

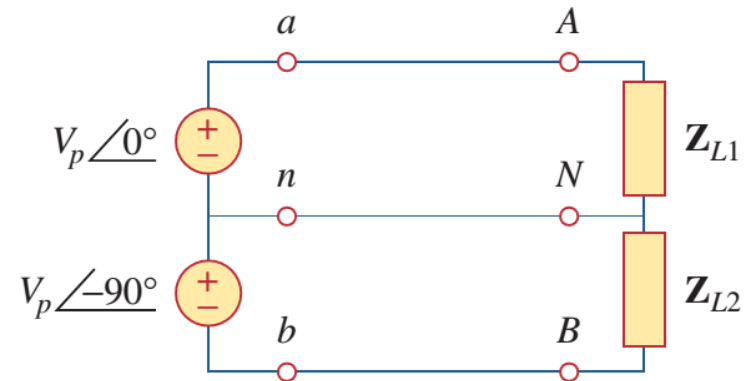
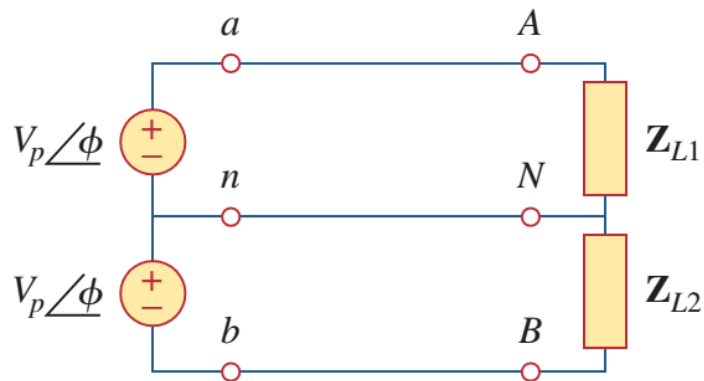


# Lecture 10

## - Three-Phase Circuits

# Single phase vs. Polyphase

- Single-phase power supply
  - For example, two 120V sources with the same phase are connected in series.
  - This allows for appliances to use either 120 or 240V
- Circuits that operate with multiple sources, at the same frequency but *at different phases* are called polyphase.





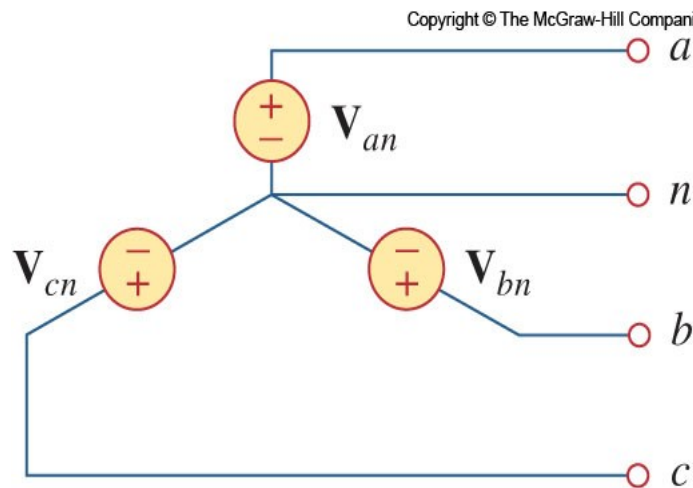
# Outline--Three-Phase Circuits

- Balanced Three-Phase System
  - Balanced sources
  - Balanced loads
- Circuit analysis
  - Phase voltage/current
  - Line voltage/current

