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Ryerson University
Department of Electrical and Computer Engineering
ELE202: Electric Circuits Analysis
Mid-Term Examination, February 2014
Duration: 1.5 hours

Student's Name: [REDACTED]

Student's Number [REDACTED]

Section: [REDACTED]

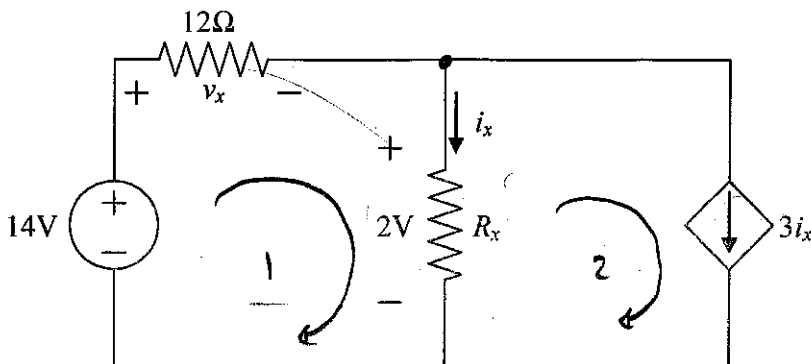
NOTES:

1. This is a **Closed Book** examination. No aids other than the approved calculators are allowed.
2. There are four questions. Answer all **four questions**.
3. **No questions are to be asked** in the examination hall. If doubt exists as to the interpretation of any question, the student is urged to submit with the answer paper, a clear statement of any assumptions made.

<i>Question No.</i>	<i>Mark of each question</i>	<i>Mark obtained</i>
Q1	25	23 A.Y.
Q2	25	24 J.S.
Q3	25	25 N.M.
Q4	25	20+5 p.h.
Total (Out of 100):		92+5=97 p.h.

Question 1(i) (10 marks):

Find v_x , i_x , and R_x in the following circuit:



$$i_2 = 3i_x$$

$$12i_1 + 2 - 14 = 0$$

$$i_1 = 1 \text{ A}$$

$$v_x = R i_1 = 12 \cdot 1$$

$$v_x = 12 \text{ V}$$

$$i_x = i_1 - i_2$$

$$i_x = 1 - 3i_x$$

$$4i_x = 1$$

$$i_x = 0.25 \text{ A}$$

$$2 = R_x i_x$$

$$2 = R_x (0.25)$$

$$R_x = 8 \Omega$$

$$v_x = 12 \text{ V}$$

(+2)

$$i_x = 0.25 \text{ A}$$

(+6)

$$R_x = 8 \Omega$$

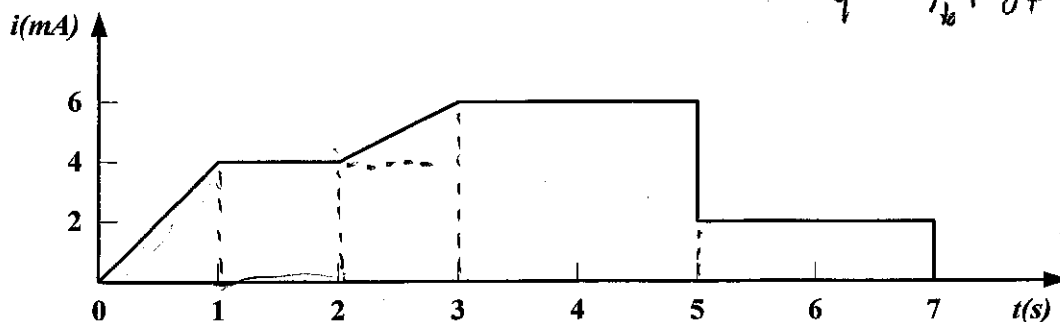
(+2)

13

Question 1(ii) (15 marks):

The current flowing through an element is as shown in the figure below. Determine the total charge that passed through the element at:

- (a) $t=1$ s (b) $t=2$ s (c) $t=3$ s (d) $t=5$ s (e) $t=7$ s



$$i = \frac{q}{t}$$

$$q = \int_0^t i \, dt$$

$$Q_{1s} = \frac{1}{2} b h$$

$$= \frac{1}{2} (1)(4)$$

$$= 2 \text{ mC}$$

$$Q_{2s} = 2 + b h$$

$$= 2 + 1 \cdot 4$$

$$= 8 \text{ mC}$$

$$Q_3 = 8 + b h_1 + \frac{1}{2} b h_2$$

$$= 8 + (1)(4) + \frac{1}{2} (1)(2)$$

$$= 8 + 4 + 1$$

$$= 13 \text{ mC}$$

$$Q_5 = 13 + b h$$

$$= 13 + 2(6)$$

$$= 13 + 12$$

$$= 25 \text{ mC}$$

$$Q_7 = 25 + b h$$

$$= 25 + 2(2)$$

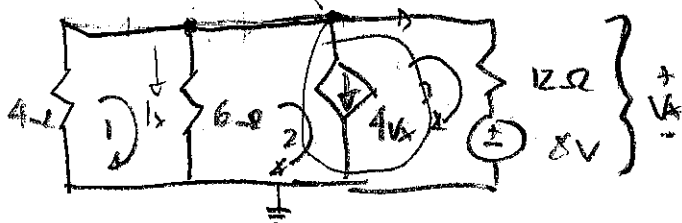
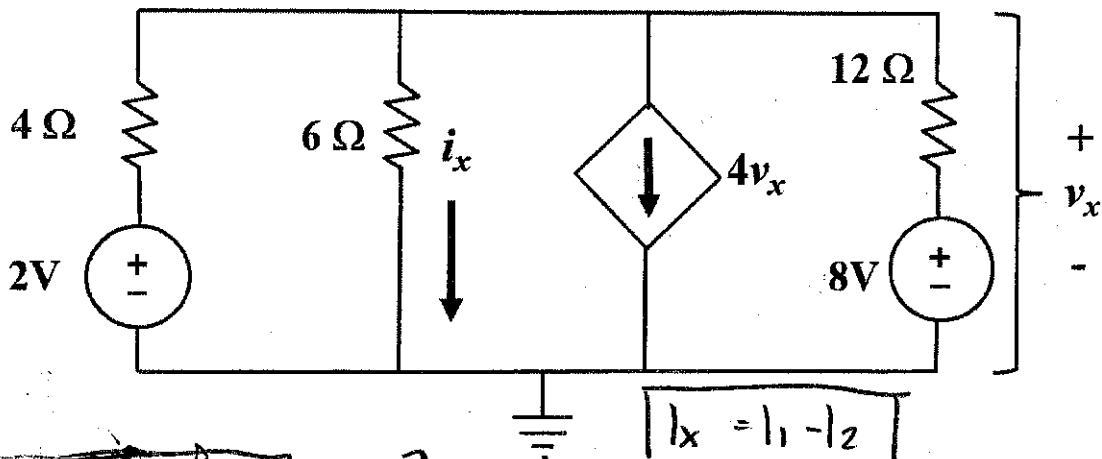
$$= 29 \text{ mC}$$

(a) $Q_{1s} = 2 \text{ mC}$ ✓	(+3)
(b) $Q_{2s} = 8 \text{ mC}$ X	(+1)
(c) $Q_{3s} = 13 \text{ mC}$ ✓	(+3)
(d) $Q_{5s} = 25 \text{ mC}$ ✓	(+2)
(e) $Q_{7s} = 29 \text{ mC}$ ✓	(+3)

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Question 2 (25 marks):

Find i_x and v_x using the superposition principle.



$$\textcircled{1} 4i_1 + 6i_1 - 6i_2 = 0$$

$$10i_1 - 6i_2 = 0$$

$$i_1 = 0.6i_2$$

$$\textcircled{SM} 6i_2 - 6i_1 + 12i_3 + 8 = 0$$

$$-6i_1 + 6i_2 + 12i_3 = -8$$

$$-6(0.6i_2) + 6(49i_3 + 32) + 12i_3 = -8$$

$$-3.6i_2 + 294i_3 + 192 + 12i_3 = -8$$

$$-3.6(49i_3 + 32) + 294i_3 + 12i_3 = -200$$

$$-176.4i_3 - 115.2 + 294i_3 + 12i_3 = -200$$

$$i_2 = -0.061728 \text{ A}$$

$$i_1 = -0.037037 \text{ A}$$

$$129.6i_3 = -84.8$$

$$i_3 = -0.654320987 \text{ A}$$

$$i_x = i_1 - i_2$$

$$v_x = 12i_3 + 8$$

$$4v_x = i_2 - i_3$$

$$4(12i_3 + 8) = i_2 - i_3$$

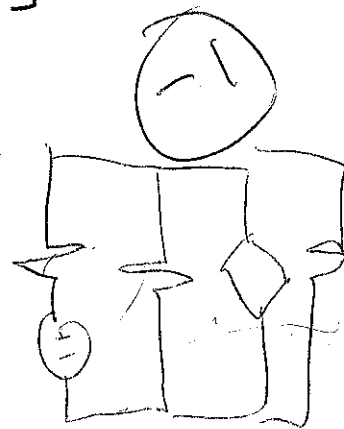
$$48i_3 + 32 = i_2 - i_3$$

$$49i_3 + 32 = i_2$$

$$v_{x2} = 0.148 \text{ V}$$

$$i_{x2} = 0.024691 \text{ A}$$

$i_x =$	$0.024691 + 0.018518$ $= 0.04321 \text{ A}$
$v_x =$	$0.1111 + 0.148$ $= 0.259 \text{ V}$

