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# Acquiring Complex Concepts with Comparative Learning

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Presenter:

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Seminar:

**Grounded Language Processing**

Academic year:

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# Table of Contents

- **Introduction**
  - Research Questions
  - Background Theories
  - Related Work
- **Proposed Methodology**
  - Dataset
  - Comparative Learning
    - Baseline
    - Hypernet
    - Modular Shared Skills (Polytropon)
  - Compound Logical Concepts
- **Evaluation**
  - Multi-Attribute Recognition
  - Logical Pattern Recognition
- **Further Directions and Discussion**

# Table of Contents

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  - Research Questions
  - Background Theories
  - Related Work
- **Proposed Methodology**
  - Dataset
  - Comparative Learning
    - Baseline
    - Hypernet
    - Modular Shared Skills (Polytropon)
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  - Multi-Attribute Recognition
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# The research question

## Machines don't learn efficiently.

- Humans learn continually, machines once for all.
- Humans learn from few examples, machines need to iterate through many of them.

## How do we acquire new words/symbols?

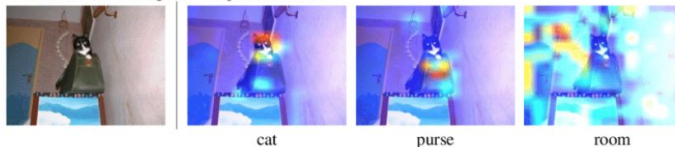
- **What to learn?** By **extracting** key information of a concept to re-use it in the future. [Tomasello and Farrar, 1986]
- **How to learn?** By finding commonalities and differences between two pieces of information. [Gentner and Markman, 1994]

Accuracy Majority Vote  
on Full Dataset

Zero-shot human	53.7	57.0
Zero-shot CLIP	<b>93.5</b>	<b>93.5</b>
One-shot human	75.7	80.3
Two-shot human	75.7	85.0

*Learning Transferable Visual Models From Natural Language Supervision. Radford et al. 2021*

Case (C): a cat sitting inside a purse in a room



*Pixel-BERT: Aligning Image Pixels with Text by Deep Multi-Modal Transformers. Huang et al. 2020*

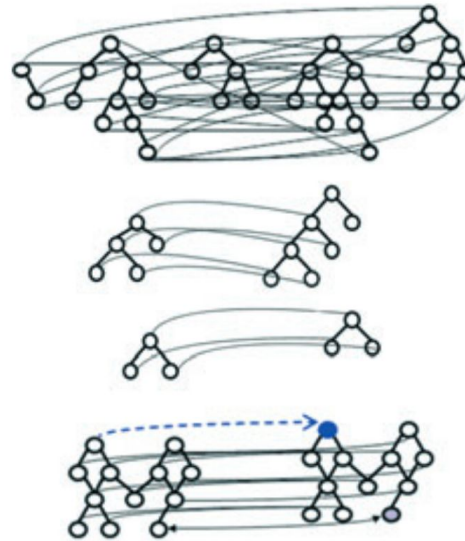
# Background theories

## The theory of Structure-Mapping

*Dedre Gentner. 1983. Structure-mapping: A theoretical framework for analogy. Cognitive science, 7(2):155–170.*

**Comparison allows to attend relational structures** in inputs, highlight differences.  
Human infants learn this with few examples.

## SME (the Structure-mapping Engine)



### Three Stages

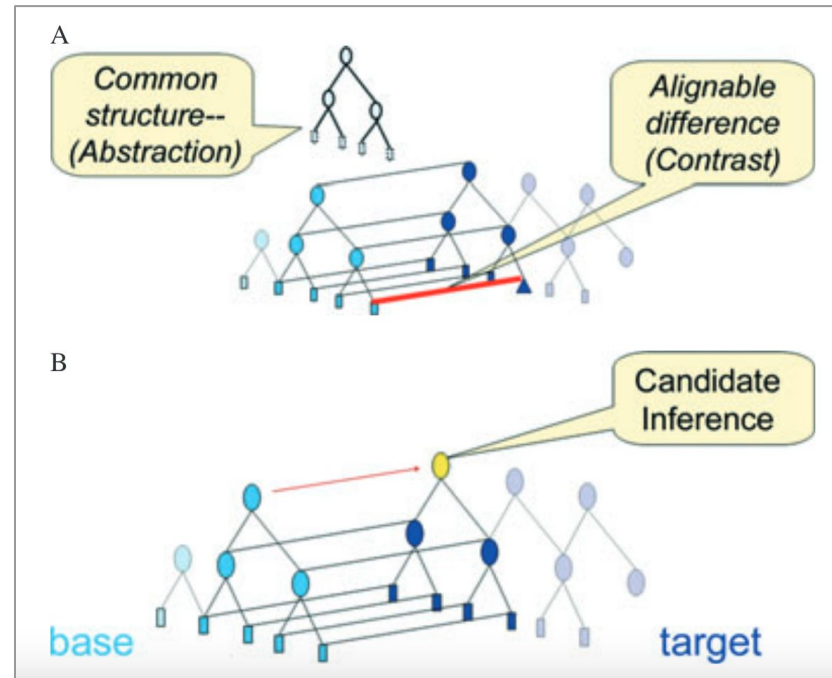
1. Local identity matches made in parallel
2. **Structural consistency** enforced → small submappings (*kernels*)
3. Kernels combined into maximal structurally consistent mapping
  - Structural evaluation
  - Candidate inferences
  - Alignable differences

[Gentner D. Bootstrapping the mind: analogical processes and symbol systems. Cogn Sci. 2010 Jul;34\(5\):752-75. doi: 10.1111/j.1551-6709.2010.01114.x. PMID: 21564235.](#)

## The theory of Structure-Mapping

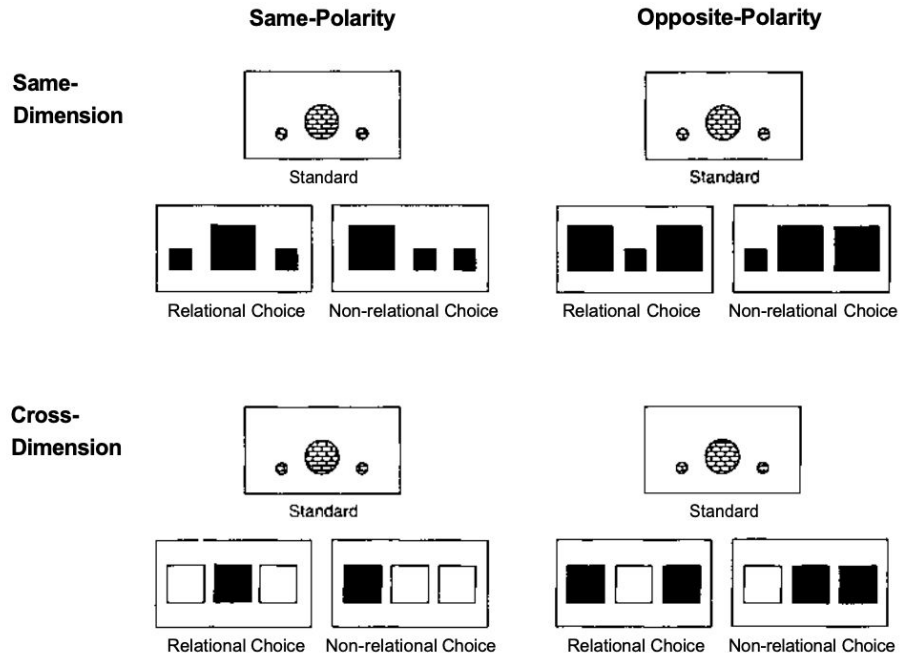
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**Comparison allows to attend relational structures** in inputs, highlight differences.  
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[Gentner D. Bootstrapping the mind: analogical processes and symbol systems. \*Cogn Sci\*. 2010 Jul;34\(5\):752-75. doi: 10.1111/j.1551-6709.2010.01114.x. PMID: 21564235.](#)

# Background theories



## Progressive Alignment

*Hespos et al. 2020 Structure-mapping processes enable infants' learning across domains including language*

*Kotovsky, Gentner. 1996. Comparison and categorization in the development of relational similarity.*

**Aligning** highly similar inputs invite young children to **reason about relational structures** for abstraction and characteristic learning.