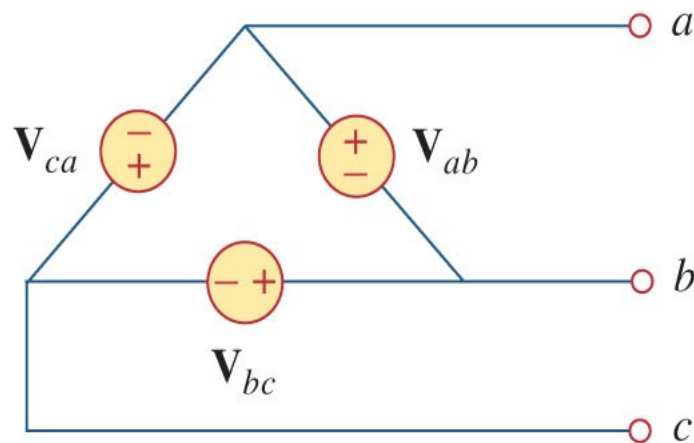
# Balanced Three-Phase Sources

## Connecting the Sources

- Three phase voltage sources can be connected by either four or three wire configurations.
  - Four-wire system accomplished using a Y(Wye) connected source.
  - Three-wire configuration accomplished by Delta connected source.



(a)



(b)

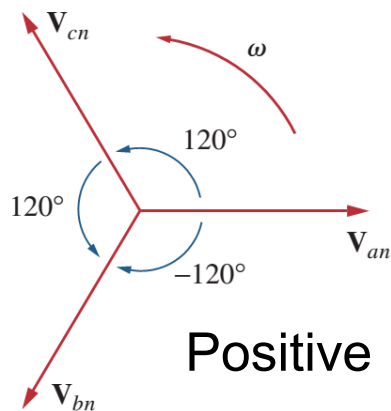
$$V_{an} = V_p \angle 0^\circ$$

$$V_{bn} = V_p \angle -120^\circ$$

$$V_{cn} = V_p \angle -240^\circ \quad , \quad p \leftarrow \dots \dots \dots$$

# Balanced Three-Phase Sources

- Balanced phase voltage are equal in magnitude and are out of phase with each other by 120deg
- It's easy to know  $V_{an} + V_{bn} + V_{cn} = 0$
- Two sequences for the phases:

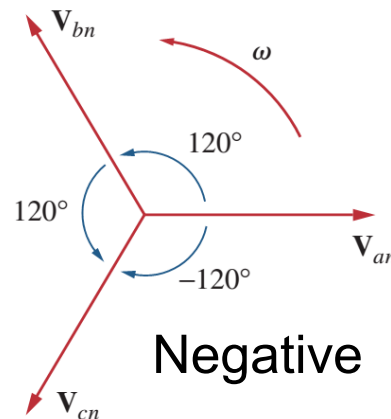


Positive

$$V_{an} = V_p \angle 0^\circ$$

$$V_{bn} = V_p \angle -120^\circ$$

$$V_{cn} = V_p \angle -240^\circ \quad , \quad p \leftarrow \cdot \cdot \cdot \cdot \cdot \cdot$$



Negative

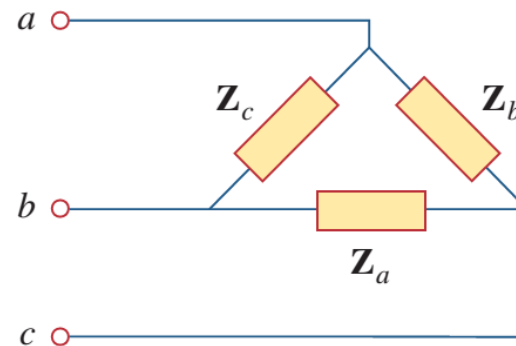
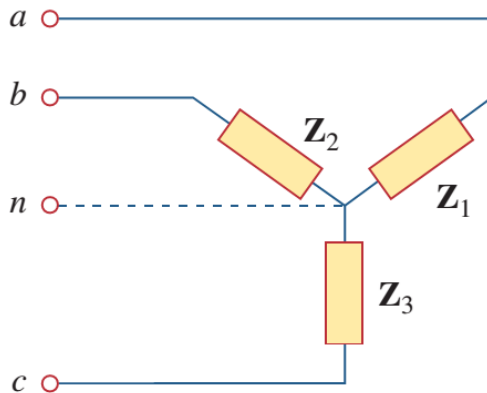
$$V_{an} = V_p \angle 0^\circ$$

$$V_{cn} = V_p \angle -120^\circ$$

$$V_{bn} = V_p \angle -240^\circ \quad , \quad p \leftarrow \cdot \cdot \cdot \cdot \cdot \cdot$$

