ACM-ICPC

D-Tesla 模板

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1 数论

1.1 线性筛打质数表,质因数分解

```
#define MAXIMUM 26
int prime[1000000];
bool isprime[1000000];
void get_prime(int listsize)
    int primesize=1;
    memset(isprime,1,sizeof(isprime));
    isprime[1] = false;
    for(int i=2;i<=listsize;i++)</pre>
        if(isprime[i]) prime[primesize++]=i;
        for(int j=1;i*prime[j]<=listsize&&j<=primesize;j++)</pre>
        {
            isprime[i*prime[j]] = false;
            if(i%prime[j]==0) break;
        }
    }
}
struct p
    int value;
    int time;
}p[MAXIMUM];
void prime_factorization(long long n)
{
    memset(p,0,sizeof(p));
    long long psize=0;
    long long a = n;
    for(int t = 1;1LL*prime[t]*prime[t]<=n;t++)</pre>
        if(a%prime[t]==0) p[++psize].value = prime[t];
        while(a%prime[t]==0)
```

```
{
           p[psize].time += 1;
           a = a / prime[t];
        if(a<=90000)
       if(isprime[a])
           p[++psize].value = a;
           p[psize].time += 1;
           a = 1;
           break;
        }
        if(a==1) break;
   }
   if(a!=1)
   {
        p[++psize].value = a;
        p[psize].time = 1;
   }
}
```

1.2 莫比乌斯函数,欧拉函数

```
const int MAX = 101000;

int mu[MAX+10];
bool isprime[MAX+10];
int prime[MAX+10];

void get_mobius(int n)
{
    mu[1] = 1;
    int tot = 0;
    memset(isprime,1,sizeof(isprime));
    for(int i=2;i<=n;i++)
    {
        if(isprime[i])
        {
            prime[++tot] = i;
            mu[i] = -1;
        }
}</pre>
```

```
for(int j=1;prime[j]*i<=n;j++)</pre>
            isprime[prime[j]*i] = 0;
            if(i%prime[j]==0)
                mu[prime[j]*i] = 0;
                break;
            mu[prime[j]*i]=-mu[i];
        }
    }
}
int euler[MAX+10];
void get_euler(int n)
    euler[1] = 1;
    int tot = 0;
    memset(isprime,1,sizeof(isprime));
    for(int i=2;i<=n;i++)</pre>
        if(isprime[i])
            prime[++tot] = i;
            euler[i] = i-1;
        for(int j=1;prime[j]*i<=n;j++)</pre>
        {
            isprime[prime[j]*i] = 0;
            if(i%prime[j]==0)
            {
                euler[prime[j]*i] = prime[j]*euler[i];
                break;
            euler[prime[j]*i] = euler[i]*(prime[j]-1);
        }
    }
}
```

1.3 Miller-Rabin 素性测试

```
typedef long long LL;
LL iprime[6] = \{2, 3, 5, 233, 331\};
LL qmul(LL x, LL y, LL mod) { // 乘法防止溢出, 如果p*p 不爆 LL 的话可以直接
乘; 0(1)乘法或者转化成二进制加法
    return (x * y - (long long)(x / (long double)mod * y + 1e-3) *mod + mod) %
mod;
}
LL qpow(LL a, LL n, LL mod) {
   LL ret = 1;
   while(n) {
       if(n & 1) ret = qmul(ret, a, mod);
       a = qmul(a, a, mod);
       n >>= 1;
   }
   return ret;
}
bool Miller_Rabin(LL p) {
   if(p < 2) return 0;</pre>
   if(p != 2 && p % 2 == 0) return 0;
   LL s = p - 1;
   while(! (s & 1)) s >>= 1;
   for(int i = 0; i < 5; ++i) {</pre>
       if(p == iprime[i]) return 1;
       LL t = s, m = qpow(iprime[i], s, p);
       while(t != p - 1 && m != 1 && m != p - 1) {
           m = qmul(m, m, p);
           t <<= 1;
       if(m != p - 1 && !(t & 1)) return 0;
   }
   return 1;
}
```

1.4 快速幂,矩阵快速幂

```
11 poww(11 a,11 b,11 mod)
{
    11 \text{ ans} = 1, \text{base} = a;
    while(b)
    {
        if(b&1)
        {
            ans *= base;
            ans %= mod;
        }
        base *= base;
        base %= base;
        b>>=1;
    }
    return ans;
}
namespace matrix
{
    const int N = 100;
    struct matrix
        11 v[N][N];
    };
    matrix multi(matrix a, matrix b)
    {
        matrix ans;
        memset(ans.v,0,sizeof(ans.v));
        for(int i=0;i<N;i++)</pre>
            for(int j=0;j<N;j++)</pre>
                 for(int k=0;k<N;k++)</pre>
                     ans.v[i][j] += a.v[i][k]*b.v[k][j];
        return ans;
    }
    matrix mat_pow(matrix a,ll b)
    {
        matrix ans;
        memset(ans.v,0,sizeof(ans.v));
        for(int i=0;i<N;i++) ans.v[i][i] = 1;</pre>
        while(b)
```

```
{
    if(b&1) ans = multi(ans,a);
    a = multi(a,a);
    b>>=1;
}
return ans;
}
```

1.5 卢卡斯、大组合数取模

```
LL PowMod(LL a, LL b, LL MOD){
   LL ret=1;
    while(b){
        if(b&1) ret=(ret*a)%MOD;
        a=(a*a)%MOD;
        b>>=1;
    }
    return ret;
}
LL fac[100005];
LL Get_Fact(LL p){
   fac[0]=1;
    for(LL i=1;i<=p;i++)</pre>
        fac[i]=(fac[i-1]*i)%p; //预处理阶乘
LL Lucas(LL n, LL m, LL p){
    LL ret=1;
    while(n&&m){
        LL a=n\%p,b=m\%p;
        if(a<b) return 0;</pre>
        ret=(ret*fac[a]*PowMod(fac[b]*fac[a-b]%p,p-2,p))%p;
        n/=p;
       m/=p;
    return ret;
}
int main(){
    int t;
    scanf("%d",&t);
```

```
while(t--){
    LL n,m,p;
    scanf("%I64d%I64d%I64d",&n,&m,&p);
    Get_Fact(p);

    printf("%I64d\n",Lucas(n,m,p));
}
    return 0;
}

/ 卡斯定理
O(Logp(n)*p)
```