## Learning in neural networks

- **Pre-training:** using internet-scale collections of data and hoping to well transfer knowledge
- **Continual learning:** training the model on subsequent sets of knowledge without forgetting
  - Rehearsal/replay methods
  - Learn with penalties on forgetting
  - Domain adaptation/generalization

→ What about gradually learning with developmental psychology theories in mind?





# Table of Contents

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    - Baseline
    - Hypernet
    - Modular Shared Skills (Polytropon)
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# Proposed Methodology: Base Work

[Human Inspired Progressive Alignment and Comparative Learning for Grounded Word Acquisition. Bao et al. 2023](#)

## Human Inspired Progressive Alignment and Comparative Learning for Grounded Word Acquisition

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Barrett Martin Lattimer<sup>§\*</sup>

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- A curated **dataset**
  - Simulated **O**bjects for **L**anguage **A**cquisition (**SOLA**)
- A **methodology** for:
  - Grounded word acquisition (Comparative Learning)
  - Concept learning: filtration & representation mapping
- **Benchmarks** to test:
  - Multi-attribute recognition
  - Continual learning
  - Novel composition reasoning

# Proposed Methodology: Dataset

*Human Inspired Progressive Alignment and Comparative Learning for Grounded Word Acquisition. Bao et al. 2023*

## Low noise and distinct attributes

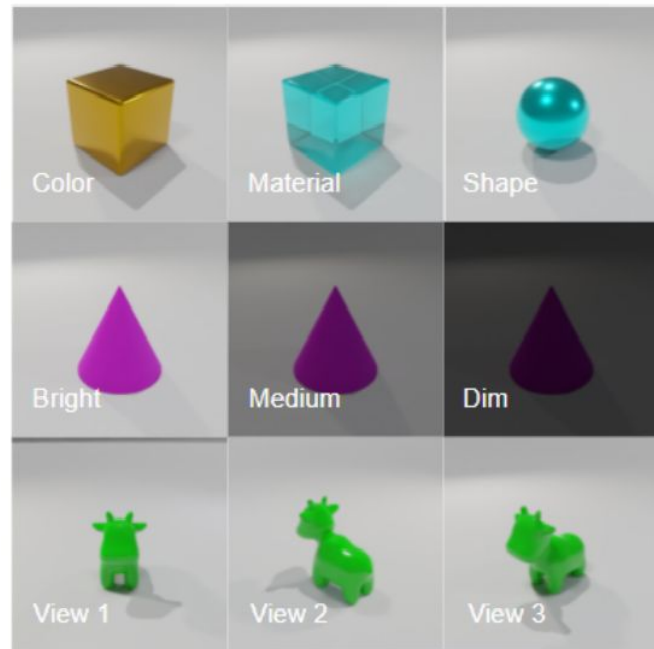
Facilitates efficient sample comparisons and mapping of language features to grounded concepts.

Combination of 8 colors, 11 shapes, and 4 materials

Variations in 3 light settings and 6 camera angles.

**6336** RGBA images of synthetic objects.

Total of **23 concepts**



SOLA dataset renders. Bao et al. 2023

# Proposed Methodology: Dataset

[Human Inspired Progressive Alignment and Comparative Learning for Grounded Word Acquisition. Bao et al. 2023](#)

## Variation Test set (Dtest\_v) → # 989

(To assess model generalizability and robustness)

- stretching along the x, y, and z axes
- shade changes
- size alterations to medium or small dimensions

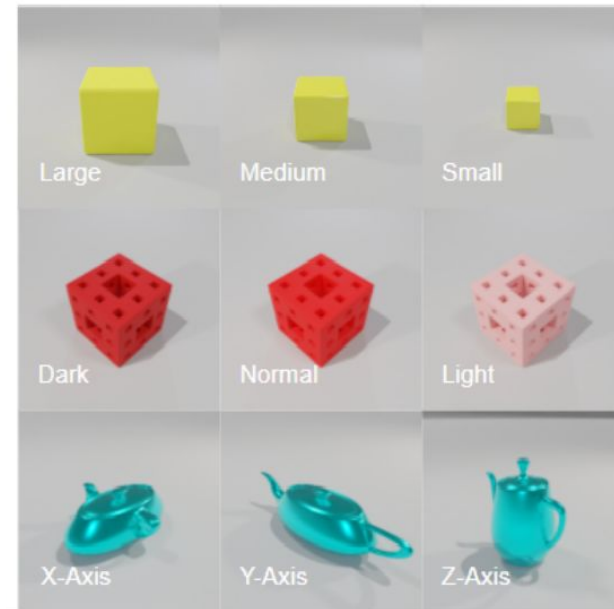
## A Novel Composition Test set (Dtest\_nc) → # 1242

(To evaluate the novel composition capability of the methods)

- 9 exclusive learning attribute pairs

## Train set (Dtrain) → # 5094

- Remaining pairs



SOLA dataset renders. Bao et al. 2023

(For complex concept acquisition)

**Dtrain\_complex** → 5760

- Merging the Dtrain and Dtest\_nc datasets

**Dtest\_no** → 576

- We subtract a set of 32 objects from Dtrain\_complex to create a test dataset of objects unseen during training

(new runs are: Dtrain\_complex: 5076 and Dtest\_no: 1260)

Split	Num Objects
$D_{train}$	5094
$D_{train\_complex}$	5760
$D_{test\_nc}$	1242
$D_{test\_no}$	576
$D_{test\_v}$	989



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- **Introduction**
  - Research Questions
  - Background Theories
  - Related Work
- **Proposed Methodology**
  - Dataset
  - Comparative Learning
    - Baseline
    - Hypernet
    - Modular Shared Skills (Polytropon)
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# Proposed Methodology: Comparative Learning

- For each learned concept  $l_i$  in an unconstrained set  $L = \{l_1, l_2, \dots\}$ , must be assembled a batch of samples  $\mathcal{B}_s = \{a_1^{l_i}, \dots, a_n^{l_i}\}$ , that share the label  $l_i$  for similarity learning, and a batch of samples  $\mathcal{B}_d = \{b_1^{l_j}, \dots, b_n^{l_j}\}, j \neq i$  that cannot be described by  $l_i$  for difference learning.
- The process of  $\text{SIM}_{l_i}$  (1) finds the similarities among the examples in  $\mathcal{B}_s$ , and extract out the representation  $\text{REP}_{l_i}$  expected to refer to  $l_i$ .
- The process of  $\text{DIFF}_{l_i}$  (2) highlights the differences between  $l_i$  and other non-compatible labels refining the representation  $\text{REP}_{l_i}$ .

$$\text{REP}_{l_i} = \text{SIM}_{l_i}(\{a^{l_i} \in \mathcal{B}_s\}) \quad (1)$$

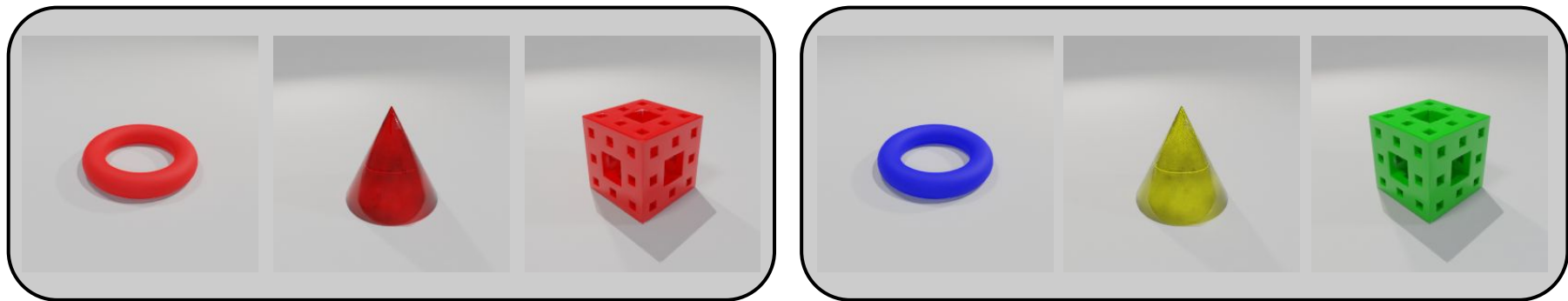
$$\text{REP}_{l_i} = \text{DIFF}_{l_i}(a^{l_i}, \{b^{l_j} \in \mathcal{B}_d\}) \quad (2)$$

