## A TRANSLATING FORT INTO SROIQ

In this section we illustrate the translation of FORT. For the application of the first, second, third, fourth, and fifth steps, we only show it on a single axiom; the specific existential dependence axiom in section A.1. Then we illustrate the output of the fifth step in section A.2, and that of sixth step in section A.3.

## A.1 Applying steps (1-5) on a single axiom

Consider the definition of the specific existential dependence relation from FORT: An entity x is specifically existentially dependent entity y, denoted SED(x, y), iff; at any time t, x cannot exist at t unless y exists at t; & x and y are different entities; & x exists at some t (D).

$$\forall (x, y) \text{SED}(x, y) \to \forall t (E(x, t) \to E(y, t)) \land \neg (x = y) \land \exists t E(x, t)$$
(D)

In the following, we express a binary predicate R(x, y) as  $R_{xy}$ , and the predicate x = y as  $Eq_{xy}$ .

A.1.1 Transforming to Clausal Form:

$$\forall (x,y) [\neg SED_{xy} \lor (\forall t (\neg E_{xt} \lor E_{yt}) \land \neg Eq_{xy} \land \exists t E_{xt})] \land$$

$$[(\exists t (E_{xt} \land \neg E_{yt}) \lor Eq_{xy} \lor \forall t \neg E_{xt}) \lor SED_{xy}]$$
(NNF)

$$\forall x, y, m \exists n, a \forall b [\neg SED_{xy} \lor ((\neg E_{xm} \lor E_{ym}) \land \neg Eq_{xy} \land E_{xn})] \land$$

$$[((E_{xa} \land \neg E_{ya}) \lor Eq_{xy} \lor \neg E_{xb}) \lor SED_{xy}]$$
(PNF)

Upon skolemization, substitute n and a by the skolem functions f and g respectively as  $\{n \leftarrow f(x, y, m)\}$  and  $\{a \leftarrow g(x, y, m)\}$ . For simplicity we will write f(x, y, m) as f and g(x, y, m) as g.

$$[\neg SED_{xy} \lor ((\neg E_{xm} \lor E_{ym}) \land \neg Eq_{xy} \land E_{xf})] \land$$

$$[((E_{xg} \land \neg E_{yg}) \lor Eq_{xy} \lor \neg E_{xb}) \lor SED_{xy}]$$
(SNF)

$$(\neg SED_{xy} \lor \neg E_{xm} \lor E_{ym}) \land (\neg SED_{xy} \lor \neg Eq_{xy}) \land (\neg SED_{xy} \lor E_{xf})$$

$$\land (E_{xg} \lor Eq_{xy} \lor \neg E_{xb} \lor SED_{xy}) \land (\neg E_{yg} \lor Eq_{xy} \lor \neg E_{xb} \lor SED_{xy})$$

$$(CNF)$$

A.1.2 Rewriting as Horn rules:

$$SED_{xy} \wedge E_{xm} \rightarrow E_{ym}$$
 (R1)

$$SED_{xy} \rightarrow \neg Eq_{xy}$$
 (R2)

$$SED_{xy} \rightarrow E_{xf}$$
 (R3)

A.1.3 Qualifying Expressible Horn rules: R3 does not qualify since the variables are not enclosed.

$$SED_{xv} \wedge E_{xm} \rightarrow E_{vm}$$
 (R1)

$$SED_{xy} \rightarrow \neg Eq_{xy}$$
 (R2)

A.1.4 Constructing the rule graphs:

$$G = \langle \{x, y, m\}, \{SED_{xy}, E_{ym}\}, \emptyset, y, m : E \rangle$$

$$(G1)$$

$$G = \langle \{x, y\}, \{SED_{xy}\}, \emptyset, x, y : \neg Eq \rangle$$
(G2)

A.1.5 Converting into axioms:

$$SED^- \circ E \sqsubseteq E$$
 (A1)

$$SED \sqsubseteq nEq, where nEq = \neg Eq$$
 (A2)

## A.2 the non-structured set of SROIO axioms

We illustrate below the output of step 5;  $FORT_{S5}$  as the set of 120 non-structured axioms, and the structures  $R_{NS}$  and I resembling the set of non-simple roles and the set of proposition builders, respectively.

