

Our SMT model can be described as follows:
 Note that, in the explanation we have taken 10 equations, whereas the problem occurs when the number of equations is quite large.
 Let us consider three cases:

- **Case 0:** Values of a set of equations are given in correct form, e.g., v_1, v_2, \dots, v_{10} are given. Then the system of equations can be formed as follows:

$$\begin{aligned} &\text{for } i \text{ in } \{1, 2, \dots, 10\} : \\ &\quad \text{equation}_i == v_i \end{aligned}$$

- **Case 1:** Instead of v_1, v_2, \dots, v_{10} we know b_1, b_2, \dots, b_{10} where,

$$\begin{aligned} b_1 &= v_1 + 2; & b_2 &= v_2 - 2; & b_3 &= v_3 + 1; & b_4 &= v_4 - 1; & b_5 &= v_5 \\ b_6 &= v_6 - 2; & b_7 &= v_7 + 2; & b_8 &= v_8 - 1; & b_9 &= v_9 + 1; & b_{10} &= v_{10} \end{aligned}$$

Here, we know only b_1, b_2, \dots, b_{10} and the highest error which is ± 2 . Since we do not know the positions of error, we can form the system of constraints as follows:

$$\begin{aligned} &\text{for } i \text{ in } \{1, 2, \dots, 10\} : \\ &\quad b_i - 2 \leq \text{equation}_i \leq b_i + 2 \end{aligned}$$

Note that the errors here are distributed uniformly, i.e., equal number of +2, -2, +1, -1 and 0.

- **Case 2:** Instead of v_1, v_2, \dots, v_{10} we know b_1, b_2, \dots, b_{10} where,

$$\begin{aligned} b_1 &= v_1 + 2; & b_2 &= v_2 - 1; & b_3 &= v_3 + 1 \\ b_i &= v_i \text{ for } i \text{ in } \{4, \dots, 10\} \end{aligned}$$

Errors are injected at 30% places. Since we do not know the positions of error, we have to model it as follows:

$$\begin{aligned} &\text{for } i \text{ in } \{1, 2, \dots, 10\} : \\ &\quad b_i - 2 \leq \text{equation}_i \leq b_i + 2 \end{aligned}$$

Problem: Now in our case, the system of equations is large and highly non-linear. We observed that **Case 0 is solvable in 10-12 sec., Case 1 is solvable in 10-20 sec., but for Case 3 we are not getting any solution even after 24 hours even though the number of errors in Case 2 is much lesser than Case 1.** We want to solve the system of constraints for Case 2 with solution time near to the solution time of Case 1. **We observed that as soon as the b_i approaches towards v_i , the solver takes more time to solve, i.e., Normally distributed error has higher solution time**

as compared to uniformly distributed error. In real life scenario, we encounter errors with normal distribution.

Note:— While solving the system of constraints in Case 2, we have the information that given sequence b_i is near to v_i for most of the cases, e.g., we know that $b_i = v_i$ for approximately 70% times; $b_i = v_i \pm 1$ for approximately 20% times; and so on.

Toy Example:— Since the actual code is quite large, we illustrated the same scenario in a toy example (script and readme file are available at https://github.com/Anonychn/SMT_Toy_Example.git). In the script, we first collected the values from a random array and its updated version. Next, we inject errors to the values as per Case 1 and Case 2 separately. Thereafter, we form the SMT constraints to recover the original array with the help of given erroneous values. Refer to the README file and comments in the scripts for explanation.

Target:— we want our model to work well with errors in normal distribution, as in this case, errors are very less.