

Printout

```
[ [-2.03315368    0.8163886    6.67385483    7.68245252]
  [ 7.48716856    1.04731142    6.52801461   -4.33628869]
  [-1.31358836    0.65553387   -1.48526632    0.98232123]]
[ [-9.6506007 ]
  [ 1.14817225]
  [13.61110443]
  [-9.62550389]]
[ [0.00308167]
  [0.98943407]
  [0.98920117]
  [0.01304751]]
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QUESTION 4(a)

Neuron1

$$\begin{aligned} &= \text{sigmoid}(x_1 * w_{0,1,0} + x_2 * w_{1,1,0} + x_3 * w_{2,1,0}) = \frac{1}{1 + e^{-(x_1 * w_{0,1,0} + x_2 * w_{1,1,0} + x_3 * w_{2,1,0})}} \\ &= \frac{1}{1 + e^{-(x_1 * -2.03315368 + x_2 * 7.48716856 + x_3 * -1.31358836)}} \end{aligned}$$

Neuron2

$$\begin{aligned} &= \text{sigmoid}(x_1 * w_{0,1,1} + x_2 * w_{1,1,1} + x_3 * w_{2,1,1}) = \frac{1}{1 + e^{-(x_1 * w_{0,1,1} + x_2 * w_{1,1,1} + x_3 * w_{2,1,1})}} \\ &= \frac{1}{1 + e^{-(x_1 * 0.8163886 + x_2 * 1.04731142 + x_3 * 0.65553387)}} \end{aligned}$$

Neuron3

$$\begin{aligned} &= \text{sigmoid}(x_1 * w_{0,1,2} + x_2 * w_{1,1,2} + x_3 * w_{2,1,2}) = \frac{1}{1 + e^{-(x_1 * w_{0,1,2} + x_2 * w_{1,1,2} + x_3 * w_{2,1,2})}} \\ &= \frac{1}{1 + e^{-(x_1 * 6.67385483 + x_2 * 6.52801461 + x_3 * -1.48526632)}} \end{aligned}$$

Neuron4

$$\begin{aligned} &= \text{sigmoid}(x_1 * w_{0,1,3} + x_2 * w_{1,1,3} + x_3 * w_{2,1,3}) = \frac{1}{1 + e^{-(x_1 * w_{0,1,3} + x_2 * w_{1,1,3} + x_3 * w_{2,1,3})}} \\ &= \frac{1}{1 + e^{-(x_1 * 7.68245252 + x_2 * -4.33628869 + x_3 * 0.98232123)}} \end{aligned}$$

Output

$$\begin{aligned} &= \text{sigmoid}(\text{neuron}_1 * w_{0,2,0} + \text{neuron}_2 * w_{1,2,0} + \text{neuron}_3 * w_{2,2,0} + \text{neuron}_4 * w_{3,2,0}) \\ &= \frac{1}{1 + e^{-(\text{neuron}_1 * w_{0,2,0} + \text{neuron}_2 * w_{1,2,0} + \text{neuron}_3 * w_{2,2,0} + \text{neuron}_4 * w_{3,2,0})}} \\ &= \frac{1}{1 + e^{-(\text{neuron}_1 * -9.6506007 + \text{neuron}_2 * 1.14817225 + \text{neuron}_3 * 13.61110443 + \text{neuron}_4 * -9.62550389)}} \\ &= \frac{1}{1 + e^{-\left(\frac{1}{1+e^{-(x_1*-2.03315368+x_2*7.48716856+x_3*-1.31358836)}}*-9.6506007+\frac{1}{1+e^{-(x_1*0.8163886+x_2*1.04731142+x_3*0.65553387)}}*1.14817225+\frac{1}{1+e^{-(x_1*6.67385483+x_2*6.52801461+x_3*-1.48526632)}}*13.61110443+\frac{1}{1+e^{-(x_1*7.68245252+x_2*-4.33628869+x_3*0.98232123)}}*-9.62550389\right)}} \end{aligned}$$

QUESTION 4(b)

(1) $x_1 = 0, x_2 = 0, x_3 = 1$

$$\begin{aligned} \text{Output} &= \frac{1}{1 + e^{-\left(\frac{1}{1+e^{-(0*-2.03315368+0*7.48716856+1*-1.31358836)}}*-9.6506007+\frac{1}{1+e^{-(0*0.8163886+0*1.04731142+1*0.65553387)}}*1.14817225+\frac{1}{1+e^{-(0*6.67385483+0*6.52801461+1*-1.48526632)}}*13.61110443+\frac{1}{1+e^{-(0*7.68245252+0*-4.33628869+1*0.98232123)}}*-9.62550389\right)}} \\ &= \frac{1}{1 + e^{-(-2.044837+0.755792+2.513063-7.003214)}} \\ &= 0.003082 \end{aligned}$$

(2) $x_1 = 0, x_2 = 1, x_3 = 1$

$$\begin{aligned} \text{Output} &= \frac{1}{1 + e^{-\left(\frac{1}{1+e^{-(0*-2.03315368+1*7.48716856+1*-1.31358836)}}*-9.6506007+\frac{1}{1+e^{-(0*0.8163886+1*1.04731142+1*0.65553387)}}*1.14817225+\frac{1}{1+e^{-(0*6.67385483+1*6.52801461+1*-1.48526632)}}*13.61110443+\frac{1}{1+e^{-(0*7.68245252+1*-4.33628869+1*0.98232123)}}*-9.62550389\right)}} \\ &= \frac{1}{1 + e^{-(-9.630533+0.971246+13.523795-0.32501)}} \\ &= 0.989434 \end{aligned}$$

(3) $x_1 = 1, x_2 = 0, x_3 = 1$

$$\begin{aligned} \text{Output} &= \frac{1}{1 + e^{-\left(\frac{1}{1+e^{-(1*-2.03315368+0*7.48716856+1*-1.31358836)}}*-9.6506007+\frac{1}{1+e^{-(1*0.8163886+0*1.04731142+1*0.65553387)}}*1.14817225+\frac{1}{1+e^{-(1*6.67385483+0*6.52801461+1*-1.48526632)}}*13.61110443+\frac{1}{1+e^{-(1*7.68245252+0*-4.33628869+1*0.98232123)}}*-9.62550389\right)}} \\ &= \frac{1}{1 + e^{-(-0.32814+0.933865+13.535578-9.623843)}} \\ &= 0.989201 \end{aligned}$$

(4) $x_1 = 1, x_2 = 1, x_3 = 1$

$$\begin{aligned} \text{Output} &= \frac{1}{1 + e^{-\left(\frac{1}{1+e^{-(1*-2.03315368+1*7.48716856+1*-1.31358836)}}*-9.6506007+\frac{1}{1+e^{-(1*0.8163886+1*1.04731142+1*0.65553387)}}*1.14817225+\frac{1}{1+e^{-(1*6.67385483+1*6.52801461+1*-1.48526632)}}*13.61110443+\frac{1}{1+e^{-(1*7.68245252+1*-4.33628869+1*0.98232123)}}*-9.62550389\right)}} \\ &= \frac{1}{1 + e^{-(-9.499408+1.06261+13.610993-9.50022)}} \\ &= 0.013048 \end{aligned}$$