# Balanced Loads

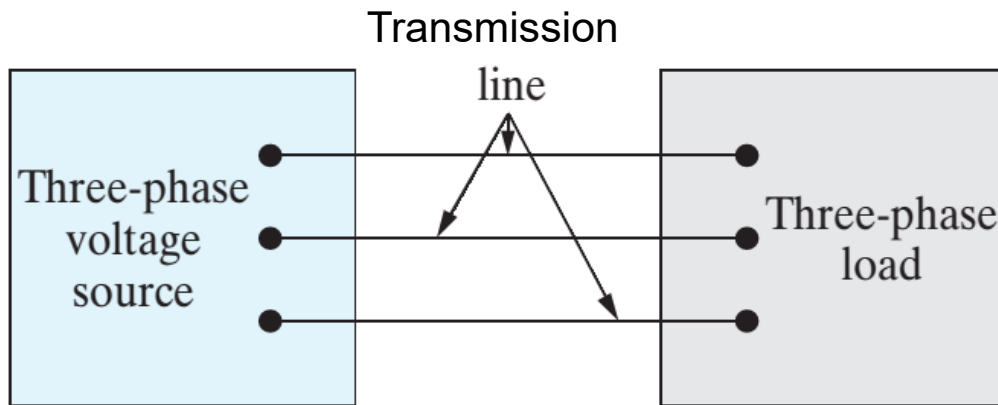
- A balanced load means the same impedance for each load.  
*-- Impedance are equal in magnitude and in phase*
- They may also be connected in either Delta or wye
  - For a balanced wye connected load:  $Z_1 = Z_2 = Z_3 = Z_Y$
  - For a balanced delta connected load:  $Z_a = Z_b = Z_c = Z_\Delta$



- The load impedance per phase for the above configurations can be **interchanged**.