1.6 中国剩余定理(不互质情况)

```
using namespace std;
const int maxn=100005;
const int inf=0x7fffffff;
typedef long long 11;
void ex_gcd(ll a,ll b,ll &d,ll &x,ll &y)//扩展欧几里得
{
   if(!b) {d=a;x=1;y=0;}
   else{
        ex_gcd(b,a%b,d,y,x);
       y-=x*(a/b);
}
11 ex_crt(ll *m,ll *r,int n)
   11 M=m[1],R=r[1],x,y,d;
   for(int i=2;i<=n;i++){</pre>
       ex_gcd(M,m[i],d,x,y);
        if((r[i]-R)%d) return -1;
       x=(r[i]-R)/d*x%(m[i]/d);
        R+=x*M;
       M=M/d*m[i];
        R\%=M;
   return R>0?R:R+M;
int main()
{
   int t,n;
```

```
scanf("%d",&t);
for(int cas=1;cas<=t;cas++){
    scanf("%d",&n);
    ll m[maxn],r[maxn];//m 除数,r 余数
    for(int i=1;i<=n;i++) scanf("%lld",&m[i]);
    for(int i=1;i<=n;i++) scanf("%lld",&r[i]);
    printf("Case %d: %I64d\n",cas,ex_crt(m,r,n));
}
return 0;
}
```

关于原理的推导:

```
\int x = a_1 \pmod{n_1}
                            (0)
 x = a_2 \pmod{n_2}
x = n_1 k_1 + a_1
                            (1)
n_1k_1 + a_1 = n_2k_2 + a_2
n_1k_1 = (a_2 - a_1) + n_2k_2
n_1 k_1 = (a_1 - a_1) \pmod{n_2}
显然,要想有解,必有 \gcd(n1,n2)|(a2-a1)。设 \gcd(n1,n2)=d,c=a_2-a_1,则有:
\frac{n_1}{d}k_1 = \frac{c}{d} \pmod{\frac{n_2}{d}}
k_1 = \frac{c}{d} * (\frac{n_1}{d})^{-1} \pmod{\frac{n_2}{d}}
x = n_1(y \frac{n_2}{d} + K) + a_1
 =\frac{n_1n_2}{d}y+n_1K+a_1
x = n_1 K + a_1 \pmod{\frac{n_1 n_2}{d}}
x = a \pmod{n}
                            (2)
式(2)中:
a = n_1 K + a_1, n = \frac{n_1 n_2}{d}
这样,成功的将(0)式的两个方程合并为式(2)的一个方程。
最终,合并 k 个方程的最小 x 的值为 a%n。
```

```
typedef __int64 int64;
int64 Mod;

int64 gcd(int64 a, int64 b)
{
    if(b==0)
        return a;
    return gcd(b,a%b);
}

int64 Extend_Euclid(int64 a, int64 b, int64&x, int64& y)
```

```
{
   if(b==0)
   {
       x=1, y=0;
       return a;
   int64 d = Extend_Euclid(b,a%b,x,y);
   int64 t = x;
   x = y;
   y = t - a/b*y;
   return d;
}
//a 在模n 乘法下的逆元,没有则返回-1
int64 inv(int64 a, int64 n)
{
   int64 x,y;
   int64 t = Extend_Euclid(a,n,x,y);
   if(t != 1)
       return -1;
   return (x%n+n)%n;
}
//将两个方程合并为一个
bool merge(int64 a1, int64 n1, int64 a2, int64 n2, int64& a3, int64& n3)
{
   int64 d = gcd(n1,n2);
   int64 c = a2-a1;
   if(c%d)
       return false;
   c = (c\%n2+n2)\%n2;
   c /= d;
   n1 /= d;
   n2 /= d;
   c *= inv(n1,n2);
   c %= n2;
   c *= n1*d;
   c += a1;
   n3 = n1*n2*d;
   a3 = (c%n3+n3)%n3;
   return true;
}
//求模线性方程组 x=ai(mod ni),ni 可以不互质
```

```
int64 China_Reminder2(int len, int64* a, int64* n)
{
    int64 a1=a[0],n1=n[0];
    int64 a2,n2;
    for(int i = 1; i < len; i++)</pre>
        int64 aa,nn;
        a2 = a[i],n2=n[i];
        if(!merge(a1,n1,a2,n2,aa,nn))
           return -1;
        a1 = aa;
        n1 = nn;
   Mod = n1;
    return (a1%n1+n1)%n1;
}
int64 a[1000],b[1000];
int main()
{
    int i;
    int k;
    while(scanf("%d",&k)!=EOF)
    {
        for(i = 0; i < k; i++)</pre>
            scanf("%I64d %I64d",&a[i],&b[i]);
        printf("%I64d\n",China_Reminder2(k,b,a));
    }
    return 0;
}
```

1.7 对前 n 个数分解质因数

```
#include<bits/stdc++.h>
using namespace std;
#define N 2000000
vector <pair<long long,int>> d[2000004];
void init()
{
    d[1].push_back({1,1});
    for(long long i=2;i<=N;i++)</pre>
        if(d[i].empty())
            for(long long j=i;j<=N;j+=i)</pre>
                 d[j].push_back({i,1});
            long long w=i*i;
            while(w<=N)</pre>
            {
                 for(long long j=w;j<=N;j+=w)</pre>
                     d[j][d[j].size()-1].second++;
                w*=i;
            }
        }
    }
}
int main()
{
    init();
    int t;
    while(cin >> t)
    for(int i=0;i<d[t].size();i++)</pre>
        cout << "factor " << d[t][i].first << " is " << d[t][i].second << endl;</pre>
    }
}
```

1.8 将根式转换为连分数形式

```
#include<bits/stdc++.h>
using namespace std;
vector<int> a;
vector<int> b;
vector<int> c;
void get_fractions(int n)
{
    a.clear();
    b.clear();
    c.clear();
    int AA;
    AA = floor(sqrt(n));
    int c0 = n-AA*AA;
    int a0 = (sqrt(n)+AA)/(n-AA*AA);
    int b0 = a0*(n-AA*AA)-AA;
    c.push_back(c0);
    a.push back(a0);
    b.push_back(b0);
    int i=0;
    do
    {
        int ccc = (n - b[i]*b[i])/c[i];
        int aaa = (sqrt(n)+b[i])/ccc;
        int bbb = aaa*ccc-b[i];
        if(a[0]==aaa&&b[0]==bbb&&c[0]==ccc)
            break;
        c.push_back(ccc);
        a.push_back(aaa);
        b.push_back(bbb);
        i++;
    }while(1);
    printf("[%d;(",AA);
    vector<int>::iterator it;
    for(it=a.begin();it!=a.end();it++)
        cout<<*it<<(it==a.end()-1?")]":",");
    //for(auto& x : a) cout << x;</pre>
    cout << endl;</pre>
}
int main()
```

```
{
   int n;
   while(cin >> n)
      get_fractions(n);
   return 0;
}
```