1

$SED^- \circ E \sqsubseteq E$	(a1)
SED ⊑ ¬equal	(a2)
$SED \circ negE \sqsubseteq \emptyset$	(a3)
$SED \circ SED \sqsubseteq SED$	(a4)
$componentOf \sqsubseteq partOf$	(a5)
Tra(componentOf)	(a6)
Irr(componentOf)	(a7)
Asy(componentOf)	(a8)
$componentOf \sqsubseteq properPartOf$	(a9)
$componentOf \circ \neg PartOf^- \sqsubseteq \varnothing$	(a10)
overlaps $\circ$ componentOf $\sqsubseteq \varnothing$	(a11)
$elementOf \sqsubseteq partOf$	(a12)
$elementOf \sqsubseteq SED$	(a13)
Tra(elementOf)	(a14)
Irr(elementOf)	(a15)
Asy(elementOf)	(a16)
$elementOf \sqsubseteq properPartOf$	(a17)
$elementOf \circ \neg PartOf^- \sqsubseteq \emptyset$	(a18)
overlaps $\circ$ elementOf $\sqsubseteq \varnothing$	(a19)
Tra(partOf)	(a20)
Ref(partOf)	(a21)
equal $\sqsubseteq$ partOf	(a22)
equal ⊑ partOf-	(a23)
Tra(equal)	(a24)
Ref(equal)	(a25)
Sym(equal)	(a26)
$properPartOf \sqsubseteq partOf$	(a27)
$properPartOf \sqsubseteq \neg partOf$	
Dis(properPartOf, partOf-)	(a28)
Tra(properPartOf)	(a29)
Irr(properPartOf)	(a30)
Asy(properPartOf)	(a31)
partOf- ∘ partOf ⊑ overlaps	(a32)
Ref(overlaps)	(a33)
Sym(overlaps)	(a34)
partOf ∘ partOf− ⊑ underlaps	(a35)
Ref (underlaps)	(a36)
Sym(underlaps)	(a37)
$overcross \sqsubseteq overlaps$	(a38)
overcross ⊑ ¬partOf	
Dis(overcross, partOf)	(a39)
Ref(overcross)	(a40)
Sym(overcross)	(a41)
$undercross \sqsubseteq underlaps$	(a42)
undercross ⊑ ¬partOf−	
Dis(undercross, partOf-)	(a43)

