Milestone 2: AGN Galaxy Simulation

Annabella Yang

The code for the project is attached to this pdf (week 2 starts from page 17 and ends at page 48) and updated to GitHub https://github.com/AnnabellaYang/PHYS129 FinalProject 2.

For this week's project, I continued developing my previously defined class, "Galaxy."

Last time, I initialized the galaxy and created a black hole accretion model. This week, I expanded the code to two other important models to consider — the cooling and heating processes and the spectra modeling. I continued using Monte Carlo simulation to examine the relationship between parameters. I examined the impact of specific parameters on a function by plotting the same function with the adjusted value of that parameter on the same plot. I also used optimization to model the spectrum I randomly generated. This is a super helpful tool that can be used in real practice in observational astrophysics.

As mentioned above, I developed the cooling and heating model and spectra model. For the cooling and heating model, I first found the cooling/heating rate of the galaxy as a function of time and density. Then, I explored the impact of density on the cooling/heating rate and the overall temperature. This helps me study some of the environmental impacts on the galaxy. Also, from the literature, the density is closely related to the radius (Panda 2022). Thus, I expressed the density as a function of radius. When it is towards the center of a galaxy, the density can be as high as 10^9 particles per cubic centimeter, As it gets further away from the central black hole, the density becomes approximately 10^6 to 10^2. For the spectra model, I created a power-law continuum and created the emission features for some high-intensity chemical components from the AGN host galaxy. I added noise to make it similar to the actual spectrum astrophysicists usually observe. I randomized the intensity of the emission lines, with oxygen, hydrogen, and

nitrogen having higher intensity since they are typically stronger than the other emission lines from AGN host galaxies. I wrote this as a function that takes a single input of redshift and randomly generates a spectrum. Then, I wrote the code to find the best fit for the randomly generated spectra. The code estimates the redshift and the intensity of emission lines very well for galaxies under redshift 1. Beyond certain redshifts, the optimization no longer works since the spectrum has shifted too much.

I have faced some problems because of the uncertainty in many things, such as density. Density, as shown in my corner plot and time evolution plots, is a significant parameter in cooling rate and temperature, but many factors could influence it. The radius is just one of the factors, and other things, such as chemical composition and energy, are so hard to trace. Therefore, I stuck with the simpler model and moved on to the spectra modeling. Since spectra modeling can tell us so many things about the AGN galaxy (for detailed information, see page 30 of the code), I think I can always come back and fix the functions after analyzing the spectrum.

For next week, there are two things I am planning on doing: the first one is to continue expanding my galaxy class. I still need to explore the gas dynamics and the interactions between galaxies or gravitational interactions. Creating models for those also helps me understand AGN host galaxies better. Also, as discussed earlier, since the spectra modeling is so crucial and helpful, I may stick with it, develop it by adding some non-obvious emission/absorption features, examine the chemical elemental abundance, and see if I can extract more information from it other than the redshift and chemical emission line intensities.

Reference:

Panda, S. (2022, February 16). *Parameterizing the AGN radius–luminosity relation from the eigenvector 1 viewpoint*. Frontiers.

https://www.frontiersin.org/articles/10.3389/fspas.2022.850409/full

Physics 129L Final Project: Investigating the Outflow Dynamics of Active Galactic Nuclei through Computational Simulations

AGN Galaxy Simulation

My goal of this project is to study the outflow dynamics of Active Galactic Nucleis (AGNs) since it is crucial for comprehending their roles in galaxy formation and evolution and aims to simulate the outflow properties of AGNs using computational techniques to understand their process and implications for galaxy evolution.

However, before starting analyzing the properties of AGN, we need some sample of AGN host galaxies to start with, and this is one of the most complex process since there are too many things to be considered. We start by considering some most important factors of AGN host galaxies in the simulation:

- 1. **Modeling the Black Holes**: Simulating the behavior of supermassive black holes at the centers of these galaxies, including their mass, spin, and accretion rates.
- 2. **Modeling the Gas Dynamics**: Modeling the accretion of gas onto the black hole and the resulting jets and winds.
- 3. **Consider the Galactic Interactions**: Considering the gravitational interactions between galaxies, especially in dense environments like galaxy clusters.
- 4. **Consider the Feedback Processes**: Including the effects of the AGN on its host galaxy, like outflows that can heat up or expel gas, affecting star formation.
- 5. Consider the Fact that it is a Part of Our Universe (Cosmological Context):

 Placing these galaxies within the larger structure of the universe, considering the expansion of the universe, dark matter distribution, and the cosmic web.
- 6. **Include the Radiation Processes**: Simulating the radiation emitted by the AGN, which includes a wide spectrum from radio to gamma rays.

I think the best way to simulate such galaxies is to create a galaxy class and define these above properties seperately. So the first step is to initiate a class called galaxy with basic parameters.

```
In [44]: # First, import useful packages (subject to change, will be adding all the p
import numpy as np
import scipy as sp
import random
import matplotlib.pyplot as plt
import corner
import seaborn as sns
from scipy.stats import norm
from scipy.optimize import minimize
from astropy import units as u
```

```
In [9]: # Second, define some constant
# (unit included by using the astropy package units)
'''Gravitational constant'''
G = 6.67430e-11 * u.m**3 / u.kg / u.s**2
'''speed of light'''
c = 299792458 * u.m / u.s
'''number of galaxies to be simulated'''
num_galaxies = 1000
'''time steps'''
time_steps = 100
```

```
In [10]: # Now we can start by defining a class of galaxy, and think about the struct
         class Galaxy:
             # initialize the galaxy
             def init (self, mass, position, velocity, black hole mass):
                 self.mass = mass
                  self.position = position
                 self.velocity = velocity
                  self.black_hole_mass = black_hole_mass
             # black hole accretion model
             def accretion model(black hole mass):
                 This will be an impliment or accresion model for black hole accretic
                 This should return accretion_rate, radiation, jets
                 pass
             # Gas Dynamics and Interstellar Medium
             def gas dynamics(galaxy):
                  1.1.1
                 This models the impliment model of the dynamics of gas in and around
                 The processes like cooling, heating, and interaction with AGN radiat
                 pass
             # Galaxy Interaction and Dynamics
             def update_galaxy_dynamics(galaxies):
                  Implement gravitational interactions between galaxies.
                 Update positions and velocities based on gravitational forces.
                  I = I \cup I
                 pass
```

A) Accretion Model

The accretion model also contains many parts:

- 1. accretion rate
- 2. radiation
- 3. jet production

I will do these step by step by using and analyzing the equations that describe each model

1. Accretion Rate

The accretion rate of a black hole often depends on the mass of the black hole, the density of the surrounding medium, and the velocity at which this medium is moving relative to the black hole.

I here use the Bondi-Hoyle-Lyttleton accretion rate model: (https://en.wikipedia.org/wiki/Bondi_accretion)

$$\dot{M}=\pi\left(rac{2G^2M^2
ho_\infty}{(v_\infty^2+c_s^2)^{3/2}}
ight)$$

$$\dot{M}$$
: Accretion rate (1)
 G : Gravitational constant (2)
 M : Mass of the accreting object (3)
 ρ_{∞} : Density of the ambient medium (far from the accreting object) (4)
 v_{∞} : Relative velocity between the object and the ambient medium (5)

 c_s : Sound speed of the ambient medium (6)

Since I am working with AGN host galaxies, some of the parameters including ρ_{∞} , v_{∞} , and c_s are constrained. However, they are also kind of randomized within the range.

I was thinking if I should use a constant or use a randomization function. However, since the blackhole mass are already an input, I will keep these three fixed first. Later on, I can also test how these values impact the output accretion rate solar masses per year. I made the default values $\rho_{\infty}=10^{-13}kg/m^3$, $v_{\infty}=5\times10^7m/s$, and $c_s=5\times10^5m/s$ just to start with.

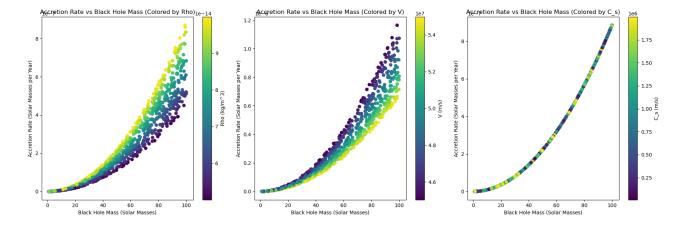
In [11]: # based on this, we can define a accretion rate function called calculate ac # returns the accretion rate solar masses per year def calculate accretion rate(black hole mass, rho = np.random.uniform(1e-14, 1e-13), v = np.random.uniform(4.5e7, 5.5e7),c s = np.random.uniform(1e4, 2e6)): 1 1 1 The input black hole mass should in the unit of solar mass $\rho = 10^{-13} \, \text{kg/m}^3$, $\rho = 5 \, \text{times} \, 10^7 \, \text{m/s}$, and $\rho = 10^7 \, \text{m/s}$ G = 6.67430e-11 * u.m**3 / u.kg / u.s**2 # gravitational constant with uM = black hole_mass * 1.98847e30 * u.kg # solar masses to kg rho = rho * u.kg / u.m**3 # density of the accreting material in kg/m^3 v = v * u.m / u.s # relative velocity in m/s $c \ s = c \ s * u.m / u.s # sound speed in the material in m/s$ # Bondi-Hoyle-Lyttleton accretion rate accretion rate = (4 * np.pi * G**2 * M**2 * rho) / ((v**2 + c s**2)**(3/s))# Convert accretion rate to solar masses per year accretion rate solar masses per year = accretion rate.to(u.kg / u.s) / (return accretion rate solar masses per year

```
In [12]: # Test the function calculate_accretion_rate
    print(calculate_accretion_rate(100))
```

4.6014328680559665e-15 yr / s

To test if this function works well, and if rho, c, c_s contributes a lot to the function (if these parameters impacts it significantly, then we want to reconsider the definition of the function)