# Proposed Methodology: Baseline

For each concept (e.g., "red"):

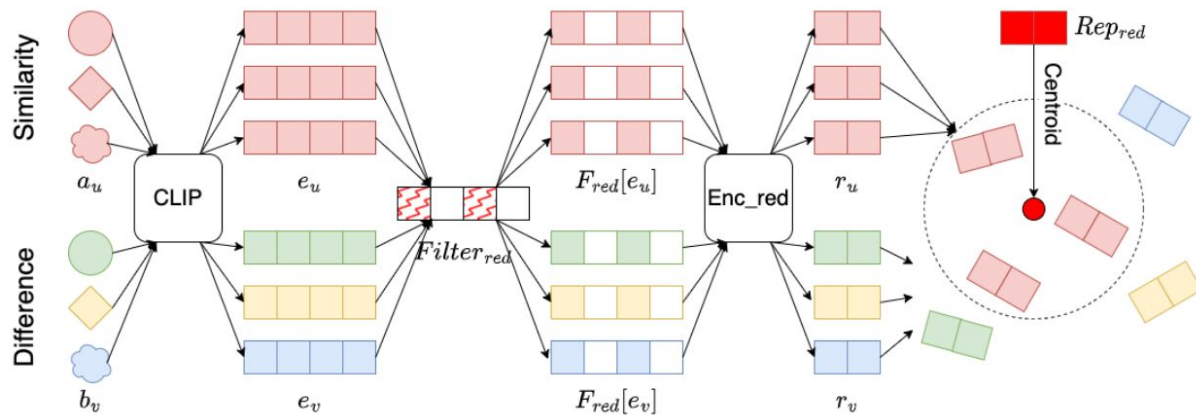
- **Similarity training:** They gather a batch of images of the specified concept ("red").
- **Difference refinement:** Another batch consists of images that are of any other color but still "red" (non-compatible).

They ensure that the rest of the attributes remain consistent across batches for better structural alignment.





# Proposed Methodology: Baseline



(a) Filter, Encoder, Representation Learning

## Algorithm 1: Comparative Learning-Word $l_i$

```

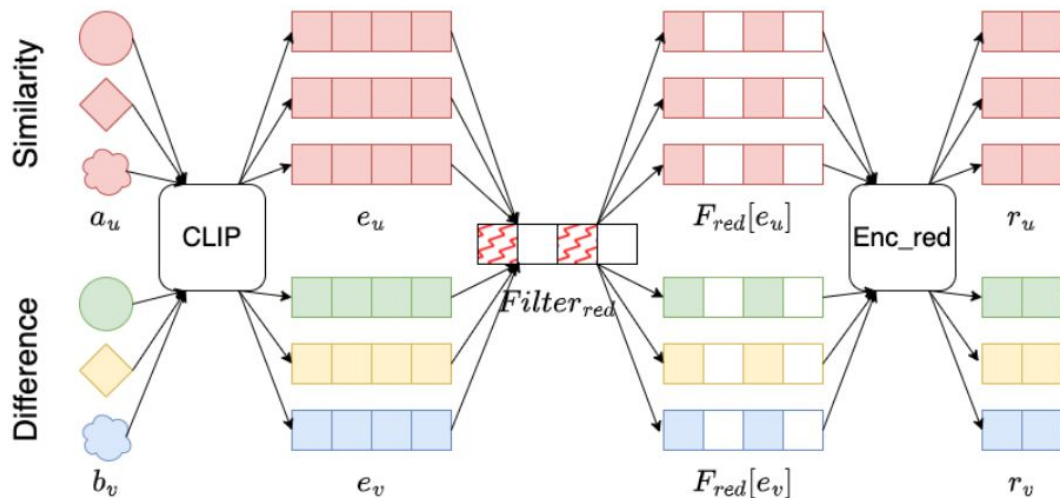
1 for Sim and Diff data batches:  $\{\mathcal{B}_s, \mathcal{B}_d\}$  do
2   // Similarity Learning
3   for  $a_u \in \mathcal{B}_s$  do
4      $e_u = \text{CLIP\_emb}[a_u]$ 
5      $r_u = \text{Enc}_{l_i}[\text{F}_{l_i}(e_u)]$ 
6    $\text{Rep}_{l_i} = \text{Centroid}[\{r_u\}_{u \in \{1, \dots, n\}}]$ 
7   // Difference Learning
8   for  $b_v \in \mathcal{B}_d$  do
9      $e_v = \text{CLIP\_emb}[b_v]$ 
10     $r_v = \text{Enc}_{l_i}[\text{F}_{l_i}(e_v)]$ 
11  // Loss
12   $\text{loss}_s = \sum_u \text{Dist}[r_u, \text{Rep}_{l_i}]$ 
13   $\text{loss}_d = \sum_v \text{Dist}[r_v, \text{Rep}_{l_i}]$ 
14   $\text{loss} = (\text{loss}_s)^2 + (1 - \text{loss}_d)^2$ 
15  Backpropagate and Optimize
Output:  $\{l_i: [\text{F}_{l_i}, \text{Enc}_{l_i}, \text{Rep}_{l_i}]\}$ 
  
```

# Proposed Methodology: Baseline

Initially, a **pre-trained frozen CLIP image embedding** is utilized.

Image embeddings undergo two processes:

- **Information denoising:** Each image embedding is subjected to an elementwise product with a filter.
- **Attention establishment:** The masked embedding passes through two fully connected layers of an encoder to output a condensed representation.



(a) Filter, Encoder, Representation Learning

# Proposed Methodology: Baseline

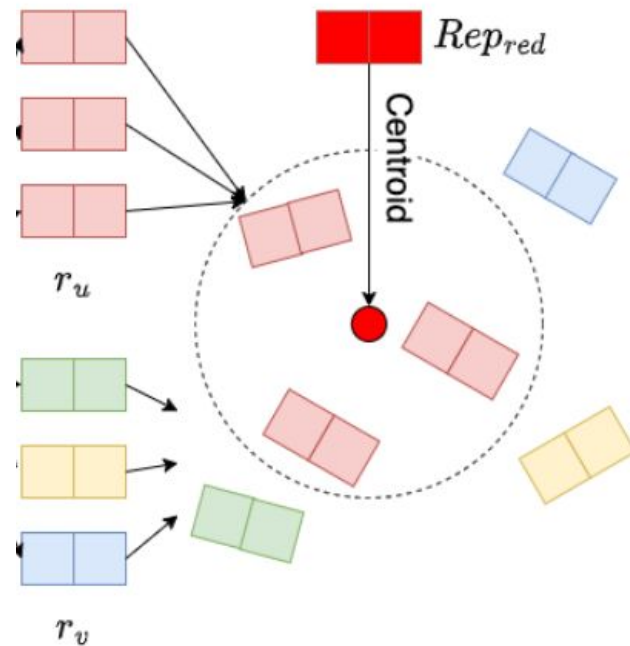
A **centroid** is computed for the representations of the similarity batch.

The loss function serves two purposes:

- It **drives the similarity** batch sample representations closer to the centroid.
- It **pushes the difference** batch sample representations further away from the centroid.

