answer:

**Histogram problem:** Given heights of bars, find the largest rectangle that fits under the histogram.

Use a **monotonic stack** to track increasing bar indices.

#### **Applications:**

- Max area in binary matrix
- · Skyline silhouette
- Text editor layout

#### 48. Solve the problem of finding the next permutation of a given array.

#### Algorithm:

- 1. Find first i where nums[i] < nums[i+1] from right.
- 2. Find j > i such that nums[j] > nums[i].
- 3. Swap nums[i] and nums[j].
- 4. Reverse nums[i+1:].

```
#include <iostream>
#include <vector>
#include <algorithm>
using namespace std;

void nextPermutation(vector<int>& nums) {
   int i = nums.size() - 2;
   while (i >= 0 && nums[i] >= nums[i+1]) i--;
   if (i >= 0) {
      int j = nums.size() - 1;
      while (nums[j] <= nums[i]) j--;
      swap(nums[i], nums[j]);
   }
   reverse(nums.begin() + i + 1, nums.end());
}</pre>
```

Time: O(n) | Space: O(1)

#### **Example:**

```
Input: [1,2,3] \rightarrow \text{Output: } [1,3,2]
```

#### 49. How to find the intersection of two linked lists.

#### Algorithm:

- 1. Use two pointers, a and b on lists A and B.
- 2. When a pointer reaches the end, move to the start of the other list.
- 3. They meet at the intersection node or nullptr.

```
struct ListNode {
  int val;
  ListNode* next;
  ListNode(int x) : val(x), next(NULL) {}
};

ListNode* getIntersectionNode(ListNode* headA, ListNode* headB) {
  ListNode* a = headA;
  ListNode* b = headB;
  while (a != b) {
      a = a ? a->next : headB;
      b = b ? b->next : headA;
  }
  return a;
}
```

Time:  $O(n + m) \mid Space: O(1)$ 

#### **Example:**

Lists intersect at node with value 8.

#### 50. Explain the concept of equilibrium index and its applications in array problems.

#### Answer:

An **equilibrium index** is a position i such that:

```
sum(arr[0..i-1]) == sum(arr[i+1..n-1])
```

#### **Applications:**

- Balance point problems
- Load distribution
- Prefix-suffix analysis

```
#include <iostream>
#include <vector>
using namespace std;

int findEquilibriumIndex(vector<int>& nums) {
    int total = 0, leftSum = 0;
    for (int num : nums) total += num;
    for (int i = 0; i < nums.size(); i++) {
        total -= nums[i];
        if (leftSum == total) return i;
        leftSum += nums[i];
    }
    return -1;
}</pre>
Time: O(n) | Space: O(1)
```