

A New Approach to Effective Circuit Clustering*

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Abstract

The complexity of next-generation VLSI systems will exceed the capabilities of top-down layout synthesis algorithms, particularly in netlist partitioning and module placement. Bottom-up clustering is needed to "condense" the netlist so that the problem size becomes tractable to existing optimization methods. In this paper, we establish the DS quality measure, the first general metric for evaluation of clustering algorithms. The DS metric in turn motivates our RW-ST algorithm, a new self-tuning clustering method based on random walks in the circuit netlist. RW-ST efficiently captures a globally good circuit clustering. When incorporated within a two-phase iterative Fiduccia-Mattheyses partitioning strategy, the RW-ST clustering method improves bisection width by an average of 17% over previous matching-based methods.

1 Introduction

Top-down approaches are widely used to cope with increasing problem complexity in layout synthesis. Recursive calls to a partitioning algorithm generate a circuit hierarchy which subsequently guides the placement/routing phases of layout. Typical partitioning objectives such as minimum-width bisection and minimum ratio cut are NP-complete and require such heuristics as simulated annealing [12], greedy k -opt interchange [11], or quadratic optimization (via relaxation [3] [13] or spectral [8] methods). However, the partitioning algorithms used in top-down layout are beginning to fail as designs approach millions of gates: (i) the space/time requirements of current partitioning approaches become infeasible; (ii) the stability and solution quality of iterative methods deteriorate; and (iii) k -way partitioning formulations may force "unnatural" solutions because of their a priori specification of k .

Given these difficulties, bottom-up clustering can enable *successful* top-down partitioning by condensing the circuit netlist and reducing problem size. Clustering is attractive because it avoids making the far-reaching decisions that are inherent in a top-down approach. Moreover, top-down partitioning solutions can be *enhanced* by first condensing the input through bottom-up clustering [1] [2]. Nevertheless, in practice

clustering is avoided because of inherent weaknesses in current bottom-up algorithms, namely, that grouping decisions are based only on local criteria such as the number of connections to modules in an existing cluster. While this locality is needed to maintain reasonable algorithm complexity, it may lead to unfortunate grouping decisions. Thus, top-down partitioning, while it remains tractable, remains the preferred method of decomposing a given layout problem. The goal of clustering is then to reduce problem size while deferring far-reaching decisions until *well-considered* top-down optimizations become feasible.

Previous work in circuit clustering ranges from highly *local* to highly *global* approaches. Generally speaking, local approaches are more efficient but can result in unnatural groupings of modules. On the other hand, global approaches give potentially more useful and "natural" results, but may require prohibitive amounts of computation. For our discussion, two particularly relevant approaches are respectively due to Bui et al. [1] [2] and to Garbers et al. [7].

In [1] [2], Bui et al. proposed a two-phase matching based compaction strategy. With this approach, the modules pairs of a maximal random matching in the netlist graph are used to induce a compacted partitioning instance on $n/2$ vertices which correspond to the matching edges. A heuristic Kernighan-Lin partitioning of this compacted netlist is found and then re-expanded into an initial "flat" starting configuration for a second Kernighan-Lin phase. The approach may be iterated, with matching performed recursively on the compacted netlist until the problem size becomes manageable [2].¹

The approach of [1] [2] in effect performs clustering by finding cliques of size 2, i.e., the matching edges. We may generalize compaction into a more global approach by finding c -cliques for $c > 2$. Even more generally, we could find netlist subgraphs that have size c and a prescribed *density* (e.g., if more than $\epsilon \cdot C(c, 2)$ edges are present among c modules in the netlist, then the c modules would be considered to form a cluster). While density-based clustering is cited in [7] as a folk-

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¹The heuristic justification for this approach [1] [2] is that the Kernighan-Lin k -opt method yields significantly better results when the graph topology is sufficiently dense, i.e., has large average degree. Bui et al. claim that compacting until average degree in the netlist is ≥ 3 suffices for K-L to become essentially optimal. The authors of [1] conjecture that this is because there are fewer local minima in the k -interchange neighborhood structure when the graph has higher average degree.

lore method, it entails checking all module subsets of cardinality c , which is impractical. Hence, the closely related concept of (k, l) -connectivity was recently proposed by Garbers et al. [7] for use in circuit clustering.