1.9 Meissel-Lehmer 算法(求 1e11 内质数个数)

```
//Meisell-Lehmer
//G++ 218ms 43252k
#include<cstdio>
#include<cmath>
using namespace std;
#define LL long long
const int N = 5e6 + 2;
bool np[N];
int prime[N], pi[N];
int getprime()
{
   int cnt = 0;
   np[0] = np[1] = true;
   pi[0] = pi[1] = 0;
   for(int i = 2; i < N; ++i)</pre>
        if(!np[i]) prime[++cnt] = i;
        pi[i] = cnt;
        for(int j = 1; j <= cnt && i * prime[j] < N; ++j)</pre>
        {
           np[i * prime[j]] = true;
           if(i % prime[j] == 0) break;
        }
   }
   return cnt;
const int M = 7;
const int PM = 2 * 3 * 5 * 7 * 11 * 13 * 17;
int phi[PM + 1][M + 1], sz[M + 1];
```

```
void init()
{
    getprime();
    sz[0] = 1;
    for(int i = 0; i <= PM; ++i) phi[i][0] = i;</pre>
    for(int i = 1; i <= M; ++i)</pre>
        sz[i] = prime[i] * sz[i - 1];
        for(int j = 1; j <= PM; ++j) phi[j][i] = phi[j][i - 1] - phi[j /</pre>
prime[i]][i - 1];
    }
}
int sqrt2(LL x)
{
    LL r = (LL) sqrt(x - 0.1);
    while(r * r <= x) ++r;</pre>
    return int(r - 1);
}
int sqrt3(LL x)
    LL r = (LL)cbrt(x - 0.1);
    while(r * r * r <= x)</pre>
    return int(r - 1);
}
LL getphi(LL x, int s)
{
    if(s == 0) return x;
    if(s <= M) return phi[x % sz[s]][s] + (x / sz[s]) * phi[sz[s]][s];</pre>
    if(x <= prime[s]*prime[s]) return pi[x] - s + 1;</pre>
    if(x <= prime[s]*prime[s] && x < N)</pre>
        int s2x = pi[sqrt2(x)];
        LL ans = pi[x] - (s2x + s - 2) * (s2x - s + 1) / 2;
        for(int i = s + 1; i <= s2x; ++i) ans += pi[x / prime[i]];</pre>
        return ans;
    return getphi(x, s - 1) - getphi(x / prime[s], s - 1);
}
LL getpi(LL x)
{
    if(x < N)
               return pi[x];
    LL ans = getphi(x, pi[sqrt3(x)]) + pi[sqrt3(x)] - 1;
    for(int i = pi[sqrt3(x)] + 1, ed = pi[sqrt2(x)]; i \le ed; ++i) ans -= getpi(x)
/ prime[i]) - i + 1;
```

```
return ans;
}
LL lehmer_pi(LL x)
{
    if(x < N) return pi[x];</pre>
    int a = (int)lehmer_pi(sqrt2(sqrt2(x)));
    int b = (int)lehmer_pi(sqrt2(x));
    int c = (int)lehmer_pi(sqrt3(x));
    LL sum = getphi(x, a) +(LL)(b + a - 2) * (b - a + 1) / 2;
    for (int i = a + 1; i <= b; i++)</pre>
    {
        LL w = x / prime[i];
        sum -= lehmer_pi(w);
        if (i > c) continue;
        LL lim = lehmer_pi(sqrt2(w));
        for (int j = i; j \leftarrow lim; j++) sum -= lehmer_pi(w / prime[j]) - (j)
- 1);
    return sum;
}
int main()
    init();
    LL n;
    while(~scanf("%lld",&n))
        printf("%11d\n",lehmer_pi(n));
    }
    return 0;
}
```

