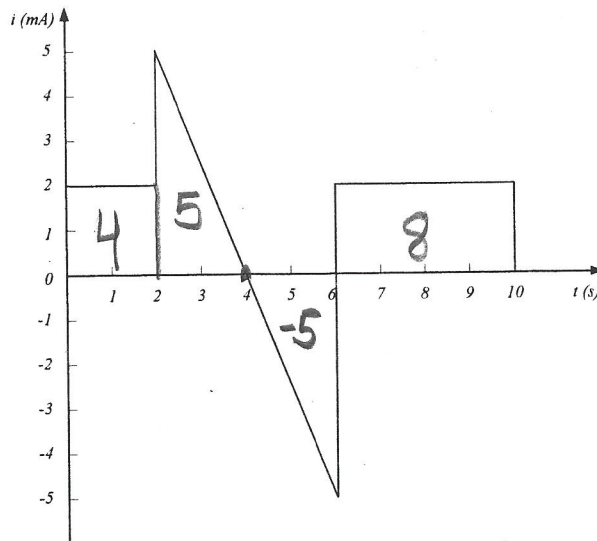


**Question 1(i) (10 marks):**

The current flowing through an element is as shown in the figure below. Determine the total charge that passed through the element from  $t=0$  s to:

- (a)  $t=2$  s    (b)  $t=4$  s    (c)  $t=6$  s    (d)  $t=10$  s



$$\begin{aligned} a) \quad i &= \frac{dq}{dt} \\ dq &= i dt \\ q &= \int_0^2 i dt \\ q &= 2 \times 2 \\ q &= 4C \end{aligned}$$

$$\begin{aligned} b) \quad q &= \int_0^4 i dt \\ q &= 4 + 5 \\ q &= 9C \end{aligned}$$

$$\begin{aligned} c) \quad q &= \int_0^6 i dt \\ &= 4 + 5 - 5 \\ &= 4C \end{aligned}$$

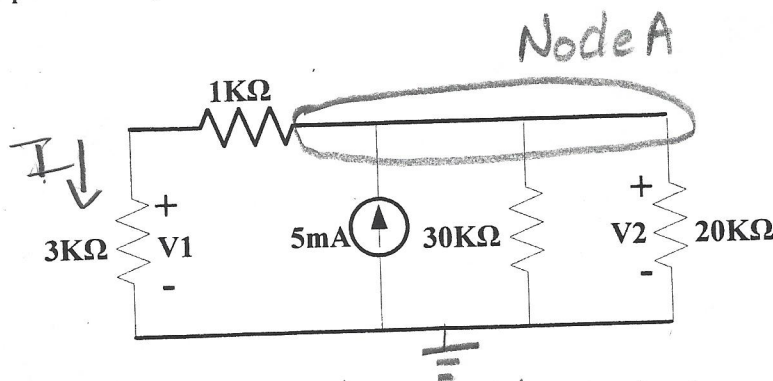
$$\begin{aligned} d) \quad q &= \int_0^{10} i dt \\ &= 4 + 5 - 5 + 8 \\ &= 12C \end{aligned}$$

$Q_{2s}$	$Q = 4C$	✓
$Q_{4s}$	$Q = 9C$	✓
$Q_{6s}$	$Q = 4C$	✓
$Q_{10s}$	$Q = 10C$	✓

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**Question 1(ii) (15 marks):**

For the circuit shown in the figure below, find: (a)  $v_1$ , (b)  $v_2$ , (c) the power dissipated in  $3\text{ k}\Omega$  (d) the power dissipated in  $20\text{ k}\Omega$ , and (e) the power supplied by the current source?