If there are k edge-disjoint paths of length l between modules u and v , then u and v are said to be (k, l) -connected; [7] showed that for certain highly structured classes of random inputs, the transitive closure of the (k, l) -connectedness relation gives an equivalent clustering to that induced by the edge density criterion. However, (k, l) -connectivity may yield nonintuitive results: modules v_i and v_j can belong to a cluster even when no module on any path between v_i and v_j belongs to the cluster. Moreover, the values of k and l which lead to the “correct” clustering must be determined experimentally for each netlist; this determination is not easy, as seen in [7].

Three other methods should be noted. The epitaxial growth or “direct” method [6] iteratively adds the most closely connected unclustered module to the current cluster. This method is highly local, and depends on heuristic choices of cluster seeds, the number of clusters, the tie-breaking rules, etc. The global “top-down clustering” method of [15] is essentially equivalent to top-down recursive application of the ratio cut partitioning approach given in [14]. We do not consider it to be a bona-fide clustering algorithm because it assumes heuristic partitioning can be performed on the flat netlist, and our premise is that if such is possible, clustering is not needed. Finally, [4] gave a global method which, like the present work, is based on a random walk in the netlist.

2 A Proper Clustering Metric

Our primary goal is to find an efficient clustering algorithm which is effective in the sense that it loses as little global structural information as possible. To this end, we first present the *DS quality* measure, which gives an objective metric for distinguishing good clustering decompositions and clustering algorithms.

The DS metric is motivated by the following question: given a graph $G = (V, E)$, how easy is it to separate two nodes $s, t \in V$? Observe that (i) if s and t are hard to separate, then there must be more s - t paths and it is more likely that s and t belong to the same natural cluster; (ii) conversely, if s and t are easy to separate, then there must be fewer s - t paths and s and t probably do not belong to the same natural cluster.

We have found that the weighted average of the cluster *degree / separation* (DS) is a robust quality measure: (i) cluster *degree* is the average number of nets incident to each module of the cluster and having at least two pins in the cluster; and (ii) cluster *separation* is the average length of a shortest path between two nodes in the cluster, with separation ∞ if two nodes in the cluster are disconnected.

We calculate the DS quality of a clustering as the weighted average of the DS quality of each cluster, with a cluster containing a single node having DS quality equal to zero. The DS qualities of several different clusterings for the same eight-node graph are shown

in Figure 1.² The intuition behind maximizing the DS quality is that we wish to find a decomposition of the graph such that nodes will *on average* have the highest possible degree and the shortest possible separation from the other nodes in their respective clusters.

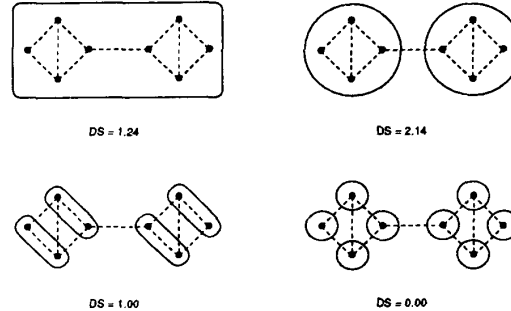


Figure 1: DS quality of various clusterings of the same graph.

The DS quality suggests that the goal of a clustering algorithm should entail finding the neighborhood structure of a node v and comparing it with the neighborhood structure of other nodes to determine which nodes should be clustered with v . This notion of recognizing a node’s neighborhood structure motivates our random walk based clustering algorithm.³

3 Random Walks for Clustering

We now present our new RW-ST methodology, which computes a circuit clustering based on a random walk in the netlist graph. A *random walk* is a discrete-time stochastic process which iteratively moves from the current module (vertex) to a random adjacent module, with all adjacencies equiprobable. The *cover time* of G is the maximum, over all possible starting vertices, of the expected length of a random walk that visits all vertices in G . The following result shows that a random walk will with high probability manage to explore the netlist structure in a small number of steps.