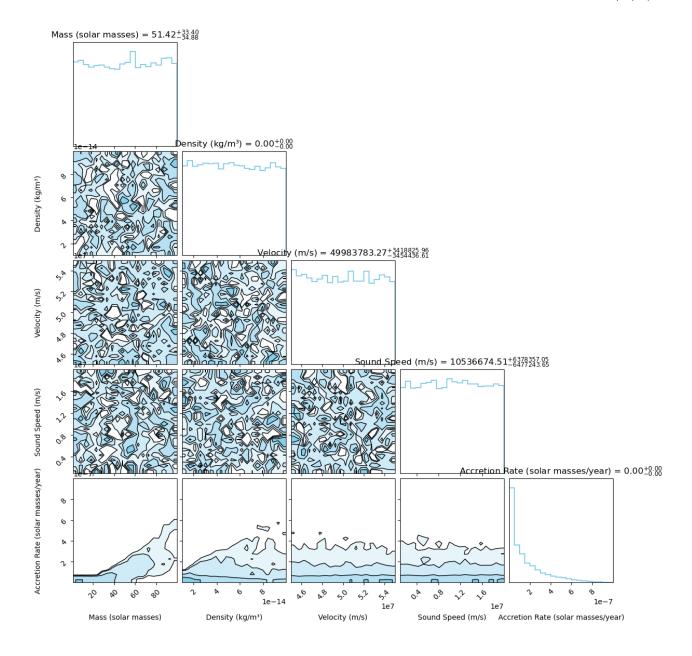
```
In [13]: '''Plot Accretion Rate in term of Black Hole Masses with varies Parameters'
         # Randomize one parameter at a time, keeping the others fixed
         num points = 1000
         fixed rho = 1e-13 # Fixed density
         fixed_v = 5e7  # Fixed relative velocity
         fixed c s = 1e5 # Fixed sound speed
         # Randomize black hole masses
         black hole masses = np.random.uniform(1, 100, num points)
         # Randomizing rho while keeping v and c s fixed
         rho values = np.random.uniform(5e-14, 1e-13, num points)
         accretion rates rho = [calculate accretion rate(mass, rho=rho, v=fixed v, c
         # Randomizing v while keeping rho and c s fixed
         v values = np.random.uniform(4.5e7, 5.5e7, num points)
         accretion rates v = [calculate accretion rate(mass, rho=fixed rho, v=v, c s=
         # Randomizing c s while keeping rho and v fixed
         c s values = np.random.uniform(1e4, 2e6, num points)
         accretion rates c s = [calculate accretion rate(mass, rho=fixed rho, v=fixed
         plt.figure(figsize=(18, 6))
         # Scatter plot for rho
         plt.subplot(131)
         plt.scatter(black hole masses, accretion rates rho, c=rho values, cmap='viri
         plt.colorbar(label='Rho (kg/m^3)')
         plt.xlabel('Black Hole Mass (Solar Masses)')
         plt.ylabel('Accretion Rate (Solar Masses per Year)')
         plt.title('Accretion Rate vs Black Hole Mass (Colored by Rho)')
         # Scatter plot for v
         plt.subplot(132)
         plt.scatter(black hole masses, accretion rates v, c=v values, cmap='viridis'
         plt.colorbar(label='V (m/s)')
         plt.xlabel('Black Hole Mass (Solar Masses)')
         plt.ylabel('Accretion Rate (Solar Masses per Year)')
         plt.title('Accretion Rate vs Black Hole Mass (Colored by V)')
         # Scatter plot for c s
         plt.subplot(133)
         plt.scatter(black hole masses, accretion rates c s, c=c s values, cmap='viri
         plt.colorbar(label='C s (m/s)')
         plt.xlabel('Black Hole Mass (Solar Masses)')
         plt.ylabel('Accretion Rate (Solar Masses per Year)')
         plt.title('Accretion Rate vs Black Hole Mass (Colored by C s)')
         plt.tight layout()
         plt.show()
```

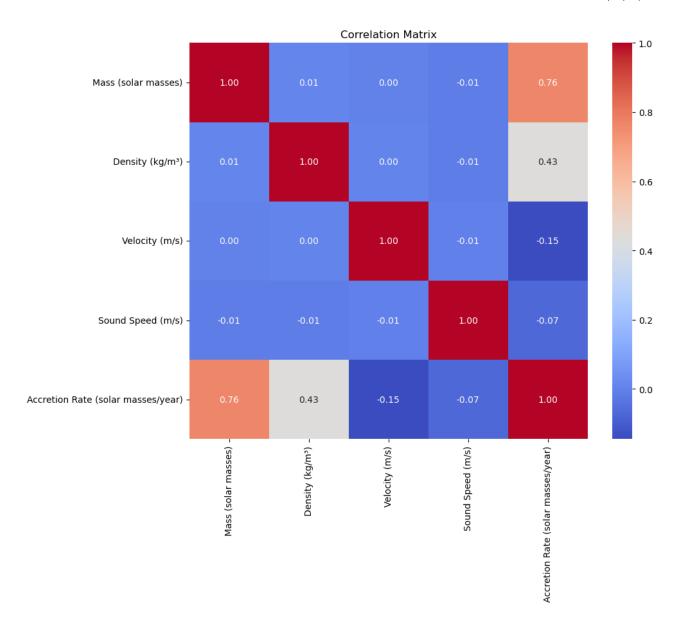


According to the output plots, adjust the randomization to an acceptable range, and update the function calculate_accretion_rate with these randomization range.

```
In [15]:
         # observe the correlation between black hole mass, density of ambient object
          # velocity between the object and the ambient medium, and Sound speed of the
         def pearson correlation(x, y):
             Calculates the Pearson correlation coefficient between two arrays x and
             mean x = np.mean(x)
             mean_y = np.mean(y)
             numerator = np.sum((x - mean_x) * (y - mean_y))
             denominator = np.sqrt(np.sum((x - mean_x)**2) * np.sum((y - mean_y)**2))
             return numerator / denominator if denominator != 0 else 0
         # Monte Carlo Simulation Parameters
         num simulations = 10000
         black hole mass range = (1, 100) # in solar masses
         rho_range = (1e-14, 1e-13) # in kg/m^3
         v range = (4.5e7, 5.5e7) # in m/s
         c_s_{name} = (1e6, 2e7) # in m/s
         masses = np.random.uniform(*black hole mass range, num simulations)
         rhos = np.random.uniform(*rho range, num simulations)
         vs = np.random.uniform(*v_range, num_simulations)
         c_ss = np.random.uniform(*c_s_range, num_simulations)
         accretion rates = np.array([calculate accretion rate(m, rho, v, c s) for m,
         data = np.vstack([masses, rhos, vs, c ss, accretion rates]).T
         # Labels for each parameter
         labels = ['Mass (solar masses)', 'Density (kg/m<sup>3</sup>)', 'Velocity (m/s)', 'Sound
         figure = corner.corner(data, labels=labels, show_titles=True, title_kwargs={
                                 color='skyblue',
                                 hist kwargs={'density': True, 'histtype': 'step', 'li
                                 plot density=True,
                                 plot datapoints=False,
```

```
fill contours=True,
                       contour kwargs={'colors': 'black', 'linewidths': 1})
plt.show()
# Monte Carlo Simulation Parameters
num simulations = 10000
black_hole_mass_range = (1, 100) # in solar masses
rho range = (1e-14, 1e-13) # in kg/m^3
v range = (4.5e7, 5.5e7) # in m/s
c_s_{nage} = (1e6, 2e7) # in m/s
# Generating random data for each parameter
masses = np.random.uniform(*black hole mass range, num simulations)
rhos = np.random.uniform(*rho range, num simulations)
vs = np.random.uniform(*v range, num simulations)
c_ss = np.random.uniform(*c_s_range, num_simulations)
# Calculating accretion rates
accretion_rates = np.array([calculate_accretion_rate(m, rho, v, c_s) for m,
# Stacking the data and calculating the correlation matrix
data = np.vstack([masses, rhos, vs, c_ss, accretion_rates]).T
correlation_matrix = np.array([[pearson_correlation(data[:, i], data[:, j])
# Labels for each parameter
labels = ['Mass (solar masses)', 'Density (kg/m<sup>3</sup>)', 'Velocity (m/s)', 'Sound
# Creating the correlation matrix heatmap
plt.figure(figsize=(10, 8))
sns.heatmap(correlation matrix, annot=True, xticklabels=labels, yticklabels=
plt.title('Correlation Matrix')
plt.show()
```





Here I run 10000 times monte carlo simulation to explore the correlation between our interested parameters. This is as what was expected: the mass of black hole contributes significantly to the accretion rate. However, note that the density also has a relatively high correlation with the accretion rate comparing to other parameters, so I should keep this in mind in the future work.

2. Radiation

Since radiation is emitted by the accretion process as luminosity, it is important to consider the radiation in doing the modeling. The luminosity is typically calculated by (https://en.wikipedia.org/wiki/Luminosity#:~:text=Luminosity%20is%20an%20absolute%20r

$$Radiation = \epsilon \times \dot{M} \times 1.98847 \times 10^{30} \times c^2$$

where

 \dot{M} : Efficiency factor - typically around 0.1 for non-rotating black holes (7)

$$c: \text{speed of light}$$
 (8)

$$R_{acc}$$
: accretion rate (9)

```
In [17]: # Test the function calculate_radiation
    print(calculate_radiation(calculate_accretion_rate(100)))
```