a) Using Result in part b)

$$V_a = 15\text{V}$$

$$I = \frac{V_a}{4} = \frac{15}{4}\text{ mA}$$

$$R = 3\text{ k}\Omega$$

$$V_1 = I \times R = \left(\frac{15}{4}\right) \times (3)$$

$$\boxed{V_1 = 11.25\text{V}}$$

b) Using nodal analysis

Node A: (Assuming all current in mA and resistance in  $\text{k}\Omega$ )

$$\frac{V_a}{20} + \frac{V_a}{30} - 5 + \frac{V_a}{4} = 0$$

$$\frac{3V_a + 2V_a - 300 + 15V_a}{60} = 0$$

$$20V_a = 300$$

$$V_a = 15\text{V}$$

Since  $V_a = V_2$

$$\boxed{V_2 = 15\text{V}}$$

c)  $P = i \times v$

$$= \frac{15}{4} \times 11.25$$

$$= 42.19\text{ mW}$$

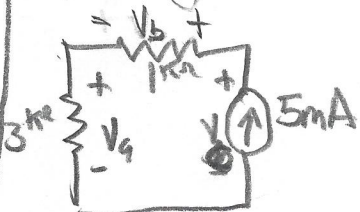
$$= 11.25\text{ mW}$$

d)  $P = i \times v$

$$= \frac{15}{20} \times 15$$

$$\boxed{V = 11.25\text{ mW}}$$

e) using KVL



$$V_a + V_b + V_c = 0$$

$$V_a = 11.25\text{V}$$

$$V_b = +15\text{V}$$

$$V_c = ?$$

$$11.25 + 15 + \frac{V_c}{4} = 0$$

$$V_c = -23.25\text{V}$$

$$P = i \times v$$

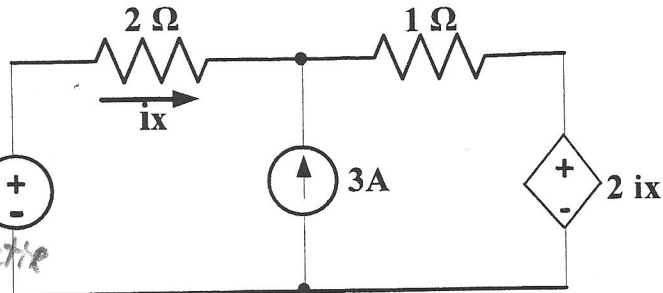
$$= 0.005 \times -23.25$$

$$\boxed{P = -116.25\text{ mW}}$$

(a)	$V_1 = 11.25\text{V}$
(b)	$V_2 = 15\text{V}$
(c)	$P_{3\text{k}\Omega} = 42.19\text{ mW}$
(d)	$P_{20\text{k}\Omega} = 11.25\text{ mW}$
(e)	$P_{\text{source}} = -116\text{ mW}$

**Question 2 (25 marks):**

For the circuit shown in the figure below, use the superposition theorem to find  $i_x$ .

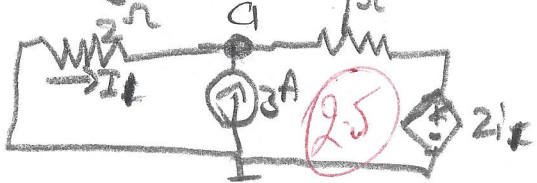


$$I_x = I_1 + I_2$$

Where  $I_1$  and  $I_2$  are currents from each respective independent source

Find  $I_1$

eliminating 10V source



Node A equation

$$-3 + \frac{V_a - 2i_1}{1} + \frac{V_a}{2} = 0$$

$$I_1 = -\frac{V_a}{2}$$

$$-6 + 2V_a - 4i_1 + V_a = 0$$

$$-6 + 2V_a + 4\left(\frac{V_a}{2}\right) + V_a = 0$$

$$5V_a = 6$$

$$V_a = \frac{6}{5} \text{ V}$$

$$I_1 = -\frac{V_a}{2}$$

$$= -\frac{6}{10} = -0.6 \text{ A}$$

Find  $I_2$

Eliminate 3A source



KVL Equation

$$2I_2 - 10 + 2I_1 + I_1 = 0 \quad (1)$$

$$I_2 = I_1 \quad (2)$$

Sub (1) into (2)

$$2I_1 - 10 + 2I_1 + I_1 = 0$$

$$5I_1 = 10$$

$$I_1 = 2 \text{ A}$$

$i_x$	$I_x = 1.4 \text{ A}$
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Since  $I_x = I_1 + I_2$