# Source-Load configurations

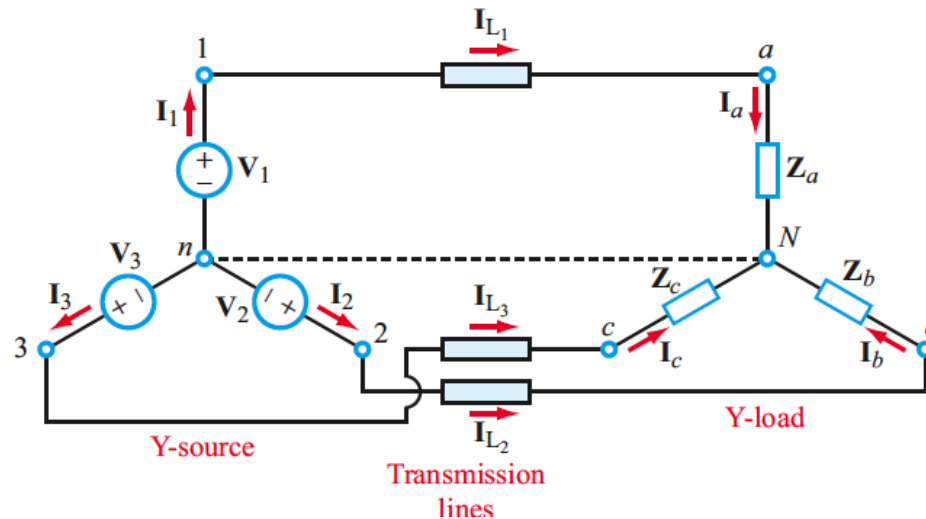


Source	Load
Y	Y
Y	$\Delta$
$\Delta$	Y
$\Delta$	$\Delta$



# Source-Load Configurations

Y-Y



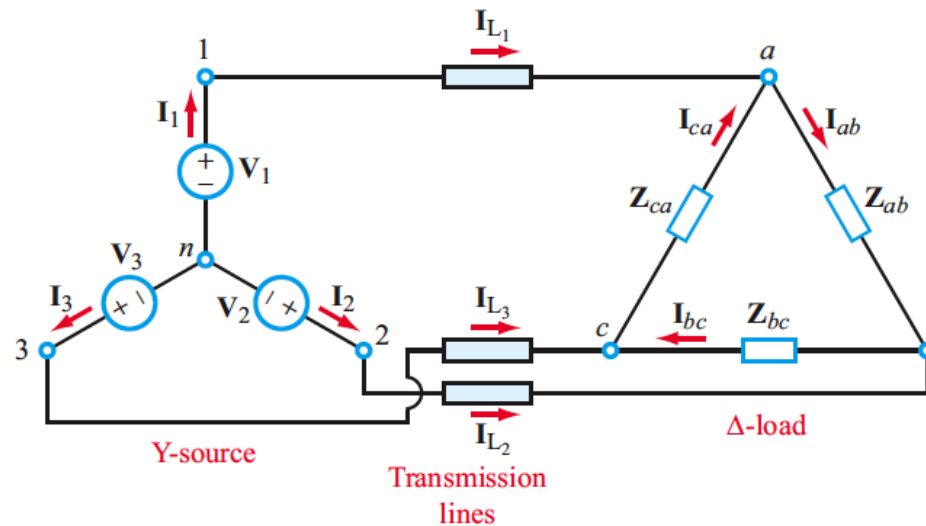
Load Phase Currents

$I_a, I_b, I_c$   
(same as line currents  
 $I_{L1}, I_{L2}, \text{ and } I_{L3}$ )