8.223440214074208e+31 m2 yr / s3

```
In [18]:
         '''Plot Radiation in term of Black Hole Masses with varies Parameters'''
         # Randomize the parameters and calculate accretion rates and radiation
         num_points = 1000
         fixed rho = 1e-13 # Fixed density
         fixed_v = 5e7  # Fixed relative velocity
         fixed_c_s = 5e6  # Fixed sound speed
         # Randomize black hole masses
         black hole masses = np.random.uniform(1, 100, num points)
         # Randomizing rho while keeping v and c s fixed
         rho values = np.random.uniform(5e-14, 1e-13, num points)
         accretion rates rho = [calculate accretion rate(mass, rho=rho, v=fixed v, c
         radiation_rho = [calculate_radiation(rate) for rate in accretion_rates_rho]
         # Randomizing v while keeping rho and c s fixed
         v values = np.random.uniform(4.5e7, 5.5e7, num points)
         accretion_rates_v = [calculate_accretion_rate(mass, rho=fixed_rho, v=v, c_s=
```

```
radiation v = [calculate radiation(rate) for rate in accretion rates v]
# Randomizing c s while keeping rho and v fixed
c_s_values = np.random.uniform(1e6, 2e7, num_points)
accretion_rates_c_s = [calculate_accretion_rate(mass, rho=fixed_rho, v=fixed_
radiation_c_s = [calculate_radiation(rate) for rate in accretion_rates_c_s]
radiation rho = [x.value for x in radiation rho]
radiation v = [x.value for x in radiation v]
radiation_c_s = [x.value for x in radiation_c_s]
# Plotting the results
plt.figure(figsize=(18, 6))
# Scatter plot for radiation vs black hole mass (Colored by Rho)
plt.subplot(131)
plt.scatter(black hole masses, radiation rho, c=rho values, cmap='viridis')
plt.colorbar(label='Rho (kg/m^3)')
plt.xlabel('Black Hole Mass (Solar Masses)')
plt.ylabel('Radiation (Watts)')
plt.title('Radiation vs Black Hole Mass (Colored by Rho)')
# Scatter plot for radiation vs black hole mass (Colored by V)
plt.subplot(132)
plt.scatter(black hole masses, radiation v, c=v values, cmap='viridis')
plt.colorbar(label='V (m/s)')
plt.xlabel('Black Hole Mass (Solar Masses)')
plt.ylabel('Radiation (Watts)')
plt.title('Radiation vs Black Hole Mass (Colored by V)')
# Scatter plot for radiation vs black hole mass (Colored by C s)
plt.subplot(133)
plt.scatter(black_hole_masses, radiation_c_s, c=c_s_values, cmap='viridis')
plt.colorbar(label='C s (m/s)')
plt.xlabel('Black Hole Mass (Solar Masses)')
plt.ylabel('Radiation (Watts)')
plt.title('Radiation vs Black Hole Mass (Colored by C_s)')
plt.tight layout()
plt.show()
 1eBadiation vs Black Hole Mass (Colored by Rho)
                             Radiation vs Black Hole Mass (Colored by V
                                                         Radiation vs Black Hole Mass (Colored by C
```

Black Hole Mass (Solar Masse

0 40 60 Black Hole Mass (Solar Mass 40 60 Black Hole Mass (Solar Masses

3. jet production

The jet which emits energy is determined by many factor and is usually very hard to model, so we here assume a simpler case where the jets are produced when the accretion rate and radiation exceed certain limit. We assume the limits to be:

- 1. accretion rate thershold = 10^{-4} solar mass per year
- 2. radiation thershold = 10^{36} watts

```
In [19]: def determine_jet_production(accretion_rate, radiation):
    # Limits when jet production takes place
    accretion_rate_threshold = 1e-4 # in solar masses per year
    radiation_threshold = 1e36

# Determine jet production
    jets = accretion_rate > accretion_rate_threshold and radiation > radiati
    return jets
    # returns true or false
```

```
In [20]: # Examples for determine_jet_production
    print(determine_jet_production(1e-7, 1e20)) # neither parameter exceeds the
    print(determine_jet_production(1, 1e30)) # the accretion rate exceeds the li
    print(determine_jet_production(1e-5, 1e40)) # the radiation exceeds the limi
    print(determine_jet_production(1, 1e40)) # both exceeds the limit
```

False False False True

combining the three function

```
In [21]: def accretion_model(black_hole_mass, accretion_radius, other_parameters):
    accretion_rate = calculate_accretion_rate(black_hole_mass, accretion_radiation = calculate_radiation(accretion_rate, other_parameters)
    jets = determine_jet_production(accretion_rate, radiation, other_parameters)
    return accretion_rate, radiation, jets
```

Now I can add these functions to the original class as the first part of the code:

```
In [22]: class Galaxy:
    '''initialize the galaxy'''
    def __init__(self, mass, position, velocity, black_hole_mass):
        self.mass = mass
        self.position = position
        self.velocity = velocity
```

```
self.black hole mass = black hole mass
'''black hole accretion model'''
def calculate_accretion_rate(black_hole_mass,
                             rho = np.random.uniform(1e-14, 1e-13),
                             v = np.random.uniform(4.5e7, 5.5e7),
                             c s = np.random.uniform(1e6, 2e7)):
    # The input black hole mass should in the unit of solar mass
    G = 6.67430e-11 * u.m**3 / u.kg / u.s**2 # gravitational constant wi
    M = black hole mass * 1.98847e30 * u.kg # solar masses to kg
    rho = rho * u.kg / u.m**3 # density of the accreting material in kg
    v = v * u.m / u.s # relative velocity in m/s
    c s = c s * u.m / u.s # sound speed in the material in m/s
    # Bondi-Hoyle-Lyttleton accretion rate
    accretion_rate = (4 * np.pi * G**2 * M**2 * rho) / ((v**2 + c s**2)*
    # Convert accretion rate to solar masses per year
    accretion rate solar masses per year = accretion rate.to(u.kg / u.s)
    return accretion_rate_solar_masses_per_year
def calculate radiation(accretion rate, epsilon = 0.1):
    # The accretion rate is obtained from the previous function calculat
    c = 299792458 * u.m / u.s
    # calculate the luminosity (or radiation)
    radiation = epsilon * accretion rate * 1.98847e30 * c**2 # Convert
    return radiation
def accretion model(black hole mass, accretion radius, other parameters)
    accretion rate = calculate accretion rate(black hole mass, accretion
    radiation = calculate radiation(accretion rate, other parameters)
    jets = determine jet production(accretion rate, radiation, other par
    return accretion_rate, radiation, jets
# Gas Dynamics and Interstellar Medium
def gas dynamics(galaxy):
    This models the impliment model of the dynamics of gas in and around
    The processes like cooling, heating, and interaction with AGN radiat
    1.1.1
    pass
# Galaxy Interaction and Dynamics
def update galaxy dynamics(galaxies):
    Implement gravitational interactions between galaxies.
    Update positions and velocities based on gravitational forces.
    pass
```

B) Cooling and Heating

According to my research of other people's work, the fully modeled dynamic of mass cannot be easily computed from a local computer and requires much more computation work. Thus, for my work, I will be creating a easier model with more idealized condition than what is actually happening in AGN galaxies but keep all the key concepts in AGN gas dynamics simulation.

The temperature change within the galaxy is another important thing to consider. From previous study (Li et al 2016), they analyzed a battle between radiative cooling and AGN heating. Thus the cooling and heating are happening at the same time within the AGN host galaxy. That being said, we want to set different rate of cooling and heating in terms of other parameters.

This is complex as a lot of parameters could contribute to the cooling/ heating rates, such as mass, cooling coefficient, environment, AGN activity, and many more. We here consider some of the most significant factor in cooling and heating, which are:

- density: Cooling processes in the ISM are significantly influenced by the gas's density, and it is usually proportional to density square
- 2. cooling coefficient
- 3. **temperature**: Cooling processes in the ISM are inversely proportional to temperature
- 4. **time**: The rate might decrease over time as the galaxy loses energy
- 5. **composition**: The composition of AGN galaxies are really hard to determine, I will keep this away from the simulation for now, but may come back to it as this project becomes more developed
- 6. metallicity
- 7. star formation rate
- 8. AGN luminosity: this was calculated above with the radiation

```
In [23]: # combining what has been discussed above, cooling rate is proportional to c
         # and inversely proportional to time and temperature
         def cooling function(temperature):
             if temperature < 1e4:</pre>
                 # Low-temperature regime
                 new temp = 1e-22 * temperature
                 return new_temp
             else:
                 # High-temperature regime
                 new_temp = 1e-24 * temperature**1.5
                 return new_temp
         def heating function(star formation initial, agn luminosity initial, density
             decay factor = 0.05 # Represents a decay over time
             # Star formation rate and AGN luminosity decrease over time
             star formation rate = star formation initial / (1 + decay factor * time)
             agn luminosity = agn luminosity initial / (1 + decay factor * time)
             return 1e-35 * (star formation rate + agn luminosity) * density
         def cooling rate(new temp, density):
             cooling_rate = new_temp * density**2
             return cooling rate
         def ism temperature evolution(initial temperature, density, metallicity, sta
             temperature = initial_temperature
             for time in range(total time):
                 # cooling and heating rates
                 cooling rate = cooling function(temperature) * density**2
                 heating rate = heating function(star formation rate, agn luminosity,
                 # Update temperature
                 temperature change = (heating rate - cooling rate) * timestep
                 temperature += temperature_change
                 if temperature < 10: # 10 K is a reasonable lower limit for ISM tem
                     temperature = 10
             return temperature
```

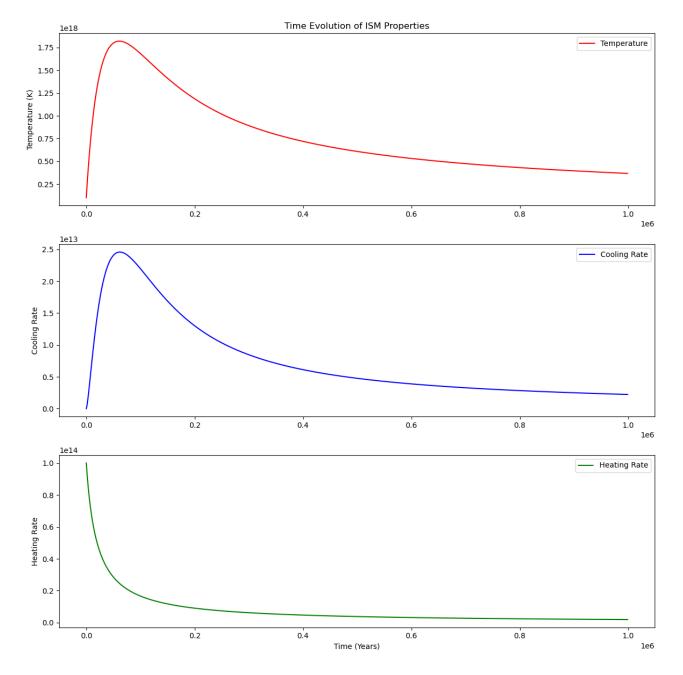
```
In [24]: # Test the function
   initial_temperature = 1000000 # in Kelvin
   density = 1.0e5 # in particles per cubic centimeter
   metallicity = 1.0 # Solar metallicity
   star_formation_rate = 2.0 # Solar masses per year
   agn_luminosity = 1e44 # in ergs per second
   timestep = 1e3 # in years
   total_time = 1000 # number of timesteps
   final_temperature = ism_temperature_evolution(initial_temperature, density,
   print(f"Final ISM Temperature: {final_temperature} K")
```

