

# 116 CSC: Symmetric Encryption

**Greece, 3rd century BC**  
**~2,300 years ago.**



# Scytale



Scytale is the key to encrypt and decrypt the message

**This is my first  
encrypted message**

|          |          |          |          |          |          |          |          |
|----------|----------|----------|----------|----------|----------|----------|----------|
| <b>G</b> | <b>H</b> | <b>S</b> | <b>T</b> | <b>I</b> | <b>N</b> | <b>H</b> | <b>A</b> |
| <b>T</b> | <b>h</b> | <b>i</b> | <b>s</b> | <b>i</b> | <b>s</b> | <b>m</b> | <b>y</b> |
| <b>f</b> | <b>i</b> | <b>r</b> | <b>s</b> | <b>t</b> | <b>e</b> | <b>n</b> | <b>c</b> |
| <b>r</b> | <b>y</b> | <b>p</b> | <b>t</b> | <b>e</b> | <b>d</b> | <b>m</b> | <b>e</b> |
| <b>e</b> | <b>s</b> | <b>a</b> | <b>g</b> | <b>e</b> |          |          |          |

Ciphertext:

Tfrehiysirpasstgiteesedmnmyce

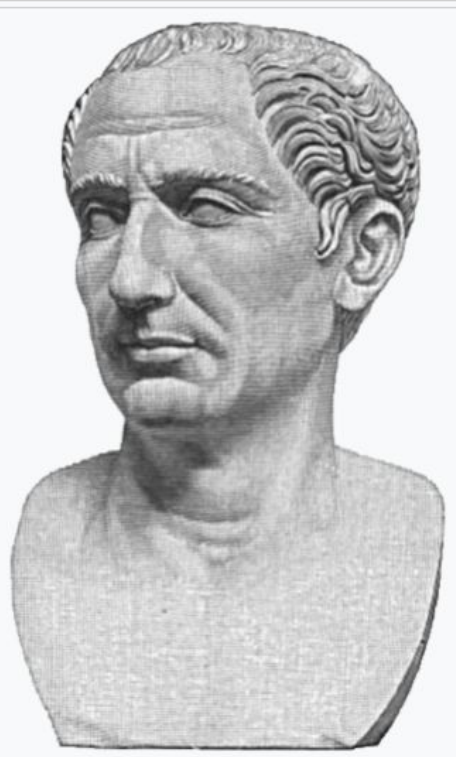
# Limitations


1. All the texts are readable which are easy to be attacked.
2. T is the first number

# Last century BC

~2000 year ago





The Caesar cipher is named  for [Julius Caesar](#), who used an alphabet where decrypting would shift three letters to the left.

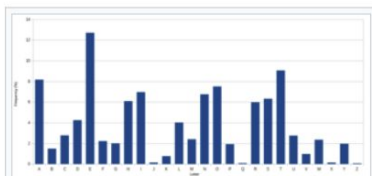
|        |   |   |   |   |   |   |   |   |       |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|--------|---|---|---|---|---|---|---|---|-------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| Plain  | A | B | C | D | E | F | G | H | I     | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
| Cipher | X | Y | Z | A | B | C | D | E | F     | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W |
| Random | T | Y | Z | B | C | F | H | J | ..... |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |

**Plaintext:** THE QUICK BROWN FOX JUMPS OVER THE LAZY DOG

**Ciphertext:** QEB NRFZH YOLTK CLU GRJMP LSBO QEB IXWV ALD

## Breaking the cipher [\[ edit \]](#)

The Caesar cipher can be easily broken even in a [ciphertext-only scenario](#). Since there are only a limited number of possible shifts (25 in English), an attacker can mount a [brute force attack](#) by deciphering the message, or part of it, using each possible shift. The correct description will be the one which makes sense as English text.<sup>[18]</sup> An example is shown on the right for the ciphertext "exxegoexsrgi"; the candidate plaintext for shift four "attackatonce" is the only one which makes sense as English text. Another type of brute force attack is to write out the alphabet beneath each letter of the ciphertext, starting at that letter. Again the correct decryption is the one which makes sense as English text. This technique is sometimes known as "completing the plain component".<sup>[19][20]</sup>



The distribution of letters in a typical sample of English language text has a distinctive and predictable shape. A Caesar shift "rotates" this distribution, and it is possible to determine the shift by examining the resultant frequency graph.

Another approach is to match up the frequency distribution of the letters. By graphing the frequencies of letters in the ciphertext, and by knowing the expected distribution of those letters in the original language of the plaintext, a human can easily spot the value of the shift by looking at the displacement of particular features of the graph. This is known as [frequency analysis](#). For example, in the English language the plaintext frequencies of the letters E, T,

(usually most frequent), and Q, Z (typically least frequent) are particularly distinctive.<sup>[21]</sup> Computers can automate this process by assessing the similarity between the observed frequency distribution and the expected distribution. This can be achieved, for instance, through the utilization of the [chi-squared statistic](#)<sup>[22]</sup> or by minimizing the sum of squared errors between the observed and known

| Decryption shift | Candidate plaintext |
|------------------|---------------------|
| 0                | exxegoexsrgi        |
| 1                | dwwdfndwrqfh        |
| 2                | cvvcemcvqpeg        |
| 3                | buubdlbupodf        |
| 4                | attackatonce        |
| 5                | zsszbjzsnmbd        |
| 6                | yrryaiyrmlac        |
| ...              |                     |
| 23               | haahjrhavujl        |
| 24               | gzzgiqgzutik        |
| 25               | fyyfhpftytshj       |

language distributions.<sup>[23]</sup>

# World War I

# Cipher Disk



**1470 AD –  
1940 AD**

600-200 years ago





Step back in time  
with this  
state-of-the-art  
encryption machine  
used during the  
conflict between  
Mexico and the  
USA before World  
War I

# Mexican–American War

🌐 73 languages

Article Talk

Read Edit View history Tools

From Wikipedia, the free encyclopedia

The **Mexican–American War**,<sup>[a]</sup> also known in the United States as the **Mexican War**, and in Mexico as the **United States intervention in Mexico**,<sup>[b]</sup> was an invasion of [Mexico](#) by the [United States Army](#) from 1846 to 1848. It followed the 1845 American [annexation of Texas](#), which Mexico still considered its territory because it refused to recognize the [Treaties of Velasco](#), signed by President [Antonio López de Santa Anna](#) after he was captured by the [Texian Army](#) during the 1836 [Texas Revolution](#). The [Republic of Texas](#) was *de facto* an independent country, but most of its Anglo-American citizens who had moved from the United States to Texas after 1822 wanted to be annexed by the United States.<sup>[5][6]</sup>