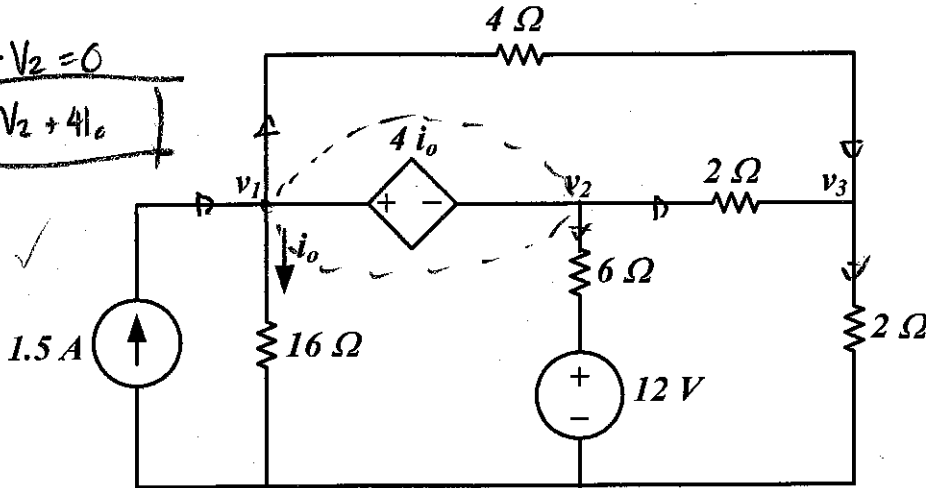


Question 3 (25 marks):

Apply nodal analysis to find the node voltages v_1 , v_2 , v_3 and the current i_o in the circuit shown below

③ $V_1 - 4i_o - V_2 = 0$
 $V_1 = V_2 + 4i_o$

$i_o = \frac{V_1}{16}$



③ $\frac{-(V_1 - V_2)}{4} + 1.5 - \frac{V_1}{16} - \frac{(V_2 - 12)}{6} - \frac{(V_2 - V_3)}{2} = 0$
 $-\frac{V_1}{4} + \frac{V_2}{4} + 1.5 - \frac{V_1}{16} - \frac{V_2}{6} + 2 - \frac{V_2}{2} + \frac{V_3}{2} = 0$
 $\frac{-5V_1}{16} - \frac{2V_2}{3} + \frac{3V_3}{4} = -3.5$

$V_1 - V_2 - \frac{4V_1}{16} = 0$

$V_1 - V_2 - \frac{V_1}{4} = 0$

$\frac{3V_1}{4} - V_2 = 0$

③ $\frac{V_1}{4} - \frac{V_3}{4} - \frac{V_3}{2} + \frac{V_2}{2} - \frac{V_3}{2} = 0$

$\frac{V_1}{4} + \frac{V_2}{2} - \frac{5V_3}{4} = 0$

$v_1 =$	8 V	✓
$v_2 =$	6 V	✓
$v_3 =$	4 V	✓
$i_o =$	0.5 A	✓

$i_o = \frac{8}{16} = 0.5 A$

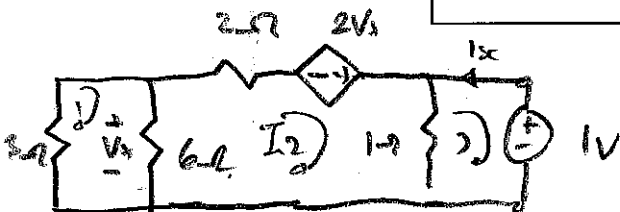
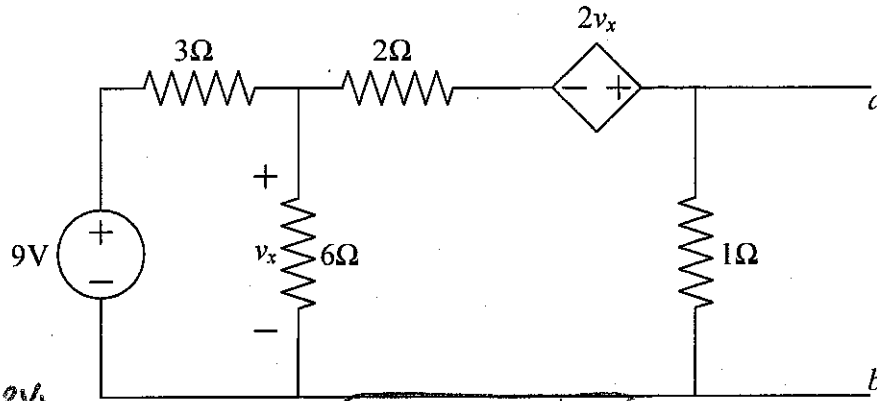
$\begin{vmatrix} -\frac{5}{16} & -\frac{2}{3} & \frac{3}{4} \\ \frac{1}{4} & \frac{1}{2} & -\frac{5}{4} \\ \frac{3}{4} & -1 & 0 \end{vmatrix} \begin{matrix} -3.5 \\ 0 \\ 0 \end{matrix} \begin{matrix} V_1 = 8 V \\ V_2 = 6 V \\ V_3 = 4 V \end{matrix}$

