



# The Wheels on the Bus

South-park Elementary is going on a picnic. There are  $n$  students and  $k$  buses to transport them to the picnic spot. The students are numbered from 1 to  $n$ , and the buses are numbered from 1 to  $k$ .

To ensure that all students are happy, Mr. PC Principal has asked for their opinions. There are a total of  $m$  opinions, each of which can be of two types:

- 1  $x$   $y$ : student  $x$  and student  $y$  cannot sit on the same bus.
- 2  $x$   $y$   $z$ : if student  $x$  is in bus  $z$ , then student  $y$  must also be in bus  $z$ , or vice versa. In other words, either both students are in bus  $z$  or neither of them is in bus  $z$ .

Your task is to determine the number of ways to assign each student to a bus such that all of the opinions are respected. Two assignments are considered different if there is at least one student who is assigned to different buses.

Note that a bus can be empty, meaning that no student is assigned to it. It can also have all the students assigned to it.

## Input

Read the input from the standard input in the following format:

- line 1:  $n$   $k$   $m$
- line  $1 + i$  ( $1 \leq i \leq m$ ): this line describes opinion  $i$  and follows one of the following formats:
  - 1  $x$   $y$
  - 2  $x$   $y$   $z$

## Output

Write the output to the standard output in the following format:

- line 1: the number of ways to assign each student to a bus such that all the opinions are satisfied

## Constraints

- $1 \leq n \leq 17$
- $2 \leq k \leq 5$
- $0 \leq m \leq \frac{1}{2} \cdot n \cdot (n - 1) \cdot (k + 1)$
- $1 \leq x, y \leq n$ ,  $x \neq y$ , and  $1 \leq z \leq k$

- No two opinions are the same.

## Subtasks

1. (9 points)  $k = 2$
2. (21 points) All opinions are of type 2.
3. (22 points)  $1 \leq n \leq 13$
4. (48 points) No further constraints.

## Examples

### Example 1

```
4 2 3
2 1 2 1
1 2 3
2 3 4 1
```

The correct output is

```
2
```

If, in an assignment, the student  $i$  is assigned to bus  $b_i$ , we denote that assignment by the sequence  $(b_1, b_2, \dots, b_n)$ . Then two possible assignments for each students are:

- $(1, 1, 2, 2)$
- $(2, 2, 1, 1)$

The following are examples of invalid assignment:

- $(1, 1, 1, 1)$  because student 2 and 3 are in the same bus.
- $(1, 1, 2, 1)$  because student 4 is in bus 1 but student 3 is not in bus 1, violating the opinion 3.

### Example 2

```
3 2 4
1 1 2
2 1 3 1
2 1 3 2
2 3 2 2
```

The correct output is:

0

There is no suitable assignment that satisfies all the opinions.

### Example 3

```
4 3 5
1 1 3
2 1 2 1
2 1 4 3
1 4 3
2 2 3 2
```

The correct output is:

7