Final ISM Temperature: 3.669852783696508e+17 K

Week 2 (Milestone 2 start)

```
In [25]: def ism_temperature_evolution_over_time(initial_temperature,
                                                   density,
                                                   metallicity,
                                                   star formation initial,
                                                   agn_luminosity_initial,
                                                   timestep,
                                                   total_time):
             temperature = initial_temperature
             temperatures, cooling_rates, heating_rates = [], [], []
             for time in range(total_time):
                  cooling rate = cooling function(temperature) * density**2
                  heating rate = heating function(star formation initial, agn luminosi
                  temperature_change = (heating_rate - cooling_rate) * timestep
                  # print(heating rate, cooling rate)
                  temperature += temperature change
                  if temperature < 10:</pre>
                      temperature = 10
                  temperatures.append(temperature)
                  cooling rates.append(cooling rate)
                  heating_rates.append(heating_rate)
             return temperatures, cooling rates, heating rates
```

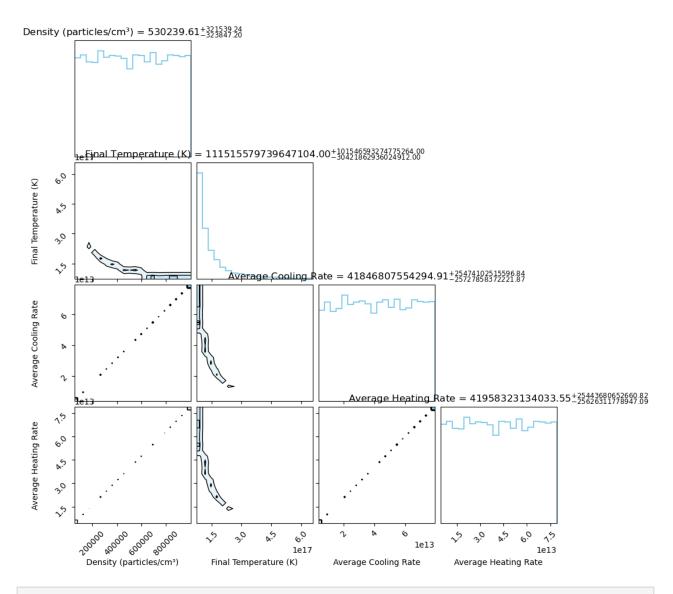
```
In [26]: # simulation
         temperatures, cooling rates, heating rates = ism temperature evolution over
         time axis = [timestep * i for i in range(total time)]
         plt.figure(figsize=(12, 12))
         # Temperature
         plt.subplot(3, 1, 1)
         plt.plot(time_axis, temperatures, label='Temperature', color='red')
         plt.ylabel('Temperature (K)')
         plt.title('Time Evolution of ISM Properties')
         plt.legend()
         # Cooling
         plt.subplot(3, 1, 2)
         plt.plot(time axis, cooling rates, label='Cooling Rate', color='blue')
         plt.ylabel('Cooling Rate')
         plt.legend()
         # Heating
         plt.subplot(3, 1, 3)
         plt.plot(time_axis, heating_rates, label='Heating Rate', color='green')
         plt.ylabel('Heating Rate')
         plt.xlabel('Time (Years)')
         plt.legend()
         plt.tight_layout()
         plt.show()
```



From this plot, it seems like the temperature follows similar evolution as the cooling rate, however, when I did the attempts of changing the value of density, this trend varies a lot. This is impressive and should be further explored, so I want to plot out the evolution of ISM temperature and cooling/heating rates corresponding to different density environment. This is crucial as it reveals potential environmental impact on AGN galaxy evolution. Some methods I could use is to

- 1. again, use the monte carlo simulation to find the correlation, and
- 2. plot out the rates and temperature at different density to observe the trends.

```
In [27]: # monte carlo simulation to find the correlation between density and rates/t
         num simulations = 10000
         density range = (5.5e4, 1e6)
         initial temperature = 1000000 # in Kelvin
         metallicity = 1.0 # Solar metallicity
         star_formation_rate = 2.0 # Solar masses per year
         agn_luminosity = 1e44 # in ergs per second
         timestep = 1e3 # in years
         total time = 1000 # number of timesteps
         densities = np.random.uniform(*density range, num simulations)
         final temperatures = []
         average_cooling_rates = []
         average heating rates = []
         for density in densities:
             temperatures, cooling rates, heating rates = ism temperature evolution of
                 initial temperature, density, metallicity, star formation rate,
                 agn_luminosity, timestep, total_time
             final temperatures.append(temperatures[-1])
             average cooling rates.append(np.mean(cooling rates))
             average heating rates.append(np.mean(heating rates))
         simulation data = np.vstack([densities, final temperatures, average cooling
         corner_labels = ['Density (particles/cm3)', 'Final Temperature (K)', 'Average
         corner_figure = corner.corner(simulation_data, labels=corner_labels, show_ti
                                        color='skyblue',
                                        hist_kwargs={'density': True, 'histtype': 'ste
                                        plot density=True,
                                        plot datapoints=False,
                                        fill contours=True,
                                        contour_kwargs={'colors': 'black', 'linewidths
         plt.show()
```

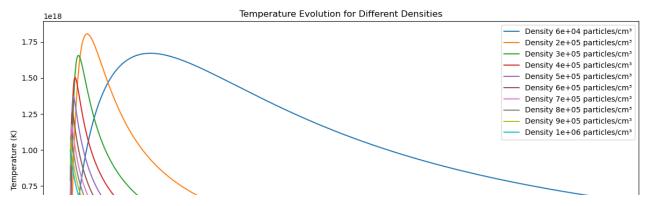


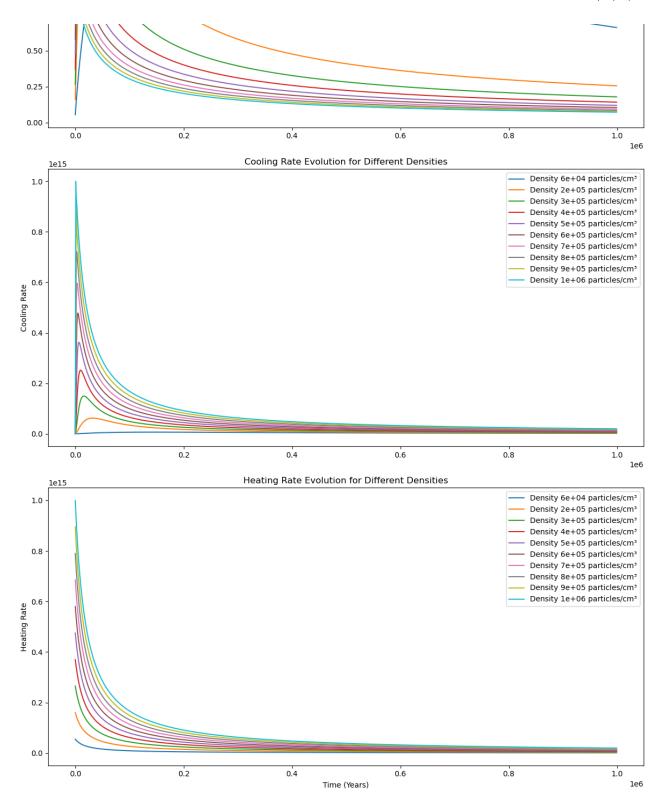
```
In [28]: # the heatmap for correlations between
# temperature, cooling rate, heating rate, and density
simulation_data_array = np.array([final_temperatures, average_cooling_rates,
correlation_matrix = np.corrcoef(simulation_data_array)
heatmap_labels = ['Final Temperature', 'Avg Cooling Rate', 'Avg Heating Rate

plt.figure(figsize=(8, 6))
sns.heatmap(correlation_matrix, annot=True, xticklabels=heatmap_labels, ytic
plt.title('Correlation Matrix Heatmap')
plt.show()
```



```
In [29]:
         selected densities = np.linspace(density range[0], density range[1], 10)
         plt.figure(figsize=(12, 18))
         for density in selected densities:
             temperatures, cooling rates, heating rates = ism temperature evolution of
                 initial_temperature, density, metallicity, star_formation_rate,
                 agn_luminosity, timestep, total_time
             time axis = [timestep * i for i in range(total time)]
             # Temperature
             plt.subplot(3, 1, 1)
             plt.plot(time axis, temperatures, label=f'Density {density:.0e} particle
             # cooling
             plt.subplot(3, 1, 2)
             plt.plot(time axis, cooling rates, label=f'Density {density:.0e} particl
             # heating
             plt.subplot(3, 1, 3)
             plt.plot(time axis, heating rates, label=f'Density {density:.0e} particl
         plt.subplot(3, 1, 1)
         plt.ylabel('Temperature (K)')
         plt.title('Temperature Evolution for Different Densities')
         plt.legend()
         plt.subplot(3, 1, 2)
         plt.ylabel('Cooling Rate')
         plt.title('Cooling Rate Evolution for Different Densities')
         plt.legend()
         plt.subplot(3, 1, 3)
         plt.ylabel('Heating Rate')
         plt.xlabel('Time (Years)')
         plt.title('Heating Rate Evolution for Different Densities')
         plt.legend()
         plt.tight layout()
         plt.show()
```





As density increases, the heating rate increases, the cooling rate increases as well, and the overall temperature peaks lower and decays faster.

Also, from the correlation matrix heat map, it is clear how things are closely related in this cooling and heading system. It is as expected because environment itself is a very deterministic factor.

The density = 1e5 to 1e6 is a fair estimation for the average density inside of an AGN galaxy, but note that the density varies a lot in different parts of a galaxy. For my targets which are AGN galaxies, they are extremely powerful towards the center mainly due to the super massive blackhole. Thus the density at broad line region (the region close to black hole) of AGN galaxies can exceed 1e9 particles per cubic centimeter. As the radius moves away from the center of the galaxy, the narrow line region typically has densities in the range of 1e2 to 1e6.