Fact: The cover time of a random walk in a d -regular graph of n nodes is $O(n^2)$ and $\Omega(n \log n)$, and there are examples which show that both bounds are tight [10]. \square

The $O(n^2)$ upper bound also applies to cover times for the class of d -bounded graphs [5], which includes gate-level netlists. Therefore, we may compute a single random walk of length $\Theta(n^2)$ and expect to sample the entire netlist graph.

We propose a method for extracting clusters from the random walk via the following concept of a *cycle*. Consider the sequence of nodes encountered during

²For example, each cluster in the 2-clustering has average node degree = 10/4, and average separation = 14/12.

³Additional motivations for the DS metric and the random-walk methodology, based on the theory of graph spectra and intrinsic graph structure, are discussed in [9].

the random walk. A *cycle* is a contiguous subsequence $\{v_p, v_{p+1}, \dots, v_q\}$ in the walk with $v_p = v_q$ and all v_i distinct, $i = p, p+1, \dots, q-1$. The set of modules in each cycle should correspond to (part of) a natural cluster because if there is a more tightly coupled node subset of the cycle, then the random walk will recur (i.e., complete a smaller cycle) within that subset and we would not have found the original cycle. This is shown intuitively in Figure 2, where the *y-y* portion of the walk does not delimit a natural cluster since it contains a denser *x-x* cycle; the *x-x* cycle does not contain any denser portion, so we say that it is a bona fide cluster.

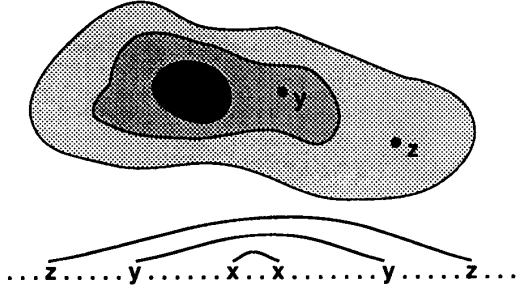


Figure 2: Progress of a random walk through areas with different edge density.

We have designed a *linear-time* algorithm for identifying all of the cycles in a random walk. This algorithm is given in Figure 3.

| Find-Cycles(<i>RW</i>) |
|--|
| Input: A sequence of nodes <i>RW</i> |
| for each node <i>i</i> |
| <i>visited</i> [<i>i</i>] := FALSE |
| <i>first</i> := 1 |
| <i>last</i> := 1 |
| <i>visited</i> [<i>last</i>] := TRUE |
| while <i>last</i> < <i>RW</i> |
| increment <i>last</i> |
| if <i>visited</i> [<i>RW</i> [<i>last</i>]] = TRUE |
| while <i>RW</i> [<i>first</i>] ≠ <i>RW</i> [<i>last</i>] |
| <i>visited</i> [<i>RW</i> [<i>first</i>]] := FALSE |
| increment <i>first</i> |
| increment <i>first</i> |
| <i>visited</i> [<i>RW</i> [<i>last</i>]] := TRUE |

Figure 3: Finding cycles in linear time.

In [4], a random walk was computed in the netlist, *maximal* cycles $C(v_j)$ were determined for all modules v_j , and then the transitive closure of the relation \bowtie , defined by $v_a \bowtie v_b$ if $v_a \in C(v_b)$ and $v_b \in C(v_a)$, was used to induce a heuristic clustering. However, the experimental results of [4] fail to reflect the intuitively “correct” circuit organization. Our present work offers a different approach, the RW-ST algorithm, which

extracts a good heuristic clustering from the cycle information. It should be emphasized that the RW-ST is a heuristic and that we do not yet have strong theoretical justification for its observed success.

