

Section A: Python programming

1. Write a python function to compute the mean and standard deviation of a list of numbers.

```

import math
def compute_mean_std(numbers):
    if not numbers:
        return None, None
    mean = sum(numbers)/len(numbers)
    variance = sum((x-mean)**2 for x in numbers)/len(numbers)
    std-dev = math.sqrt(variance)
    return mean, std-dev.

input_str = input("Enter numbers separated by spaces")
numbers = list(map(float, input_str.strip().split()))
mean, std = compute_mean_std(numbers)
print("Mean", mean)
print("Standard Deviation", std)

```

2. What is the difference between a list, a tuple, and a dictionary in python? Give an example of each

Feature	List	Tuple	Dictionary
Syntax	[]	()	{ }
ordered	✓	✓	✓
Mutable	✓	✗	✓
Duplicates	✓	✓	✗ (keys must be unique)

Example of List

Fruits = ["apple", "banana", "cherry"]

Tuple

coordinates = (10.5, 20.3)

Dictionary

student = {"name": "Alice", "age": 21, "grade": "A"}

3. Implement a simple linear regression using numpy without using scikit-learn.

```
import numpy as np
```

```
import matplotlib.pyplot as plt
```

```
u = np.array([1, 2, 3, 4, 5])
```

```
y = np.array([2, 4, 5, 4, 5])
```

```
n = len(x)
```

```
m = (n * np.sum(u * y) - np.sum(u) * np.sum(y)) /
```

```
(n * np.sum(u ** 2) - np.sum(u) ** 2)
```

```
c = (np.sum(y) - m * np.sum(u)) / n
```

```
y_pred = m * u + c
```

```
print(f" slope (m): {m} ")
```

```
print(f" Intercept (c): {c} ")
```

```
plt.scatter(u, y, color="blue", label="original Data")
```

```
plt.plot(u, y_pred, color="red", label="fitted Line")
```

```
plt.xlabel("x")
```

```
plt.ylabel("y")
```

```
plt.title("Simple Linear Regression")
```

```
plt.legend()
```

```
plt.show()
```

(4)

Explain how to handle missing data on a Pandas DataFrame. Provide an example.

Handling missing data on a pandas DataFrame is a common data preprocessing task. Missing values are typically represented as:

Example

```
import pandas as pd
```

```
import numpy as np
```

```
data = { 'Name': ['Alice', 'Bob', 'Charlie', 'David'],
         'Age': [25, np.nan, 30, 22],
         'City': ['New York', 'Los Angeles', np.nan,
                  'Chicago']}
```

3)

```
df = pd.DataFrame(data)
```

print("Original Data Frame")

```
print(df)
```

print("In missing value locations")

```
print(df.isnull())
```

```
df_dropped = df.dropna()
```

print("In After dropping rows with missing data")

```
print(df_dropped)
```

```
df_filled = df.fillna({
```

'Age': df['Age'].mean(),

'City': 'Unknown'

3)

print("In After filling missing values")

```
print(df_filled)
```

Original

	Name	Age	City
0	Alice	25.0	New York
1	Bob	NaN	Los Angeles
2	Charlie	30.0	NaN
3	David	22.0	Chicago

After Drop

	NAME	Age	CITY
0	Alice	25.0	New York
3	David	22.0	Chicago

- ⑤ write a python script to load a csv file and normalize its numeric columns.

```
import pandas as pd
from sklearn.preprocessing import MinMaxScaler
file_path = 'your-file.csv'
df = pd.read_csv(file_path)
print("Original Data:")
print(df.head())
numeric_cols = df.select_dtypes(include=['number']).columns
scaler = MinMaxScaler()
df[numeric_cols] = scaler.fit_transform(df[numeric_cols])
print("In Normalized Data:")
print(df.head())
df.to_csv('normalized_output.csv', index=False)
```

Section B: Probability and statistics.

1. Define the following with examples: conditional probability, Baye's theorem.

Conditional Probability: Probability of the probability of an event A, given that another event B has already occurred

$$P(A|B) = \frac{P(A \cap B)}{P(B)} \text{ where } P(B) > 0$$

Ex: A: card is a king

B: card is a face card

$$P(A \cap B) = P(\text{king}) = \frac{4}{52}$$

$$P(B) = \frac{12}{52}$$

$$P(\text{king} | \text{face card}) = \frac{P(A \cap B)}{P(B)} = \frac{\frac{4}{52}}{\frac{12}{52}} = \frac{1}{3}$$

Bayes Theorem: Bayes theorem gives the probability of an event based on prior knowledge of related events

$$P(A|B) = \frac{P(B|A) \cdot P(A)}{P(B)}$$

Ex: 1% of people have a rare disease, $P(D) = 0.01$

A test detects the disease with

$$99\% \text{ accuracy } P(\text{positive}|D) = 0.99$$

5.1. false $P(C \text{ positive} | \text{NO disease}) > 0.05$

$$P(C|D(\text{positive})) = \frac{P(C|\text{positive}|D) \cdot P(D)}{P(\text{positive})}$$

$$\begin{aligned} P(\text{positive}) &= P(\text{positive}|D) \cdot P(D) + P(\text{positive}|\sim D) \\ &\quad \cdot P(\sim D) \\ &= 0.0594 \end{aligned}$$

$$P(C|D(\text{positive})) = 0.1667$$

2. Given two datasets of exam scores, how would you test if their means are significantly different?

1. Hypothesis

Null hypothesis (H_0): $\mu_1 = \mu_2$

Alternative hypothesis (H_1): $\mu_1 \neq \mu_2$

The two datasets are independent
The data in each group is approximately normally distributed
variances are equal.

```
import numpy as np
```

```
from scipy.stats import ttest_ind
```

```
group1 = [85, 90, 88, 92, 87]
```

```
group2 = [78, 75, 80, 76, 79]
```

```
print(f"t-statistic: {t_stat}")
```

```
print(f"p-value: {p_value}")
```

If $P\text{-value} < 0.05$:

Print("Reject the null hypothesis")

else:

Print("Fail to reject the null hypothesis")

$P\text{-value} < 0.05 \rightarrow$ Significant diff b/w means

$P\text{-value} \geq 0.05 \rightarrow$ No significant difference

3. Explain bias and variance with help of probability distribution.

Bias \rightarrow Error due to simplifying assumptions in the model. It causes the model to miss relevant relationships.

Variance \rightarrow Error due to model sensitivity to training data fluctuations. It causes the model to learn noise.

High Bias

models are too simple

predictions from multiple datasets are clustered together but far from the function.

Distribution: predictions are narrowly centered but not near correct answer.

High variance

Model is too complex

predictions vary widely depending on the dataset

Distribution: predictions are spread out, some near = the true value, some far

4. You roll two dice. The sum is 9. What is the probability that both numbers are even?

Total possible outcomes: $6 \times 6 = 36$.

1. Probability that the sum is 9.

(1,6), (2,5), (3,4), (4,3), (5,2), (6,1) = 6 outcomes

$$\text{Probability} = \frac{6}{36} = \frac{1}{6}$$

2. Probability that both numbers are even, = 9.

$$\text{Probability} = \frac{9}{36} = \frac{1}{4}$$

5. Describe the central limit theorem and give an example in machine learning.

If you take many random samples from any population, and calculate the mean of each sample:

The distribution of those sample means will look like a normal curve as the no. of samples increase even if the original data is not normal.

Example:

Imagine collecting the average test scores from many small classrooms.

Importance

1. Makes predictions easier
2. confidence intervals
3. model evaluation
4. sampling stability