To make the system more realistic, I can write a function of density in terms of the radius. The typical relationship between density and radius can be expressed as

$$ho(r)=
ho_0(rac{r}{r_0})^{-lpha}$$

where

 $\rho(r)$: The density as a function of radius from the center

 ρ_0 : the reference density, I here take it to be 1.0×10^5 particles per cubic c

 r_0 : reference radius, I here take it to be 1 parsec

r: the radius from the center, in unit of parsec

 α : the index of this power law, I here take it to be 1.5, this varies for differ

```
In [30]: # we can define the function density
def density_radius(r, rho_0 = 1e5, r_0 = 1, alpha = 1.5):
    """

    Density as a function of radius for an AGN environment.
    r: Radius in parsec
    rho_0: Reference density at reference radius r_0
    r_0: Reference radius
    alpha: Power-law index
    """

    rho_r = rho_0 * (r / r_0) ** (-alpha)
    return rho_r
```

Then, I can update the previous functions:

```
In [31]: def heating_function(star_formation_initial,
```

```
r,
                     time,
                     agn luminosity initial = 1e44,
                     rho_0 = 1e5,
                     r 0 = 1,
                     alpha = 1.5):
   decay factor = 0.05
   star formation rate = star formation initial / (1 + decay factor * time)
   agn_luminosity = agn_luminosity_initial / (1 + decay_factor * time)
   density = density_radius(r, rho_0, r_0, alpha)
   new temp = 1e-35 * (star formation rate + agn luminosity) * density
   return new temp
def cooling function(temperature, r, rho_0 = 1e5, r_0 = 1, alpha = 1.5):
   density = density radius(r, rho 0, r 0, alpha)
   if temperature < 1e4:</pre>
        new temp = 1e-22 * temperature * density**2
   else:
        new_temp = 1e-24 * temperature**1.5 * density**2
   return new temp
def cooling_rate(new_temp, density):
   cooling rate = new temp * density**2
   return cooling rate
def ism temperature evolution(initial temperature,
                              r,
                              metallicity,
                              star formation rate,
                              agn_luminosity, timestep, total_time):
   temperature = initial_temperature
   density = density radius(r, rho 0, r 0, alpha)
    for time in range(total time):
        # cooling and heating rates
        cooling rate = cooling function(temperature, r, rho 0 = 1e5, r 0 = 1
        heating rate = heating function(star formation rate, agn luminosity,
        temperature_change = (heating_rate - cooling_rate) * timestep
        temperature += temperature_change
        if temperature < 10: # 10 K is a reasonable lower limit for ISM ten
            temperature = 10
   return temperature
def ism temperature evolution over time(initial temperature,
                                         rho 0=1e5,
                                         r = 0 = 1,
                                         alpha=1.5,
                                         metallicity=1.0,
                                         star_formation_initial=2.0,
                                         agn_luminosity_initial=1e44,
                                         timestep=1e3,
                                         total_time=10000):
    temperature = initial_temperature
```

```
temperatures, cooling_rates, heating_rates = [], [], []
for time in range(total_time):
    density = density_radius(r, rho_0, r_0, alpha)
    cooling_rate = cooling_function(temperature, r, rho_0, r_0, alpha) *
    heating_rate = heating_function(star_formation_initial, agn_luminosi
    temperature_change = (heating_rate - cooling_rate) * timestep
    temperature += temperature_change
    if temperature < 10:
        temperature = 10
    temperatures.append(temperature)
    cooling_rates.append(cooling_rate)
    heating_rates.append(heating_rate)
    return temperatures, cooling_rates, heating_rates</pre>
```

```
In [32]: # Example
    r = 2.0 # radius in parsecs
    initial_temperature = 100000 # in Kelvin
    temperatures, cooling_rates, heating_rates = ism_temperature_evolution_over_
    temperatures[:10]

Out[32]: [50589.411559869055,
    32810.32404018419,
    23524.171671272197,
    17886.6070103183,
    14148.842176469958,
    11519.171404028086,
    9587.417107373523,
    8089.3831843464095,
    6825.417061792283,
```

Add these to the previously defined class:

5758.945645887238]

```
In [33]: class Galaxy:
             '''initialize the galaxy'''
             def __init__(self, mass, position, velocity, black_hole_mass):
                 self.mass = mass
                 self.position = position
                 self.velocity = velocity
                 self.black_hole_mass = black_hole_mass
              '''black hole accretion model'''
             def calculate_accretion_rate(black_hole_mass,
                                           rho = np.random.uniform(1e-14, 1e-13),
                                           v = np.random.uniform(4.5e7, 5.5e7),
                                           c_s = np.random.uniform(1e6, 2e7)):
                 # The input black hole mass should in the unit of solar mass
                 G = 6.67430e-11 * u.m**3 / u.kg / u.s**2 # gravitational constant wi
                 M = black_hole_mass * 1.98847e30 * u.kg # solar masses to kg
                 rho = rho * u.kg / u.m**3 # density of the accreting material in kg
                 v = v * u.m / u.s # relative velocity in m/s
                 c s = c s * u.m / u.s # sound speed in the material in m/s
                 # Bondi-Hoyle-Lyttleton accretion rate
```

```
accretion rate = (4 * np.pi * G**2 * M**2 * rho) / ((v**2 + c s**2)*
    # Convert accretion rate to solar masses per year
    accretion rate solar masses per year = accretion rate.to(u.kg / u.s)
    return accretion_rate_solar_masses_per_year
def calculate radiation(accretion rate, epsilon = 0.1):
    # The accretion rate is obtained from the previous function calculat
    c = 299792458 * u.m / u.s
    # calculate the luminosity (or radiation)
    radiation = epsilon * accretion_rate * 1.98847e30 * c**2 # Convert
    return radiation
def accretion model(black hole mass, accretion radius, other parameters)
    accretion rate = calculate accretion rate(black hole mass, accretion
    radiation = calculate radiation(accretion rate, other parameters)
    jets = determine jet production(accretion rate, radiation, other par
    return accretion_rate, radiation, jets
'''cooling and heating process in different radius of the galaxy'''
def heating function(star formation initial,
                     r,
                     time,
                     agn luminosity initial = 1e44,
                     rho_0 = 1e5,
                     r 0 = 1,
                     alpha = 1.5):
    decay factor = 0.05
    star formation rate = star formation initial / (1 + decay factor * t
    agn luminosity = agn luminosity initial / (1 + decay factor * time)
    density = density radius(r, rho 0, r 0, alpha)
    new_temp = 1e-35 * (star_formation_rate + agn_luminosity) * density
    return new temp
def cooling function(temperature, r, rho_0 = 1e5, r_0 = 1, alpha = 1.5):
    density = density radius(r, rho 0, r 0, alpha)
    if temperature < 1e4:</pre>
        new_temp = 1e-22 * temperature * density**2
        new temp = 1e-24 * temperature**1.5 * density**2
    return new_temp
def cooling rate(new temp, density):
    cooling rate = new temp * density**2
    return cooling rate
def ism temperature evolution(initial temperature,
                              metallicity,
                              star formation_rate,
                              agn_luminosity, timestep, total_time):
    temperature = initial temperature
    density = density_radius(r, rho_0, r_0, alpha)
    for time in range(total_time):
```

```
# cooling and heating rates
        cooling rate = cooling function(temperature, r, rho 0 = 1e5, r 0
        heating rate = heating function(star formation rate, agn luminos
        temperature_change = (heating_rate - cooling_rate) * timestep
        temperature += temperature change
        if temperature < 10: # 10 K is a reasonable lower limit for ISM
            temperature = 10
    return temperature
def ism_temperature_evolution_over_time(initial_temperature,
                                         rho 0=1e5,
                                         r = 0 = 1,
                                         alpha=1.5,
                                         metallicity=1.0,
                                         star formation initial=2.0,
                                         agn luminosity initial=1e44,
                                         timestep=1e3,
                                         total_time=10000):
    temperature = initial temperature
    temperatures, cooling rates, heating rates = [], [], []
    for time in range(total time):
        density = density radius(r, rho 0, r 0, alpha)
        cooling_rate = cooling_function(temperature, r, rho_0, r_0, alph
        heating rate = heating function(star formation initial, agn lumi
        temperature change = (heating rate - cooling rate) * timestep
        temperature += temperature change
        if temperature < 10:</pre>
            temperature = 10
        temperatures.append(temperature)
        cooling rates.append(cooling rate)
        heating rates.append(heating rate)
    return temperatures, cooling rates, heating rates
# Gas Dynamics and Interstellar Medium
def gas_dynamics(galaxy):
    1.1.1
    This models the impliment model of the dynamics of gas in and around
    The processes like cooling, heating, and interaction with AGN radiat
    1 1 1
    pass
# Galaxy Interaction and Dynamics
def update galaxy dynamics(galaxies):
    Implement gravitational interactions between galaxies.
    Update positions and velocities based on gravitational forces.
    I = I - I
    pass
```

C) Spectra Modeling for AGN galaxies

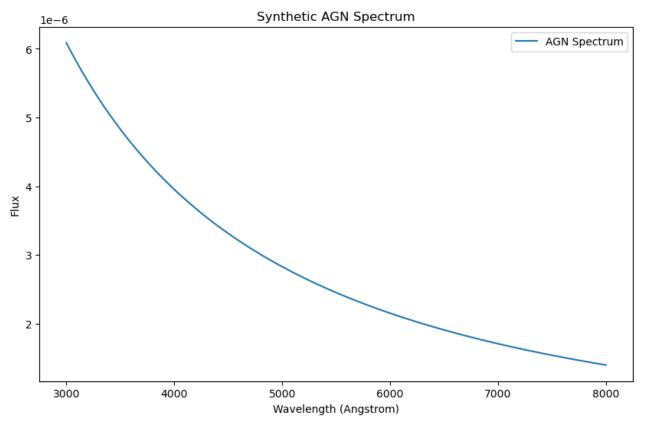
Spectra modeling is significant for studying gakaxies because it gives us information about a various things. Some typical ones includes:

- composition and chemical elemental abundances: from analyzing a spectra of a
 galaxy, we can tell from the emission and absorption lines which components exists
 in the galaxies, also, the ratio between certain emission lines give us the chemical
 elemental abundances, which reveals the history of the galaxy because some
 element are more produced in certain age or phase of galaxy evolution.
- 2. **redshift**: by looking at the obvious emission and absorption lines from a galaxy's spectrum, we can compare it with the wavelength of that element in the rest frame spectrum, and by using $1+z=\frac{\lambda_{observed}}{\lambda_e}$ we can find the redshift of the galaxy, and thus how far the galaxy is from us.
- 3. **stellar population**: since different stars have very different physical properties, we can tell from the spectra which kind of stars do the galaxy have and thus better understand the stellar populations of certain types of galaxies.
- 4. Spectra modeling also plays critical roles in understanding black holes of AGN, studying dark matter and dark matter halo, and providing insights into the temperature and density. Thus we want to understand how AGN galaxies look like and potentially build AGN galaxy spectrum.

