Appendix

The following appendix will not be included in the camera-ready version (if accepted)⁵

A DETAILS OF THE CASE STUDIES

In this section, we provide the corresponding APCTL*/APCTL specifications of the properties discussed in the paper in natural language across each case study. We also provide the embedded PCTL*/PCTL property correspondingly generated using the logical embeddings sldl'/sldl. We believe this will help readers better understand the property formulation process. We also present the other relevant model details, viz., the number of states and transitions in the final SDTMC on which model checking was performed. The entire implementation process was run on a Windows 10 PC having Intel(R) Core(TM) i5-7500 CPU @ 3.40GHz, 3401 Mhz, 4 Core(s), 4 Logical Processor(s) with 20GB RAM. The codes took a minute max to give the final outputs on average. The DFS is the costliest operation, and we are trying to make it more efficient. Although, since the LTS is fixed, we save the DFS traversels once achieved. So, in the future, if the LTS needs to be transformed back into an ADTMC, the DFS step can be skipped and hence the run time of the code is minimized substantially to a minute. PRISM model checking took a maximum of 1 second for each property across all the case studies. ProM took 2 minutes to discover the process model and construct the reachability graphs depending on the amount of data analysed. mcRL2 took 30 – 45 minutes to simulate the new event logs up to 50000 events.

In the codes written in the Jupyter Notebook, the same segment of code responsible for performing a specific task may be found in multiple copies; they are to serve various situations that may arise. For example, whether to consider the lifecycle of the transition in the event log or not, whether a final state exists or not, such different scenarios have been tackled individually.

For each case study, we first list the APCTL/APCTL* formulas that were constructed corresponding to the queries discussed in the paper in natural language. The corresponding PCTL/PCTL* formulas constructed using the logical embeddings *sldl'/sldl* respectively are then listed for each query.

More details, codes, and the property files as listed below can be found at:

https://github.com/Anonymous-uploader/Prob_Verif_Process_Models

A.1 Loan Application Process

APCTL/APCTL* Specifications:

(1) The decision on the application is always intimated.

```
\mathcal{P} = ?((true)_{true}U_{senddecisionemail}(true))
```

(2) Was a decision on the application made without checking the credit? If yes, what is the probability that this occurs?

$$\mathcal{P} = ?((\textbf{true})_{\neg checkcredit} U_{senddecisionemail}(\textbf{true}))$$

(3) Was a decision on the application made without checking the system? If yes, what is the probability that this occurs?

$$\mathcal{P} = ?((\mathbf{true})_{\neg checksystem} \mathbf{U}_{senddecisionemail}(\mathbf{true}))$$

(4) What is the probability that check credit (if it occurred) is immediately followed by capacity calculation?

$$\mathcal{P}_{=?}((X_{checkcredit}true \rightarrow X_{checkcredit}(true_{false}U_{calculatecapacity}true))_{true}U_{senddecisionemail}true)$$

(5) What is the probability that capacity calculation immediately follows check credit?

$$\mathcal{P}_{=?}(true_{true}U_{\textit{checkcredit}}(true_{false}U_{\textit{calculatecapacity}}(true_{true}U_{\textit{senddecisionemail}}true)))$$

(6) What is the probability that capacity is calculated before making either of the checks?

$$\mathcal{P} = ?((\textbf{true})_{\neg(checkcredit \lor checksystem)} U_{calculatecapacity}(\textbf{true}))$$

(7) What is the probability that a loan application is accepted/rejected?

```
\begin{split} \mathcal{P} = &?((\mathbf{true})_{true} \mathbf{U}_{accept}(\mathbf{true})) \\ \mathcal{P} = &?((\mathbf{true})_{true} \mathbf{U}_{reject}(\mathbf{true})) \end{split}
```

(8) What is the probability that a loan application was accepted/rejected, given that the capacity calculation was performed before the checks?

```
 \begin{split} \mathcal{P} = &?((\mathbf{true})_{\neg(checkcredit \lor checks \, ystem)} U_{calculate capacity}(\mathbf{true}_{true} U_{accept}(\mathbf{true}))) \\ \mathcal{P} = &?((\mathbf{true})_{\neg(checkcredit \lor checks \, ystem)} U_{calculate capacity}(\mathbf{true}_{true} U_{reject}(\mathbf{true}))) \end{split}
```

Translated PCTL/PCTL* Specifications:

(1) The decision on the application is always intimated.

(2) Was a decision on the application made without checking the credit? If yes, what is the probability that this occurs?

