1 Operational semantics

The rules that define the operational semantics of applied pi-calculus and ProVerif are adapted from [1]. The identifiers a, b, c, k and similar ones range over names, and x, y and z range over variables. As detailed in [1], set of symbols is also assumed for constructors and destructors such that f for a constructor and g for a destructor. Constructors are used to build terms. Therefore, the terms are variables, names, and constructor applications of the form $f(M_1, \ldots, M_n)$.

We use the constructors and destructors defined in [1] as an initial step to represent the cryptographic operations as depicted in Figure 1. We added other different constructors/destructors which are used to define our protocol. Constructors and destructors can be public or private. The public ones can be used by the adversary, which is the case when not stated otherwise. The private ones can be used only by honest participants.

Symmetric enc/dec:

Constructor: encryption of x with the shared secret key k, senc(x, k)

Destructor: decryption $sdec(senc(x, k), k) \rightarrow x$

Asymmetric enc/dec:

Constructor: encryption of x with the public key generation from a secret key

k, pk(k), aenc(x, pk(k))

Destructor: decryption $adec(aenc(x, pk(k)), k) \rightarrow x$

Signatures:

Constructors: signature of x with the secret key k, sign(x, k)

Destructors: signature verification using he public key generation from a secret key $k, pk(k), verify(sign(x, k), pk(k)) \rightarrow x$

One-way garbling function:

Constructors: garbling of x with the key k, garble(x, k)

Evaluation function:

Constructors: evaluation function of garbling of variables x and y with the key k, garble(x, k), evaluate(garble(x, k), garble(y, k))

Commitment:

Constructors: committing x with a fresh nonce n k, commit(x, n)

Fig. 1. Constructors and destructors

The operational semantics used are presented in the Figure 2. A semantic configuration is a pair \mathcal{E},\mathcal{P} where the \mathcal{E} is a finite set of names and \mathcal{P} is a finite multiset of closed processes. The semantics of the calculus is defined by a reduction relation \rightarrow on semantic configurations, shown in Figure 2. The process event(M).P executes the event event(M) and then executes P. The input process in(M,x).P inputs a message, with x bound to tit, on channel M, and executes P. The output process out(M,N).P outputs the message N on the channel M and then executes P.

The nil process 0 does nothing. The process P|Q is the parallel composition of P and Q. The replication !P represents an unbounded number of copies of P in

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 \begin{array}{ll} (Nill) & \mathcal{E}, \mathcal{P} \cup \{0\} \rightarrow \mathcal{E}, \mathcal{P} \\ (Repl) & \mathcal{E}, \mathcal{P} \cup \{ !P \} \rightarrow \mathcal{E}, \mathcal{P} \cup \{ P, !P \} \\ (Par) & \mathcal{E}, \mathcal{P} \cup \{ P|Q \} \rightarrow \mathcal{E}, \mathcal{P} \cup \{ P, Q \} \\ (Par) & \mathcal{E}, \mathcal{P} \cup \{ P|Q \} \rightarrow \mathcal{E}, \mathcal{P} \cup \{ P, Q \} \\ (New) & \mathcal{E}, \mathcal{P} \cup \{ (\mathbf{new} \ a)P \} \rightarrow \mathcal{E} \cup \{ a' \}, \mathcal{P} \cup \{ P\{a'/a \} \} \ \text{where} \ a' \notin \mathcal{E} \\ (I/O) & \mathcal{E}, \mathcal{P} \cup \{ (\mathbf{new} \ a)P \} \rightarrow \mathcal{E} \cup \{ a' \}, \mathcal{P} \cup \{ P\{a'/a \} \} \ \text{where} \ a' \notin \mathcal{E} \\ (I/O) & \mathcal{E}, \mathcal{P} \cup \{ (\mathbf{new} \ a)P \} \rightarrow \mathcal{E}, \mathcal{P} \cup \{ Q, P\{M/x \} \} \\ (Cond1) & \mathcal{E}, \mathcal{P} \cup \{ \text{if} \ M = N \ \text{then} \ P \ \text{else} \ Q \} \rightarrow \mathcal{E}, \mathcal{P} \cup \{ P \} \ \text{if} \ M = N \\ (Cond2) & \mathcal{E}, \mathcal{P} \cup \{ \text{if} \ M = N \ \text{then} \ P \ \text{else} \ Q \} \rightarrow \mathcal{E}, \mathcal{P} \cup \{ P\{M'/x \} \} \\ \text{if} \ g(M_1, \dots, M_n) \rightarrow M' \\ \end{array}
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Fig. 2. Operational semantics

parallel. (new a)P creates a new name a and then executes P. The conditional if M=N then P else Q executes P if M and N reduce to the same term at runtime; otherwise, it executes Q. Finally, let x=M in P as syntactic sugar for $P\{M/x\}$ which is the process obtained from P by replacing every occurrence of x with M. As usual, we may omit an else clause when it consists of 0.

2 Protocol model

In this section we model the Qese protocol presented in the submitted paper as depicted in Figure 3.

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\begin{split} &\mathsf{P}_{\mathsf{CSP}}(sk_{\mathsf{CSP}}, pk_{\mathsf{CSP}}) = !in(c, m).let(x_{\mathsf{B}}) = adec(m, sk_{\mathsf{CSP}})inevent(e_2(x_f, x_c, x_b, sk_{\mathsf{CSP}})).\\ &out(c, (senc(x_f, sk_{\mathsf{CSP}}), senc(x_c, sk_{\mathsf{CSP}}), senc(x_b, sk_{\mathsf{CSP}})).c(m'') \\ &\mathsf{P}_{\mathsf{B}}(sk_{\mathsf{B}}, pk_{\mathsf{B}}) = (\mathbf{new}\ b)event(e_1(pk_{\mathsf{CSP}}, y_{\mathsf{B}}, b)).out(c, commit(y_{\mathsf{B}}, b)).in(c, m').\\ &let((y_f, y_c, y_b) = m')in \end{split}
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Fig. 3. Tokens encryption and secure computation protocol (QeSe)

References

1. B. Blanchet. Automatic verification of correspondences for security protocols. $Journal \ of \ Computer \ Security, \ 17(4):363-434, \ 2009.$