There are several things and steps I need to consider towards doing spectra modeling:

- 1. I need to generate a power-law continuum
- 2. consider emission lines
- 3. add in noise
- 4. consider **absorption feature** I here use units that is typically used in experimental astrophysics, which are arbitrary unit for flux (we do not actually care about the unit of flux, what we care is the intensity and the ratios)

```
In [34]: # Step 1
         # we first assumed redshift 0 and generalize the power-law continuum
         # most of the emission lines and absorption features are within wavelength in
         # so I choose the wavelength range from 3000 to 10000
         # alpha is the power-law slope
         wavelengths = np.linspace(3000, 8000, 10000)
         alpha = -1.5
         flux_continuum = wavelengths ** alpha
         # Plotting
         plt.figure(figsize=(10, 6))
         plt.plot(wavelengths, flux_continuum, label='AGN Spectrum')
         plt.xlabel('Wavelength (Angstrom)')
         plt.ylabel('Flux')
         plt.title('Synthetic AGN Spectrum')
         plt.legend()
         plt.show()
```

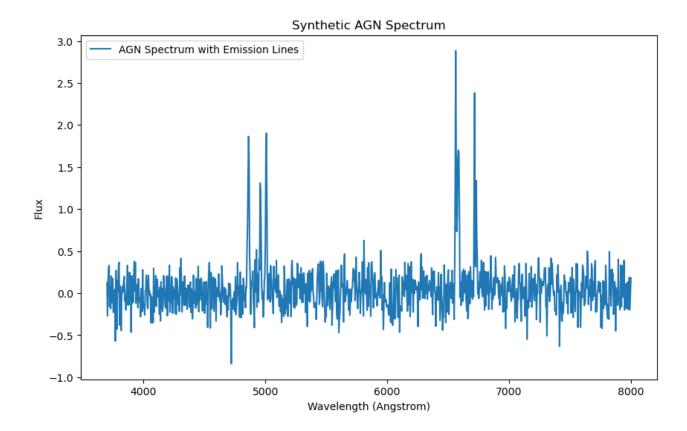


The **width** and **height** of each emission line is usually based on observation, these are determined by a various factor such as pressure, abundance, temperature, density, and ionization state. I here randomize them, and for next week, I want to use the randomized spectra to observe the correlation between these parameters. The emission lines that are usually visible are:

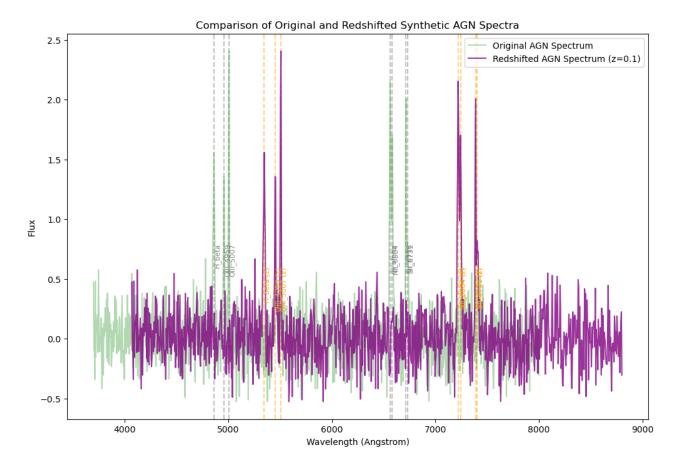
- 1. H_alpha = 6563 # H-alpha
- 2. H_beta = 4861 # H-beta
- 3. OIII_5007 = 5007 # O III line
- 4. OIII_4959 = 4959 # O III line
- 5. NII_6584 = 6584 # N II line
- 6. SII_6716 = 6716 # S II line
- 7. SII_6731 = 6731 # S II line

among them, for AGN host galaxies, elements like Hydrogen, Oxygen, and Nitrogen are commonly observed with relatively intense lines, so I time their flux by a factor of 1.5

```
In [35]: # Step 2
         # now I want to add in some typical emission lines for an AGN host galaxies
         wavelengths = np.linspace(3700, 8000, 1000)
         alpha = -15
         flux continuum = wavelengths ** alpha
         # the emission lines include:
         # Randomization ranges
         width_range = (2, 10) # Width range in Angstroms
         base height range = (10, 20) # Base height range for less intense lines
         emission lines = {
              "H_alpha": {"center": 6563, "element": "H"},
              "H_beta": {"center": 4861, "element": "H"},
             "OIII_5007": {"center": 5007, "element": "O"},
              "OIII_4959": {"center": 4959, "element": "O"},
             "NII_6584": {"center": 6584, "element": "N"},
              "SII 6716": {"center": 6716, "element": "S"},
             "SII_6731": {"center": 6731, "element": "S"}
         def add_emission_line(wavelength_center, width, height):
             return height * norm.pdf(wavelengths, wavelength center, width)
         for line in emission lines.values():
             width = random.uniform(*width_range)
             height = random.uniform(*base_height_range)
             if line["element"] in ["H", "O", "N"]:
                 height *= 1.5
             flux continuum += add emission line(line["center"], width, height)
         # Step 3: The spectrum usually also have noise, I also want to include that:
         noise level = 0.2
         noise = np.random.normal(0, noise level, wavelengths.shape)
         flux continuum += noise
         # Plotting
         plt.figure(figsize=(10, 6))
         plt.plot(wavelengths, flux_continuum, label='AGN Spectrum with Emission Line
         plt.xlabel('Wavelength (Angstrom)')
         plt.ylabel('Flux')
         plt.title('Synthetic AGN Spectrum')
         plt.legend()
         plt.show()
```



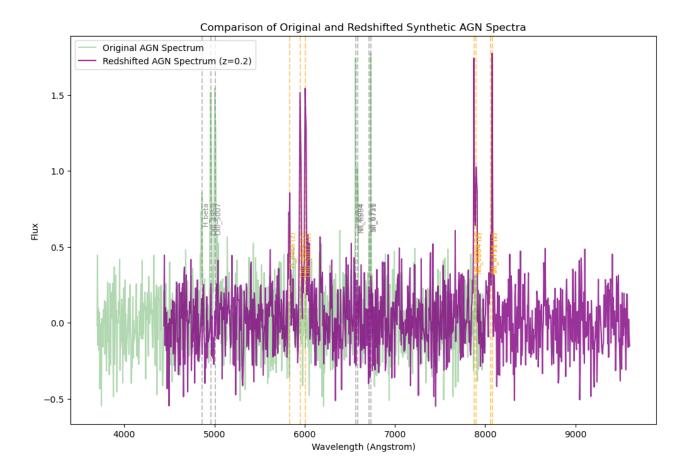
```
In [36]: wavelengths = np.linspace(3700, 8000, 1000)
         alpha = -15
         flux continuum = wavelengths ** alpha
         emission lines = {
             "H_alpha": {"center": 6563, "element": "H"},
             "H_beta": {"center": 4861, "element": "H"},
             "OIII_5007": {"center": 5007, "element": "O"},
             "OIII_4959": {"center": 4959, "element": "O"},
             "NII 6584": {"center": 6584, "element": "N"},
             "SII_6716": {"center": 6716, "element": "S"},
             "SII 6731": {"center": 6731, "element": "S"}
         def add emission line(wavelength center, width, height):
             return height * norm.pdf(wavelengths, wavelength center, width)
         width range = (2, 10)
         base height range = (10, 20)
         for line in emission lines.values():
             width = random.uniform(*width range)
             height = random.uniform(*base height range)
             if line["element"] in ["H", "O", "N"]:
                 height *= 1.5
             flux_continuum += add_emission_line(line["center"], width, height)
         noise level = 0.2
         noise = np.random.normal(0, noise level, wavelengths.shape)
         flux continuum += noise
         z = 0.1
         original flux continuum = flux continuum.copy()
         redshifted wavelengths = wavelengths * (1 + z)
         redshifted flux continuum = original flux continuum
         plt.figure(figsize=(12, 8))
         for line name, line in emission lines.items():
             original_center = line["center"]
             redshifted_center = original_center * (1 + z)
             plt.axvline(x=original_center, color='gray', linestyle='--', alpha=0.5)
             plt.axvline(x=redshifted_center, color='orange', linestyle='--', alpha=0
             plt.text(original center, plt.ylim()[1]*0.8, line name, rotation=90, ver
             plt.text(redshifted_center, plt.ylim()[1]*0.6, f'{line_name} (z)', rotat
         plt.plot(wavelengths, original flux continuum, label='Original AGN Spectrum'
         plt.plot(redshifted wavelengths, redshifted flux continuum, label=f'Redshift
         plt.xlabel('Wavelength (Angstrom)')
         plt.ylabel('Flux')
         plt.title('Comparison of Original and Redshifted Synthetic AGN Spectra')
         plt.legend()
         plt.show()
```



```
In [41]: # define a function that takes a single input of redshift and produce the sp
         def generate redshifted spectrum(redshift):
             wavelengths = np.linspace(3700, 8000, 1000)
             alpha = -15
             flux_continuum = wavelengths ** alpha
             emission lines = {
                  "H alpha": {"center": 6563, "element": "H"},
                  "H_beta": {"center": 4861, "element": "H"},
                  "OIII_5007": {"center": 5007, "element": "O"},
                  "OIII_4959": {"center": 4959, "element": "O"},
                  "NII_6584": {"center": 6584, "element": "N"},
                  "SII 6716": {"center": 6716, "element": "S"},
                  "SII_6731": {"center": 6731, "element": "S"}
             }
             def add emission line(wavelength center, width, height):
                 return height * norm.pdf(wavelengths, wavelength_center, width)
             width range = (2, 10)
             base height range = (10, 20)
             for line in emission lines.values():
                 width = random.uniform(*width_range)
                 height = random.uniform(*base_height_range)
                 if line["element"] in ["H", "O", "N"]:
```

```
height *= 1.5
    flux continuum += add emission line(line["center"], width, height)
noise level = 0.2
noise = np.random.normal(0, noise_level, wavelengths.shape)
flux continuum += noise
original flux continuum = flux continuum.copy()
redshifted wavelengths = wavelengths * (1 + redshift)
redshifted_flux_continuum = original_flux_continuum
plt.figure(figsize=(12, 8))
for line name, line in emission lines.items():
    original center = line["center"]
    redshifted center = original center * (1 + redshift)
    plt.axvline(x=original center, color='gray', linestyle='--', alpha=0
    plt.axvline(x=redshifted center, color='orange', linestyle='--', alp
    plt.text(original_center, plt.ylim()[1]*0.8, line_name, rotation=90,
    plt.text(redshifted_center, plt.ylim()[1]*0.6, f'{line_name} (z)', r
plt.plot(wavelengths, original flux continuum, label='Original AGN Spect
plt.plot(redshifted_wavelengths, redshifted_flux_continuum, label=f'Reds
plt.xlabel('Wavelength (Angstrom)')
plt.ylabel('Flux')
plt.title('Comparison of Original and Redshifted Synthetic AGN Spectra')
plt.legend()
plt.show()
return redshifted wavelengths, flux continuum
```

```
In [38]: # example
generate_redshifted_spectrum(0.2)
```