properOverlap ⊑ overcross	(a44)
properOverlap ⊑ overcross-	(a45)
$negPartOf \equiv \neg partOf$	(a46)
negOverlaps ≡ ¬overlaps	(a47)
properUnderlap ⊑ undercross	(a48)
properUnderlap ⊑ undercross–	(a49)
properExtension ⊑ ¬partOf	` ,
Dis(properExtension, partOf)	(a50)
properExtension ⊑ partOf-	(a51)
$C_{\text{overlaps}} \equiv \exists \text{overlaps.} \top$	(a52)
$C_{\text{overlaps}} \sqsubseteq \exists R_{\text{overlaps}}.\text{SELF}$	(a53)
$R_{\text{overlaps}} \circ \neg \text{overlaps} \circ \text{underlaps} \sqsubseteq \text{overlaps}$	(a54)
$C_{\text{partOf}} \equiv \exists \text{partOf.} \top$	(a55)
$C_{\text{partOf}} \sqsubseteq \exists R_{\text{partOf}}.\text{SELF}$	(a56)
$R_{partOf} \circ \neg partOf \circ overlaps \sqsubseteq partOf$	(a57)
Ref(connected)	(a58)
Sym(connected)	(a59)
$externallyConnected \sqsubseteq connected$	(a60)
$externallyConnected \sqsubseteq \neg overlaps$	
Dis(externallyConnected, overlaps)	(a61)
$tangentialPartOf \sqsubseteq partOf$	(a62)
$internalPartOf \sqsubseteq partOf$	(a63)
$internalPartOf \sqsubseteq \neg tangentialPartOf$	
Dis (internal Part Of, tangential Part Of)	(a64)
Ref(EL)	(a65)
Tra(EL)	(a66)
$partOf \sqsubseteq EL$	(a67)
$partOf \circ R_{EL} \sqsubseteq EL$	(a68)
$C_{\text{EL}} \equiv \exists \text{EL.T}$	(a69)
$C_{EL} \sqsubseteq \exists R_{EL}.SELF$	(a70)
$EL \circ partOf \sqsubseteq EL$	(a71)
$EL \circ L \sqsubseteq WL$	(a72)
$L$ - $\circ$ $EL$ $\circ$ $L$ $\sqsubseteq$ partOf	(a73)
$L$ - $\circ$ $L$ $\sqsubseteq$ equal	(a74)
$partOf - \circ L \sqsubseteq PL$	(a75)
$\neg partOf \circ PL \sqsubseteq \emptyset$	(a76)
$PL \circ L^- \sqsubseteq \emptyset$	(a77)
$tangential PartOf - \circ L \sqsubseteq TPL$	(a78)
$\neg tangentialPartOf \circ TPL \sqsubseteq \emptyset$	(a79)
$TPL \circ L^{\perp} \sqsubseteq \varnothing$	(a80)
$internalPartOf \neg \circ L \sqsubseteq IPL$	(a81)
$\neg$ internalPartOf $\circ$ IPL $\sqsubseteq \varnothing$	(a82)
$\mathrm{IPL} \circ \mathrm{L}\text{-}\sqsubseteq\varnothing$	(a83)
$L \circ partOf \sqsubseteq WL$	(a84)
$WL \circ \neg partOf - \sqsubseteq \emptyset$	(a85)
$WL$ - $\circ \neg L \sqsubseteq \varnothing$	(a86)

$L \circ tangentialPartOf \sqsubseteq TWL$	(a87)
$TWL \circ \neg tangentialPartOf - \sqsubseteq \emptyset$	(a88)
$TWL^{\perp} \circ \neg L \sqsubseteq \varnothing$	(a89)
$L \circ internalPartOf \sqsubseteq IWL$	(a90)
$IWL \circ \neg internalPartOf \neg \sqsubseteq \emptyset$	(a91)
$\mathrm{IWL}\text{-}\circ\neg\mathrm{L}\sqsubseteq\varnothing$	(a92)
$L \sqsubseteq PL$	(a93)
$L \sqsubseteq WL$	(a94)
$L \circ partOf - \sqsubseteq PL$	(a95)
$L \circ tangentialPartOf - \sqsubseteq TPL$	(a96)
$L \circ internalPartOf - \sqsubseteq IPL$	(a97)
$PL \circ partOf - \sqsubseteq PL$	(a98)
$TPL \circ partOf - \sqsubseteq TPL$	(a99)
$IPL \circ partOf - \sqsubseteq IPL$	(a100)
$partOf \circ WL \sqsubseteq WL$	(a101)
$internalPartOf \circ IWL \sqsubseteq IWL$	(a102)
$partOf \circ PL \sqsubseteq PL$	(a103)
$IPL \sqsubseteq PL$	(a104)
$TPL \sqsubseteq PL$	(a105)
$IWL \sqsubseteq WL$	(a106)
$TWL \sqsubseteq WL$	(a107)
Irr(memberOf)	(a108)
Asy(memberOf)	(a109)
$memberOf \sqsubseteq properPartOf$	(a110)
$negMemberOf \equiv \neg memberOf$	(a111)
$properOverlap- \circ memberOf \sqsubseteq \neg memberOf$	(a112)
$properPartOf - \circ memberOf \sqsubseteq \neg memberOf$	(a113)
$properPartOf \circ memberOf \sqsubseteq \neg memberOf$	(a114)
overlaps $\circ$ memberOf $\circ$ R <sub>memberOf</sub> $\sqsubseteq$ overlaps	(a115)
$C_{\text{memberOf}} \equiv \exists \text{memberOf} \top$	(a116)
$C_{\text{memberOf}} \sqsubseteq \exists R_{\text{memberOf}}.SELF$	(a117)
Irr(constitutes)	(a118)
Asy(constitutes)	(a119)
Tra(constitutes)	(a120)
$partOf \circ R_{constitutes} \sqsubseteq elementOf$	(a121)
$C_{constitutes} \equiv \exists constitutes. \top$	(a122)
$C_{constitutes} \sqsubseteq \exists R_{constitutes}.SELF$	(a123)
$negEqual \equiv \neg equal$	(a124)