The RW-ST algorithm clusters node pairs based on their *sameness*. The sameness of nodes u and v reflects the commonality of the sets of nodes that are visited in cycles originating at u and at v . To calculate the sameness, for each node v we must keep track of how often a node u occurs in some cycle originating at v . This number is saved in the array *CC* (CycleCount).

| Sameness(<i>u</i> , <i>v</i>) |
|--|
| Input: A pair of nodes <i>u</i> and <i>v</i> |
| Output: The sameness value <i>S</i> of <i>u</i> , <i>v</i> |
| if (<i>CC</i> [<i>u</i>][<i>v</i>] = 0) or (<i>CC</i> [<i>v</i>][<i>u</i>] = 0) |
| <i>S</i> := 0 |
| else |
| <i>S</i> := 2 · (<i>CC</i> [<i>u</i>][<i>v</i>] + <i>CC</i> [<i>v</i>][<i>u</i>]) |
| for each node <i>w</i> in the circuit |
| if (<i>w</i> ≠ <i>u</i>) and (<i>w</i> ≠ <i>v</i>) |
| if <i>CC</i> [<i>u</i>][<i>w</i>] > <i>CC</i> [<i>v</i>][<i>w</i>] |
| <i>S</i> := <i>S</i> + 4 · <i>CC</i> [<i>v</i>][<i>w</i>] - <i>CC</i> [<i>u</i>][<i>w</i>] |
| else |
| <i>S</i> := <i>S</i> + 4 · <i>CC</i> [<i>u</i>][<i>w</i>] - <i>CC</i> [<i>v</i>][<i>w</i>] |

Figure 4: Computing sameness of two nodes.

Using the *CC* array, the sameness value for nodes u and v is calculated as shown in Figure 4. If both *CC*[*u*][*v*] and *CC*[*v*][*u*] are greater than zero, i.e., each node occurs at least once in the other's cycles, sameness is initialized to $2 \cdot (\text{CC}[u][v] + \text{CC}[v][u])$. For each node w , the u - v sameness is increased if the values *CC*[*u*][*w*] and *CC*[*u*][*v*] are approximately equal; the sameness is decreased if these quantities vary by a significant amount. To be specific, for each node w in the circuit other than nodes u and v , we add $4 \cdot \min - \max$ to the sameness value, where *min* and *max* are respectively the smaller and larger of the two values *CC*[*u*][*w*] and *CC*[*v*][*w*].

Note that the term $4 \cdot \min - \max$ measures the commonality of nodes u and v with respect to w . If *min* and *max* are equal, sameness is increased by $3 \cdot \min$; if *min* is zero or if *max* is considerably greater than *min*, sameness is decreased by *max*. Intuitively, this bias toward increasing the sameness affords some leeway in how close *min* and *max* must be in order to still have a positive impact on the sameness value; this is because the random walk cannot guarantee to visit u and v equally often even if they look identical to the rest of the circuit.

As shown in Figure 5, algorithm RW-ST first finds and processes all cycles in the random walk, then computes sameness for all node pairs, and finally clusters those node pairs with sameness greater than zero. In some sense, the sameness computation within the random walk implicitly compares the neighborhood structures of a given node pair. The time complexity of RW-ST is a function of the time required to process

| |
|--|
| RW-ST(G) |
| Input: A graph G |
| Output: A set of clusters C |
| Construct a random walk RW on G |
| Find-Cycles(RW) |
| for each node u in G |
| $C(u) := u$ |
| for each pair of nodes u and v in G |
| $S := \text{Sameness}(u, v)$ |
| if $S > 0$ |
| $C(u) := C(u) \cup C(v)$ |

Figure 5: High-level description of RW-ST.

the random walk and the time required to calculate sameness for all node pairs. As mentioned above, we use a random walk of length $O(n^2)$ and find all cycles in the random walk in $O(n^2)$ time. Processing a cycle of length l_c requires $O(l_c)$ operations, yielding worst-case time complexity of $O(n^3)$ to process the random walk. However, in practice the average l_c value seems to grow sublinearly in n . Calculating the sameness of a node pair requires $O(n)$ operations, resulting in $O(n^3)$ time to calculate sameness values for all $O(n^2)$ node pairs. Since processing the random walk and calculating sameness values both have complexity $O(n^3)$, the overall worst-case complexity of RW-ST is $O(n^3)$. RW-ST is observed to be much faster since most node pairs have no cycles in common, thus eliminating the need to calculate their sameness. The space requirements of our heuristic are $O(n^2)$ because the CC array records the cycle count for each node pair. Sparse matrix techniques can be used to reduce the required space at the expense of added time complexity.