Add this into the class:

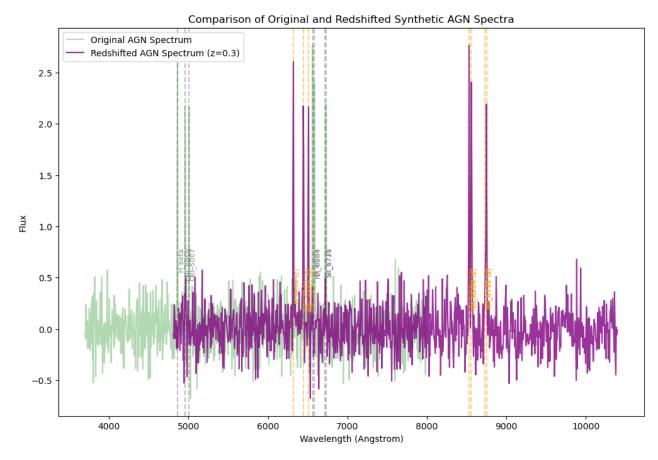
```
In [42]: class Galaxy:
              '''initialize the galaxy'''
             def __init__(self, mass, position, velocity, black_hole_mass, initial_te
                 self.mass = mass
                 self.position = position
                 self.velocity = velocity
                 self.black hole mass = black hole mass
              '''black hole accretion model'''
             def calculate accretion rate(black hole mass,
                                           rho = np.random.uniform(1e-14, 1e-13),
                                           v = np.random.uniform(4.5e7, 5.5e7),
                                           c s = np.random.uniform(1e6, 2e7)):
                 # The input black hole mass should in the unit of solar mass
                 G = 6.67430e-11 * u.m**3 / u.kg / u.s**2 # gravitational constant wi
                 M = black hole mass * 1.98847e30 * u.kg # solar masses to kg
                 rho = rho * u.kg / u.m**3 # density of the accreting material in kg
                 v = v * u.m / u.s # relative velocity in m/s
                 c s = c s * u.m / u.s # sound speed in the material in m/s
                 # Bondi-Hoyle-Lyttleton accretion rate
                 accretion rate = (4 * np.pi * G**2 * M**2 * rho) / ((v**2 + c s**2)*
                 # Convert accretion rate to solar masses per year
                 accretion rate solar masses per year = accretion rate.to(u.kg / u.s)
                 return accretion rate solar masses per year
```

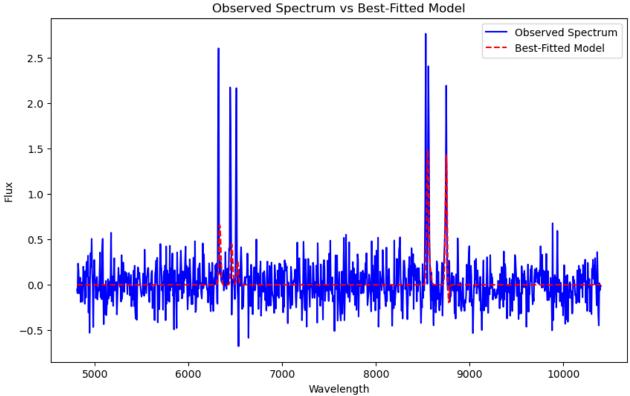
```
def calculate_radiation(accretion_rate, epsilon = 0.1):
    # The accretion rate is obtained from the previous function calculat
    c = 299792458 * u.m / u.s
    # calculate the luminosity (or radiation)
    radiation = epsilon * accretion rate * 1.98847e30 * c**2 # Convert
    return radiation
def accretion model(black hole mass, accretion radius, other parameters)
    accretion rate = calculate accretion rate(black hole mass, accretion
    radiation = calculate radiation(accretion rate, other parameters)
    jets = determine jet production(accretion rate, radiation, other par
    return accretion rate, radiation, jets
'''cooling and heating process in different radius of the galaxy'''
def heating function(r,
                     time,
                     agn_luminosity_initial = 1e44,
                     star_formation_initial = 2.0,
                     rho 0 = 1e5,
                     r_0 = 1,
                     alpha = 1.5):
    decay factor = 0.05
    star_formation_rate = star_formation_initial / (1 + decay_factor * t
    agn_luminosity = agn_luminosity_initial / (1 + decay_factor * time)
    density = density radius(r, rho 0, r 0, alpha)
    new temp = 1e-35 * (star formation rate + agn luminosity) * density
    return new temp
def cooling function(temperature, r, rho 0 = 1e5, r 0 = 1, alpha = 1.5):
    density = density_radius(r, rho_0, r_0, alpha)
    if temperature < 1e4:</pre>
        new_temp = 1e-22 * temperature * density**2
    else:
        new temp = 1e-24 * temperature**1.5 * density**2
    return new_temp
def cooling_rate(new_temp, density):
    cooling rate = new temp * density**2
    return cooling_rate
def ism temperature evolution(initial temperature,
                              r,
                              metallicity,
                              star formation rate,
                              agn_luminosity, timestep, total_time):
    temperature = initial temperature
    density = density radius(r, rho 0, r 0, alpha)
    for time in range(total time):
        # cooling and heating rates
        cooling rate = cooling function(temperature, r, rho 0 = 1e5, r 0
        heating rate = heating function(star formation rate, agn luminos
        temperature_change = (heating_rate - cooling_rate) * timestep
```

```
temperature += temperature change
        if temperature < 10: # 10 K is a reasonable lower limit for ISM
            temperature = 10
    return temperature
def ism temperature evolution over time(initial temperature,
                                         r,
                                         rho 0=1e5,
                                         r = 0 = 1,
                                         alpha=1.5,
                                         metallicity=1.0,
                                         star formation initial=2.0,
                                         agn luminosity initial=1e44,
                                         timestep=1e3,
                                         total time=10000):
    temperature = initial temperature
    temperatures, cooling rates, heating rates = [], [], []
    for time in range(total_time):
        density = density_radius(r, rho_0, r_0, alpha)
        cooling rate = cooling function(temperature, r, rho 0, r 0, alph
        heating rate = heating function(star formation initial, agn lumi
        temperature_change = (heating_rate - cooling_rate) * timestep
        temperature += temperature change
        if temperature < 10:</pre>
            temperature = 10
        temperatures.append(temperature)
        cooling rates.append(cooling rate)
        heating rates.append(heating rate)
    return temperatures, cooling rates, heating rates
'''spectra modeling'''
def generate redshifted spectrum(redshift):
    wavelengths = np.linspace(3700, 8000, 1000)
    alpha = -15
    flux continuum = wavelengths ** alpha
    emission_lines = {
        "H_alpha": {"center": 6563, "element": "H"},
        "H beta": {"center": 4861, "element": "H"},
        "OIII_5007": {"center": 5007, "element": "O"},
        "OIII_4959": {"center": 4959, "element": "O"},
        "NII_6584": {"center": 6584, "element": "N"},
        "SII 6716": {"center": 6716, "element": "S"},
        "SII 6731": {"center": 6731, "element": "S"}
    }
    def add emission line(wavelength center, width, height):
        return height * norm.pdf(wavelengths, wavelength center, width)
    width_range = (2, 10)
    base height range = (10, 20)
    for line in emission_lines.values():
```

```
width = random.uniform(*width range)
        height = random.uniform(*base height range)
        if line["element"] in ["H", "O", "N"]:
            height *= 1.5
        flux continuum += add emission line(line["center"], width, heigh
    noise level = 0.2
    noise = np.random.normal(0, noise level, wavelengths.shape)
    flux continuum += noise
    original flux continuum = flux continuum.copy()
    redshifted wavelengths = wavelengths * (1 + redshift)
    redshifted flux continuum = original flux continuum
    plt.figure(figsize=(12, 8))
    for line name, line in emission lines.items():
        original center = line["center"]
        redshifted center = original_center * (1 + redshift)
        plt.axvline(x=original_center, color='gray', linestyle='--', alp
        plt.axvline(x=redshifted center, color='orange', linestyle='--',
        plt.text(original center, plt.ylim()[1]*0.8, line name, rotation
        plt.text(redshifted_center, plt.ylim()[1]*0.6, f'{line_name} (z)
    plt.plot(wavelengths, original_flux_continuum, label='Original AGN S
    plt.plot(redshifted wavelengths, redshifted flux continuum, label=f'
    plt.xlabel('Wavelength (Angstrom)')
    plt.ylabel('Flux')
    plt.title('Comparison of Original and Redshifted Synthetic AGN Spect
    plt.legend()
    plt.show()
    return redshifted wavelengths, flux continuum
# Gas Dynamics and Interstellar Medium
def gas_dynamics(galaxy):
    This models the impliment model of the dynamics of gas in and around
    The processes like cooling, heating, and interaction with AGN radiat
    1.1.1
    pass
# Galaxy Interaction and Dynamics
def update galaxy dynamics(galaxies):
    Implement gravitational interactions between galaxies.
    Update positions and velocities based on gravitational forces.
    pass
```