Based on the preceding 124 axioms, we specify the set of non-simple roles  $R_{NS}$ , and the set of proposition builders I (all proposition builder are stated afterwards) as follows. In  $R_{NS}$ , the denotation  $rolename^n$  refers to a rolename that is added to  $R_{NS}$  because of axiom number n in  $S_5$  i.e. axiom n lead to the non-simplicity of the role rolename.

 $R_{NS} = \{E^{1}, negEqual^{2}, SED^{4}, partOf^{5}, componentOf^{6}, elementOf^{14}, ppartOf^{9,17}, equal^{24}, overlaps^{32}, underlaps^{35}, EL^{66}, WL^{72}, PL^{75,95}, TPL^{78}, IPL^{81}, TWL^{87}, IWL^{90}, negMemberOf^{108}, constitutes^{114}\}.$ 

 $I = \{\mathbb{I}_{2}, \mathbb{I}_{5}, \mathbb{I}_{9}, \mathbb{I}_{12}, \mathbb{I}_{13}, \mathbb{I}_{17}, \mathbb{I}_{22}, \mathbb{I}_{23}, \mathbb{I}_{27}, \mathbb{I}_{32}, \mathbb{I}_{35}, \mathbb{I}_{38}, \mathbb{I}_{42}, \mathbb{I}_{44}, \mathbb{I}_{45}, \mathbb{I}_{48}, \mathbb{I}_{49}, \mathbb{I}_{51}, \mathbb{I}_{54}, \mathbb{I}_{57}, \mathbb{I}_{60}, \mathbb{I}_{62}, \mathbb{I}_{63}, \mathbb{I}_{67}, \mathbb{I}_{68}, \mathbb{I}_{72}, \mathbb{I}_{73}, \mathbb{I}_{74}, \mathbb{I}_{75}, \mathbb{I}_{78}, \mathbb{I}_{81}, \mathbb{I}_{84}, \mathbb{I}_{87}, \mathbb{I}_{90}, \mathbb{I}_{93}, \mathbb{I}_{94}, \mathbb{I}_{95}, \mathbb{I}_{96}, \mathbb{I}_{97}, \mathbb{I}_{98}, \mathbb{I}_{99}, \mathbb{I}_{100}, \mathbb{I}_{101}, \mathbb{I}_{102}, \mathbb{I}_{103}, \mathbb{I}_{104}, \mathbb{I}_{105}, \mathbb{I}_{106}, \mathbb{I}_{107}, \mathbb{I}_{110}, \mathbb{I}_{112}, \mathbb{I}_{113}, \mathbb{I}_{114}, \mathbb{I}_{115}, \mathbb{I}_{121}\}.$ 