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Question 4 (25 marks):

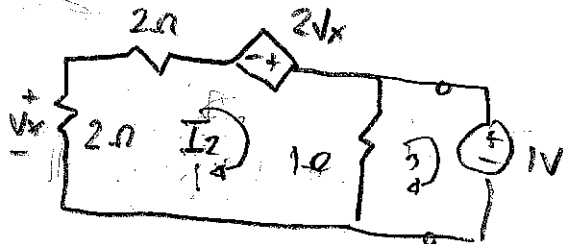
2018 p. 6.

Find the Thevenin equivalent between terminals $a-b$ of the following circuit:



$$I_3 = -1.5 \text{ A}$$

+ Using KVL in parallel, $3 \parallel 6$ still hold with V_x it needs more detail.



$$V_x = -2I_2$$

$$I_3 = 1.125 \text{ A}$$

$$2I_2 + 2I_2 - 2V_x + I_2 - I_3 = 0$$

$$4I_2 - 2(-2I_2) + I_2 - I_3 = 0$$

$$4I_2 + 4I_2 + I_2 - I_3 = 0$$

$$9I_2 = I_3$$

$$I_3 - I_2 + 1 = 0$$

$$9I_2 - I_2 = -1$$

$$8I_2 = -1$$

$$I_2 = -0.125 \text{ A}$$

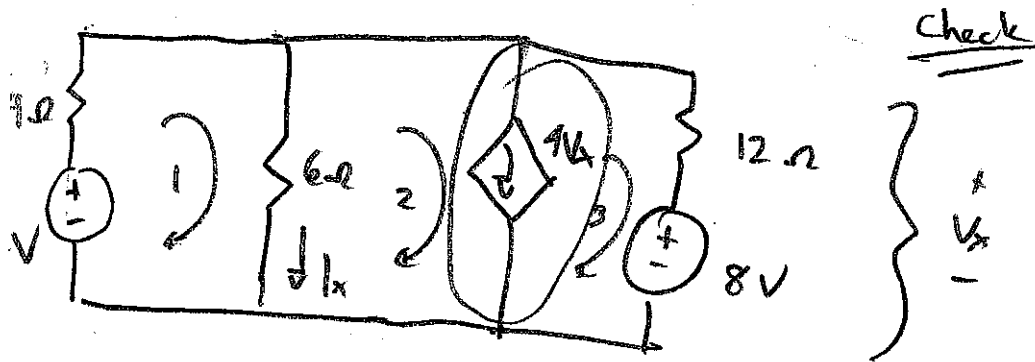
$$I_3 = -1.125 \text{ A}$$

$$R_{Th} = \frac{1}{1.125}$$

$$R_{Th} = 0.888 \Omega$$

$$V_{th} = -2 \text{ V}$$

$$R_{th} = 0.888 \Omega$$



$$SM \Rightarrow 4V_x = I_2 - I_3$$

$$V_x = 12I_3 + 8$$

$$I_x = I_1 - I_2$$

$$6I_1 - 6I_2 - 2 + 4I_1 = 0$$

$$10I_1 - 6I_2 = 2$$

$$6I_2 - 6I_1 + 12I_3 + 8 = 0$$

$$-6I_1 + 6I_2 + 12I_3 = -8$$

$$4(12I_3 + 8) = I_2 - I_3$$

$$48I_3 + 32 = I_2 - I_3$$

$$-I_2 + 49I_3 = -32$$

$$\begin{vmatrix} 10 & -6 & 0 & 2 \\ 0 & -1 & 49 & -32 \\ -6 & 6 & 12 & -8 \end{vmatrix}$$

$$I_1 = 0.435185185$$

$$I_2 = 0.391975308$$

$$I_3 = -0.645061728$$

$$I_x = 0.04321 \text{ A}$$

$$V_x = 0.25926 \text{ V}$$