4 Experimental Results

We tested the RW-ST method on two very distinct classes of inputs: (i) the random clustered inputs $G_{Gar}(m, n, p_{int}, p_{ext})$ studied by Garbers et al. [7], and (ii) the Primary and Test circuit netlists from the MCNC benchmark suite. Three different experiments were performed: (1) discovery of known clusters in G_{Gar} graphs; (2) DS measures of MCNC benchmark clusterings generated by RW-ST and the matching based compaction (MBC) scheme of Bui et al. [2]; (3) two-phase Fiduccia-Mattheyses (FM) style partitioning using RW-ST and MBC clusterings.

Garbers et al. [7] presented a class of random graphs $G_{Gar}(m, n, p_{int}, p_{ext})$, where m is the number of clusters, n is the size of a cluster, and an edge (u, v) is independently present with probability p_{int} if u and v are in the same cluster and probability p_{ext} otherwise. We used this class of random examples in our first set of experiments, to determine whether RW-ST could find the “correct” graph clustering. Our results are compared against the published statistics in [7]. The RW-ST algorithm was run on walks of length $(nm)^2$ and $10(nm)^2$ in order to see how walk

length affected solution quality. The results of Table 1 show that RW-ST gives much more consistent results than (k, l) -connectivity. For walks of length $10(nm)^2$, RW-ST found 10 distinct clusters for each benchmark tested. In contrast, (k, l) -connectivity found “correct” clusterings for only two of the benchmarks, even when we allow the best results over a range of k values. This gives experimental confirmation of the self-tuning property inherent in RW-ST.

The “proper” field in the table indicates which of the 10-clustering or the 1-clustering (i.e., the complete circuit) has higher DS quality. Note that for $G_{Gar}(10, 100, 0.1, 0.004)$ these two values are nearly identical, i.e. this circuit no longer has an obvious clustering structure by our criterion.

The second set of experiments compared the RW-ST method with the matching based compaction (MBC) method of Bui et al. [2] by examining the DS quality of their respective clusterings on MCNC benchmarks. To ensure a “fair” comparison, we required the MBC clustering to have the same number of clusters as the RW-ST clustering. The original MBC results in [2] were based on constructing a clustering by finding a random maximal matching of the nodes. However, the number of clusters in an RW-ST clustering will normally be much less than half the original size of the circuit. We therefore modified the original MBC code to iteratively compute maximal random matchings, with each new matching performed on the graph induced from the previous clustering, until the desired reduction in problem size was obtained.

Table 2 shows the DS quality of the RW-ST and MBC clusterings. The RW-ST clusterings uniformly dominate the MBC clusterings in terms of DS quality. In addition, the improvement in DS quality is greater for larger circuits, possibly indicating that the random matching method breaks down as the problem size increases. For the two large examples Test04 and Test05, we observe improvements in DS quality of over 30%. Finally, note that the work of [4] only analyzed the Primary1 and bml benchmarks, obtaining DS qualities of 0.922 and 0.852, respectively.

To further confirm the greater utility of the RW-ST clusterings over MBC clusterings, we ran Fiduccia-Mattheyses (FM) partitioning on the resulting clustered graphs. These results are also summarized in Table 2, and we readily observe that the MBC clusterings produce very poor partitionings. This is somewhat surprising, since random matching based clustering was reported to be an efficient way of obtaining good initial starting points for the Kernighan-Lin approach [1] [2].

Our final experiments tested the original conjecture in [1], namely, that a good clustering will improve the solution quality of FM partitioning. For each heuristic clustering, we applied a two-phase FM algorithm which in the first phase partitioned the graph induced by the clustering, and then in the second phase used the expanded partition from the first phase as the starting point for FM partitioning on the “flat” circuit.