 $\mathbb{I}_2 \rightarrow (SED < negEqual) \land (SED - < negEqual)$ 

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\mathbb{I}_5 \to (componentOf < partOf) \land (componentOf - < partOf)
\mathbb{I}_9 \to (componentOf < ppartOf) \land (componentOf - < ppartOf)
\mathbb{I}_{12} \rightarrow (elementOf < partOf) \land (elementOf - < partOf)
\mathbb{I}_{13} \rightarrow (elementOf < SED) \land (elementOf - < SED)
\mathbb{I}_{17} \to (elementOf < ppartOf) \land (elementOf - < ppartOf)
\mathbb{I}_{22} \rightarrow (equal < partOf) \land (equal - < partOf)
\mathbb{I}_{23} \rightarrow (equal < partOf -) \land (equal - < partOf -)
\mathbb{I}_{27} \rightarrow (ppartOf < partOf) \land (ppartOf - < partOf)
\mathbb{I}_{32} \rightarrow (partOf < overlaps) \land (partOf - < overlaps)
\mathbb{I}_{35} \rightarrow (partOf < underlaps) \land (partOf - < underlaps)
\mathbb{I}_{38} \rightarrow (overcross < overlaps) \land (overcross - < overlaps)
\mathbb{I}_{42} \rightarrow (undercross < underlaps) \land (undercross - < underlaps)
\mathbb{I}_{44} \rightarrow (poverlaps < overcross) \land (poverlaps - < overcross)
\mathbb{I}_{45} \rightarrow (poverlaps < overcross-) \land (poverlaps- < overcross-)
\mathbb{I}_{48} \rightarrow (punderlaps < undercross) \land (punderlaps - < undercross)
\mathbb{I}_{49} \rightarrow (punderlaps < undercross-) \land (punderlaps- < undercross-)
\mathbb{I}_{51} \rightarrow (pExtension < partOf-) \land (pExtension- < partOf-)
\mathbb{I}_{54} \rightarrow (R_{overlaps} < overlaps) \land (R_{overlaps}^{-} < overlaps)
 \land (negOverlaps \prec overlaps) \land (negOverlaps \neg \prec overlaps)
 \land (underlaps \prec overlaps) \land (underlaps-\prec overlaps)
\mathbb{I}_{57} \rightarrow (R_{partOf} < partOf) \land (R_{partOf}^{-} < partOf)
 \land (negPartOf \prec partOf) \land (negPartOf - \prec partOf)
 \land (overlaps \prec partOf) \land (overlaps \neg \prec partOf)
\mathbb{I}_{60} \rightarrow (externallyConnected < connected)
 \land (externallyConnected- \prec connected)
\mathbb{I}_{62} \rightarrow (tangentialPartOf < partOf) \land
(tangentialPartOf - < partOf)
\mathbb{I}_{63} \to (internalPartOf < partOf) \land (internalPartOf - < partOf)
\mathbb{I}_{67} \rightarrow (partOf < EL) \land (partOf - < EL)
\mathbb{I}_{68} \to (R_{EL} \prec EL) \land (R_{FL}^- \prec EL)
 \land (partOf \prec EL) \land (partOf-\prec EL)
\mathbb{I}_{72} \rightarrow (EL \prec WL) \land (EL - \prec WL) \land (L \prec WL) \land (L - \prec WL)
\mathbb{I}_{73} \rightarrow (L < partOf) \land (L^- < partOf)
\land (EL \prec partOf) \land (EL \vdash \prec partOf)
\mathbb{I}_{74} \to (L < equal) \land (L - < equal)