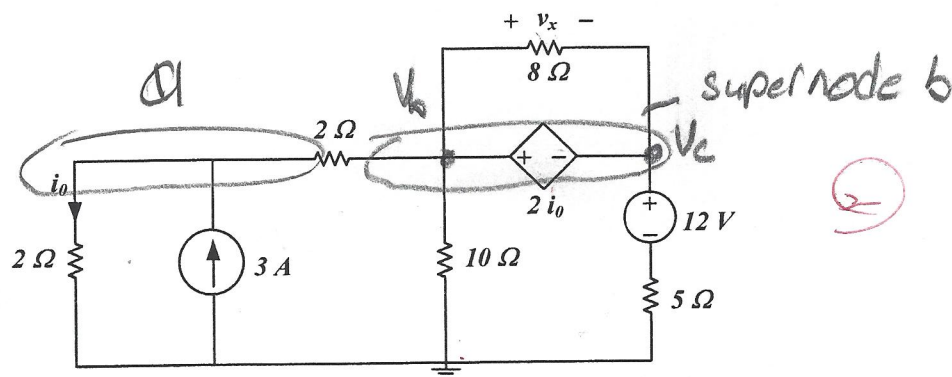
$$I_x = -0.6 + 2$$

$$I_x = 1.4 \text{ A}$$



**Question 3 (25 marks):**

Apply nodal analysis to find the current  $i_o$  and the voltage  $v_x$  in the circuit shown below