Sectional politics over [slavery in the United States](#) had previously prevented annexation because Texas would have been admitted as a slave state, upsetting the balance of power between Northern free states and Southern slave states.<sup>[7]</sup> In the [1844 United States presidential election](#), Democrat [James K. Polk](#) was elected on a platform of expanding U.S. territory to [Oregon](#), [California](#) (also a Mexican territory), and Texas by any means, with the 1845 annexation of Texas furthering that goal.<sup>[8]</sup> However, the boundary between Texas and Mexico was disputed, with the Republic of Texas and the U.S. asserting it to be the [Rio Grande](#) and Mexico claiming it to be the more-northern [Nueces River](#). Polk sent a diplomatic mission to Mexico in an attempt to buy the disputed territory, together with California and everything in between for \$25 million (equivalent to \$778 million in 2023), an offer the Mexican government refused.<sup>[9][10]</sup> Polk then sent a group of 80 soldiers across the disputed territory to the Rio Grande, ignoring Mexican demands to withdraw.<sup>[11][12]</sup> Mexican forces interpreted this as an attack and [repelled the U.S. forces](#) on April 25, 1846,<sup>[13]</sup> a move which Polk used to convince the Congress of the United States to declare war.<sup>[11]</sup>

## Mexican–American War



Clockwise from top: [Winfield Scott](#) entering [Plaza de la Constitución](#) after the [Fall of Mexico City](#), U.S. soldiers engaging the retreating Mexican force during the [Battle of Resaca de la Palma](#), U.S. victory at [Churubusco](#) outside of Mexico City, Marines storming [Chapultepec castle](#) under a large U.S. flag, [Battle of Cerro Gordo](#)

|          |  |
|----------|--|
| Date     | April 25, 1846 – February 2, 1848<br>(1 year, 9 months, 1 week and 1 day)  |
| Location | <a href="#">Texas</a> , <a href="#">New Mexico</a> , <a href="#">California</a> ; Northern, Central, and Eastern Mexico; <a href="#">Mexico City</a> |
| Result   | American victory <sup>[1]</sup>  |

# World War II



# Enigma == Puzzle



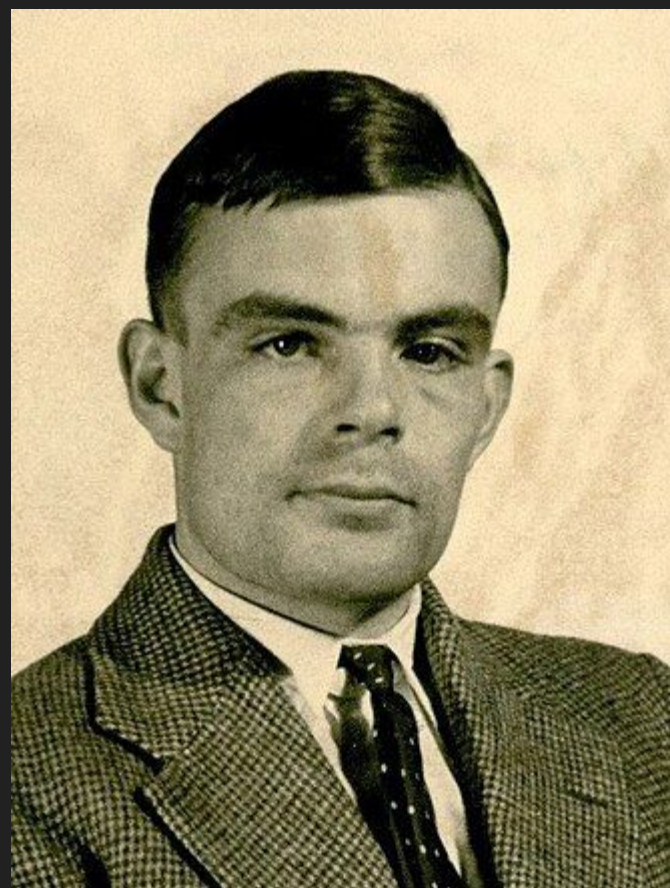
Change Keys every day in the wars



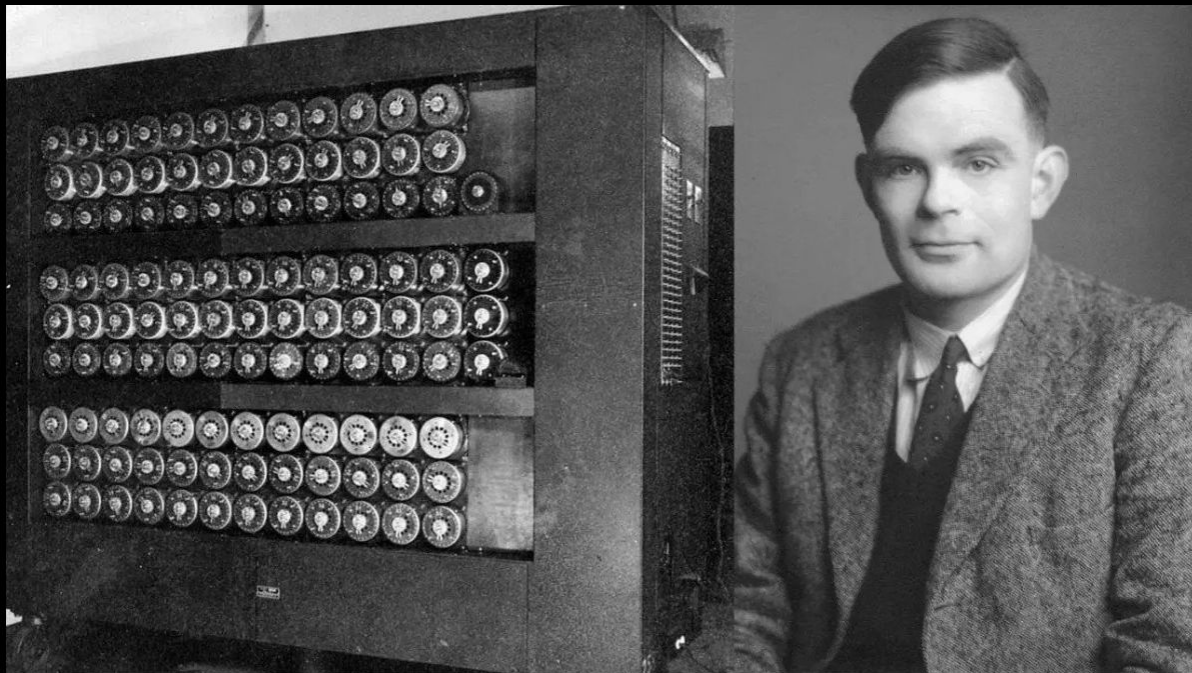
Fig. 4. Standard military ENIGMA

<https://www.cryptomuseum.com/crypto/enigma/i/index.htm>

The "Enigma" was a cipher machine extensively used by **Nazi Germany** during World War II to encode secret messages, considered so secure at the time that it was believed to be unbreakable



# 1936: Alan Turing & The Turing Machine - Pivotal Moments



Welcome to our fourth Pivotal Moments blog. If you follow us on [social media](#), you'll know what this is all about. To paraphrase Confucius, it's only by knowing where we've been that we can understand where we're going.