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\mathbb{I}_{75} \rightarrow (partOf < PL) \land (partOf - < PL) \land (L < PL) \land (L - < PL)
\mathbb{I}_{78} \rightarrow (TP \prec TPL) \land (TP - \prec TPL) \land (L \prec TPL) \land (L - \prec TPL)
\mathbb{I}_{81} \to (\mathit{IP} \prec \mathit{IPL}) \land (\mathit{IP}^- \prec \mathit{IPL}) \land (\mathit{L} \prec \mathit{IPL}) \land (\mathit{L}^- \prec \mathit{IPL})
\mathbb{I}_{84} \rightarrow (L \prec WL) \land (L - \prec WL) \land (partOf \prec WL) \land (partOf - \prec WL)
\mathbb{I}_{87} \rightarrow (L < TWL) \land (L^- < TWL) \land (TP < TWL) \land (TP^- < TWL)
\mathbb{I}_{90} \to (L \prec IWL) \land (L^- \prec IWL) \land (IP \prec IWL) \land (IP^- \prec IWL)
\mathbb{I}_{93} \rightarrow (L \prec PL) \land (L^- \prec PL)
\mathbb{I}_{94} \rightarrow (L \prec WL) \land (L - \prec WL)
\mathbb{I}_{95} \rightarrow (L < PL) \land (L^{-} < PL) \land (partOf < PL) \land (partOf^{-} < PL)
\mathbb{I}_{96} \to (L \prec TPL) \land (L^- \prec TPL) \land (TP \prec TPL) \land (TP^- \prec TPL)
\mathbb{I}_{97} \rightarrow (L \prec IPL) \land (L^- \prec IPL) \land (IP \prec IPL) \land (IP^- \prec IPL)
\mathbb{I}_{98} \rightarrow (partOf < PL) \land (partOf - < PL)
\mathbb{I}_{99} \rightarrow (partOf < TPL) \land (partOf - < TPL)
\mathbb{I}_{100} \rightarrow (partOf < IPL) \land (partOf - < IPL)
\mathbb{I}_{101} \rightarrow (partOf < WL) \land (partOf - < WL)
\mathbb{I}_{102} \rightarrow (partOf < IWL) \land (partOf - < IWL)
\mathbb{I}_{103} \rightarrow (partOf < PL) \land (partOf - < PL)
\mathbb{I}_{104} \rightarrow (IPL \prec PL) \wedge (IPL - \prec PL)
\mathbb{I}_{105} \rightarrow (TPL \prec PL) \land (TPL^- \prec PL)
\mathbb{I}_{106} \rightarrow (IWL \prec WL) \wedge (IWL^- \prec WL)
\mathbb{I}_{107} \rightarrow (TWL < WL) \land (TWL^- < WL)
\mathbb{I}_{110} \to (memberOf < ppartOf) \land (memberOf - < ppartOf)
\mathbb{I}_{112} \rightarrow (properOverlap < negMemberOf) \land
(properOverlap- < negMemberOf) \land (memberOf < negMemberOf)
 \land (memberOf-\prec negMemberOf)
\mathbb{I}_{113} \to (ppartOf < negMemberOf) \land (ppartOf - < negMemberOf)
 \land (memberOf \prec negMemberOf) \land (memberOf \neg \prec negMemberOf)
\mathbb{I}_{114} \rightarrow (ppartOf < negMemberOf) \land (ppartOf - < negMemberOf)
 \land (memberOf \prec negMemberOf) \land (memberOf \neg \prec negMemberOf)
\mathbb{I}_{115} \rightarrow (memberOf < overlaps) \land (memberOf - < overlaps)
 \land (R_{memberOf} < overlaps) \land (R_{memberOf}^- < overlaps)
\mathbb{I}_{121} \to (partOf < elementOf) \land (partOf - < elementOf)
 \land (R_{constitutes} \prec elementOf) \land (R_{constitutes}^- \prec elementOf)
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## A.3 generalization and establishing decidability

