

Ryerson University
Department of Electrical and Computer Engineering
ELE302: Electric Networks
Final Examination, December, 2005
Duration: 3 hours

Student's Name:

Student's Number: Section:

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NOTES:

1. Please **TICK** mark against the name of your professor.
2. This is a **Closed Book** examination. No aids other than the approved calculators are allowed.
3. Answer **all** questions.
4. **Laplace Table** is provided in the back of this question paper.
5. **No questions are to be asked** in the examination hall. If needed, make any valid assumptions to solve the question, but please state clearly the assumptions used.

<i>Question No.</i>	<i>Mark of each question</i>	<i>Mark obtained</i>
Q1	20	
Q2	20	
Q3	20	
Q4	20	
Q5	20	
Q6	20	
Total:		

Q1:Part-A

In the circuit shown in Figure-1, the switch is opened after a long time at $t = 0$.

- (a) Calculate $v_c(0+)$, $i_L(0+)$, $\frac{dv_c}{dt}(0+)$ and $\frac{di_L}{dt}(0+)$ [6]
- (b) Write the differential equation of $v_c(t)$. [4]

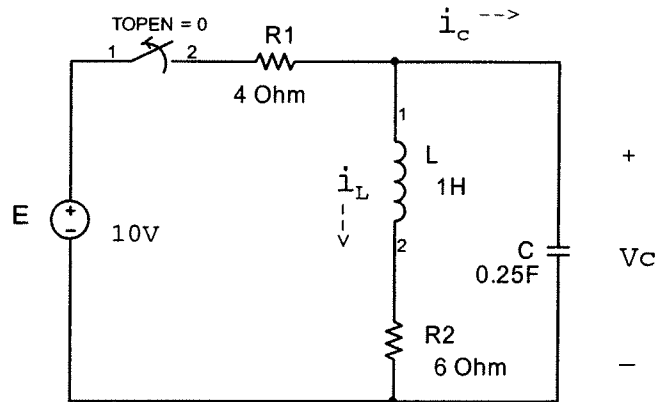


Figure-1

Q1: Part-B

The circuit response of a circuit due to impulse excitation is given as

$h(t) = 5 e^{-2t} \sin 4t \cdot u(t)$. Determine the step response of the circuit. [10]

Q2:

(a) Draw the Laplace Transformed equivalent circuit of Figure-2, when $v_c(0) = 1V$ and $i_L(0) = 1A$. [5]

(b) Solve for $v_L(t)$. [15]

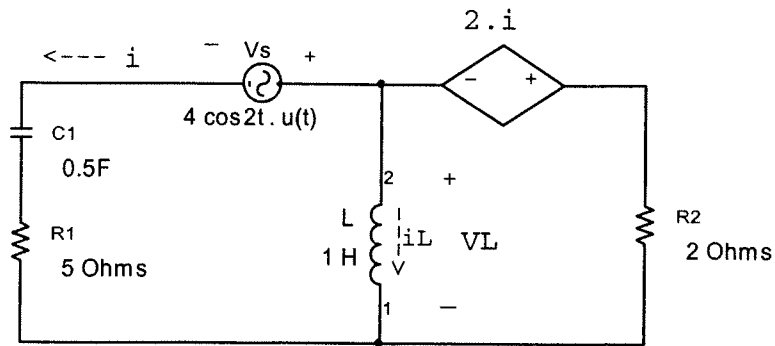


Figure-2

Q3: Part-A

Derive the transfer function $H(s) = \frac{V_o(s)}{V_i(s)}$ of the circuit shown in Figure-3A. [10]