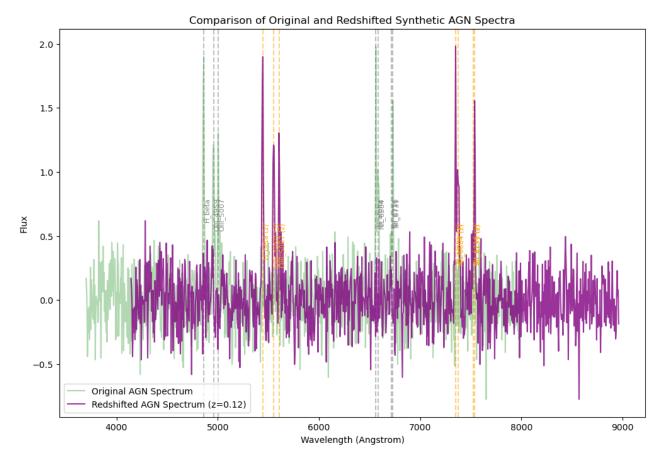
```
In [51]: observed wavelengths, observed_flux = generate_redshifted_spectrum(0.3)
         emission line centers = [6563, 4861, 5007, 4959, 6584, 6716, 6731]
         line width = 10
         def model spectrum(wavelengths, redshift, line intensities):
             model flux = wavelengths ** -1.5
             for i, line center in enumerate(emission line centers):
                 shifted_center = line_center * (1 + redshift)
                 model flux += line intensities[i] * norm.pdf(wavelengths, shifted ce
             return model flux
         def chi squared(obs flux, model flux):
             return np.sum((obs_flux - model_flux) ** 2)
         def fit spectrum(line intensities, redshift):
             model flux = model spectrum(observed wavelengths, redshift, line intensi
             return chi squared(observed flux, model flux)
         N = len(emission_line_centers) # number of emission lines
         initial line intensities = [10] * N # Initial guess for each line intensity
         # Optimization Model
         best_fit = None
         for redshift in np.linspace(0, 1, 100):
             result = minimize(fit_spectrum, initial_line_intensities, args=(redshift
             if best_fit is None or result.fun < best_fit[1]:</pre>
                 best fit = (redshift, result.fun, result.x)
         best fit flux = model spectrum(observed wavelengths, best fit[0], best fit[2]
         plt.figure(figsize=(10, 6))
         plt.plot(observed_wavelengths, observed_flux, label="Observed Spectrum", col
         plt.plot(observed wavelengths, best fit flux, label="Best-Fitted Model", col
         plt.xlabel("Wavelength")
         plt.ylabel("Flux")
         plt.title("Observed Spectrum vs Best-Fitted Model")
         plt.legend()
         plt.show()
         print(f"Best fit redshift: {best fit[0]}")
         print(f"Best fit line intensities: {best fit[2]}")
```

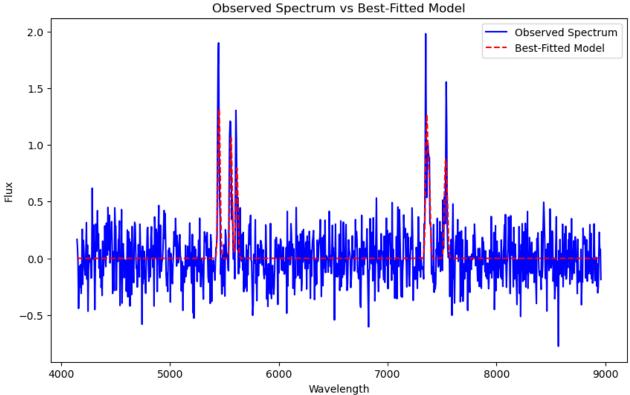




Best fit redshift: 0.30303030303030304

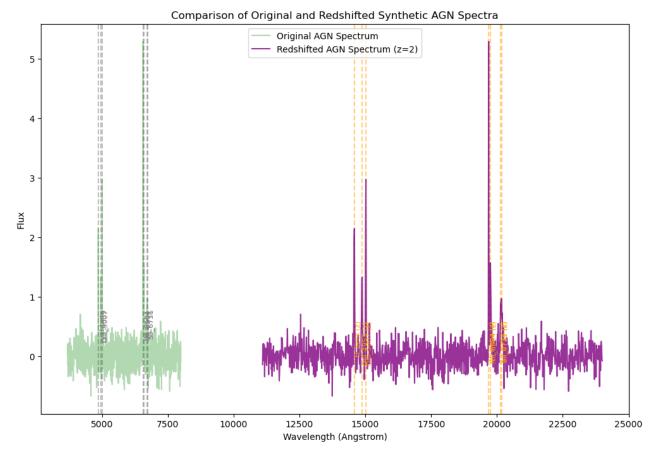
```
Best fit line intensities: [37.68670118 16.85764465 6.57833353 11.32152371
         4.18197575 37.20292448
          -7.59929968]
In [53]: # do another attempt z = 3
         observed wavelengths, observed flux = generate redshifted spectrum(0.12)
         emission line centers = [6563, 4861, 5007, 4959, 6584, 6716, 6731]
         line width = 10
         def model spectrum(wavelengths, redshift, line intensities):
             model flux = wavelengths ** -1.5
             for i, line center in enumerate(emission line centers):
                  shifted center = line center * (1 + redshift)
                 model flux += line intensities[i] * norm.pdf(wavelengths, shifted ce
             return model flux
         def chi_squared(obs_flux, model_flux):
             return np.sum((obs_flux - model_flux) ** 2)
         def fit spectrum(line intensities, redshift):
             model_flux = model_spectrum(observed_wavelengths, redshift, line intensi
             return chi squared(observed flux, model flux)
         N = len(emission line centers) # number of emission lines
         initial line intensities = [10] * N # Initial guess for each line intensity
         # Optimization Model
         best fit = None
         for redshift in np.linspace(0, 1, 100):
             result = minimize(fit spectrum, initial line intensities, args=(redshift
             if best fit is None or result.fun < best fit[1]:</pre>
                  best fit = (redshift, result.fun, result.x)
         best fit flux = model spectrum(observed wavelengths, best fit[0], best fit[2]
         plt.figure(figsize=(10, 6))
         plt.plot(observed wavelengths, observed flux, label="Observed Spectrum", col
         plt.plot(observed wavelengths, best fit flux, label="Best-Fitted Model", col
         plt.xlabel("Wavelength")
         plt.ylabel("Flux")
         plt.title("Observed Spectrum vs Best-Fitted Model")
         plt.legend()
         plt.show()
         print(f"Best fit redshift: {best fit[0]}")
         print(f"Best fit line intensities: {best fit[2]}")
```

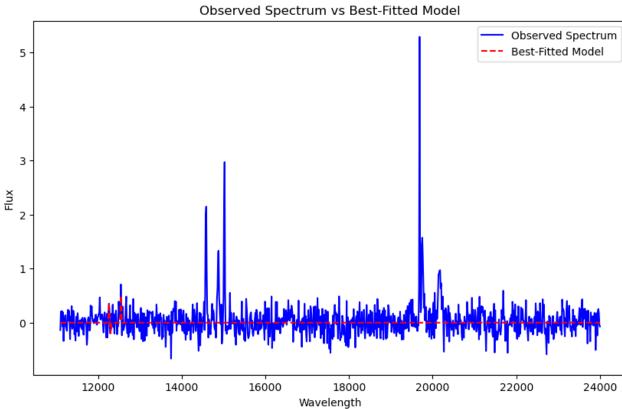




```
Best fit redshift: 0.121212121212122
Best fit line intensities: [30.55266864 32.91603416 19.95838356 26.76956041 16.69475791 18.83784394 10.20122782]
```

```
In [54]: # this does not work for extremely large z (example z = 2) It cannot be corn
         observed wavelengths, observed flux = generate redshifted spectrum(2)
         emission line centers = [6563, 4861, 5007, 4959, 6584, 6716, 6731]
         line width = 10
         def model spectrum(wavelengths, redshift, line intensities):
             model flux = wavelengths ** -1.5
             for i, line center in enumerate(emission line centers):
                  shifted center = line center * (1 + redshift)
                 model flux += line intensities[i] * norm.pdf(wavelengths, shifted_ce
             return model flux
         def chi_squared(obs_flux, model_flux):
             return np.sum((obs_flux - model_flux) ** 2)
         def fit spectrum(line intensities, redshift):
             model_flux = model_spectrum(observed_wavelengths, redshift, line intensi
             return chi squared(observed flux, model flux)
         N = len(emission line centers) # number of emission lines
         initial line intensities = [10] * N # Initial guess for each line intensity
         # Optimization Model
         best fit = None
         for redshift in np.linspace(0, 1, 100):
             result = minimize(fit_spectrum, initial_line_intensities, args=(redshift
             if best fit is None or result.fun < best fit[1]:</pre>
                  best fit = (redshift, result.fun, result.x)
         best fit flux = model spectrum(observed wavelengths, best fit[0], best fit[2]
         plt.figure(figsize=(10, 6))
         plt.plot(observed wavelengths, observed flux, label="Observed Spectrum", col
         plt.plot(observed wavelengths, best fit flux, label="Best-Fitted Model", col
         plt.xlabel("Wavelength")
         plt.ylabel("Flux")
         plt.title("Observed Spectrum vs Best-Fitted Model")
         plt.legend()
         plt.show()
         print(f"Best fit redshift: {best fit[0]}")
         print(f"Best fit line intensities: {best fit[2]}")
```





In []: