

# Interval Set Cover

Alice has an array of n empty sets:  $A[1], A[2], \ldots, A[n]$ . Since the empty sets are not interesting, she wants to perform k operations on them. On operation i, Alice selects two integers l[i] and r[i] such that  $1 \leq l[i] \leq r[i] \leq n$ , and adds the element i to all sets A[j] such that  $l[i] \leq j \leq r[i]$ .

For example, if n=3 and k=2, and Alice picks (l[1],r[1])=(2,3) and (l[2],r[2])=(1,3), then, after the first operation,

$$A[1]=\{\},\ A[2]=\{1\},\ \text{and}\ A[3]=\{1\},$$

and after the second operation,

$$A[1] = \{2\}, A[2] = \{1, 2\}, \text{ and } A[3] = \{1, 2\}.$$

After all k operations are done, Alice's sets have a really cool structure. However, Farhan is jealous of this, so he concocts an wicked plan:

- First, he chooses a permutation  $p=(p_1,p_2,\ldots,p_n)$  of the integers  $1,2,\ldots,n$ ; that is, p has each of the numbers from 1 to n exactly once in some order of Farhan's choosing.
- Then he creates another array B of sets  $B[1], B[2], \ldots, B[n]$  such that  $B[i] = A[p_i]$ .
- Finally, he masterfully replaces Alice's array A with his new array B when she is not around.

Alice, of course, notices that her array of sets has been messed around. Unfortunately, she no longer remembers the integers l[i] and r[i]. It makes Alice sad, so she wants to keep some of sets from the new array and throw the rest of them away. But she wants to do it in a such that every element from 1 to k is in at least of one the sets that she keeps.

More formally, Alice wants to select the minimum number of sets such that their union is  $\{1,2,\ldots,k\}$ .

### Input

You will be given the array of sets B in the input. Let's assume that the set B[i] has  $c_i$  unique elements. Let those elements be  $B[i][1], B[i][2], \ldots, B[i][c_i]$  without duplication.

Read the input from the standard input in the following format:

- line 1: n k
- line 2i ( $1 \le i \le n$ ):  $c_i$
- line 2i + 1  $(1 \le i \le n)$ : B[i][1] B[i][2] ...  $B[i][c_i]$

### Output

Suppose the minimum number of sets Alice has to keep is m, and the m sets she chooses are  $B[t_1], B[t_2], \ldots, B[t_m]$ . Write the output to the standard output in the following format:

```
• line 1: m
• line 2: t[1] t[2] \cdots t[m]
```

You can output the indices in any order. If there are multiple solutions, you may print any of them.

#### **Constraints**

```
• 1 \le n \le 2000
```

- $1 \le k \le 2000$
- $1 \le t_i \le k$  (for all  $1 \le i \le n$ )
- $1 \leq B[i][j] \leq k$  (for all  $1 \leq i \leq n$  and  $1 \leq j \leq t_i$ )
- For each integer j such that  $1 \le j \le k$ , there is at least one set which contains j.

### **Subtasks**

```
1. (4 points) n \leq 15
```

- 2. (5 points)  $k \leq 15$
- 3. (11 points)  $p_i = i$  (for all  $1 \le i \le n$ )
- 4. (17 points)  $n, k \leq 80$ , and for any two i, j, the ranges [l[i], r[i]] and [l[j], r[j]] must either be disjoint, or one must be contained by another.
- 5. (20 points)  $n, k \le 80$
- 6. (15 points)  $n, k \le 300$
- 7. (28 points) No further constraints.

## Example 1

```
3 2
2
1 2
1
2
2
1 2
```

The correct output is:

```
1
1
```

This example is described in the problem statement. Notice that p=(2,1,3). The optimal solution chooses the set B[1] which includes all elements. Choosing the set B[3] is also a valid solution.

# Example 2



The correct output is:

```
2
2 3
```

Here, it's optimal to keep sets B[2] and B[3], which covers all 5 elements. It's easy to see that there cannot be any solution that includes only one set, hence this is optimal.