1.10 Min_25 自动机(亚线性处理积性函数前缀和)

```
#include<bits/stdc++.h>
```

```
using namespace std;
#define ll long long
const int maxn = 2000;
const int N = 710000;
const int mod = 1e9+7;
int b[maxn],c[maxn][maxn],Inv[maxn];
11 sqr,n; /// sqr 为 sqrt(n)
11 w[N],id1[N],id2[N];
int tot; ///记录对于要筛的n,sqrt(n)以内质数的个数
int isp[N],p[N];
ll zh[N][3]; ///zh[i][k]记录(p[1])^k + (p[2])^k + ... + (p[i])^k
11 g[N][3];
11 poww(11 a, int b)
{
   11 ans = 1,base = a%mod;
   while(b)
   {
       if(b&1)
       {
           ans*=base;
           ans%=mod;
       }
       base*=base;
       base%=mod;
       b>>=1;
   }
   return ans;
}
ll sigma_f(ll n,int k) ///得到∑i^k, i:1~n
{
   if(k==0) return n;
   n++;
   n%=mod;
   11 \text{ tmp} = n;
   ll ans=0;
   for (int i=1;i<=k+1;i++)</pre>
   {
       ans += 1LL*c[k+1][i]*b[k+1-i]%mod*n%mod;
```

```
ans %= mod;
        n *= tmp%mod;
        n \% = mod;
    ans *= Inv[k+1];
    ans %= mod;
    ans += mod;
    ans %= mod;
    return ans;
}
void get_p(int n,int w)
{
    tot = 0;
    memset(isp,1,sizeof(isp));
    isp[0] = 0;
    isp[1] = 0;
    for(int i=2;i<=n;i++)</pre>
        if(isp[i])
            p[++tot] = i;
            11 \text{ wait} = 1;
            for(int j=0;j<=w;j++)</pre>
                zh[tot][j] = zh[tot-1][j] + wait;
                zh[tot][j] %= mod;
                wait *= i;
            }
        }
        for(int j=1;p[j]*i<=n&&j<=i;j++)</pre>
        {
            isp[i*p[j]] = 0;
            if(i%p[j]==0) break;
        }
    }
}
void get_g(ll n,int t) ///对每个 x=n/i, 求出∑[i 是质数](i^t) (i from 1 to x)。
每个对应的值存储在 g[x][t] 中
{
```

```
int m = 0;
    ll i=1,r;
    while(i<=n)</pre>
        11 len = n/i;
        r = n/len;
        if(len<=sqr) id1[len] = ++m;</pre>
        else id2[r] = ++m;
        for(int ww=0;ww<=t;ww++)</pre>
        {
            g[m][ww] = sigma_f(len,ww)-1;
            g[m][ww] %= mod;
            g[m][ww] += mod;
            g[m][ww] %= mod;
        }
        w[m] = len; ///w[i] 记录了形如 n/k 的第 i 大的取值是多少
        i = r+1;
    }
    for(int i=1;i<=tot;i++)</pre>
        for(int j=1;j<=m;j++)</pre>
            if(1LL*p[i]*p[i]>w[j]) break;
            else
            {
                int op;
                if(w[j]/p[i]<=sqr) op = id1[w[j]/p[i]];</pre>
                else op = id2[n/(w[j]/p[i])];
                for(int ww=0;ww<=t;ww++)</pre>
                {
                    g[j][ww] = g[j][ww] -
poww(p[i],ww)*((g[op][ww]-zh[i-1][ww])%mod);
                    g[j][ww] %= mod;
                    g[j][ww] += mod;
                    g[j][ww] %= mod;
                }
            }
        }
    }
}
inline 11 get_value(int wz,int k)
```

```
{
   11 w = (g[wz][2] + 2*g[wz][1] - g[wz][0]) - (zh[k-1][2] + 2*zh[k-1][1]
- zh[k-1][0]);
   w %= mod;
   w += mod;
   w \% = mod;
   //ll w = (g[wz][1]-g[wz][0])-(zh[k-1][1]-zh[k-1][0]);
   return w; ///自己填写 f(x) 的表达式(在质数时)
   ///比如f(x) = x^2 + 2x - 1,就写(g[wz][2] + 2g[wz][1] - g[wz][0]) -
(zh[k-1][2] + 2*zh[k-1][1] - zh[k-1][0])
}
ll f(ll p,ll k) ///计算f(p^k)处的值
{
   if(k==1) return (p*p+2*p-1)%mod;
   return -3; ///自己填写
}
11 get_s(11 x,int k)
{
   if(x<=1||p[k]>x) return 0;
   int wz;
   if(x \le sqr) wz = id1[x];
   else wz = id2[n/x];
   11 ans = get_value(wz,k);
   //if(k==1) ans += 2;
   for(int i=k;i<=tot&&1LL*p[i]*p[i]<=x;++i)</pre>
   {
       for(ll l=p[i],e=1;l*p[i]<=x;l=l*p[i],++e)</pre>
           ans = ans + (get_s(x/1,i+1)*f(p[i],e)%mod)%mod+f(p[i],e+1);
           ans %= mod;
       }
   }
   ans += mod;
   ans %= mod;
   return ans;
}
void init()
{
```

```
c[0][0]=1;
    for (int i=1;i<maxn;i++)</pre>
        for (int j=1;j<=i;j++) c[i][j]=(c[i-1][j-1]+c[i-1][j]) % mod;</pre>
        c[i][0]=1;
    }
    Inv[1]=1;
    for (int i=2;i<maxn;i++) Inv[i]=1LL*Inv[mod % i] * (mod-mod/i) % mod;</pre>
    b[0]=1;
    for (int i=1;i<maxn;i++)</pre>
        b[i]=0;
        for (int k=0; k<i; k++) b[i]=(b[i]+1 L L*c[i+1][k]*b[k] % mod) % mod;
        b[i]=(1LL*b[i]*(-Inv[i+1]) % mod+mod)%mod;
    }
}
void solve(ll n)
{
    init();
    sqr = sqrt(n);
    get_p(sqr,2);
    get_g(n,2);
    ll ans = get_s(n,1)+1;
    cout << ans << endl;</pre>
}
int main()
    while(cin >> n)
    {solve(n);}
}
```

1.11 求解同余方程(x^2=a(mod p))

```
11 poww(ll a,ll b,ll p)
{
```

```
ll ans = 1, base = a;
    while(b)
    {
        if(b&1)
        {
            ans*=base;
           ans %= p;
        base*= base;
        base %= p;
        b>>=1;
    }
    return ans;
}
11 b[20],m[20];
ll shank(ll a,ll p) ///get x^2=a \pmod{p}
{
    if(!isprime[p]) return -1;
    a%=p;
    a+=p;
    a%=p;
    if(poww(a,(p-1)/2,p)!=1) return -1;
    11 q = p-1;
    11 k = 0;
    while(q%2==0)
    {
        k++;
       q/=2;
    }
    11 f;
    for(int i=2;i<p;i++)</pre>
        if(poww(i,(p-1)/2,p)!=1)
        {
            f = i;
           break;
        }
    }
    11 g = poww(f,q,p);
    b[1] = poww(a,q,p);
    int i = 1;
    while(b[i]!=1)
    {
        m[i] = 1;
```

```
int wa = 2;
        while(poww(b[i],wa,p)!=1)
        {
           m[i]++;
           wa *= 2;
        }
        i++;
        b[i] = b[i-1]%p*poww(g,poww(2,k-m[i-1],p-1),p)%p;
    }
    int r = i-1;
    11 x = poww(a,(q+1)/2,p);
    11 times = 0;
    for(int i=1;i<=r;i++)</pre>
        times += poww(2,k-1-m[i],p-1);
    x *= poww(g,times,p);
    x \%= p;
    return x;
}
```

1.12 类欧几里得算法

求解:
$$f(a,b,c,n,r) = \sum_{i=1}^{n} \left[i \frac{a\sqrt{r} + b}{c} \right]$$

```
11 f_sqr(ll a,ll b,ll c,ll n,ll r)
{
    double w = sqrt(r);
    if(n==0) return 0;
    if(n==1) return (a*w+b)/c;
    ll gg = __gcd(a,__gcd(b,c));
    a/=gg,b/=gg,c/=gg;
    ll res = (ll)(w*a + 1.0*b)/(1.0*c);
    if(res==0)
    {
        ll gcd = __gcd(a*c,__gcd(b*c,a*a*r-b*b));
        ll nn = (w*a + 1.0*b)/(1.0*c)*n;
        return nn*n - f_sqr(a*c/gcd,b*c*(-1)/gcd,(a*a*r-b*b)/gcd,nn,r);
    }
    else return n*(n+1)/2*res + f_sqr(a,b-res*c,c,n,r);
}
```

$$f(a,b,c,n) = \sum_{i=0}^{n} \left\lfloor \frac{ai+b}{c} \right\rfloor$$

求解:

```
11 f(ll a,ll b,ll c,ll n) ///Sigma_{i=0}^{n} floor((a*i+b)/c)
{
    ll m = (a*n+b)/c;
    if(n==0||m==0) return (b/c);
    if(n==1) return ((b/c)+((a+b)/c));
    if(a<c&&b<c) return m*n - f(c,c-b-1,a,m-1);
    else return (a/c)*n*(n+1)/2 + (b/c)*(n+1) + f(a%c,b%c,c,n);
}</pre>
```

$$g(a,b,c,n) = \sum_{i=0}^{n} i \left\lfloor \frac{ai+b}{c} \right\rfloor$$

求解:

```
if(a<c&&b<c) return ((n+1)*n*m - f(c,c-b-1,a,m-1) - h(c,c-b-1,a,m-1))/2;
else return g(a%c,b%c,c,n) + (a/c)*n*(n+1)*(2*n+1)/6 + (b/c)*n*(n+1)/2;
}</pre>
```

$$h(a,b,c,n) = \sum_{i=0}^{n} \left(\left\lfloor \frac{ai+b}{c} \right\rfloor \right)^{2}$$

求解:

2 字符串

2.1 KMP 字符串匹配

```
const int MAX = 200;
int nextt[MAX];
void getNext(string t)
{
   int j, k;
   memset(nextt,0,sizeof(nextt));
   j = 0; k = -1; nextt[0] = -1;
   while(j < t.length())</pre>
       if(k == -1 || t[j] == t[k])
           nextt[++j] = ++k;
       else
           k = nextt[k];
   }
}
/*
返回模式串t 在主串s 中首次出现的位置
返回的位置是从 0 开始的。
*/
int KMP_Index(string t,string s)
{
   int i = 0, j = 0;
   getNext(t);
   while(i < s.length() && j < t.length())</pre>
   {
       if(j == -1 || s[i] == t[j])
           i++; j++;
       }
       else
           j = nextt[j];
   if(j == t.length())
       return i - t.length();
   else
       return -1;
```

```
}
/*
返回模式串t在主串s中出现的次数
int KMP_Count(string t,string s)
{
   int ans = 0;
   int i, j = 0;
   if(s.length() == 1 && t.length() == 1)
   {
       if(s[0] == t[0])
           return 1;
       else
           return 0;
   }
   getNext(t);
   for(i = 0; i < s.length(); i++)</pre>
       while(j > 0 && s[i] != t[j])
           j = nextt[j];
       if(s[i] == t[j])
           j++;
       if(j == t.length())
           ans++;
           j = nextt[j];
       }
   }
   return ans;
}
```

3 数据结构

3.1 并查集

```
#define MAX 10000;
struct UF
 int ranking;
 int parent;
}UF[MAX];
void init(int n)
 for(int i=0;i<=n;i++)</pre>
   UF[i].parent=i;
   UF[i].ranking=0;
 }
}
int get_parent(int x)
   if(UF[x].parent==x) return x;
   return get_parent(UF[x].parent);
}
void Union(int a,int b)
 a=get_parent(a);
 b=get_parent(b);
 if(UF[a].rank>UF[b].rank) UF[b].parent = UF[a].parent;
 else
 {
   UF[a].parent = UF[b].parent;
   if(UF[a].rank==UF[b].rank) UF[a].rank++;
 }
}
```

3.2 链表

```
const int SIZE = 500000+5;
int tot,head,tail;
struct node
   int value;
   int prev,next;
}node[SIZE];
int _init()
{
   tot = 2;
   head = 1, tail = 2;
   node[head].next = tail;
   node[tail].prev = head;
}
int _insert(int p,int val)
{
   int q = ++tot;
   node[q].value = val;
   node[node[p].next].prev = q;
   node[q].next = node[p].next;
   node[p].next = q;
   node[q].prev = p;
}
void _remove(int p)
{
   node[node[p].prev].next = node[p].next;
   node[node[p].next].prev = node[p].prev;
}
void _clear()
   memset(node,0,sizeof(node));
   head = tail = tot = 0;
}
```

3.3 线段树

```
const int maxn = 100007;
struct Tree
   int 1,r,sum;
   int vis;
}t[maxn<<2];</pre>
void push_up(int step)
{
   t[step].sum = t[step*2].sum + t[step*2+1].sum;
}
void push_down(int step)
   if(!t[step].vis) return;
   t[step*2].vis += t[step].vis;
   t[step*2+1].vis += t[step].vis;
   t[step*2].sum += t[step].vis*(t[step*2].r-t[step*2].l+1);
   t[step*2+1].sum += t[step].vis*(t[step*2+1].r-t[step*2+1].l+1);
   t[step].vis = 0;
}
void build(int l,int r,int step)
{
   t[step].l = l,t[step].r = r,t[step].sum = t[step].vis = 0;
   if(l==r) return;
   int mid = (1+r)/2;
    build(1,mid,step*2);
   build(mid+1,r,step*2+1);
}
void update(int l,int r,int val,int step)
   if(l==t[step].1&&r==t[step].r)
   {
        t[step].vis += val;
        t[step].sum += (r-l+1)*val;
        return;
   }
```

```
int mid = (t[step].l+t[step].r)/2;
   push_down(step);
   if(r<=mid) update(l,r,val,step*2);</pre>
   else if(l>mid) update(l,r,val,step*2+1);
   else update(1,mid,val,step*2),update(mid+1,r,val,step*2+1);
   push_up(step);
}
int query(int l,int r,int step)
{
   if(l==t[step].1&&r==t[step].r)
        return t[step].sum;
   int mid = (t[step].l+t[step].r)/2;
   push_down(step);
   if(r<=mid) return query(1,r,step*2);</pre>
   else if(1>mid) return query(1,r,step*2+1);
   else return query(1,mid,step*2)+query(mid+1,r,step*2+1);
}
```

3.4 zkw 线段树

3.5 主席树

3.6 树状数组

```
#include<bits/stdc++.h>
using namespace std;
const int maxn = 100007;
int c[maxn];
int lowbit(int n)
    return n & (-n);
}
int query(int x)
{
    int res = 0;
    while(x>0)
    {
        res += c[x];
        x -= lowbit(x);
    return res;
}
int update(int x,int val)
{
    while(x<maxn)</pre>
    {
        c[x] += val;
        x += lowbit(x);
    }
}
int main()
{
    int n;
    cin >> n;
    for(int i=1;i<=n;i++)</pre>
    {
        int x,y;
        cin >> x >> y;
        update(x,y);
    }
```

```
cout << "give me your question!" << endl;
int l,r;
while(cin >> l >> r)
{
    cout << "In [" << l << "," << r << "] ,all the number's sum is: " << query(r)-query(l-1) << endl;
}
}</pre>
```

3.7 树链剖分

```
const int MAX = 100000+5;
const int mod = 1e9+7;
int head[MAX]; ///head[x]存储以x 为起点的第一条边的编号 如果没有以x 为起点的边,
head[x]=0;
int cnt = 0;
struct edge
  int next; ///e[i].next 存储与i 号边同起点的下一条有向边的编号, 如果i 号边
已经是最后一条边,e[i].next=0;
  int to; ///e[i].to 存储 i 号边所指向的终点(点的编号)
}e[MAX<<1];
void add_edge(int x,int y)
{
  e[++cnt].next = head[x];///建新边,标号为i = cnt+1,让当前以 x 为起点的第
一条边作为他的下一条边(为接下来将他设为以 x 为起点的第一条边做铺垫)
                 ///这条边指向了y 节点
  e[cnt].to = y;
  head[x] = cnt; ///将这条边作为以x 为起点的第一条边
}
```

```
/* *****************************
int f[MAX],d[MAX],sz[MAX],heavy_son[MAX];
int rk[MAX],top[MAX],id[MAX];
void dfs1(int u,int fa,int depth) /// 当前节点 他的爸爸 当前深度
   f[u] = fa;
   d[u] = depth;
   sz[u] = 1;
   for(int i=head[u];i!=0;i=e[i].next)
   {
       int v = e[i].to;
       if(v==fa) continue;///根
       dfs1(v,u,depth+1);
       sz[u] += sz[v];
       if(sz[v]>sz[heavy_son[u]])
          heavy_son[u] = v; ///重儿子的 size 最大
   }
}
int cnt2 = 0;
void dfs2(int u,int t) /// 当前节点 重链的顶端
   top[u] = t;
   id[u] = ++cnt2; ///标记dfs 序
   rk[cnt2] = u; ///构造一个从新 dfs 序的标号 -> 原始节点标号的映射
   if(heavy_son[u]==0) return;///根
   dfs2(heavy_son[u],t);
   for(int i=head[u];i!=0;i=e[i].next)
       int v=e[i].to;
       if(v!=heavy_son[u]&&v!=f[u]) dfs2(v,v);
   }
}
```

```
int dis(int x,int y)
{
   int res = 0;
   int fx = top[x], fy = top[y];
   while(fx!=fy)
       if(d[fx]>=d[fy])
       {
           res += d[x] - d[fx];
           res += d[fx] - d[f[fx]];
           x = f[fx];
           fx = top[x];
       }
       else
           res += d[y] - d[fy];
           res += d[fy] - d[f[fy]];
           y = f[fy], fy = top[y];
       }
   }
   //cout << id[x] << " " << id[y] << endl;
   if(id[x]<=id[y])</pre>
       res += id[y]-id[x];
   else res += id[x] - id[y];
   return res;
}
11 sum(int x,int y)
{
   11 ans = 0;
   int fx=top[x],fy=top[y];
   while(fx!=fy) ///两点不在同一条重链
       if(d[fx]>=d[fy])
       {
           ans+=query(id[fx],id[x],1);
```

```
ans %= mod; ///线段树区间求和,处理这条重链的贡献
                            ///将x设置成原链头的父亲结点,走轻边,继续
          x=f[fx],fx=top[x];
循环
       }
       else
       {
          ans+=query(id[fy],id[y],1);
          ans %= mod;
          y=f[fy],fy=top[y];
       }
   }
   ///循环结束,两点位于同一重链上,但两点不一定为同一点,统计这两点之间的贡献
   if(id[x]<=id[y])
       ans+=query(id[x],id[y],1),ans%=mod;
   else
       ans+=query(id[y],id[x],1),ans%=mod;
   return ans;
}
void updates(int x,int y,ll c) ///x->y 的路径上第一个点+c,第二个点+2*c,...
   int fx=top[x],fy=top[y];
   int dis_xy = dis(x,y);
   11 lazy1 = c;
   11 lazy2 = c;
   while(fx!=fy)
   {
       if(d[fx]>=d[fy])
          ll dd = id[x] - id[fx];
          update(id[fx],id[x],(1LL*lazy1 +
(dd)*c)%mod,(1LL*(-1)*lazy2)%mod,1);
          x=f[fx];
          lazy1 = ((1LL*c*(dd+1) + lazy1)%mod);
          lazy1 %= mod;
       }
       else
       {
          ll dd = dis(x,fy);
          update(id[fy],id[y],(1LL*lazy1+lazy2*dd)%mod,lazy2,1);
          y=f[fy];
```

4 计算几何

4.1 基础模板

```
struct spot ///存储点,也可指代向量
   double x;
   double y;
   double z;
};
spot cross(const spot &a,const spot &b) /// 并算向量 a 和向量 b 的叉乘(有顺序)
{
   spot w;
   w.x = a.y*b.z-b.y*a.z;
   w.y = a.z*b.x-a.x*b.z;
   w.z = a.x*b.y-a.y*b.x;
   return w;
}
double dot(const spot &a,const spot &b) /// 计算向量 a 和向量 b 的点乘积
{
   return a.x*b.x+a.y*b.y+a.z*b.z;
}
double norm(const spot &a) /// 计算向量 a 的模长
{
   return sqrt(a.x*a.x+a.y*a.y+a.z*a.z);
}
```

5 杂项

5.1 罗马-数字转换

```
#include<bits/stdc++.h>
using namespace std;
char str[10]="IVXLCDM";
int num[10]={1,5,10,50,100,500,1000};
int roman_to_num(char s[])
{
    int len=strlen(s);
    int cnt=0,a[20];
    for(int i=0;i<len;i++)</pre>
    {
        int f=0,t;
        if(s[i]==s[i+1]&&i!=len-1)
            if(s[i]==s[i+2]&&i!=len-2)
            {
                f=2;
            else
                f=1;
        for(int k=0; k<7; k++)
            if(s[i]==str[k])
        {
            t=k;
            break;
        a[cnt++]=num[t]*(f+1);
        i+=f;
    }
    int sum=0;
    for(int i=0;i<cnt;i++)</pre>
        sum+=a[i];
```

```
for(int i=0;i<cnt-1;i++)</pre>
        if(a[i]<a[i+1])sum-=2*a[i];</pre>
    }
   return sum;
}
string num_to_roman(int num)
{
   char* digit[10] = {"","I","II","III","IV","V","VI","VII","VIII","IX"};
        char* ten[10] =
{"","X","XX","XXX","XL","L","LX","LXX","LXXX","XC"};
        char* hundreds[10] = {"", "C", "CC", "CCC", "CD", "D", "DCC",
"DCCC", "CM"};
        char* thousand[7] = {"","M","MM","MMMM","MMMMM","MMMMMM"};
        string ans;
        ans = string(thousand[num/1000]) + string(hundreds[num%1000/100])
+ string(ten[num%100/10]) + string(digit[num%10]);
        return ans;
}
int main()
{
   char a[101];
   scanf("%s",a);
   cout << roman_to_num(a) << endl;</pre>
   cout << num_to_roman(roman_to_num(a)) << endl;</pre>
}
```

5.2 Bm 算法求解线性递推

```
#include <bits/stdc++.h>
using namespace std;
#define rep(i,a,n) for (long long i=a;i<n;i++)</pre>
#define per(i,a,n) for (long long i=n-1;i>=a;i--)
#define pb push back
#define mp make_pair
#define all(x) (x).begin(),(x).end()
#define fi first
#define se second
#define SZ(x) ((long long)(x).size())
typedef vector<long long> VI;
typedef long long 11;
typedef pair<long long,long long> PII;
const ll mod=1e9+7;
11 powmod(l1 a,l1 b) {l1 res=1;a%=mod; assert(b>=0);
for(;b;b>>=1){if(b&1)res=res*a%mod;a=a*a%mod;}return res;}
// head
long long ,n;
namespace linear_seq
{
   const long long N=10010;
    11 res[N],base[N],_c[N],_md[N];
   vector<long long> Md;
    void mul(ll *a,ll *b,long long k)
    {
        rep(i,0,k+k) _c[i]=0;
        rep(i,0,k) if (a[i]) rep(j,0,k)
           _{c[i+j]=(_{c[i+j]+a[i]*b[j])mod;}
        for (long long i=k+k-1;i>=k;i--) if (_c[i])
           rep(j,0,SZ(Md))
_{c[i-k+Md[j]]=(_{c[i-k+Md[j]]-_{c[i]}*_{md[Md[j]]})\%mod;}
        rep(i,0,k) a[i]=_c[i];
    }
   long long solve(ll n,VI a,VI b)
   { // a 系数 b 初值 b[n+1]=a[0]*b[n]+...
//
         printf("%d\n",SZ(b));
        11 ans=0,pnt=0;
        long long k=SZ(a);
        assert(SZ(a)==SZ(b));
```

```
rep(i,0,k) _md[k-1-i]=-a[i];_md[k]=1;
        Md.clear();
        rep(i,0,k) if (_md[i]!=0) Md.push_back(i);
        rep(i,0,k) res[i]=base[i]=0;
        res[0]=1;
        while ((111<<pnt)<=n) pnt++;</pre>
        for (long long p=pnt;p>=0;p--)
            mul(res,res,k);
            if ((n>>p)&1)
            {
                for (long long i=k-1;i>=0;i--) res[i+1]=res[i];res[0]=0;
                rep(j,0,SZ(Md))
res[Md[j]]=(res[Md[j]]-res[k]*_md[Md[j]])%mod;
        }
        rep(i,0,k) ans=(ans+res[i]*b[i])%mod;
        if (ans<0) ans+=mod;</pre>
        return ans;
   }
   VI BM(VI s)
       VI C(1,1),B(1,1);
        long long L=0,m=1,b=1;
        rep(n,0,SZ(s))
        {
            11 d=0;
            rep(i,0,L+1) d=(d+(l1)C[i]*s[n-i])%mod;
            if (d==0) ++m;
            else if (2*L<=n)</pre>
                VI T=C;
                11 c=mod-d*powmod(b,mod-2)%mod;
                while (SZ(C) < SZ(B) + m) C.pb(0);
                rep(i,0,SZ(B)) C[i+m]=(C[i+m]+c*B[i])%mod;
                L=n+1-L; B=T; b=d; m=1;
            }
            else
            {
                11 c=mod-d*powmod(b,mod-2)%mod;
                while (SZ(C)<SZ(B)+m) C.pb(0);</pre>
                rep(i,0,SZ(B)) C[i+m]=(C[i+m]+c*B[i])%mod;
                ++m;
            }
```

```
}
       return C;
   }
   long long gao(VI a,ll n)
       VI c=BM(a);
       c.erase(c.begin());
       rep(i,0,SZ(c)) c[i]=(mod-c[i])%mod;
       return solve(n,c,VI(a.begin(),a.begin()+SZ(c)));
   }
};
int main()
{
   int t;
   cin >> t;
   while(t--)
   {
       int n;
       cin >> n;
printf("%I64d\n",linear_seq::gao(VI{2,24,96,416,1536,5504,18944,64000,21
2992,702464},n-1));
   }
}
```

5.3 FFT 求多项式乘法

```
#include <map>
#include <set>
#include <cmath>
#include <ctime>
#include <stack>
#include <queue>
#include <cstdio>
#include <cctype>
#include <bitset>
#include <string>
#include <vector>
#include <cstring>
#include <iostream>
#include <algorithm>
#include <functional>
#define fuck(x) cout<<"["<<x<<"]";</pre>
#define FIN freopen("input.txt", "r", stdin);
#define FOUT freopen("output.txt","w+",stdout);
//#pragma comment(linker, "/STACK:102400000,102400000")
using namespace std;
typedef long long LL;
typedef pair<int, int> PII;
const int MX = 3e5 + 5;
const int INF = 0x3f3f3f3f3f;
const int mod = 1e9 + 7;
const double pi = acos(-1.0);
struct cp {
   double x, y;
    cp() {}
    cp (double x, double y): x(x), y(y) {}
    inline cp operator + (const cp &b) {
        return cp(x + b.x, y + b.y);
    inline cp operator - (const cp &b) {
        return cp(x - b.x, y - b.y);
   }
    inline cp operator * (const cp &b) {
        return cp(x * b.x - y * b.y, x * b.y + y * b.x);
    }
```

```
} a[MX], b[MX];
int r[MX];
void fft(cp a[], int opt, int n) {
   for(int i = 0; i < n; i++) {</pre>
        if(i < r[i]) swap(a[i], a[r[i]]);</pre>
   }
   for(int i = 1; i < n; i <<= 1) {</pre>
        cp wn(cos(pi / i), opt * sin(pi / i));
        for(int p = i << 1, j = 0; j < n; j += p) {
           cp w(1, 0);
           for(int k = 0; k < i; k++, w = wn * w) {
               cp x = a[j + k], y = w * a[j + k + i];
               a[j + k] = x + y; a[j + k + i] = x - y;
           }
        }
   }
/*多项式a,最高次为n,多项式b,最高次为m
从 0 到 n 项的系数
卷积结果等于后来 a[].x
复杂度O(nLogn),最后的最高项为n+m
*/
void solve(cp a[], cp b[], int n, int m) {
   int 1 = 0, nn, nm = n + m;
    for(nn = 1; nn <= nm; nn <<= 1) l++;</pre>
   for(int i = n + 1; i \le nn; i++) a[i] = cp(0, 0);
   for(int i = m + 1; i <= nn; i++) b[i] = cp(0, 0);
   n = nn; m = nm;
   for(int i = 0; i < n; i++) {</pre>
        r[i] = (r[i >> 1] >> 1) | ((i & 1) << (1 - 1));
   }
   fft(a, 1, n); fft(b, 1, n);
   for(int i = 0; i <= n; i++) {</pre>
        a[i] = a[i] * b[i];
   }
   fft(a, -1, n);
   for(int i = 0; i <= m; i++) {</pre>
        a[i].x /= n;
    }
}
int main() {
```

```
int n, m; //FIN;
scanf("%d%d", &n, &m);
for(int i = 0; i <= n; i++) scanf("%lf", &a[i].x);
for(int i = 0; i <= m; i++) scanf("%lf", &b[i].x);
solve(a, b, n, m);
for(int i = 0; i <= n + m; i++) {
    printf("%d%c", (int)(a[i].x + 0.5), i == n + m ? '\n' : ' ');
}</pre>
```

5.4 拉格朗日插值

```
#include<iostream>
#include<string>
#include<vector>
using namespace std;
double Lagrange(int N,vector<double>&X,vector<double>&Y,double x);
int main(){
 char a='n';
   cout<<"请输入差值次数 n 的值: "<<endl;
   int N;
   cin>>N;
   vector<double>X(N,0);
   vector<double>Y(N,0);
   cout<<"请输入插值点对应的值及函数值(Xi,Yi): "<<endl;
   for(int a=0;a<N;a++){</pre>
       cin>>X[a]>>Y[a];
   }
   cout<<"请输入要求值 x 的值: "<<endl;
   double x;
   cin>>x;
   double result=Lagrange(N,X,Y,x);
   cout<<"由拉格朗日插值法得出结果: "<<result<<endl;
   cout<<"是否要继续? (y/n): ";
   cin>>a;
  }while(a=='y');
 return 0;
```

```
double Lagrange(int N,vector<double>&X,vector<double>&Y,double x){
  double result=0;
  for(int i=0;i<N;i++){
    double temp=Y[i];
    for(int j=0;j<N;j++){
        if(i!=j){
            temp = temp*(x-X[j]);
            temp = temp/(X[i]-X[j]);
        }
    }
    result += temp;
}
return result;
};</pre>
```

5.5 高速大数 (longlong) 运算

```
#include <bits/stdc++.h>
using namespace std;
#ifndef ONLINE_JUDGE
#define dbg(args...)
                                                  ١
   do
    {
        cout << "\033[32;1m" << #args << " -> "; \
        err(args);
    } while (0)
#else
#define dbg(...)
#endif
void err()
{
    cout << "\033[39;0m" << endl;</pre>
template <template <typename...> class T, typename t, typename... Args>
void err(T<t> a, Args... args)
{
    for (auto x : a) cout << x << ' ';</pre>
    err(args...);
}
```

```
template <typename T, typename... Args>
void err(T a, Args... args)
{
   cout << a << ' ';
   err(args...);
/*****************************
************************
typedef long long 11;
typedef unsigned long long ull;
using i64 = long long;
using u64 = unsigned long long;
using u128 = __uint128_t;
struct Mod64
   Mod64() : n_{0}  {}
   Mod64(u64 n) : n_(init(n)) {}
   static u64 modulus() { return mod; }
   static u64 init(u64 w) { return reduce(u128(w) * r2); }
   static void set_mod(u64 m)
       mod = m;
       assert(mod & 1);
       inv = m;
       for (int i = 0; i < 5; ++i) inv *= 2 - inv * m;</pre>
       r2 = -u128(m) \% m;
   }
   static u64 reduce(u128 x)
       u64 y = u64(x >> 64) - u64((u128(u64(x) * inv) * mod) >> 64);
       return i64(y) < 0 ? y + mod : y;
   }
   Mod64& operator+=(Mod64 rhs)
   {
       n_ += rhs.n_ - mod;
       if (i64(n_) < 0) n_ += mod;</pre>
       return *this;
   Mod64 operator+(Mod64 rhs) const { return Mod64(*this) += rhs; }
   Mod64& operator*=(Mod64 rhs)
   {
```

```
n_ = reduce(u128(n_) * rhs.n_);
       return *this;
   }
   Mod64 operator*(Mod64 rhs) const { return Mod64(*this) *= rhs; }
   u64 get() const { return reduce(n_); }
   static u64 mod, inv, r2;
   u64 n_;
};
u64 Mod64::mod, Mod64::inv, Mod64::r2;
int main()
{
   int T;
   scanf("%d", &T);
   while (T--)
   {
       ull A0, A1, M0, M1, C, M;
        int k;
        scanf("%llu%llu%llu%llu%llu%d", &A0, &A1, &M0, &M1, &C, &M, &k);
       Mod64::set_mod(M);
       Mod64 a0(A0), a1(A1), m0(M0), m1(M1), c(C), ans(1), a2(0);
        for (int i = 0; i <= k; i++)</pre>
        {
           ans = ans * a0;
           a2 = m0 * a1 + m1 * a0 + c;
           a0 = a1;
           a1 = a2;
        printf("%llu\n", ans.get());
   }
}
```