American University of Armenia CS 121 Data Structures A

Homework Assignment 1

- 1. (2 points) The number of operations executed by algorithms A and B is $100n^3$ and 5×2^n , respectively. Determine n_0 such that A is better than B for $n \ge n_0$.
- 2. (2 points) Order the following functions by asymptotic growth rate.

$$\begin{array}{cccc}
 13n + 2 \log n & 5n^3 & 3n + 2n \log n \\
 3 \times 2^n & 15n & 10 + \log n \\
 2n^2 + 4n^3 & 1250 \times 2^{45} & 2n^2
 \end{array}$$

3. (2 points) Give a big-Oh characterization, in terms of n, of the running time of the method shown below. Implement an alternative method $alt_example$ that performs the same task in O(n).

Java:

```
/** Returns the number of times second array stores sum of prefix sums from first. */
   public static int example(int[] first, int[] second) { // assume equal-length arrays
3
     int n = first.length, count = 0, total = 0;
                                                  // loop from 0 to n-1 // loop from 0 to j
4
     for (int j=0; j < n; j++)
        for (int k=0; k \le j; k++)
5
6
          total += first[k];
7
     for (int i=0; i < n; i++)
                                                  // loop from 0 to n-1
8
        if (second[i] == total) count++;
9
     return count;
10
  }
   C++:
   /* Returns the number of times second array stores sum of prefix sums from first. */
   int example(int first[], int second[], int n) // assume equal-length arrays
3
     int count = 0, total = 0;
4
                                                  // loop from 0 to n-1 // loop from 0 to j
     for (int j=0; j < n; j++)
5
        for (int k=0; k <= j; k++)
6
          total += first [k];
7
                                                  // loop from 0 to n-1
     for (int i=0; i < n; i++)
8
        if (second[i] == total) count++;
9
10
     return count;
  }
```

- 4. (2 points) Perform an experimental analysis that compares the relative running times of the two methods (given method example and your implementation alt_example) from the previous task. Briefly discuss your findings.
- **5.** (2 points) Show that f(n) is O(g(n)) if and only if g(n) is $\Omega(f(n))$.
- **6.** (2 points) Write a Java/C++ program that given a sorted array a of integers and a separate integer b, for each of the factors of b checks whether a contains that factor. In your implementation you should have a separate method that constructs the factors of a given number and another method that checks if a given array contains a given integer. What is the complexity

of each of those methods? Is it optimal? Test your program on a few inputs of growing size and make a record of the running times. How do these times reflect the asymptotic complexity of your methods?

- 7. (3 points) Assume that you are writing an application that needs to work with the following types of shapes:
 - rectangle (which is defined by it width and height),
 - square (which is defined by the length of its side),
 - ellipse (which is defined by its semi-major and semi-minor axes), and
 - circle (which is defined by its radius).

Design and implement a set of Java/C++ classes that represent these shapes. Your design should support the following operations:

- For each shape, it should be possible to retrieve and change its size.
- Given a set of shapes, it should be possible to identify all squares.
- Given a set of shapes, it should be possible to identify all circles.
- For each shape, it should be possible to get and print its area.

Note that your implementation should follow the principles of good object-oriented design. Include a test program that shows how your design works.