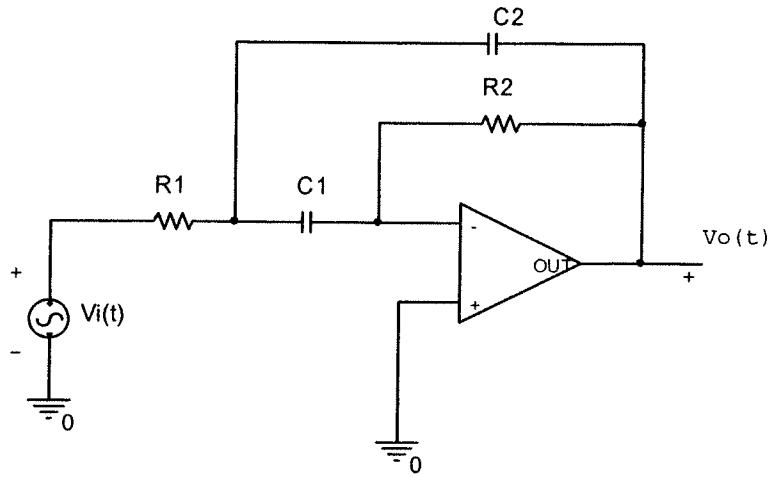


Figure-3A

Q3: Part-B

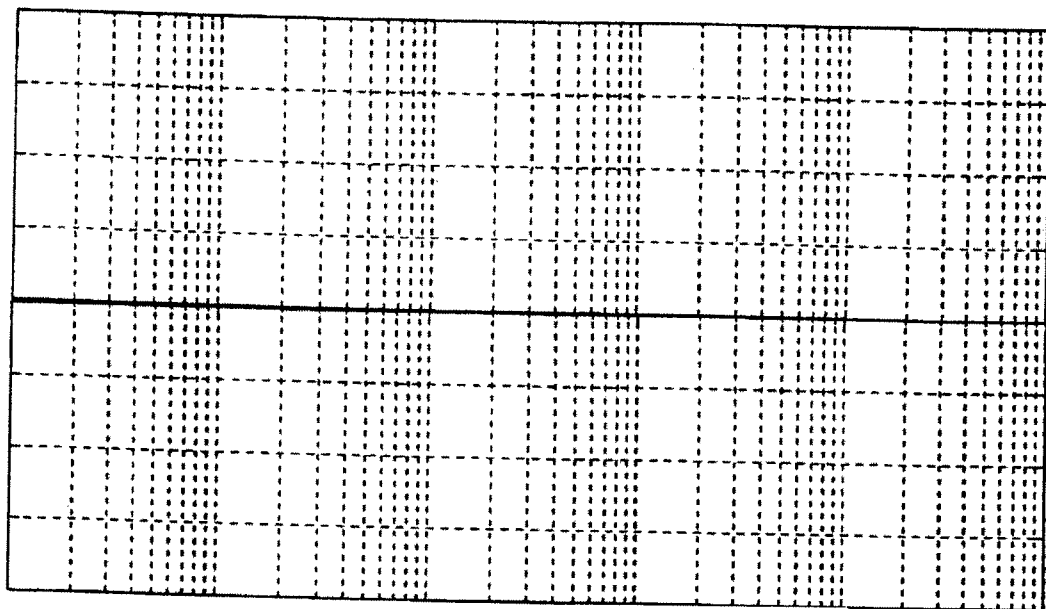
Construct the Bode plots of amplitude in dB and phase in degrees of the following transfer function.

$$H(s) = \frac{100 s^2}{(s + 50)(s + 200)}$$

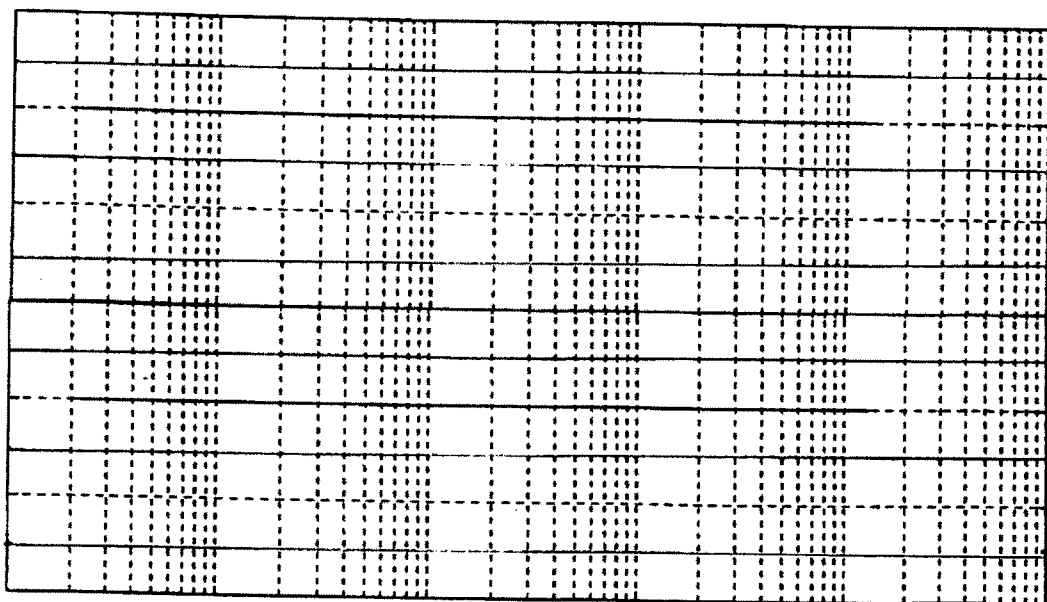
Use the graph paper attached with this question paper.