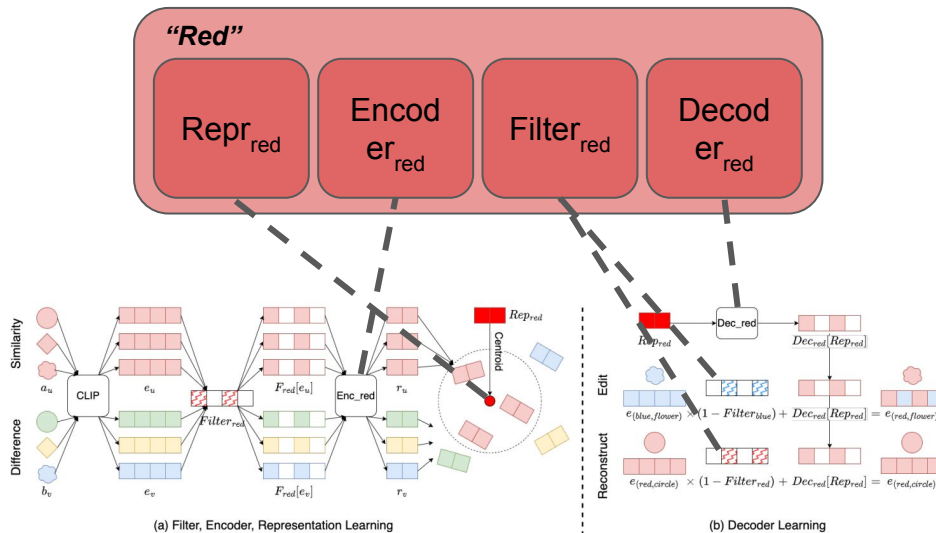
```

11  // Loss
12   $\text{loss}_s = \sum_u \text{Dist}[r_u, \text{Rep}_{l_i}]$ 
13   $\text{loss}_d = \sum_v \text{Dist}[r_v, \text{Rep}_{l_i}]$ 
14   $\text{loss} = (\text{loss}_s)^2 + (1 - \text{loss}_d)^2$ 
  
```



# Proposed Methodology: Baseline

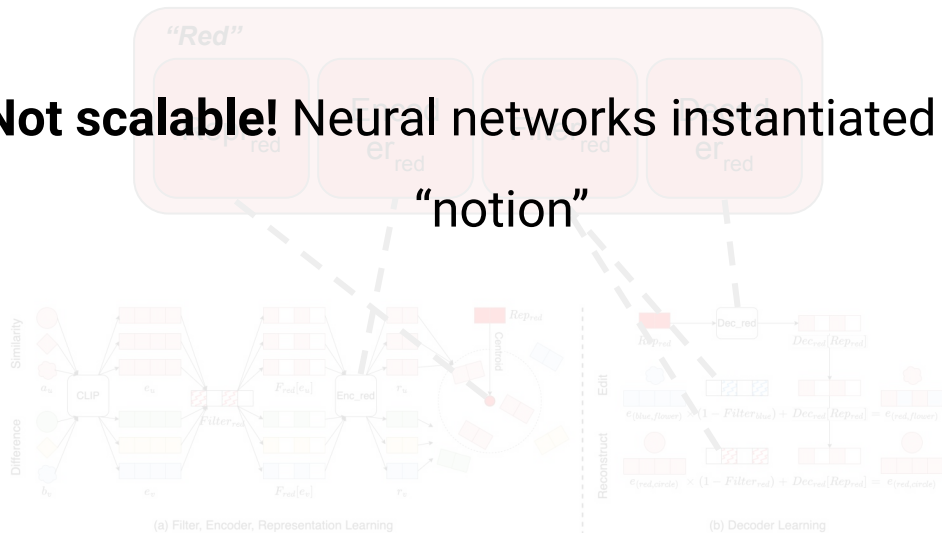
- This approach jointly trains the **filter**, the **encoder**, and the **representation**, producing a different set of these three objects **for each of the learned concepts**.



# Proposed Methodology: Baseline

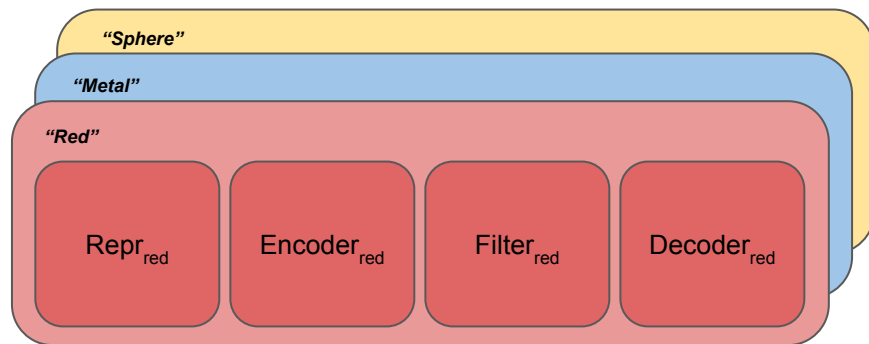
- This approach jointly trains the **filter**, the **encoder**, and the **representation**, producing a different set of these three objects **for each of the learned concepts**.

**Not scalable!** Neural networks instantiated per  
“notion”



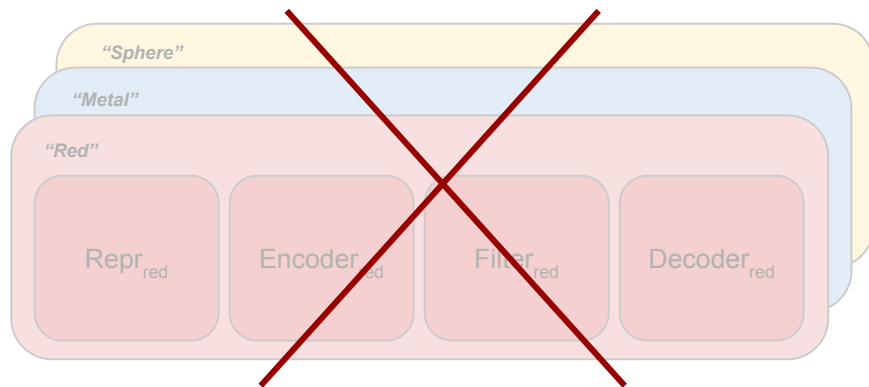
## Proposed Methodology: Baseline

- Our first goal is **to unify** the learning of multiple concepts **under the same single architecture** while keeping the same training process.



## Proposed Methodology: Baseline

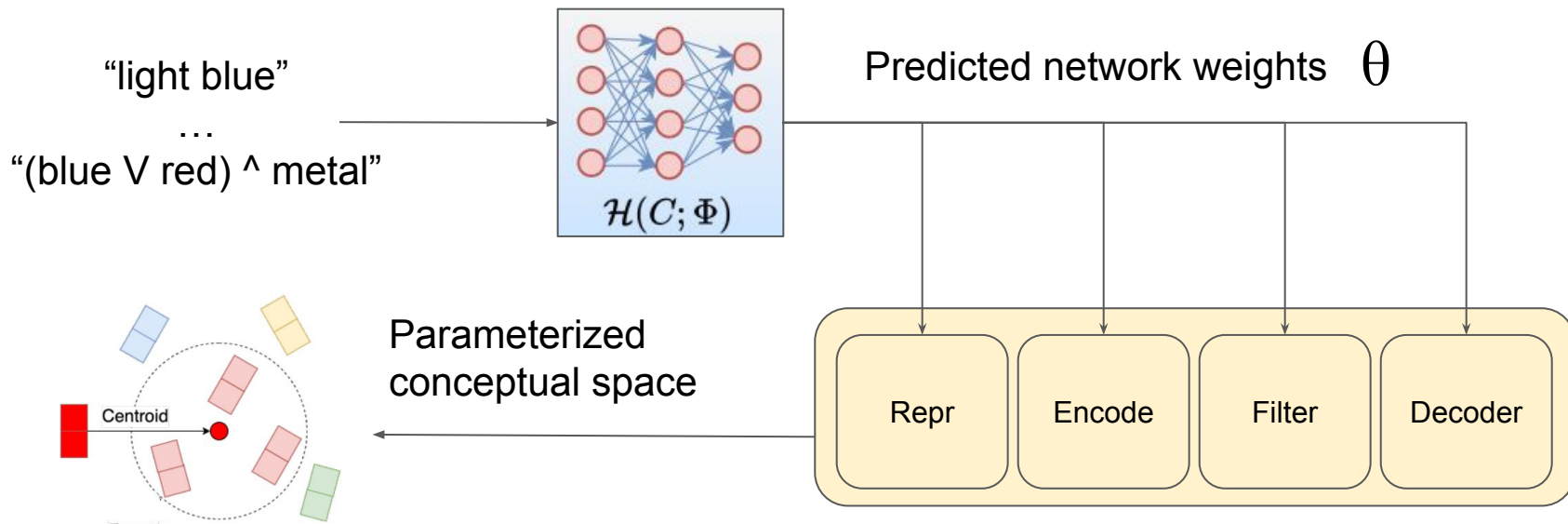
- Our first goal is **to unify** the learning of multiple concepts **under the same single architecture** while keeping the same training process.