⁵These additional details, e.g., APCTL/APCTL*, and PCTL/PCTL* properties are also available on the Github repository.

```
P=? [ (!("checkcredit")) U ((!("bot"))&("senddecisionemail"))&(P>=1 [ X ("bot") ]) ]
1393
                                                                                                                                                            1451
1394
                                                                                                                                                            1452
           (3) Was a decision on the application made without checking the system? If yes, what is the probability that this occurs?
1395
                                                                                                                                                            1453
                             P=? [ (!("checksystem")) \cup ((!("bot"))&("senddecisionemail"))&(P>=1 [ X ("bot") ]) ]
           (4) What is the probability that check credit (if it occurred) is immediately followed by capacity calculation?
1397
                                                                                                                                                            1455
1398
                                                                                                                                                            1456
               P=?[((!(X ("checkcredit"))))|(X ("checkcredit"&(X (("bot" U "calculatecapacity")))))) U ("senddecisionemail")]
1399
                                                                                                                                                            1457
1400
           (5) What is the probability that capacity calculation immediately follows check credit?
                                                                                                                                                            1458
1401
                                                                                                                                                            1459
                     P=? [ (true U ("checkcredit"&(X ("bot" U ("calculatecapacity"&(true U "senddecisionemail")))))) ]
                                                                                                                                                            1460
           (6) What is the probability that capacity is calculated before making either of the checks?
1403
                                         P=? [ !(("checkcredit")|("checksystem")) U ("calculatecapacity") ]
                                                                                                                                                            1462
1404
           (7) What is the probability that a loan application is accepted/rejected?
1405
                                                                                                                                                            1463
1406
                                             P=? [ true U ((!("bot"))&("accept"))&(P>=1 [ X ("bot") ]) ]
                                                                                                                                                            1464
1407
                                                                                                                                                            1465
                                             P=? [ true U ((!("bot"))&("reject"))&(P>=1 [ X ("bot") ]) ]
1408
                                                                                                                                                            1466
           (8) What is the probability that a loan application was accepted/rejected, given that the capacity calculation was performed before the
1409
               checks?
                                                                                                                                                            1468
                             P=? [ !(("checkcredit")|("checksystem")) U ("calculatecapacity"&(true U "accept")) ]
1411
                                                                                                                                                            1469
1412
                                                                                                                                                            1470
                             P=? [ !(("checkcredit")|("checksystem")) U ("calculatecapacity"&(true U "reject")) ]
1413
                                                                                                                                                            1471
1414
       A.2 Manuscript Review Process
                                                                                                                                                            1472
1415
                                                                                                                                                            1473
       APCTL/APCTL* Specifications:
1416
           (1) A decision (accept/reject) on the manuscript is always made.
1417
                                                                                                                                                            1475
                                                               \mathcal{P} = ?((true)_{true}U_{accept \lor reject}(true))
1418
                                                                                                                                                            1476
           (2) What is the probability that none of the original reviewers timed out while submitting the reviews?
1419
                                                                                                                                                            1477
1420
                                                                                                                                                            1478
                                                 \mathcal{P} = ?((true)_{\neg(timeout1 \lor timeout2 \lor timeout3)} U_{accpet \lor reject}(true))
                                                                                                                                                            1479
1421
           (3) What is the probability that the decision phase is reached without a single review from the original reviewers?
1422
                                              \mathcal{P} = ?((\mathbf{true})_{\neg(getreview1 \lor getreview2 \lor getreview3)} U_{accpet \lor reject}(\mathbf{true}))
1423
                                                                                                                                                            1481
           (4) What is the probability that an additional reviewer will be invited to decide on the paper?
1424
                                                                                                                                                            1482
1425
                                            \mathcal{P} = ?((\mathbf{true})_{true} \mathbf{U}_{invite additional reviewer}((\mathbf{true}_{true}) \mathbf{U}_{accept \lor reject}(\mathbf{true})))
                                                                                                                                                            1483
1426
                                                                                                                                                            1484
           (5) What is the probability that a manuscript will be accepted/rejected?
1427
                                                                                                                                                            1485
                                                                  \mathcal{P} = ?((true)_{true}U_{accept}(true))
1428
                                                                                                                                                            1486
                                                                   \mathcal{P} = ?((true)_{true}U_{reject}(true))
                                                                                                                                                            1487
           (6) What is the probability that manuscripts that did not require an additional reviewer were accepted/rejected?
1430
                                                                                                                                                            1488
                                                        \mathcal{P} = ?((true)_{\neg inviteadditional reviewer} U_{accept}(true))
                                                                                                                                                            1489
1431
                                                        \mathcal{P} = ?((\mathbf{true})_{\neg inviteadditional reviewer} \mathbf{U}_{reject}(\mathbf{true}))
                                                                                                                                                            1490
                                                                                                                                                            1491
           (7) The reward-based property since is a direct state-based property has been discussed later.
1434
                                                                                                                                                            1492
       Translated PCTL/PCTL* Specifications:
1435
                                                                                                                                                            1493
           (1) A decision (accept/reject) on the manuscript is always made.
1436
                                                                                                                                                            1494
1437
                                       P=? [ true U ((!("bot"))&("accept"|"reject"))&(P>=1 [ X ("bot") ]) ]
                                                                                                                                                            1495
1438
                                                                                                                                                            1496
           (2) What is the probability that none of the original reviewers timed out while submitting the reviews?
1439
                                                                                                                                                            1497
                    P=? [(!("timeout1"|"timeout2"|"timeout3"|))U((!("bot"))&("accept"|"reject"))&(P>=1 [ X ("bot") ])]
1440
                                                                                                                                                            1498
           (3) What is the probability that the decision phase is reached without a single review from the original reviewers?
1441
                                                                                                                                                            1499
                 P=? [(!("getreview1"|"getreview2"|"getreview3"))U((!("bot"))&("accept"|"reject"))&(P>=1 [ X ("bot") ])]
                                                                                                                                                            1500
1443
           (4) What is the probability that an additional reviewer will be invited to decide on the paper?
                                                                                                                                                            1501
1444
                                                                                                                                                            1502
                          P=? [(("invite additional reviewer"))U((!("bot"))&("accept"|"reject"))&(P>=1 [ X ("bot") ])]
                                                                                                                                                            1503
           (5) What is the probability that a manuscript will be accepted/rejected?
1446
                                                                                                                                                            1504
                                             P=? [ true U ((!("bot"))&("accept"))&(P>=1 [ X ("bot") ]) ]
1447
                                                                                                                                                            1505
                                             P=? [ true U ((!("bot"))&("reject"))&(P>=1 [ X ("bot") ]) ]
1448
                                                                                                                                                            1506
           (6) What is the probability that manuscripts that did not require an additional reviewer were accepted/rejected?
1449
                                                                                                                                                            1507
1450
                                                                                                                                                            1508
```

Conference'17, July 2017, Washington, DC, USA Anon P=? [(!("inviteadditionalreviewer")) U ((!("bot"))&("accept"))&(P>=1 [X ("bot")])]P=? [(!("inviteadditionalreviewer")) U ((!("bot"))&("reject"))&(P>=1 [X ("bot")])](7) Reward Based Property: What is the expected number of timeouts during the manuscript review process to reach the point of decision-making? For this query, we assigned a state reward of 1 to all states where either timeout1,timeout2,timeout3, or timeoutX was true as they correspond to time-outs. Then, we calculated the following property on the model: R{"TIMEOUT"}=?[F ("accept"|"reject"))] A.3 Telephone Repair Process APCTL/APCTL* Specifications: (1) What is the probability that a telephone went for a simple/complex repair only or no repair at all? $\mathcal{P} = ?((\mathbf{true})_{RepairSimple \lor \neg RepairComplex} \mathbf{U}_{ArchiveRepair}(\mathbf{true}))$ $\mathcal{P} = ?((\mathbf{true})_{RepairComplex \lor \neg RepairSimple} \mathbf{U}_{ArchiveRepair}(\mathbf{true}))$ (2) What is the probability that the user is informed before testing any repairs on the telephone? $\mathcal{P}_{=?}((\mathbf{true})_{\neg TestRepair}\mathbf{U}_{InformUser}(\mathbf{true}_{\mathbf{true}}\mathbf{U}_{ArchiveRepair}(\mathbf{true})))$ (3) What is the probability that a repair must be restarted along its journey from start to finish? $\mathcal{P}_{=?}((true)_{true}U_{RestartRepair}(true_{true}U_{ArchiveRepair}(true)))$ (4) After a complex repair is done, what is the maximum probability in the model that it is tested and the repair is archived subsequently? For all states reached after performing the action RepairComplex, we wish to calculate the average probability of the value evaluated for the following formula for each of them: $\mathcal{P}_{=?}((true_{false})U_{\textit{TestRepair}}(true_{false}U_{\textit{ArchiveRepair}}(true)))$ (5) After a repair is tested, what is the average probability that the order is immediately archived? For all states reached after performing the action TestRepair, we wish to calculate the average probability of the value evaluated for the following formula for each of them: $\mathcal{P}_{=?}((\mathbf{true_{false}})\mathbf{U}_{ArchiveRepair}(\mathbf{true}))$ Translated PCTL/PCTL* Specifications: (1) What is the probability that a telephone went for a simple/complex repair only or no repair at all? P=? [(("RepairSimple")|(!("RepairComplex"))) U ((!("bot"))&("ArchiveRepair"))&(P>=1 [X ("bot")])]

```
P=? [ (("RepairComplex")|(!("RepairSimple"))) U ((!("bot"))&("ArchiveRepair"))&(P>=1 [ X ("bot") ]) ]
```

(2) What is the probability that the user is informed before testing any repairs on the telephone?

```
P=? [ (!("TestRepair")) U ((!("bot"))&("InformUser")&(true U "ArchiveRepair")) ]
```

(3) What is the probability that a repair must be restarted along its journey from start to finish?

```
P=? [ (true U ((!("bot"))&("RestartRepair")&(true U "ArchiveRepair")) ]
```

(4) After a complex repair is done, what is the maximum probability in the model that it is tested and the repair is archived subsequently? We use it as a PRISM filter property to identify states that satisfy a certain property and then calculate their probabilities. PRISM allows the calculation of the maximum, minimum, or average of the probabilities that satisfy the proposition.

```
filter(max,,P=? [ (X("bot" U ("TestRepair"&(X("bot"U"ArchiveRepair"))))) ],"RepairComplex")
```

filter(a,b,c) refers to the following: a can take values like max, min, avg, etc. to denote the obvious quantification they will be expected to evaluate to, b is a PCTL/PCTL* formula which will be evaluated from all states which satisfy the PCTL state formula c. We identify all states that are labeled RepairComplex, and then evaluate the formula from the next state onwards, as all such states will reach the states reached in the original ADTMC after performing an action labeled *RepairComplex* with probability 1.

(5) After a repair is tested, what is the average probability that the order is immediately archived?

```
filter(avg,P=? [ (X("bot" U "ArchiveRepair")) ],"TestRepair")
```

A.4 Claim Settlement Process

APCTL/APCTL* Specifications:

(1) What is the probability that sufficient information is unavailable in a case?

```
\mathcal{P} = ?((true)_{checkifsufficientinformationis available} U_{end}(true))
```

(2) What is the probability that the claim is not assessed?

$$\mathcal{P} = ?((\mathbf{true})_{\neg assessclaim} \mathbf{U}_{end}(\mathbf{true}))$$

(3) What is the probability that the claim was not assessed, given it was registered prior?

```
\mathcal{P} = ?((\mathbf{true})_{\mathbf{true}} \mathbf{U}_{registerclaim}((\mathbf{true})_{\neg assessclaim} \mathbf{U}_{end}(\mathbf{true})))
1625
1626
            (4) What is the probability that payment was initiated on a claim?
1627
                                                                \mathcal{P} = ?((true)_{\neg initiatepayment}U_{end}(true))
            (5) What is the probability that the claimant was not notified of the reimbursement after initiating the payment?
1629
                                        \mathcal{P} = ?((true)_{true} U_{initiate payment}((true)_{\neg advise claim anton reimbur sement} U_{end}(true)))
1630
            (6) What is the probability that the claimant is notified of the reimbursement before the payment was initiated?
1631
                                         \mathcal{P} = ?((\mathbf{true})_{\mathbf{true}} \mathbf{U}_{adviseclaimantonreimbursement}((\mathbf{true})_{initiatepayment} \mathbf{U}_{end}(\mathbf{true})))
1632
1633
        Translated PCTL/PCTL* Specifications:
1634
            (1) What is the probability that sufficient information is unavailable in a case?
                                          P=? [ ("checkifsufficientinformationisavailable"|"bot") U ("end") ]
1636
            (2) What is the probability that the claim is not assessed?
1637
                                        P=? [ (!("assessclaim")) U ((!("bot"))&("end"))&(P>=1 [ X ("bot") ]) ]
1638
1639
            (3) What is the probability that the claim was not assessed given it was registered prior?
1640
                                             P=? [ (true) U (("registerclaim"))&(!("assessclaim")U("end")) ]
            (4) What is the probability that payment was initiated on a claim?
1642
                                     P=? [ (!("initiatepayment")) U ((!("bot"))&("end"))&(P>=1 [ X ("bot") ]) ]
1643
            (5) What is the probability that the claimant was not notified of the reimbursement after initiating the payment?
1644
                               P=? [ (true) U (("initiatepayment"))&(!("adviseclaimantonreimbursement")U("end")) ]
1645
1646
            (6) What is the probability that the claimant is notified of the reimbursement before the payment was initiated?
                           P=? [ (true) U (("adviseclaimantonreimbursement"))&((true U("initiatepayment"))U("end")) ]
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