[10]

dB



0



Q4: Part-A

- (a) Figure-4A shows a mutually coupled circuit. Write the mesh equations. [5]
- (b) If $R_1 = 1 \, \Omega$, $X_1 = X_2 = X_3 = X_c = 2 \, \Omega$, and $X_{13} = X_{31} = 1.5 \, \Omega$, solve the voltage V_0 across the capacitor.

[5]

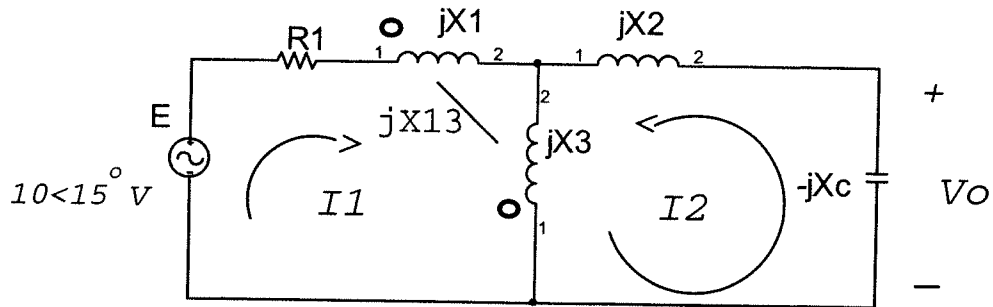


Figure-4A

Q4: Part-B

In Figure-4B , T1 and T2 are two ideal transformers. Calculate the power output in the $1.5\ \Omega$ resistance. [5]

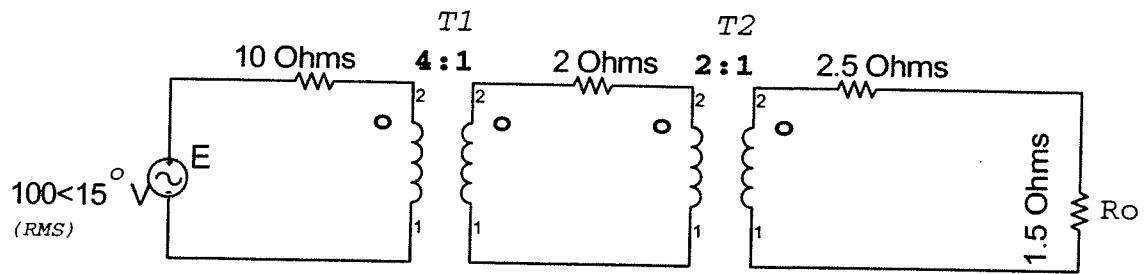


Figure-4B

Q5: Figure-5 is a balanced 3-phase circuit of 60 Hz frequency. The line voltages in RMS for abc phase sequence are given as:

$$V_{AB} = 220 \angle 0^\circ V, V_{BC} = 220 \angle -120^\circ V, \text{ and } V_{CA} = 220 \angle 120^\circ V.$$

- When $Z = 3 + j6 \Omega$, calculate the line currents without the capacitors in the circuit. [5]
- Calculate the power factor, the total complex power, total real power and total reactive power without the capacitors in the circuit. [4]
- Calculate the capacitor C per phase needed to improve the total power factor to one. [6]
- Calculate the new line current after the capacitors are connected. [5]

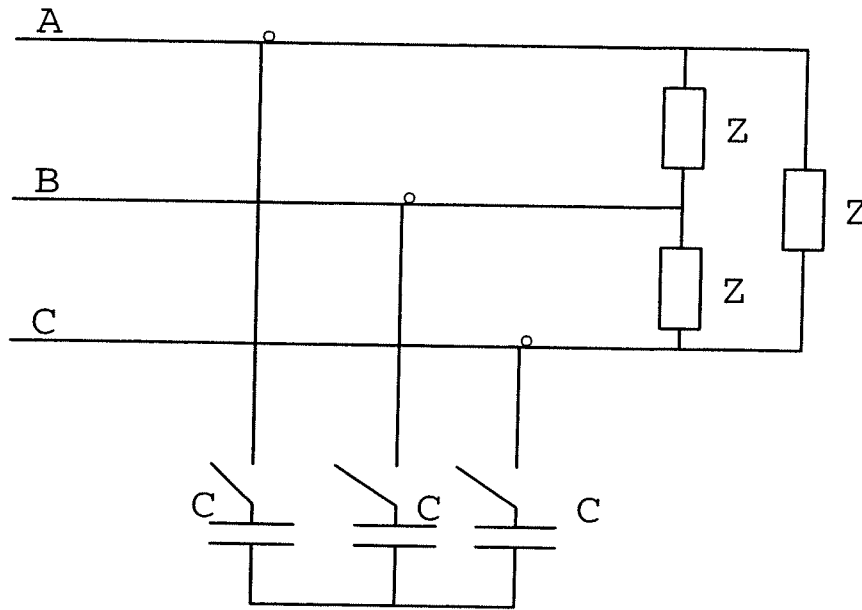


Figure-5

Q6: Part-A

Figure-5A shows a periodic voltage function.

- (a) Calculate the Fourier coefficients in terms of n , where n is the number of harmonics present.
- (b) Write the expression of $v(t)$ as function of first four (non-zero) terms of the Fourier series.

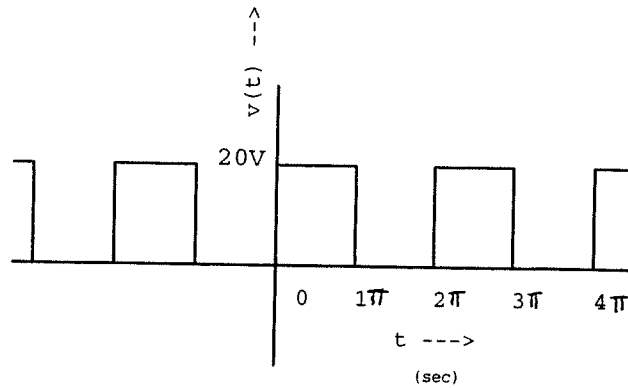


Figure-5A

Q6: Part-B

The Fourier series of the source $v_s(t)$ in Figure-6B is given as $v_s = 5 + \sum_{n=1}^{\infty} \left(\frac{10}{n^2} \sin n\omega_0 t \right)$,

where n is odd integer and $\omega_0 = 50$ rad/sec.

Find the dc- and 2nd harmonic components in $V_o(t)$.

[10]

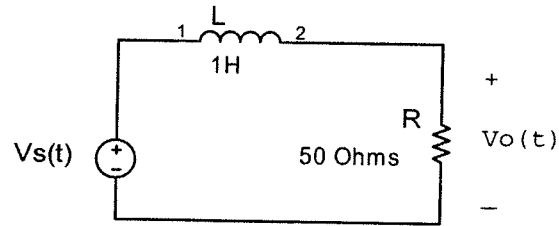


Figure-6B

Laplace Table

<u>f(t)</u>	→	<u>F(s)</u>
$\delta(t)$		1
$Ku(t)$		K/s
$t.u(t)$		$1/s^2$
$f(t-a)u(t-a)$		$e^{-as}F(s)$
$e^{-at}u(t)$		$1/(s+a)$
$e^{-at}f(t)$		$F(s+a)$
$\sin(wt).u(t)$		$w/(s^2+w^2)$
$\cos(wt).u(t)$		$s/(s^2+w^2)$
$e^{-at}\cos(wt).u(t)$		$\frac{s+a}{(s+a)^2+w^2}$
$e^{-at}\sin(wt).u(t)$		$\frac{w}{(s+a)^2+w^2}$
$\frac{df(t)}{dt}$		$sF(s) - f(0^-)$
$\frac{d^2f(t)}{dt^2}$		$s^2F(s) - sf(0^-) - f'(0^-)$
$\int_{-\infty}^t f(q) dq$		$\frac{F(s)}{s} + \int_{-\infty}^0 f(q) dq$