Load Phase Voltages

$V_{aN}, V_{bN}, V_{cN}$

Y-Delta



Load Phase Currents

$I_{ab}, I_{bc}, I_{ca}$

Load Phase Voltages

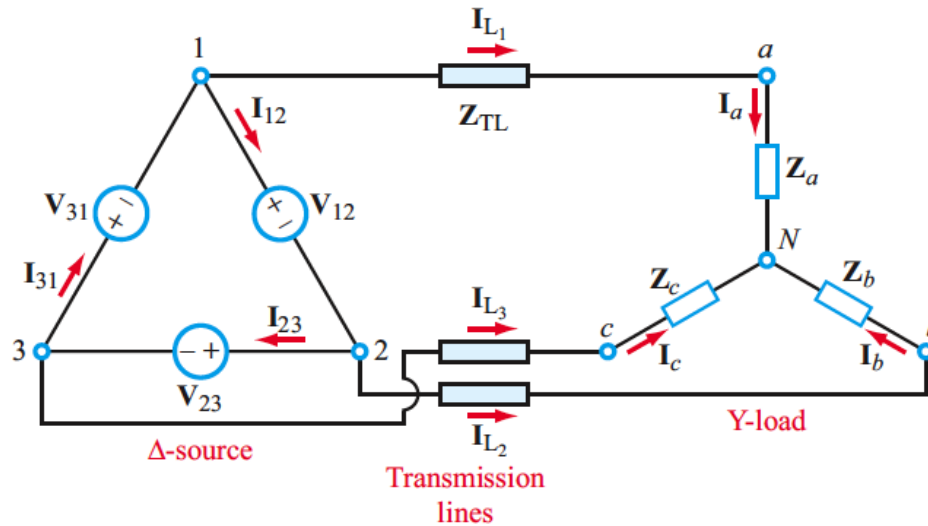
$V_{ab}, V_{bc}, V_{ca}$





# Source-Load Configurations (optional)

Delta-Y



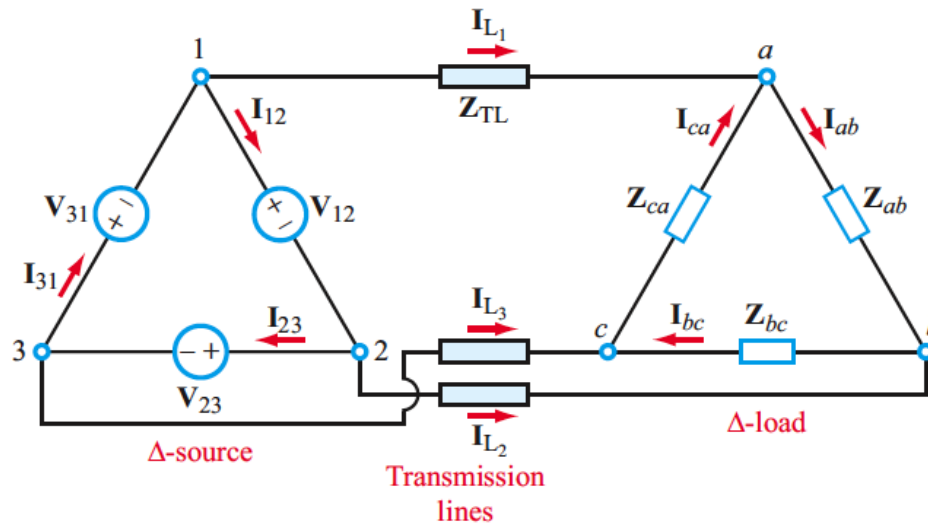
Load Phase Currents

$I_a, I_b, I_c$   
(same as line currents  
 $I_{L1}, I_{L2},$  and  $I_{L3}$ )

Load Phase Voltages

$V_{aN}, V_{bN}, V_{cN}$

Delta-Delta



Load Phase Currents

$I_{ab}, I_{bc}, I_{ca}$

Load Phase Voltages

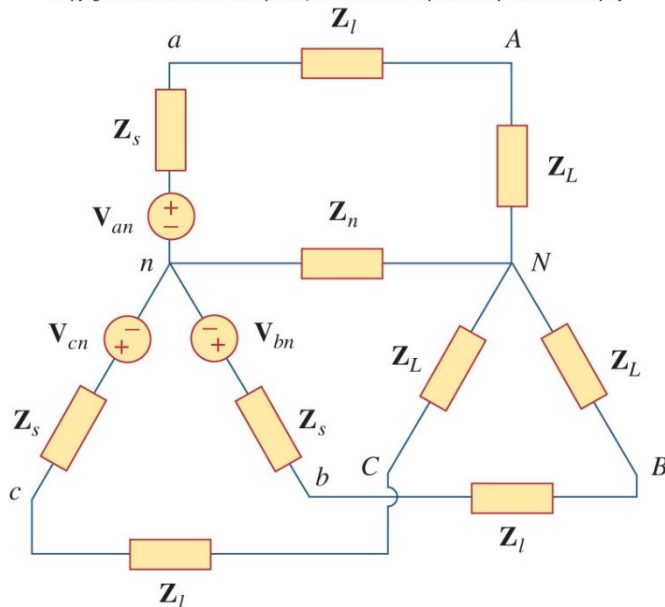
$V_{ab}, V_{bc}, V_{ca}$   
(same as source voltages  
if  $Z_{TL}$  is negligible)

# Balanced Y-Y connection

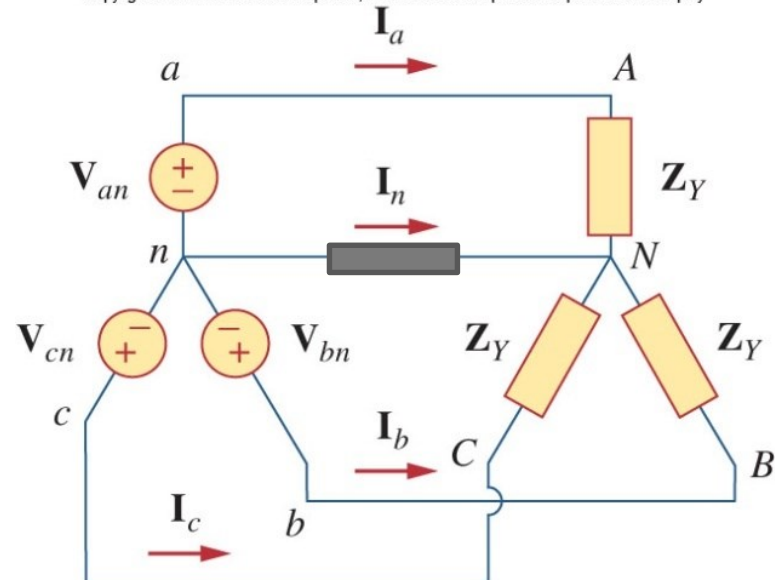
- The load impedances  $Z_Y$  will be assumed to be balanced.
  - This can be the source  $Z_S$ , line  $Z_l$  and load  $Z_L$  together.