The results of this experiment are summarized in Table 3. Note that the results presented in Tables 2

| m | n | p_{int} | p_{ext} | proper (by DS) | Garbers (k, l) Big/Small | RW-ST (nm) ² Big/Small | RW-ST $10(nm)$ ² Big/Small |
|-----|-----|-----------|-----------|-------------------|---------------------------------|--|--|
| 100 | 10 | 0.1 | 0.0001 | 10 | (2,2) 9/3 | 10/57 | 10/20 |
| 100 | 10 | 0.1 | 0.0002 | 10 | (2,2) 3/3 | 10/62 | 10/20 |
| 100 | 10 | 0.1 | 0.0003 | 10 | (2,2) 3/0 | 10/90 | 10/24 |
| 100 | 10 | 0.1 | 0.0004 | 10 | (2,2) 1/0 | 10/88 | 10/27 |
| 100 | 10 | 0.1 | 0.001 | 10 | (3,2) 9/49 | 10/264 | 10/61 |
| 100 | 10 | 0.1 | 0.002 | 10 | (3,2) 1/45 | 6/881 | 10/242 |
| 100 | 10 | 0.1 | 0.003 | 10 | (3,2) 2/40 | 0/1000 | 10/427 |
| 100 | 10 | 0.1 | 0.004 | 10/1 | (3,2) 1/40 | 0/1000 | 10/527 |

Table 1: Comparison of random walk based clustering with (k, l) -connectivity based clustering. Randoms walks of lengths $(nm)^2$ and $10(nm)^2$ were examined. The results give the numbers “Big” and “Small” for each clustering: following the presentation of Garbers et al., “Big” is defined as the number of clusters containing more than $\frac{1}{10}n$ nodes, while “Small” is the number of nodes that do not belong to any “Big” cluster.

| Benchmark | Size | MBC | | | RW-ST | | |
|-----------|------|-------|-------------|---------|-------|-------------|---------|
| | | DS | Areas | Net cut | DS | Areas | Net cut |
| 19ks | 2844 | 1.166 | 5619:5383 | 456 | 1.578 | 5501:5501 | 153 |
| bm1 | 882 | 1.189 | 1812:1668 | 94 | 1.221 | 2197:1283 | 39 |
| PrimGA1 | 833 | 1.258 | 1719:1712 | 82 | 1.325 | 2180:1251 | 37 |
| PrimSC1 | 833 | 1.258 | 1377:1376 | 91 | 1.325 | 1701:1052 | 40 |
| PrimGA2 | 3014 | 1.238 | 4187:4186 | 303 | 1.566 | 4464:3909 | 154 |
| PrimSC2 | 3014 | 1.238 | 3877:3829 | 266 | 1.566 | 4079:3627 | 145 |
| Test02 | 1663 | 1.231 | 38141:18909 | 75 | 1.593 | 37132:19918 | 42 |
| Test03 | 1607 | 1.185 | 14748:7481 | 132 | 1.566 | 12629:9600 | 74 |
| Test04 | 1515 | 1.297 | 21105:20935 | 61 | 1.879 | 21055:20985 | 45 |
| Test05 | 2595 | 1.275 | 62437:10161 | 51 | 1.689 | 39067:33531 | 10 |
| Test06 | 1752 | 1.331 | 8485:8483 | 381 | 1.367 | 9444:7524 | 89 |

Table 2: DS qualities and Fiduccia-Mattheyses partitioning results of RW-ST and MBC clusterings.

and 3 are the best of 20 trials. We compared the results from running the two-phase FM partitioning algorithm on RW-ST and MBC clusterings against the results from running FM partitioning on the original circuit. Also in conformance with [2] we verified that the average degrees of the MBC clustering graphs were all greater than three (in fact, they ranged from 8 to 15, which more than meets the criterion given by Bui et al. [2] for the two-phase strategy to return “near-optimal” Kernighan-Lin results). In both cases there was a significant improvement over the standard FM solution quality, with a 12% improvement obtained using MBC clusterings and a 17% improvement obtained using RW-ST clusterings. These results in some sense confirm the conclusions of [2].