# Proposed Methodology: Hypernetworks (HyperMem)

Parameter-efficient Multi-task Fine-tuning for Transformers via Shared Hypernetworks. Mahabadi et al. 2021

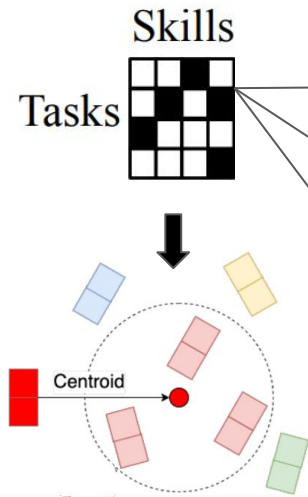
- Our first goal is **to unify** the learning of multiple concepts **under the same single architecture** while keeping the same training process.



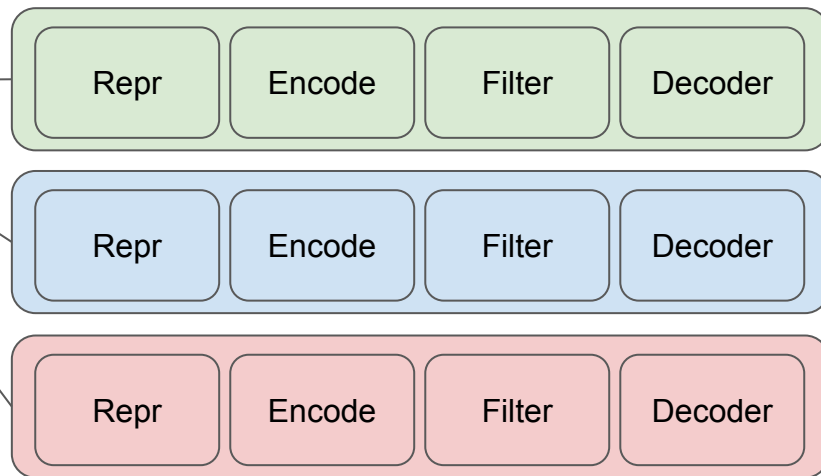


- Our first goal is **to unify** the learning of multiple concepts **under the same single architecture** while keeping the same training process.

## *Learned skills allocation*



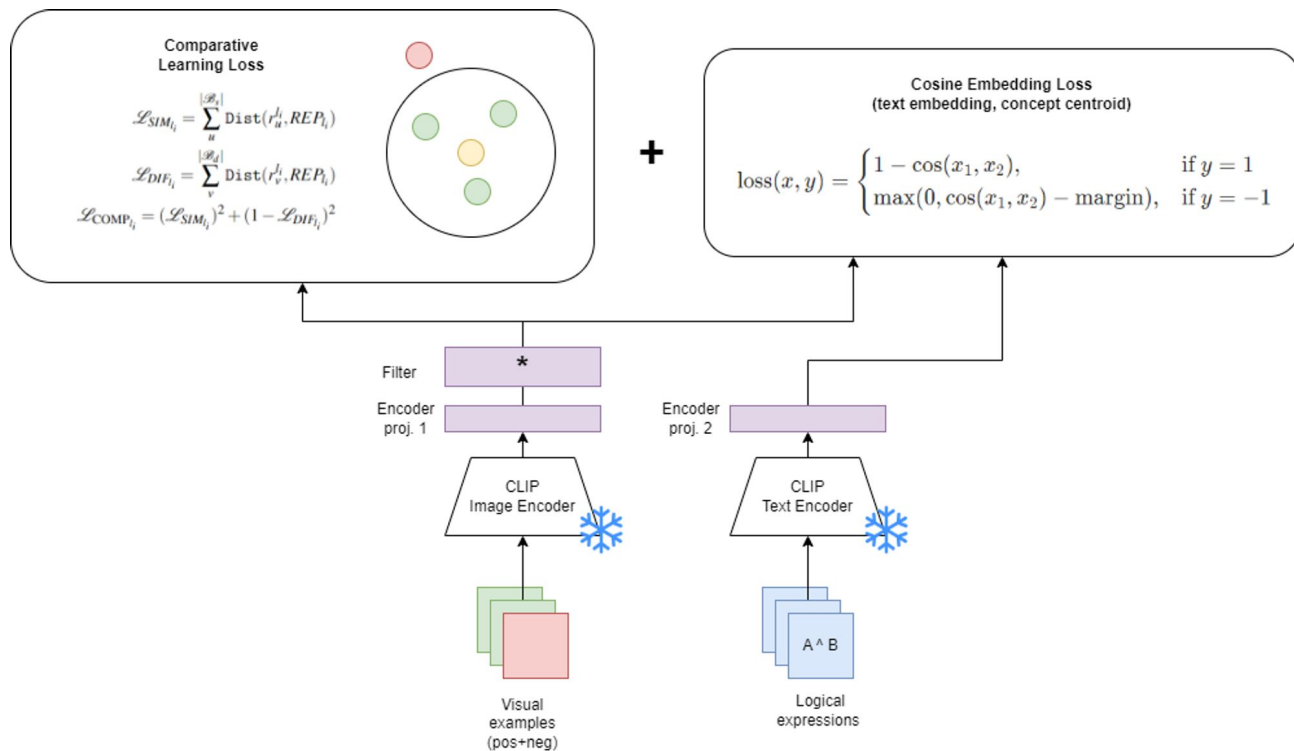
## *Redundant networks (skills)*



“light blue”  
...  
“(blue V red)  
^ metal”

# Proposed Methodology: Modular Shared Skills (Polytropon)

Combining Modular Skills in Multitask Learning. Ponti et al. 2023





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    - Baseline
    - Hypernet
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It is possible to teach more complex concepts through the same training process?

We compose simple concepts into logical expressions with basic logic operators: **NOT**, **AND**, and **OR**.

Given an unconstrained set of base concepts (e.g., “red” and “cone”), we considered all possible logical pairs obtaining the set of complex concepts:

- “NOT red”,
- “NOT cone”,
- “red AND cone”,
- “red OR cone”.

Total of **351 new concepts**

- **Similarity batch** of images with positive samples where the logical relation between the two simple concepts is respected.
- **Difference batch** with negative samples was generated where the relation is violated.