We show below how step 6 is applied on  $FORT_{S5}$  by applying both simplicity and regularity rules, and we provide the final output of the procedure; the structured SROIQ set  $FORT_{S6}$ .

A.3.1 Applying the simplicity rule. Upon checking the non-simple roles in  $R_{NS}$  and the corresponding axioms in  $S_5$  in which they are found, the simplicity rule obliges the suppression of some axioms:

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S_5' = S_5 - \{a_7, a_8, a_{15}, a_{16}, a_{28}, a_{30}, a_{31}, a_{39}, a_{43}, a_{50}, a_{61}, a_{118}, a_{119}\}
```

A.3.2 Applying the regularity rule. Based on  $S'_5$ , we construct the (irregular) role hierarchy by translating each RIA into a regular order between its roles and add it into the role hierarchy. The resulting hierarchy is shown in figure 1. It shows three incompatibilities due to the orders shown blue which violate the totality of the regularity of the role hierarchy. We identify the following incompatibilities in function of the axioms that induced them as follows:

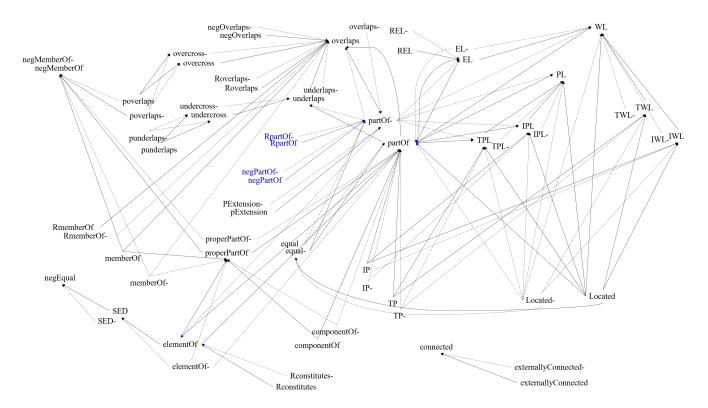


Figure 1: The role hierarchy of FORT presenting the regular orders in black, and the irregular ones in blue.

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\begin{split} &m_1: \mathbb{I}_{57} \to \neg \mathbb{I}_{32} \\ &m_2: \mathbb{I}_{73} \to \neg \mathbb{I}_{67} \land \neg \mathbb{I}_{68} \\ &m_3: \mathbb{I}_{121} \to \neg \mathbb{I}_{12} \end{split}
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Thus, besides  $S'_5$  we have the following structures:

$$\mathcal{M} = \{m_1, m_2, m_3\}$$
  
 $\mathcal{U} = \{a_{57}, a_{32}, a_{73}, a_{67}, a_{68}, a_{121}, a_{12}\}$ 

Now, we are able to compute the structured subsets of  $\mathcal U$  by computing the sub-theories as follows:

$$\mathbb{M}_1 = \{m_1\}, where \mathbb{U}_1 = \langle \{a_{57}\}, \{a_{32}\} \rangle$$
  
 $\mathbb{M}_2 = \{m_2\}, where \mathbb{U}_2 = \langle \{a_{73}\}, \{a_{67}, a_{68}\} \rangle$   
 $\mathbb{M}_3 = \{m_3\}, where \mathbb{U}_3 = \langle \{a_{121}\}, \{a_{12}\} \rangle$ 

As a last step, from each tuple  $\mathbb{U}_n$ , we make the choice of suppressing one set yielding in  $S_6$  as a structured subset of  $S_5'$ , such that  $S_6 = S_5' - \{a_{57}, a_{73}, a_{121}\}$ .

As final considerations, the final structured subset  $S_6$  consists of 108 axioms where the inputted set  $S_5$  consisted of 124 axioms. Thus 16 axioms ( $a_7$ ,  $a_8$ ,  $a_{15}$ ,  $a_{16}$ ,  $a_{28}$ ,  $a_{30}$ ,  $a_{31}$ ,  $a_{39}$ ,  $a_{43}$ ,  $a_{50}$ ,  $a_{61}$ ,  $a_{118}$ ,  $a_{119}$ ,  $a_{57}$ ,  $a_{73}$ ,  $a_{121}$ ) were suppressed in total upon applying the simplicity and regularity rules.