$$i_o = \frac{V_a}{2}$$

Node Equation at node A

$$-3 + \frac{V_a}{2} - V_b + \frac{V_a}{2} = 0 \quad (4)$$

$$-6 + 2V_a - V_b = 0$$

Super node Equation  $2V_a - V_b = 6 \quad (1)$

$$2i_o = V_b - V_c$$

$$V_c = V_b - 2i_o$$

$$\frac{V_b}{10} + \frac{V_b - 2i_o - 12}{5} + \frac{V_b - V_c + 2i_o}{8} = 0$$

$$\frac{3V_b + 4i_o - 24}{10} + \frac{i_o}{4} = 0 \quad (3)$$

$$\frac{6V_b - 8i_o - 48 + 5i_o}{20} = 0$$

$$6V_b - 3i_o = 48$$

$$6V_b - \frac{3V_a}{2} = 48$$

$$12V_b - 3V_a = 96 \quad (2)$$

$$V_a = 8V \quad \checkmark$$

$$V_b = 10V \quad \checkmark$$

Find  $i_o$

$$i_o = \frac{V_a}{2} = \frac{8}{2} = 4A$$

$$= 4A \quad \checkmark$$

Find  $V_x$

$$V_x = \frac{10}{4} \times 8$$

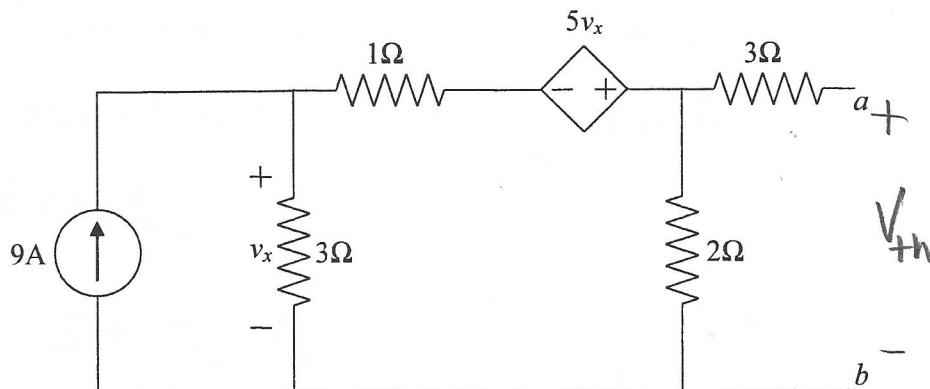
$$= \frac{4}{4} \times 8$$

$$= 8V$$

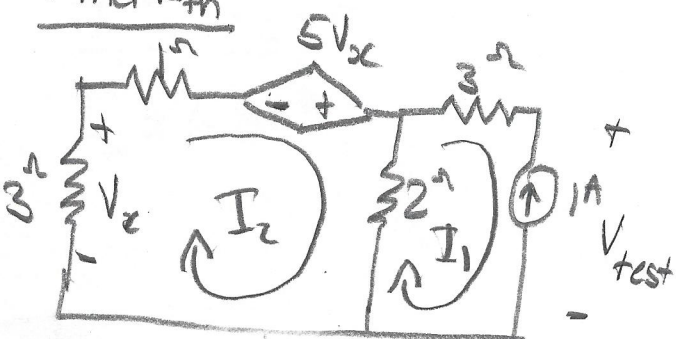
$i_o(A) =$	4A	$\checkmark$
$v_x(V) =$	8V	$\checkmark$

**Question 4 (25 marks):**

Find the Thevenin equivalent between terminals  $a-b$  of the following circuit:



Find  $R_{th}$



$$I_1 = -1A$$

$$I_2: -5V_x + 2(I_2 - (-1)) + 3I_2 + I_2 = 0$$

$$V_x = -3I_2$$

$$15I_2 + 2I_2 + 2 + 3I_2 + I_2 = 0$$

$$2I_2 = -2$$

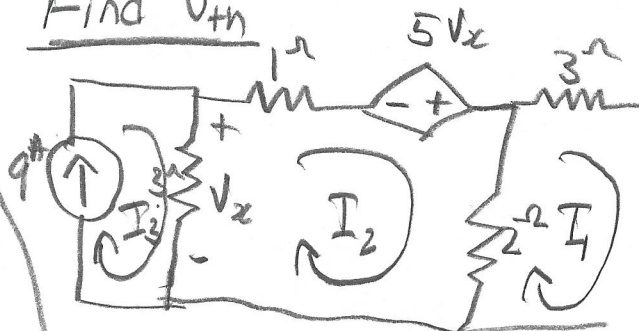
$$I_2 = -\frac{2}{21}$$

Find  $V_{test}$

$$V_{test} + 2(I_1 - I_2) + 3I_1 = 0 \quad \left| \quad V_{test} = -4.81_{10} V \right.$$

$$V_{test} + 2(-1 + \frac{2}{21}) + 3 = 0$$

Find  $V_{th}$



$$I_3 = 9A$$

$$I_2: 3(I_2 - 9) + I_2 - 5V_x + 2(I_2 - I_1) = 0$$

$$I_1: 2(I_1 - I_2) + 3I_1 = 0$$

$$5I_1 - 2I_2 = 0 \quad (1)$$

$$3I_2 - 27 + I_2 - 5V_x + 2I_2 - 2I_1 = 0$$

$$V_{th} = -12.84 V$$

$$R_{th} = +4.81 \Omega$$

$$6I_2 - 5V_x - 2I_2 = 0$$

$$V_x = 3(I_3 - I_2)$$

$$I_2 = 27 - 8I_2 \quad (3)$$

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Find  $R_{th}$

$$R_{th} = \frac{4.81}{1}$$

$$= 4.81 \Omega$$

Resistance has no negative

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$$5I_1 - 2I_2 = 0 \quad (1)$$

$$-2I_1 - 5V_{oc} + 6I_2 = 0 \quad (2)$$

$$V_{oc} = 27 - 3I_2$$

$$-2I_1 - 135 + 15I_2 + 6I_2 = 0$$

$$-2I_1 + 21I_2 = 135 \quad (3)$$

$$I_1 = 2.67^A$$

$$I_2 = 6.68^A$$

$$I_1 = I_N$$

$$I_N = 2.67^A$$

$$V_{th} = I_N \times R_{th}$$

$$= 2.67 \times 4.81$$

$$= 12.84^V$$