What is the scaling limit, i.e. the number of MPI ranks corresponding to the maximum performance, for each grid size and for each MPI point-to-point call?

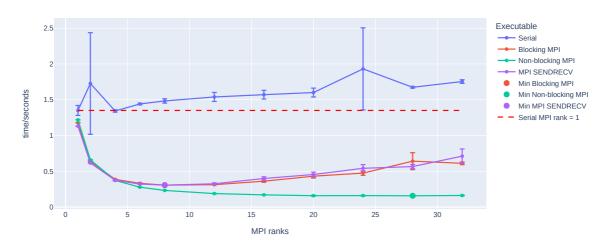
I ran Fortran programs for grid sizes of 100, 200, 300, and MPI ranks in the range (1 2 4 6 8 12 16 20 24 28 32). I ran them three times to find the standard deviation, which is represented as error bars on the graphs. In the graph below for a grid size of 100, there are some noticeable outlier points for Serial 2 and 24, but it's important to consider the scale on the Y-axis. Notably, even though serial is defined as running on 1 CPU, out of curiosity, I decided to also run the program with input data for other MPI ranks. Logically, one would expect to see a constant value ±, but as the graphs show, this is not the case. The likely reasons are scheduling overhead and resource sharing. This is also one of the motivations for running the programs multiple times, to check the reproducibility of the timing results.

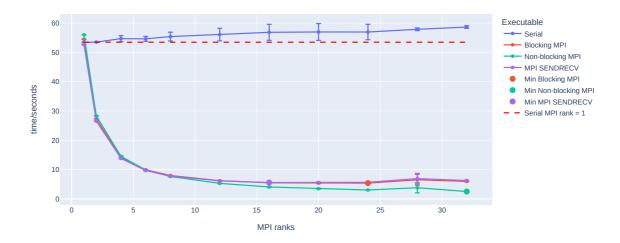
For grid sizes of 200 and 300, the minimum occurs with Non-blocking MPI at the maximum value of 32.

Generally speaking, a border point cannot be considered a global minimum, but considering that for other parallel computations, the global minimums occur at higher time values, this does not affect the answer to "which version of MPI gives the best result." Therefore, 32 is the scaling limit only within the chosen range of MPI ranks.

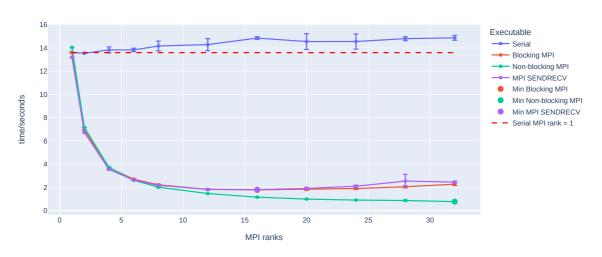
For a grid size of 100, the scaling limit is at MPI rank 28, but the time saving is not as significant compared to 8, which is where the scaling limits of other MPI versions lie. It is also worth noting that the increase in time with increasing MPI ranks is associated with increased synchronization overhead. The same can be said for other grid size values (only instead of 8 -- 16).







Execution Time vs MPI Ranks for Grid Size 200



**Table 1**: scaling limit corresponding to grid size

| Grid<br>Size | Min<br>time, s | Scaling<br>limit | Executable          | Serial time/Min<br>time |
|--------------|----------------|------------------|---------------------|-------------------------|
| 100          | 0.157          | 28               | Non-blocking<br>MPI | 8.6                     |
| 200          | 0.768          | 32               | Non-blocking<br>MPI | 17.7                    |
| 300          | 2.522          | 32               | Non-blocking<br>MPI | 21.2                    |

**Table 2**: scaling limit corresponding to MPI rank, grid size = 100

| Executable       | Grid Size | MPI Ranks | Execution Time Mean, s |
|------------------|-----------|-----------|------------------------|
| MPI SENDRECV     | 100       | 1         | 1.130                  |
| MPI SENDRECV     | 100       | 2         | 0.616                  |
| Non-blocking MPI | 100       | 4         | 0.372                  |
| Non-blocking MPI | 100       | 6         | 0.278                  |
| Non-blocking MPI | 100       | 8         | 0.232                  |
| Non-blocking MPI | 100       | 12        | 0.188                  |
| Non-blocking MPI | 100       | 16        | 0.170                  |
| Non-blocking MPI | 100       | 20        | 0.159                  |
| Non-blocking MPI | 100       | 24        | 0.160                  |
| Non-blocking MPI | 100       | 28        | 0.157                  |
| Non-blocking MPI | 100       | 32        | 0.162                  |