# Modern Cryptography

100 year ago ~ present

# Symmetric Encryption

Symmetric encryption is a type of encryption key management solution where only one key (a secret key) is used to both encrypt and decrypt.

## DES (Data Encryption Standard)

- Originally designed **by IBM** and adopted by the U.S. government in 1977 as a Federal Data Processing Standard.
- Uses a 56-bit key and supports multiple operation modes (e.g., ECB, CBC).
- Now considered insecure primarily due to its relatively short key length, making it vulnerable to **brute-force attacks**.



## AES (Advanced Encryption Standard)

- Also known as Rijndael, designed by Joan Daemen and Vincent Rijmen.
- One of the **most widely used symmetric encryption** algorithms today.
- Supports key sizes of 128, 192, or 256 bits.
- Offers strong security and high performance, making it the top choice in most modern applications.

## Blowfish

- Designed by Bruce Schneier; supports a variable key length ranging from 32 to 448 bits.
- Known for its fast encryption speed and high security.
- Particularly suitable for environments with limited resources (e.g., embedded systems).

## ChaCha20

- Designed by Daniel J. Bernstein; typically classified as a **stream cipher** but also considered a form of symmetric encryption.
- Renowned for its efficiency, speed, and strong security properties.
- Widely used in modern protocols, including certain cipher suites in TLS 1.3.

## ASCII Table

Dec = Decimal Value  
Char = Character

'5' has the int value 53

if we write '5'-'0' it evaluates to 53-48, or the int 5

if we write char c = 'B'+32; then c stores 'b'

# 128 chars

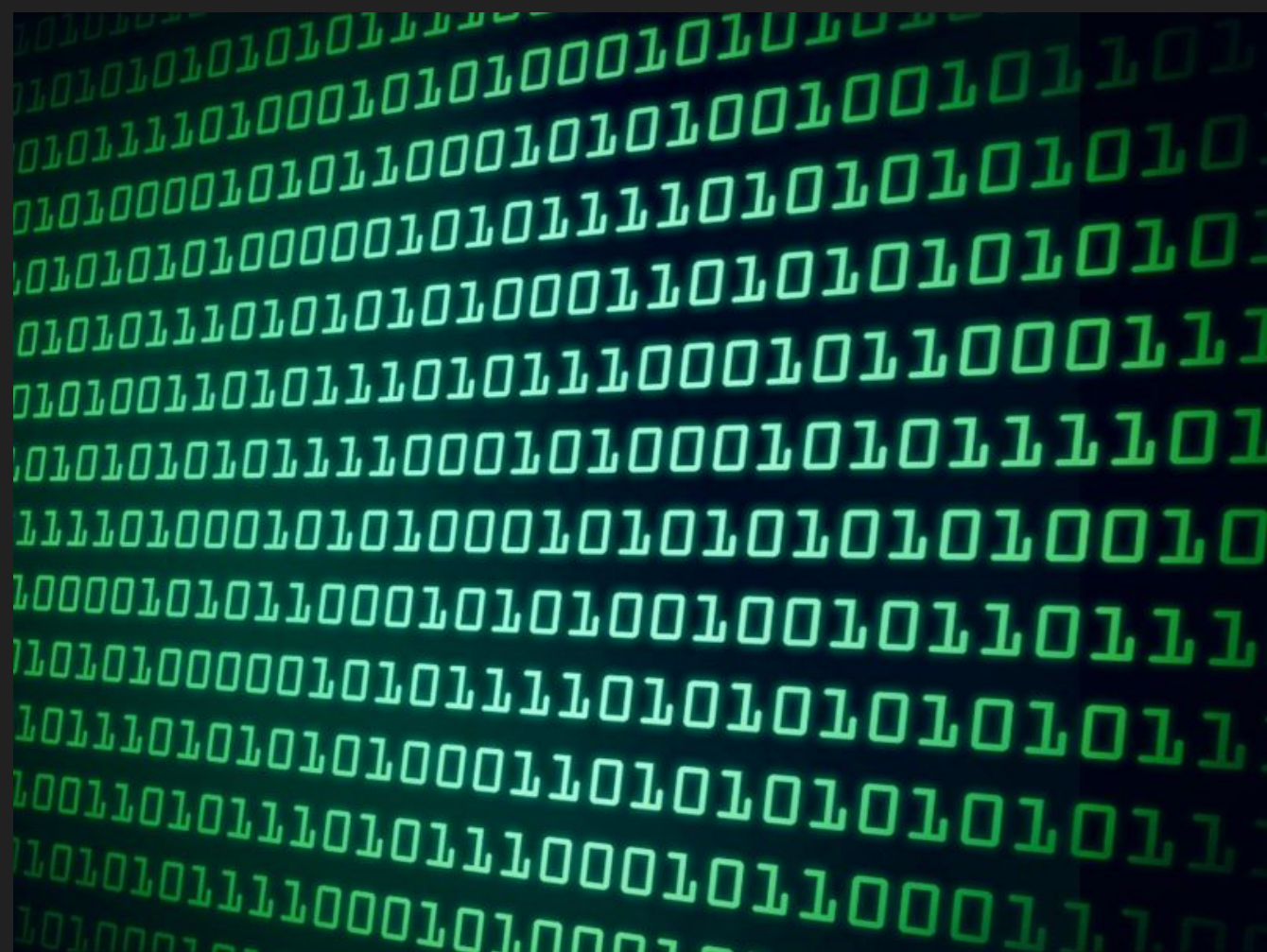
| Dec | Char                        | Dec | Char  | Dec | Char | Dec | Char |
|-----|-----------------------------|-----|-------|-----|------|-----|------|
| 0   | NUL (null)                  | 32  | SPACE | 64  | @    | 96  | `    |
| 1   | SOH (start of heading)      | 33  | !     | 65  | A    | 97  | a    |
| 2   | STX (start of text)         | 34  | "     | 66  | B    | 98  | b    |
| 3   | ETX (end of text)           | 35  | #     | 67  | C    | 99  | c    |
| 4   | EOT (end of transmission)   | 36  | \$    | 68  | D    | 100 | d    |
| 5   | ENQ (enquiry)               | 37  | %     | 69  | E    | 101 | e    |
| 6   | ACK (acknowledge)           | 38  | &     | 70  | F    | 102 | f    |
| 7   | BEL (bell)                  | 39  | '     | 71  | G    | 103 | g    |
| 8   | BS (backspace)              | 40  | (     | 72  | H    | 104 | h    |
| 9   | TAB (horizontal tab)        | 41  | )     | 73  | I    | 105 | i    |
| 10  | LF (NL line feed, new line) | 42  | *     | 74  | J    | 106 | j    |
| 11  | VT (vertical tab)           | 43  | +     | 75  | K    | 107 | k    |
| 12  | FF (NP form feed, new page) | 44  | ,     | 76  | L    | 108 | l    |
| 13  | CR (carriage return)        | 45  | -     | 77  | M    | 109 | m    |
| 14  | SO (shift out)              | 46  | .     | 78  | N    | 110 | n    |
| 15  | SI (shift in)               | 47  | /     | 79  | O    | 111 | o    |
| 16  | DLE (data link escape)      | 48  | 0     | 80  | P    | 112 | p    |
| 17  | DC1 (device control 1)      | 49  | 1     | 81  | Q    | 113 | q    |
| 18  | DC2 (device control 2)      | 50  | 2     | 82  | R    | 114 | r    |
| 19  | DC3 (device control 3)      | 51  | 3     | 83  | S    | 115 | s    |
| 20  | DC4 (device control 4)      | 52  | 4     | 84  | T    | 116 | t    |
| 21  | NAK (negative acknowledge)  | 53  | 5     | 85  | U    | 117 | u    |
| 22  | SYN (synchronous idle)      | 54  | 6     | 86  | V    | 118 | v    |
| 23  | ETB (end of trans. block)   | 55  | 7     | 87  | W    | 119 | w    |
| 24  | CAN (cancel)                | 56  | 8     | 88  | X    | 120 | x    |
| 25  | EM (end of medium)          | 57  | 9     | 89  | Y    | 121 | y    |
| 26  | SUB (substitute)            | 58  | :     | 90  | Z    | 122 | z    |
| 27  | ESC (escape)                | 59  | ;     | 91  | [    | 123 | {    |
| 28  | FS (file separator)         | 60  | <     | 92  | \    | 124 |      |
| 29  | GS (group separator)        | 61  | =     | 93  | ]    | 125 | }    |
| 30  | RS (record separator)       | 62  | >     | 94  | ^    | 126 | ~    |
| 31  | US (unit separator)         | 63  | ?     | 95  | _    | 127 | DEL  |

<https://www.rapidtables.com/convert/number/decimal-to-binary.html?x=97>

Hello == 72 101 108 108 111

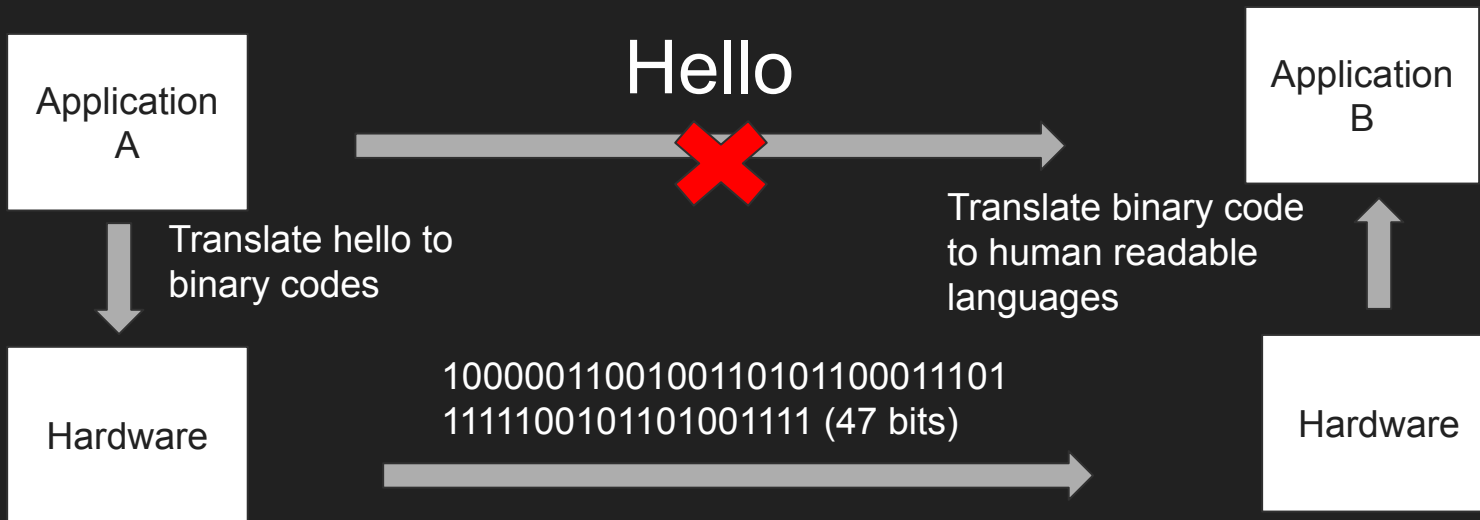
1000 0011 0010 0110 1011 0001  
1101 1111 1001 0110 1001 111 ==  
47 bits

hello



# COMPUTER A

# COMPUTER B



Hello World!

Question?

01001000 01100101 01101100  
01101100 01101111 00100000  
01010111 01101111 01110010  
01101100 01100100 00100001

96 Bits == 12 Bytes



8 Bits == 1 Byte

Binary Data



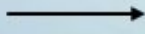
1 0 0 1 0 1 0 1

Algorithm Function



$f(x)$

Random  
Encryption Key



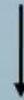
0 1 1 1 0 0 1 0

## Stream Cipher

Stream ciphers are the algorithms that encrypt basic information, one byte/bit at a time.

---

1 0 1 1 1 0 0 1



W<sup>3</sup>KO#

Ciphertext

Each Block

Encryption Key

## Block Cipher

Encrypted Block

01001000

+



01100101

+



01101100

+



01011100

+



01101111

+



10101110

01110101

01001001

10110010

11101001



block ciphers separate the raw information into chunks of data of a fixed size.

10101110 + 01110101 + 01001001 + 10110010 + 11101001



10101110 01110101 01001001 10110010 11101001



W\$2M&

Ciphertext

Encryption is the process of transforming a message, usually called cyphered message, in such a way that only the intended parties can reverse it. The process of reversing encryption is called decryption. This implies that, as opposed to hashes, encryption is reversible.

There are two main types of encryption, symmetric and asymmetric, this chapter will cover symmetric encryption.

In symmetric encryption, the message to be sent is encrypted using a single secret password, also called key. Anyone with that secret key and decrypt the message and see the original content.

1000 Bytes

Key = 32 Bytes

**AES (32 Bytes 256 bits)**

Why secure ?

Let's put it this way: **brute-forcing** an AES-256 key—even with massive GPU power—is effectively impossible with current (and near-future) technology. The size of the AES-256 key space is  $2^{256}$ , which is around  $1.16 \times 10^{77}$ . Even if you had a hypothetical machine that could test  $10^{18}$  (one quintillion) keys per second—which is vastly more powerful than any general-purpose GPU cluster today—you would still need on the order of:

$$\frac{2^{256}}{10^{18}} \approx 10^{59} \text{ seconds}$$

To give that some perspective:

- There are about  $3.154 \times 10^7$  seconds in a year.
- So that's about  $10^{52}$  years of brute-forcing, many orders of magnitude greater than the age of the universe (roughly  $1.38 \times 10^{10}$  years).

In other words:

1. **It's not feasible** to brute-force AES-256 using any practical amount of GPUs.
2. **It's effectively negligible** (i.e., you can treat the probability of a successful brute force as zero for all realistic purposes).

Brute Force Attack is  
**Negligible** to attack AES-256



**Keys can include more than just numbers and characters.**

**They can be very long—up to 256 bits.**

**Even with GPU acceleration, guessing these keys remains extremely difficult.**

# Asymmetric Encryption

Asymmetric encryption, also known as public-key cryptography, is a method of encryption that uses **two different** keys: **a public key** that can be shared freely and **a private key that must be kept secret**, where data encrypted with the public key can only be decrypted using the corresponding private key, allowing secure communication without the need to pre-share a secret key with the recipient.

Game time!

**RSA** (Rivest–Shamir–Adleman)  
ElGamal “**el-guh-MAHL**” Encryption  
ECC (Elliptic Curve Cryptography)  
Paillier (**‘pie-yay’**) Cryptosystem

1. Asymmetric encryption is NOT used for encrypting large messages.
2. Instead, it is mainly used to encrypt small secrets (like an AES key)

#### How Large Can RSA, ECC, or ElGamal Encrypt?

| Asymmetric Algorithm | Max Message Size (for 2048-bit key)      |
|----------------------|--|
| RSA (2048-bit key)   | ~245 bytes (with padding)                |
| ECC (256-bit key)    | Very small, used for key exchange        |
| ElGamal              | Similar to RSA, also slow for large data |

## Symmetric Encryption (Symmetric Encryption)

- **Advantages:** **Fast speed**, suitable for quickly encrypting and decrypting large-scale data.
- **Disadvantages:** Key management is difficult; the key must be securely shared and protected.

## Asymmetric Encryption (Public-Key Encryption)

- **Advantages:** Public keys can be distributed openly, enabling secure key exchange and supporting digital signatures and identity authentication.
- **Disadvantages:** **Slower speed**, more complex algorithms, generally used only to encrypt a small amount of sensitive information or to exchange symmetric keys.

We usually use a combined  
solution. How?

# Demo





```
from cryptography.fernet import Fernet

# we will be encrypting the below string.
message = "hello geeks"

# generate a key for encryption and decryption
# You can use fernet to generate
# the key or use random key generator
# here I'm using fernet to generate key

key = Fernet.generate_key()

# Instance the Fernet class with the key

fernet = Fernet(key)

# then use the Fernet class instance
# to encrypt the string string must
# be encoded to byte string before encryption
encMessage = fernet.encrypt(message.encode())

print("original string: ", message)
print("encrypted string: ", encMessage)

# decrypt the encrypted string with the
# Fernet instance of the key,
# that was used for encrypting the string
# encoded byte string is returned by decrypt method,
# so decode it to string with decode methods
decMessage = fernet.decrypt(encMessage).decode()

print("decrypted string: ", decMessage)
```

## Output:

```
(venv) C:\Users\user>python3 fernet.py
original string:  hello geeks
encrypted string:  b'gAAAAABgE4gyG_0ceYqYzE8_qRFb1Q6EO_6ms-uSX1CK9af2PTp4a8e_ONxc2Xy071rzaKxPHvG-jh0iq0CDEky3F_Qmjv8Cdw=='
decrypted string:  hello geeks
```



```
import rsa

# generate public and private keys with
# rsa.newkeys method, this method accepts
# key length as its parameter
# key length should be atleast 16
publicKey, privateKey = rsa.newkeys(512)

# this is the string that we will be encrypting
message = "hello geeks"

# rsa.encrypt method is used to encrypt
# string with public key string should be
# encode to byte string before encryption
# with encode method
encMessage = rsa.encrypt(message.encode(),
                          publicKey)

print("original string: ", message)
print("encrypted string: ", encMessage)

# the encrypted message can be decrypted
# with ras.decrypt method and private key
# decrypt method returns encoded byte string,
# use decode method to convert it to string
# public key cannot be used for decryption
decMessage = rsa.decrypt(encMessage, privateKey).decode()

print("decrypted string: ", decMessage)
```

## Output:

```
original string: hello geeks
encrypted string: b'\x8f\xd0>\xce\xdf>\xec\x14\xb4R\x93\xab+\xcd\x18\xaci\x949\xfcCr\x8e\xe9\xfb'
decrypted string: hello geeks
```

# One time pad

The **One-Time Pad (OTP)** is a cryptographic method that provides **perfect secrecy**, meaning it is theoretically **unbreakable**

## Why Isn't OTP Used in Practice?

### ✗ Key Distribution Problem

- The sender and receiver **must share the same key in advance**, which must be as long as the message.
- If you can securely transmit the key, why not send the message directly?

### ✗ Key Must Be Truly Random

- If the key is predictable, encryption is **not secure**.

### ✗ Key Can Only Be Used Once

- If a key is reused, attackers can detect patterns and **break the encryption**.

- ♦ **One-Time Pad is the only encryption method proven to be unbreakable.**
- ♦ **However, it is impractical for everyday use due to key management issues.**
- ♦ **Modern encryption (AES, RSA) is used instead, balancing security and usability.**

Encryption is the process of transforming a message, usually called cyphered message, in such a way that only the intended parties can reverse it. The process of reversing encryption is called decryption. This implies that, as opposed to hashes, encryption is reversible.

1024 Bits

There are two main types of encryption, symmetric and asymmetric, this chapter will cover symmetric encryption.


In symmetric encryption, the message to be sent is encrypted using a single secret password, also called key. Anyone with that secret key and decrypt the message and see the original content.

KEY length == 1024 Bits

Future:

Quantum Computing is trying to  
destory all the existed solutions



Peter Shor (pictured here in ) showed in 1994 that a scalable quantum computer would be able to break RSA encryption.

**Post-quantum cryptography (PQC) is a new generation of cryptographic algorithms that are designed to protect against attacks from quantum computers.**

# Lattice-Based Cryptographic Algorithm



# ZOOM IN PHOTOGRAPHY



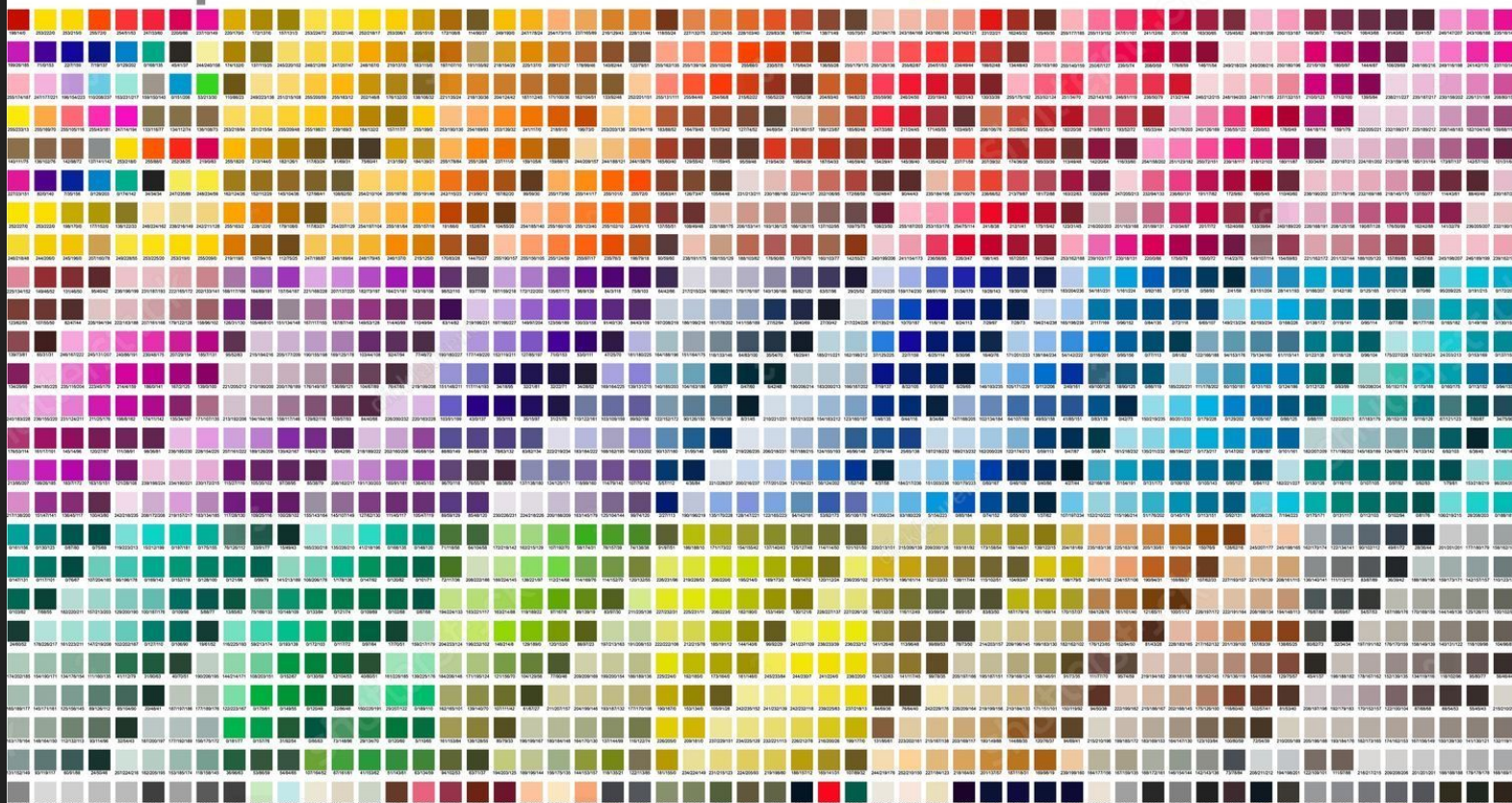


shutterstock

[www.shutterstock.com](http://www.shutterstock.com) • 1592483047

# Color palette to RGB

# RGB number values



|        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |        |  |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--|
| 241001 | 241002 | 241003 | 241004 | 241005 | 241006 | 241007 | 241008 | 241009 | 241010 | 241011 | 241012 | 241013 | 241014 | 241015 | 241016 | 241017 | 241018 | 241019 | 241020 | 241021 | 241022 | 241023 | 241024 | 241025 | 241026 | 241027 | 241028 | 241029 | 241030 | 241031 | 241032 | 241033 | 241034 | 241035 | 241036 | 241037 | 241038 | 241039 | 241040 | 241041 | 241042 | 241043 | 241044 | 241045 | 241046 | 241047 | 241048 | 241049 | 241050 | 241051 | 241052 | 241053 | 241054 | 241055 | 241056 | 241057 | 241058 | 241059 | 241060 | 241061 | 241062 | 241063 | 241064 | 241065 | 241066 | 241067 | 241068 | 241069 | 241070 | 241071 | 241072 | 241073 | 241074 | 241075 | 241076 | 241077 | 241078 | 241079 | 241080 | 241081 | 241082 | 241083 | 241084 | 241085 | 241086 | 241087 | 241088 | 241089 | 241090 | 241091 | 241092 | 241093 | 241094 | 241095 | 241096 | 241097 | 241098 | 241099 | 241100 | 241101 | 241102 | 241103 | 241104 | 241105 | 241106 | 241107 | 241108 | 241109 | 241110 | 241111 | 241112 | 241113 | 241114 | 241115 | 241116 | 241117 | 241118 | 241119 | 241120 | 241121 | 241122 | 241123 | 241124 | 241125 | 241126 | 241127 | 241128 | 241129 | 241130 | 241131 | 241132 | 241133 | 241134 | 241135 | 241136 | 241137 | 241138 | 241139 | 241140 | 241141 | 241142 | 241143 | 241144 | 241145 | 241146 | 241147 | 241148 | 241149 | 241150 | 241151 | 241152 | 241153 | 241154 | 241155 | 241156 | 241157 | 241158 | 241159 | 241160 | 241161 | 241162 | 241163 | 241164 | 241165 | 241166 | 241167 | 241168 | 241169 | 241170 | 241171 | 241172 | 241173 | 241174 | 241175 | 241176 | 241177 | 241178 | 241179 | 241180 | 241181 | 241182 | 241183 | 241184 | 241185 | 241186 | 241187 | 241188 | 241189 | 241190 | 241191 | 241192 | 241193 | 241194 | 241195 | 241196 | 241197 | 241198 | 241199 | 241200 | 241201 | 241202 | 241203 | 241204 | 241205 | 241206 | 241207 | 241208 | 241209 | 241210 | 241211 | 241212 | 241213 | 241214 | 241215 | 241216 | 241217 | 241218 | 241219 | 241220 | 241221 | 241222 | 241223 | 241224 | 241225 | 241226 | 241227 | 241228 | 241229 | 241230 | 241231 | 241232 | 241233 | 241234 | 241235 | 241236 | 241237 | 241238 | 241239 | 241240 | 241241 | 241242 | 241243 | 241244 | 241245 | 241246 | 241247 | 241248 | 241249 | 241250 | 241251 | 241252 | 241253 | 241254 | 241255 | 241256 | 241257 | 241258 | 241259 | 241260 | 241261 | 241262 | 241263 | 241264 | 241265 | 241266 | 241267 | 241268 | 241269 | 241270 | 241271 | 241272 | 241273 | 241274 | 241275 | 241276 | 241277 | 241278 | 241279 | 241280 | 241281 | 241282 | 241283 | 241284 | 241285 | 241286 | 241287 | 241288 | 241289 | 241290 | 241291 | 241292 | 241293 | 241294 | 241295 | 241296 | 241297 | 241298 | 241299 | 241300 | 241301 | 241302 | 241303 | 241304 | 241305 | 241306 | 241307 | 241308 | 241309 | 241310 | 241311 | 241312 | 241313 | 241314 | 241315 | 241316 | 241317 | 241318 | 241319 | 241320 | 241321 | 241322 | 241323 | 241324 | 241325 | 241326 | 241327 | 241328 | 241329 | 241330 | 241331 | 241332 | 241333 | 241334 | 241335 | 241336 | 241337 | 241338 | 241339 | 241340 | 241341 | 241342 | 241343 | 241344 | 241345 | 241346 | 241347 | 241348 | 241349 | 241350 | 241351 | 241352 | 241353 | 241354 | 241355 | 241356 | 241357 | 241358 | 241359 | 241360 | 241361 | 241362 | 241363 | 241364 | 241365 | 241366 | 241367 | 241368 | 241369 | 241370 | 241371 | 241372 | 241373 | 241374 | 241375 | 241376 | 241377 | 241378 | 241379 | 241380 | 241381 | 241382 | 241383 | 241384 | 241385 | 241386 | 241387 | 241388 | 241389 | 241390 | 241391 | 241392 | 241393 | 241394 | 241395 | 241396 | 241397 | 241398 | 241399 | 241400 | 241401 | 241402 | 241403 | 241404 | 241405 | 241406 | 241407 | 241408 | 241409 | 241410 | 241411 | 241412 | 241413 | 241414 | 241415 | 241416 | 241417 | 241418 | 241419 | 241420 | 241421 | 241422 | 241423 | 241424 | 241425 | 241426 | 241427 | 241428 | 241429 | 241430 | 241431 | 241432 | 241433 | 241434 | 241435 | 241436 | 241437 | 241438 | 241439 | 241440 | 241441 | 241442 | 241443 | 241444 | 241445 | 241446 | 241447 | 241448 | 241449 | 241450 | 241451 | 241452 | 241453 | 241454 | 241455 | 241456 | 241457 | 241458 | 241459 | 241460 | 241461 | 241462 | 241463 | 241464 | 241465 | 241466 | 241467 | 241468 | 241469 | 241470 | 241471 | 241472 | 241473 | 241474 | 241475 | 241476 | 241477 | 241478 | 241479 | 241480 | 241481 | 241482 | 241483 | 241484 | 241485 | 241486 | 241487 | 241488 | 241489 | 241490 | 241491 | 241492 | 241493 | 241494 | 241495 | 241496 | 241497 | 241498 | 241499 | 241500 | 241501 | 241502 | 241503 | 241504 | 241505 | 241506 | 241507 | 241508 | 241509 | 241510 | 241511 | 241512 | 241513 | 241514 | 241515 | 241516 | 241517 | 241518 | 241519 | 241520 | 241521 | 241522 | 241523 | 241524 | 241525 | 241526 | 241527 | 241528 | 241529 | 241530 | 241531 | 241532 | 241533 | 241534 | 241535 | 241536 | 241537 | 241538 | 241539 | 241540 | 241541 | 241542 | 241543 | 241544 | 241545 | 241546 | 241547 | 241548 | 241549 | 241550 | 241551 | 241552 | 241553 | 241554 | 241555 | 241556 | 241557 | 241558 | 241559 | 241560 | 241561 | 241562 | 241563 | 241564 | 241565 | 241566 | 241567 | 241568 | 241569 | 241570 | 241571 | 241572 | 241573 | 241574 | 241575 | 241576 | 241577 | 241578 | 241579 | 241580 | 241581 | 241582 | 241583 | 241584 | 241585 | 241586 | 241587 | 241588 | 241589 | 241590 | 241591 | 241592 | 241593 | 241594 | 241595 | 241596 | 241597 | 241598 | 241599 | 241600 | 241601 | 241602 | 241603 | 241604 | 241605 | 241606 | 241607 | 241608 | 241609 | 241610 | 241611 | 241612 | 241613 | 241614 | 241615 | 241616 | 241617 | 241618 | 241619 | 241620 | 241621 | 241622 | 241623 | 241624 | 241625 | 241626 | 241627 | 241628 | 241629 | 241630 | 241631 | 241632 | 241633 | 241634 | 241635 | 241636 | 241637 | 241638 | 241639 | 241640 | 241641 | 241642 | 241643 | 241644 | 241645 | 241646 | 241647 | 241648 | 241649 | 241650 | 241651 | 241652 | 241653 | 241654 | 241655 | 241656 | 241657 | 241658 | 241659 | 241660 | 241661 | 241662 | 241663 | 241664 | 241665 | 241666 | 241667 | 241668 | 241669 | 241670 | 241671 | 241672 | 241673 | 241674 | 241675 | 241676 | 241677 | 241678 | 241679 | 241680 | 241681 | 241682 | 241683 | 241684 | 241685 | 241686 | 241687 | 241688 | 241689 | 241690 | 241691 | 241692 | 241693 | 241694 | 241695 | 241696 | 241697 | 241698 | 241699 | 241700 | 241701 | 241702 | 241703 | 241704 | 241705 | 241706 | 241707 | 241708 | 241709 | 241710 | 241711 | 241712 | 241713 | 241714 | 241715 | 241716 | 241717 | 241718 | 241719 | 241720 | 241721 | 241722 | 241723 | 241724 | 241725 | 241726 | 241727 | 241728 | 241729 | 241730 | 241731 | 241732 | 241733 | 241734 | 241735 | 241736 | 241737 | 241738 | 241739 | 241740 | 241741 | 241742 | 241743 | 241744 | 241745 | 241746 | 241747 | 241748 | 241749 | 241750 | 241751 | 241752 | 241753 | 241754 | 241755 | 241756 | 241757 | 241758 | 241759 | 241760 | 241761 | 241762 | 241763 | 241764 | 241765 | 241766 | 241767 | 241768 | 241769 | 241770 | 241771 | 241772 | 241773 | 241774 | 241775 | 241776 | 241777 | 241778 | 241779 | 241780 | 241781 | 241782 | 241783 | 241784 | 241785 | 241786 | 241787 | 241788 | 241789 | 241790 | 241791 | 241792 | 241793 | 241794 | 241795 | 241796 | 241797 | 241798 | 241799 | 241800 | 241801 | 241802 | 241803 | 241804 | 241805 | 241806 | 241807 | 241808 | 241809 | 241810 | 241811 | 241812 | 241813 | 241814 | 241815 | 241816 | 241817 | 241818 | 241819 | 241820 | 241821 | 241822 | 241823 | 241824 | 241825 | 241826 | 241827 | 241828 | 241829 | 241830 | 241831 | 241832 | 241833 | 241834 | 241835 | 241836 | 241837 | 241838 | 241839 | 241840 | 241841 | 241842 | 241843 | 241844 | 241845 | 241846 | 241847 | 241848 | 241849 | 241850 | 241851 | 241852 | 241853 | 241854 | 241855 | 241856 | 241857 | 241858 | 241859 | 241860 | 241861 | 241862 | 241863 | 241864 | 241865 | 241866 | 241867 | 241868 | 241869 | 241870 | 241871 | 241872 | 241873 | 241874 | 241875 | 241876 | 241877 | 241878 | 241879 | 241880 | 241881 | 241882 | 241883 | 241884 | 241885 | 241886 | 241887 | 241888 | 241889 | 241890 | 241891 | 241892 | 241893 | 241894 | 241895 | 241896 | 241897 | 241898 | 241899 | 241900 | 241901 | 241902 | 241903 | 241904 | 241905 | 241906 | 241907 | 241908 | 241909 | 241910 | 241911 | 241912 | 241913 | 241914 | 241915 | 241916 | 241917 | 241918 | 241919 | 241920 | 241921 | 241922 | 241923 | 241924 | 241925 | 241926 | 241927 | 241928 | 241929 | 241930 | 241931 | 241932 | 241933 | 241934 | 241935 | 241936 | 241937 | 241938 | 241939 | 241940 | 241941 | 241942 | 241943 | 241944 | 241945 | 241946 | 241947 | 241948 | 241949 | 241950 | 241951 | 241952 | 241953 | 241954 | 241955 | 241956 | 241957 | 241958 | 241959 | 241960 | 241961 | 241962 | 241963 | 241964 | 241965 | 241966 | 241967 | 241968 | 241969 | 241970 | 241971 | 241972 | 241973 | 241974 | 241975 | 241976 | 241977 | 241978 | 241979 | 241980 | 241981 | 241982 | 241983 | 241984 | 241985 | 241986 | 241987 | 241988 | 241989 | 241990 | 241991 | 241992 | 241993 | 241994 | 241995 | 241996 | 241997 | 241998 | 241999 | 242000 | 242001 | 242002 | 242003 | 242004 | 242005 | 242006 | 242007 | 242008 | 242009 | 242010 | 242011 | 242012 | 242013 | 242014 | 242015 | 242016 | 242017 | 242018 | 242019 | 242020 | 242021 | 242022 | 242023 | 242024 | 242025 | 242026 | 242027 | 242028 | 242029 | 242030 | 242031 | 242032 | 242033 | 242034 | 242035 | 242036 | 242037 | 242038 | 242039 | 242040 | 242041 | 242042 | 242043 | 242044 | 242045 | 242046 | 242047 | 242048 | 242049 | 242050 | 242051 | 242052 | 242053 | 242054 | 242055 | 242056 | 242057 | 242058 | 242059 | 242060 | 242061 | 242062 | 242063 | 242064 | 242065 | 242066 | 242067 | 242068 | 242069 | 242070 | 242071 | 242072 | 242073 | 242074 | 242075 | 242076 | 242077 | 242078 | 242079 | 242080 | 242081 | 242082 | 242083 | 242084 | 242085 | 242086 | 242087 | 242088 | 242089 | 242090 | 242091 | 242092 | 242093 | 242094 | 242095 | 242096 | 242097 | 242098 | 242099 | 242100 | 242101 | 242102 | 242103 | 242104 |  |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--|



1. **Original Image:** Load and display the image.
2. **Lattice-Based Encryption:** Convert the image into pixel values and apply encryption (adding controlled noise).
3. **Transmission of Encrypted Image:** The noisy image is stored or sent.
4. **Decryption Using the Secret Key:** The receiver applies the secret key to remove noise and reconstruct the original image.

Why add noises work?