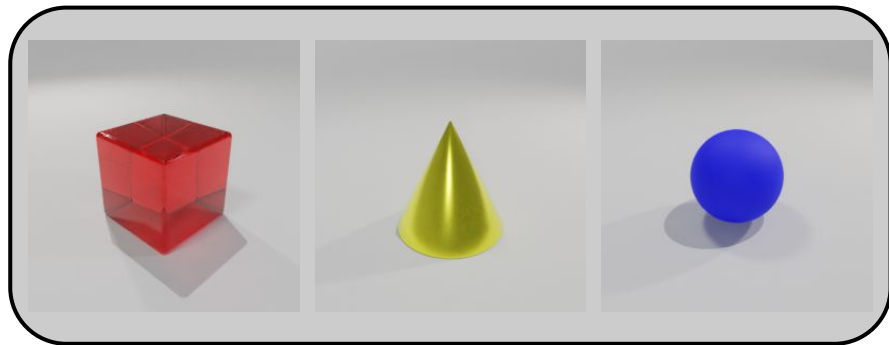
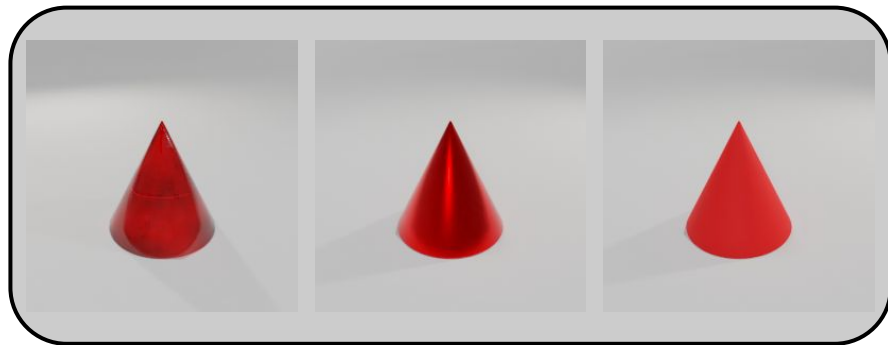
The samples were paired so that, except for the attributes significant for the truth value of the relation, all other features were kept constant.

## Proposed Methodology: Compound Logical Concepts

**AND**

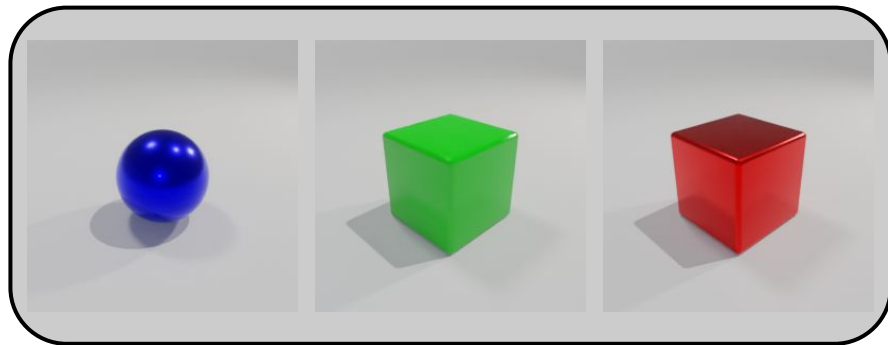
$$\mathcal{B}_s = \{a \mid \text{red AND cone}\} \quad (9)$$

$$\mathcal{B}_d = \{a \mid \text{red AND NOT cone} \oplus \text{NOT red AND cone} \oplus \text{NOT red AND NOT cone}\}$$



OR

$$\mathcal{B}_s = \{a \mid \text{metallic AND NOT cube} \oplus \text{NOT metallic AND cube} \oplus \text{metallic AND cube}\} \quad (10)$$
$$\mathcal{B}_d = \{a \mid \text{NOT metallic AND NOT cube}\}$$





# Table of Contents

- **Introduction**
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  - Dataset
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    - Baseline
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To test the **acquisition of primitives**, we employ the same cognitive task introduced by Bao et al.: Multi-Attribute Recognition (MAR).

We thus compare:

- the memory-of-networks model (**Baseline**)
- our multi-task hyper-network (**HyperMem**)
- shared modular skills (**Polytropon**)

For **complex logical expressions**, we modify MAR and thus define Logical Pattern Recognition (LPR).

## Evaluation: Multi-Attribute Recognition

- Go through the memory
- Apply the corresponding filter and encoder of each concept
- Retrieve the **top-3 concepts** with the least MSE between *Enc\_word* and *Learned\_rep*

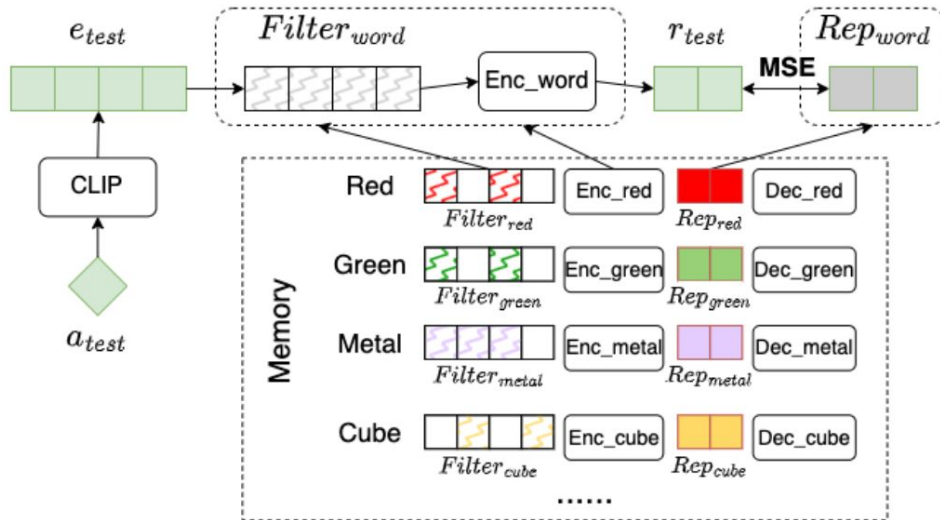


Figure 3: Multi-Attribute Recognition Inference

# Evaluation: Multi-Attribute Recognition

## Observations:

- Polytropon is comparable to HyperMem, with 10x less parameters
- Distinguishing materials remains the hardest task
- The “baseline” (upper bound) follows a similar pattern

Split	Model	Color	Material	Shape
$D_{test\_v}$	Baseline	0.95	0.75	0.89
	HyperMem	0.56	0.26	0.66
	HyperMem (DER++)	0.74	0.37	0.70
$D_{test\_nc}$	Baseline	0.96	0.48	0.98
	HyperMem	0.37	0.25	0.73
	HyperMem (DER++)	0.71	0.28	0.89
	Polytropon	0.73	0.21	0.67

*Multi-Attribute Recognition. Accuracy scores on test variation and novel composition sets.  
Calanzone and Merlo 2024*

## Evaluation: Logical Pattern Recognition

- AND, OR, and NOT relations of the three attributes constituting the image, amount to a total of **66 true relations per image**.
- Within the **top-66 concepts** retrieved, we count as hit only the ones that are true for the evaluated image.

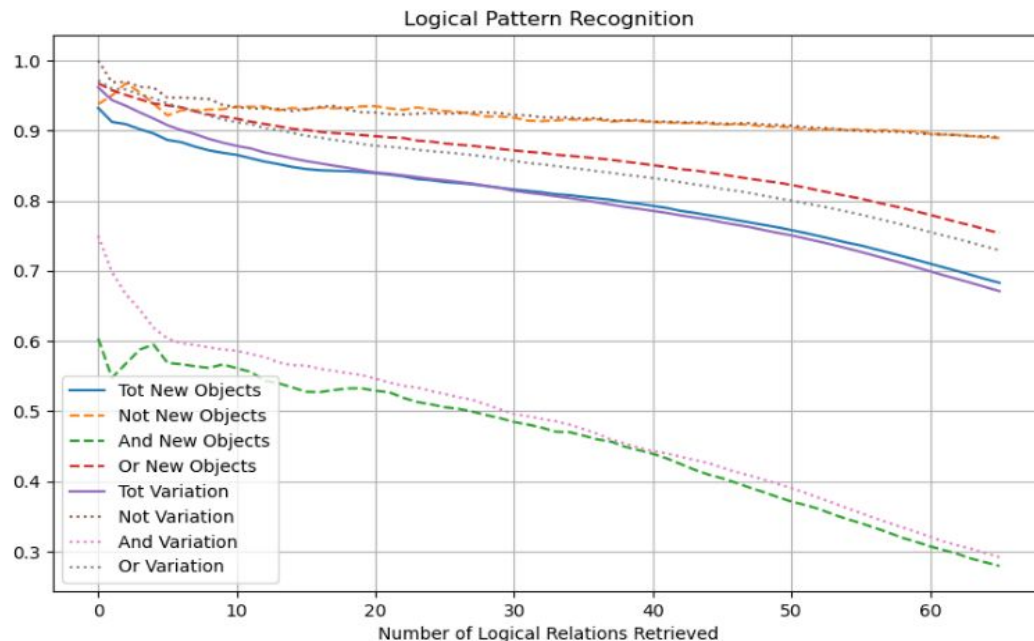
### Purple Plastic Torus



1. Aqua or Torus,
2. Red or Torus,
3. Purple or Glass,
4. Brown or Torus,
5. Purple and Plastic,
6. Plastic and Torus,
7. **Not Plastic,**
8. Purple or Gear,
9. Purple or Rubber,
10. Purple and Torus

# Evaluation: Logical Pattern Recognition

- LPR in multiple iterations, **systematically altering the top-k parameter** for concept retrieval, ranging from 1 to 66
- AND relations presents a worse performance



# Evaluation: Logical Pattern Recognition

## Observations:

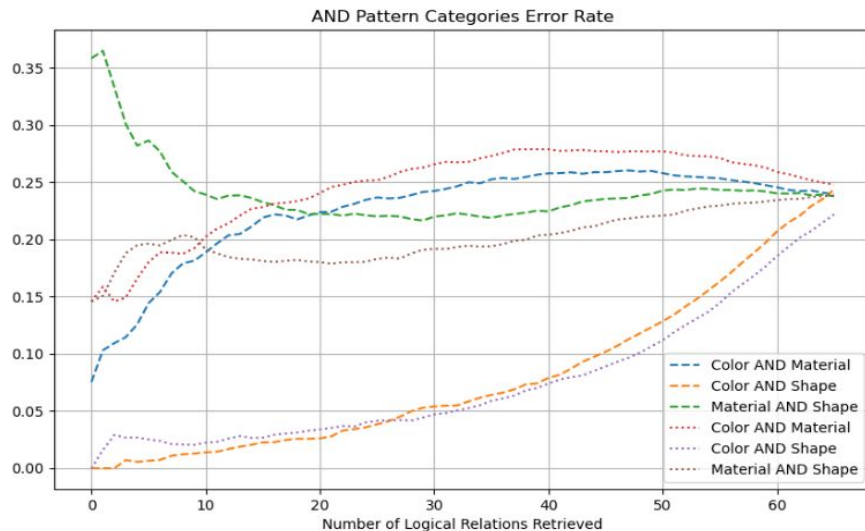
- We only test the baseline model.
- Logical conjunction (AND) is a stricter operator, learned with more difficulty
- Early experiments with HyperMem and Polytropon haven't converged or shown comparable results

Top-k Num	Split	Tot	NOT	AND	OR
10	$D_{test\_no}$	0.8682	0.9305	0.5667	0.9201
	$D_{test\_y}$	0.8827	0.9364	0.5878	0.9158
20	$D_{test\_no}$	0.8411	0.9344	0.5326	0.8935
	$D_{test\_y}$	0.8435	0.9261	0.5516	0.8809
30	$D_{test\_no}$	0.8185	0.9201	0.4900	0.8738
	$D_{test\_y}$	0.8179	0.9248	0.5025	0.8599
40	$D_{test\_no}$	0.7957	0.9137	0.4444	0.8533
	$D_{test\_y}$	0.7884	0.9150	0.4478	0.8348
50	$D_{test\_no}$	0.7621	0.9057	0.3776	0.8259
	$D_{test\_y}$	0.7543	0.9081	0.3965	0.8035
60	$D_{test\_no}$	0.7157	0.8990	0.3136	0.7847
	$D_{test\_y}$	0.7052	0.8960	0.3276	0.7605
66	$D_{test\_no}$	0.6830	0.8893	0.2794	0.7538
	$D_{test\_y}$	0.6712	0.8906	0.2919	0.7294

Top-K accuracy in Logical Pattern Recognition.  
Calanzone and Merlo 2024

# Evaluation: Logical Pattern Recognition

- We analyzed the error rate contributions of the three distinct categories of **AND patterns**: Color AND Material, Color AND Shape, and Material AND Shape.
- The error contribution from **Color AND Shape** remained negligible in the initial trials but exhibited an upward trend as the number of representations retrieved increased.





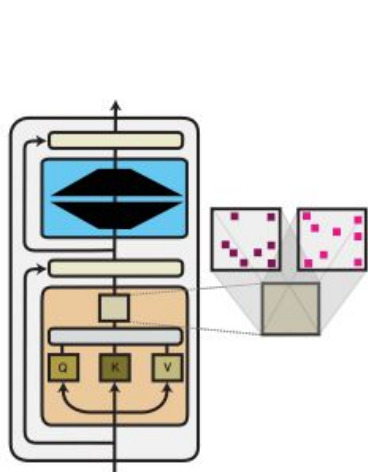
# Table of Contents

- **Introduction**
  - Research Questions
  - Background Theories
  - Related Work
- **Proposed Methodology**
  - Dataset
  - Comparative Learning
    - Baseline
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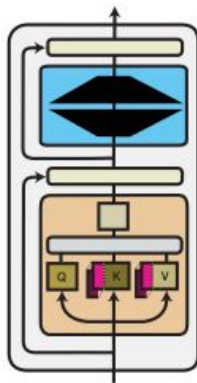


## Where to go from here?

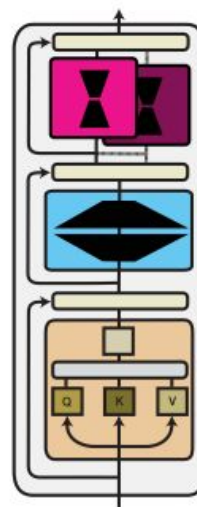
- [Modular Deep Learning \(Ponti et al. 2023\)](#) suggests sound and efficient multi-task learning architectures.



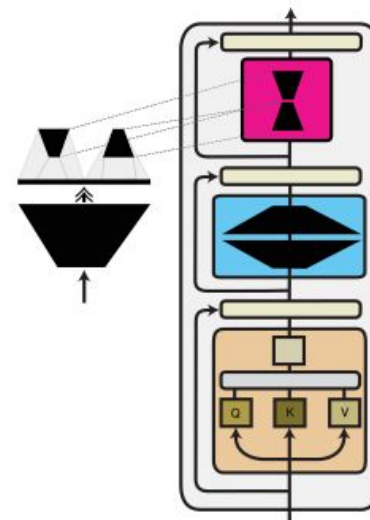
(a) Parameter Composition



(b) Input Composition



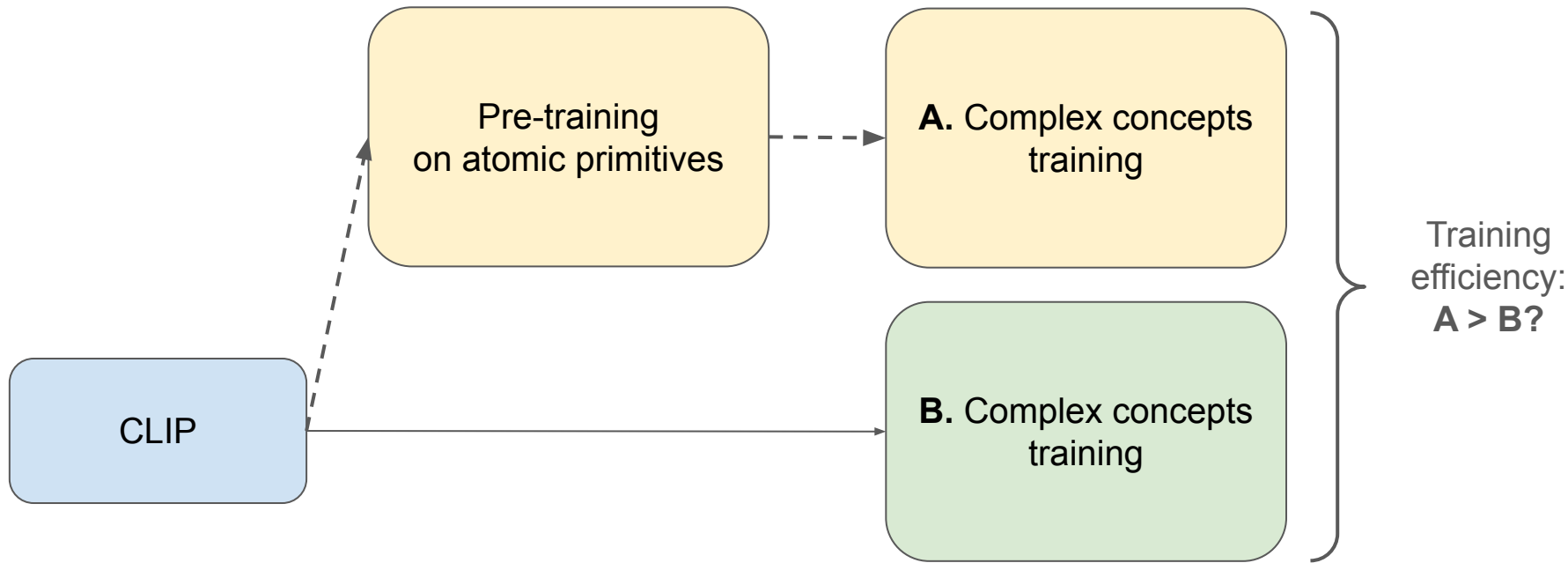
(c) Function Composition



(d) Hypernetwork

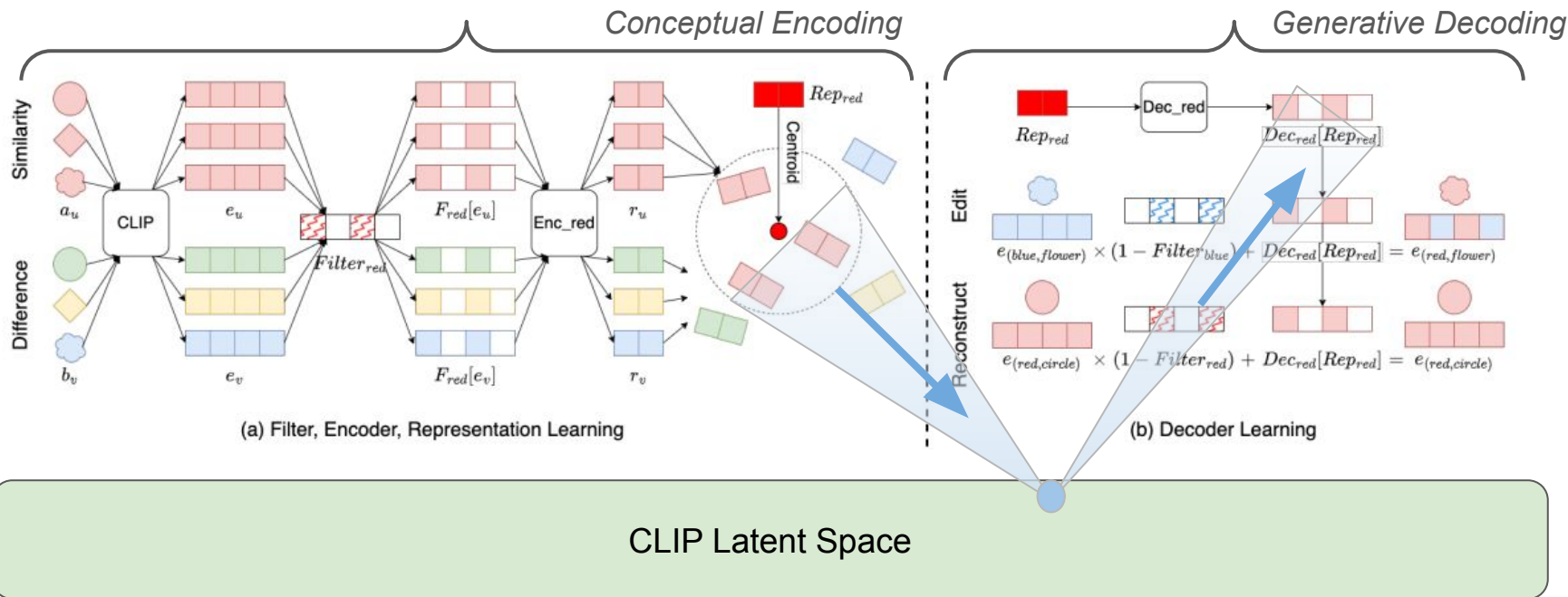
## Where to go from here?

- How to test the effects of progressive alignment?



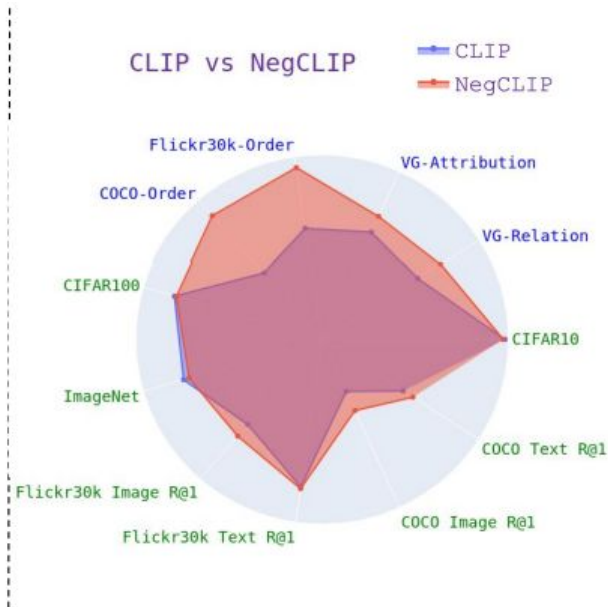
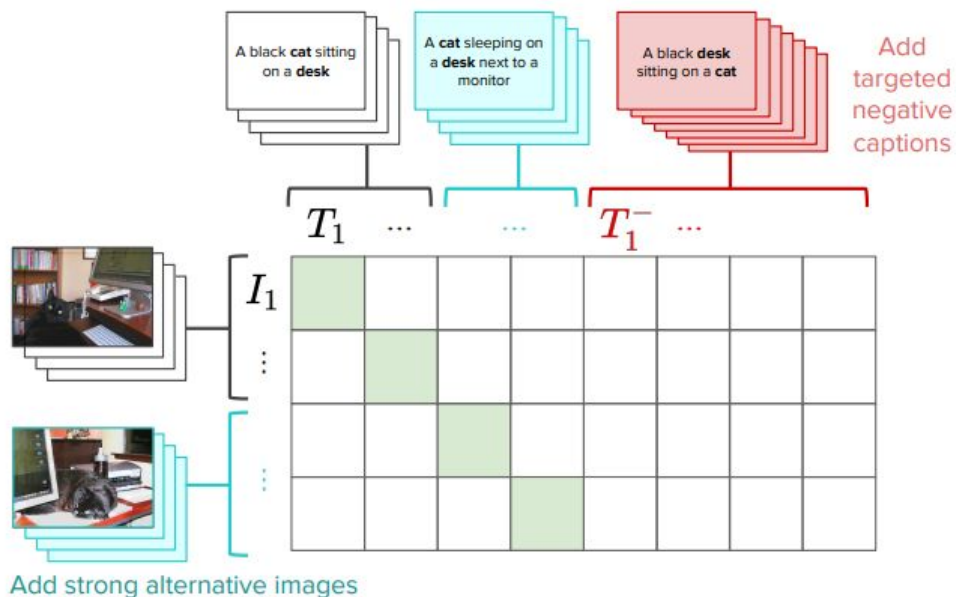
# Where to go from here?

- (1/2) Should we work directly in VLMs' conceptual spaces?



# Where to go from here?

- (2/2) Should we work directly in VLMs' conceptual spaces? eg. [NegCLIP](#)





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Thank you for your  $\text{Attention}(Q, K, V) = \text{softmax}(\frac{QK^T}{\sqrt{d_k}})V$  !

Comments?

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