$$Z_Y = Z_S + Z_l + Z_L$$

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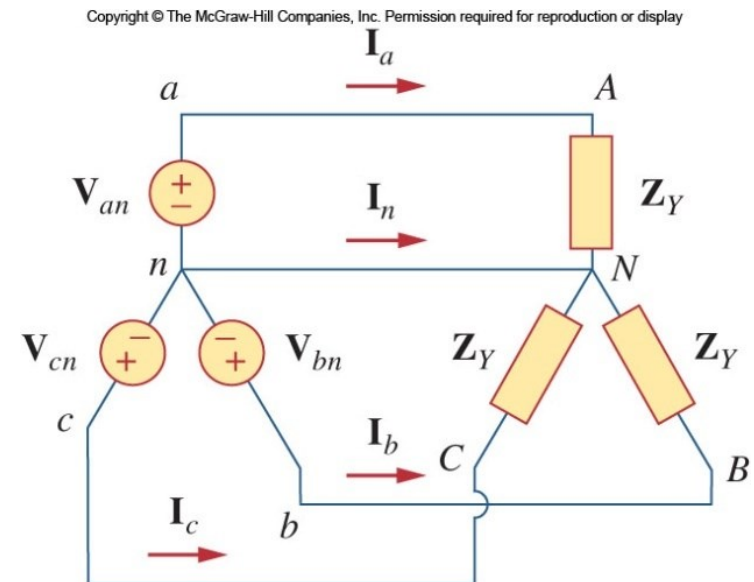
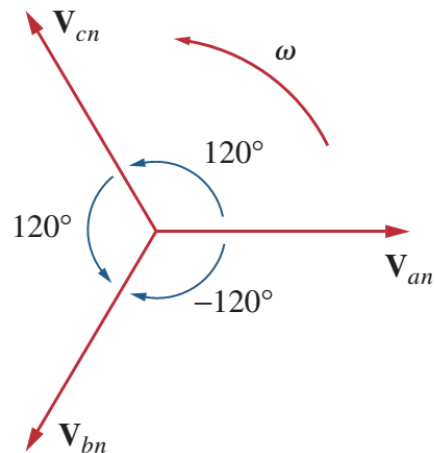
# Phase Voltage & Line-to-Line Voltage

- Use the positive sequence:

Phase Voltage

$$V_{an} = V_p \angle 0^\circ$$

$$V_{bn} = V_p \angle -120^\circ$$

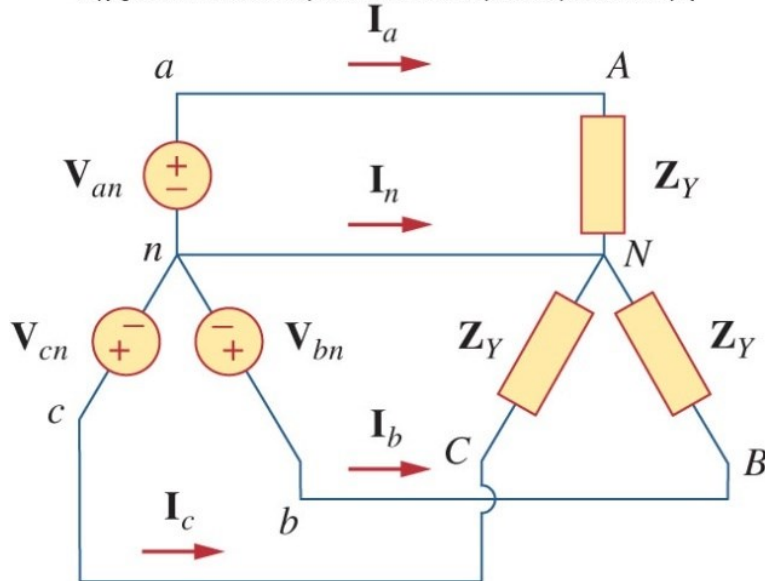


- The line to line voltages (or just line voltages in short):**



# Line Currents

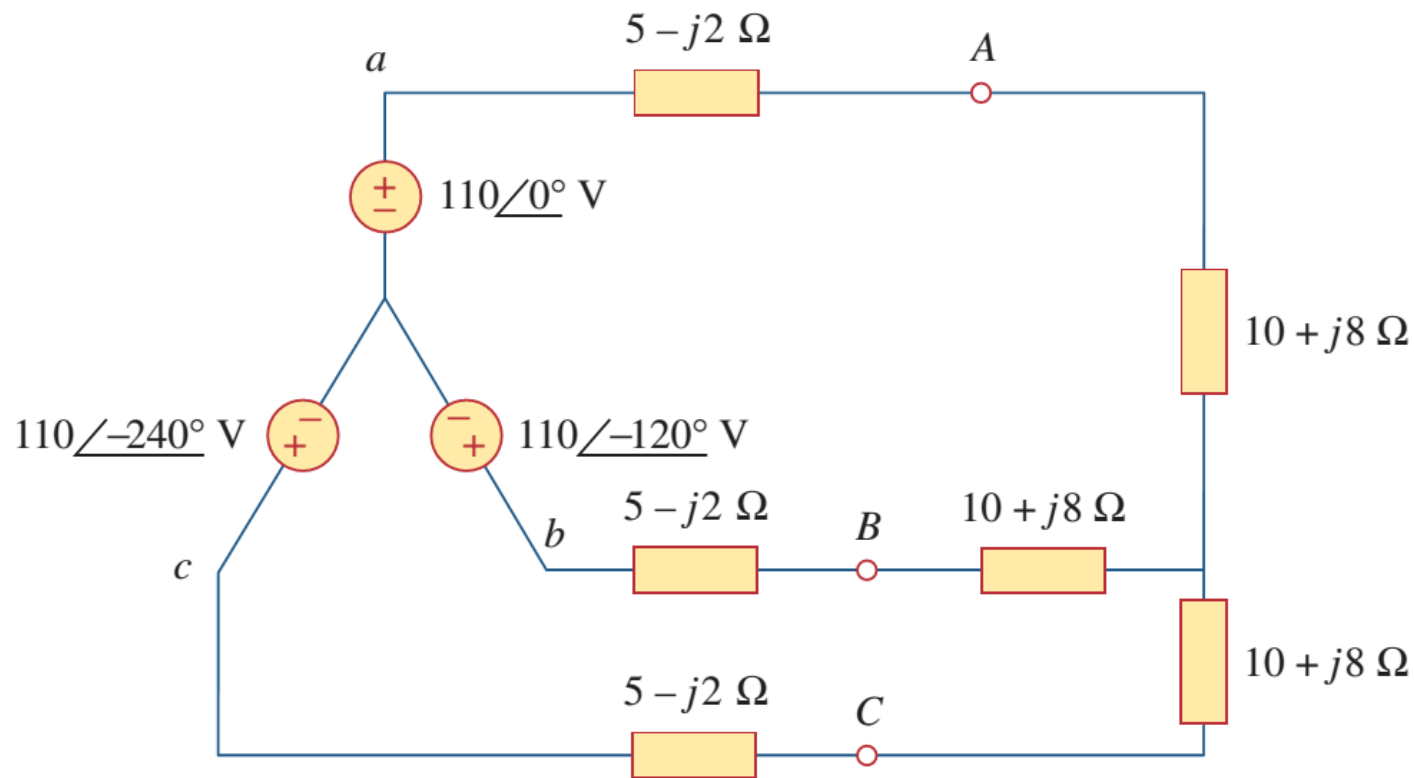
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## Example

- Calculate the line currents.





# Wye- $\Delta$