An interesting observation is that the huge discrepancy in FM partition quality between the RW-ST and MBC clusterings, as shown in Table 2, are not reflected in the two-phase FM partitioning results, i.e., a large improvement in the quality of the starting partition does not translate into a correspondingly large

increase in the quality of the final partition.

5 Extensions

There are many promising directions for future work. We are currently pursuing a parallel implementation of the random walk methodology. In other words, we partition the random walk computation evenly among p available processors; the cycle-finding within the random walks is also performed on separate processors. This is appropriate for two reasons: (i) the hierarchical organization and sparsity of real netlist graphs permit only very short self-avoiding walks (i.e., cycles), and so little information is lost by breaking the random walk up among several processors; and (ii) results of Coppersmith et al. [5] show that the separate walks together will reproduce a single long walk.⁴ This parallel approach would achieve perfect speedup over our current uniprocessor formulation.

⁴This is in the sense that two random walks will “collide” within a very short time when the graph is of low maximum degree and small diameter, as is the case with netlist graphs.

| Benchmark | Size | Standard FM | | MBC | | RW-ST | |
|-----------|------|-------------|-------------|-------------|-------------|-------------|-------------|
| | | Areas | Net cut | Areas | Net cut | Areas | Net cut |
| 19ks | 2844 | 5501:5501 | 151 (1.000) | 5501:5501 | 156 (1.033) | 5501:5501 | 146 (0.967) |
| bm1 | 882 | 1740:1740 | 65 (1.000) | 1740:1740 | 54 (0.831) | 1740:1740 | 58 (0.892) |
| PrimGA1 | 833 | 1716:1715 | 66 (1.000) | 1718:1713 | 48 (0.727) | 1716:1715 | 47 (0.712) |
| PrimSC1 | 833 | 1377:1376 | 59 (1.000) | 1377:1376 | 61 (1.034) | 1377:1376 | 58 (0.983) |
| PrimGA2 | 3014 | 4187:4186 | 242 (1.000) | 4187:4186 | 187 (0.773) | 4187:4186 | 165 (0.682) |
| PrimSC2 | 3014 | 3853:3853 | 235 (1.000) | 3858:3848 | 175 (0.745) | 3853:3853 | 159 (0.677) |
| Test02 | 1663 | 37132:19918 | 42 (1.000) | 37132:19918 | 42 (1.000) | 37132:19918 | 42 (1.000) |
| Test03 | 1607 | 11115:11114 | 84 (1.000) | 13729:8500 | 59 (0.702) | 13188:9041 | 71 (0.845) |
| Test04 | 1515 | 40732:1308 | 12 (1.000) | 40938:1102 | 20 (1.667) | 40932:1108 | 14 (1.167) |
| Test05 | 2595 | 38753:33845 | 24 (1.000) | 62586:10012 | 4 (0.167) | 39089:33509 | 5 (0.208) |
| Test06 | 1752 | 8484:8484 | 87 (1.000) | 8484:8484 | 83 (0.954) | 8484:8484 | 82 (0.943) |

Table 3: Comparison of two-phase Fiduccia-Mattheyses partitioning of random walk clusterings and random matching based clusterings. Standard Fiduccia-Mattheyses partitioning results are included as a control. RW-ST clusterings lead to a 17% improvement in net cut over standard FM.

We also hope to use the DS quality measure as the basis of other “implicitly global” clustering methods. Certainly, standard combinatorial methods and direct epitaxial-growth approaches can both be modified to incorporate the DS criterion within the clustering objective. Finally, the concept of a “natural clustering” – one that is independent of both the number and size of the clusters – gives rise to new and interesting layout problems. In particular, the placement phase of layout becomes one of placing *malleable*, variable-size clusters which are of varying DS quality; this is certainly of independent research interest. Following the basic premise of our work, the natural clustering will also enable use of more sophisticated optimizations such as the spectral and relaxation methods in the context of “fast placement” for the next generation standard-cell and sea of gates designs.

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