**Table 3**: scaling limit corresponding to MPI rank, grid size = 200

| Executable       | Grid Size | MPI Ranks | Execution Time Mean, s |
|------------------|-----------|-----------|------------------------|
| MPI SENDRECV     | 200       | 1         | 13.191                 |
| MPI SENDRECV     | 200       | 2         | 6.719                  |
| MPI SENDRECV     | 200       | 4         | 3.539                  |
| Non-blocking MPI | 200       | 6         | 2.606                  |
| Non-blocking MPI | 200       | 8         | 2.011                  |
| Non-blocking MPI | 200       | 12        | 1.464                  |
| Non-blocking MPI | 200       | 16        | 1.153                  |
| Non-blocking MPI | 200       | 20        | 0.987                  |
| Non-blocking MPI | 200       | 24        | 0.902                  |
| Non-blocking MPI | 200       | 28        | 0.862                  |
| Non-blocking MPI | 200       | 32        | 0.768                  |

**Table 4**: scaling limit corresponding to MPI rank, grid size = 300

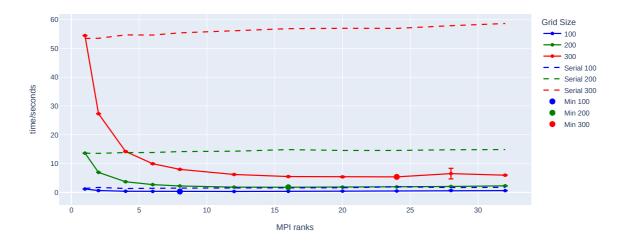
| Executable       | Grid Size | MPI Ranks | Execution Time Mean, s |
|------------------|-----------|-----------|------------------------|
| MPI SENDRECV     | 300       | 1         | 52.647                 |
| MPI SENDRECV     | 300       | 2         | 26.531                 |
| MPI SENDRECV     | 300       | 4         | 13.813                 |
| MPI SENDRECV     | 300       | 6         | 9.696                  |
| Non-blocking MPI | 300       | 8         | 7.658                  |
| Non-blocking MPI | 300       | 12        | 5.300                  |
| Non-blocking MPI | 300       | 16        | 4.078                  |
| Non-blocking MPI | 300       | 20        | 3.491                  |
| Non-blocking MPI | 300       | 24        | 3.034                  |
| Non-blocking MPI | 300       | 28        | 3.811                  |
| Non-blocking MPI | 300       | 32        | 2.523                  |

Globally, Non-blocking MPI shows better results, but when considering segments with MPI ranks ≤ 6, in some cases MPI SENDRECV demonstrates better performance. Moreover, the larger the Grid size, the wider the range of MPI ranks at which MPI SENDRECV is faster.

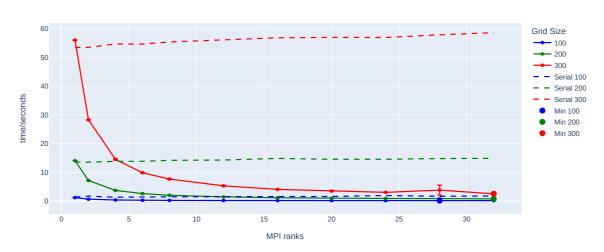
How does this change as the grid gets bigger and why?

The larger the grid size, the greater the delta with the serial version. It is also obvious that the larger the grid size, the more time is required. Put simply, the larger the dimension, the more efficient it is to use parallelization (see Table 1, 'Serial time/Min time' column).

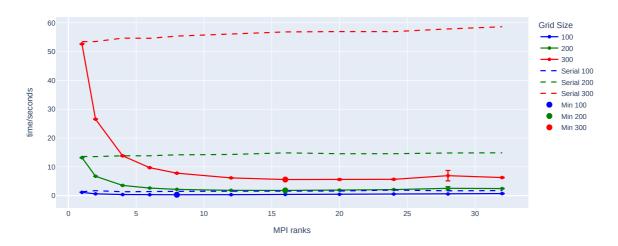
## Execution Time vs MPI Ranks for Blocking MPI



## Execution Time vs MPI Ranks for Non-blocking MPI



## Execution Time vs MPI Ranks for MPI SENDRECV



Which MPI version gives the best performance: blocking MPI SEND and RECV, non-blocking MPI SEND and RECV or MPI SENDRECV?

Answer: non-blocking MPI