

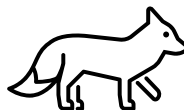
$\times 10$



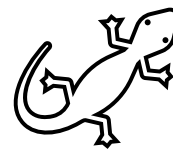
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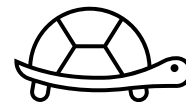
$\times 3$



$\times 2$



$\times 5$



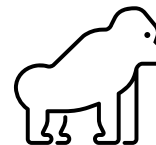
$\times 5$



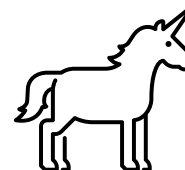
$\times 4$



$\times 3$



$\times 2$

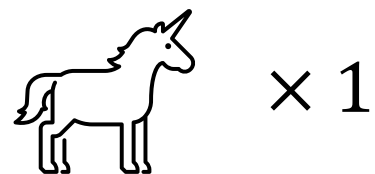
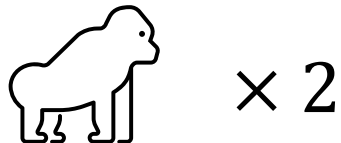
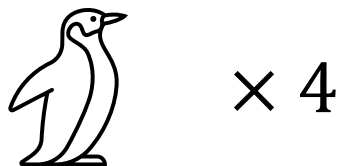
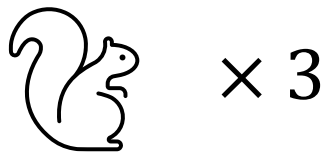
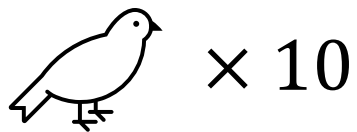


$\times 1$



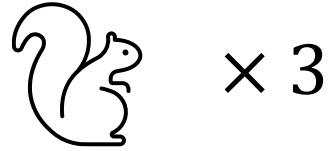
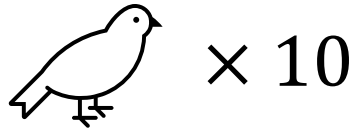


Richness?



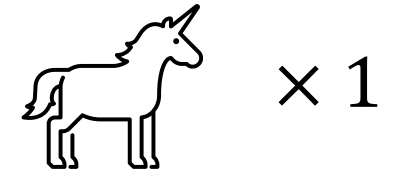
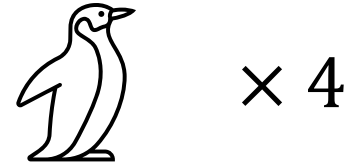
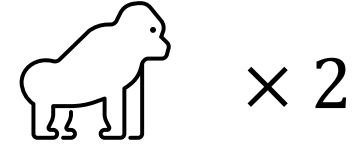


Richness?



4 unique species

species richness = 4



6 unique species

species richness = 6



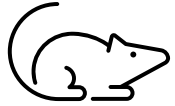
Abundance?



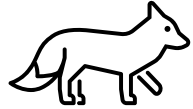
$\times 10$



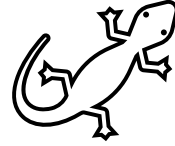
$\times 3$



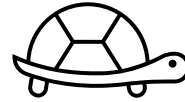
$\times 5$



$\times 2$



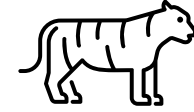
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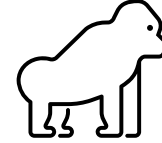
$\times 5$



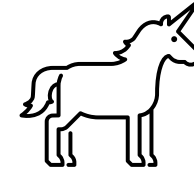
$\times 4$



$\times 3$



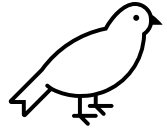
$\times 2$



$\times 1$



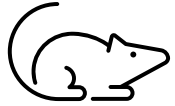
Abundance?



$\times 10$



$\times 3$

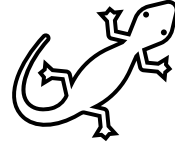


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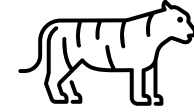


$\times 2$

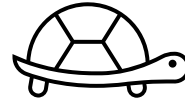
(10, 3, 5, 2)



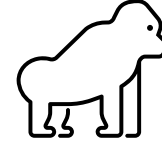
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$\times 3$



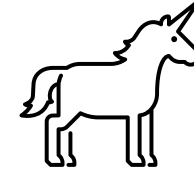
$\times 5$



$\times 2$



$\times 4$

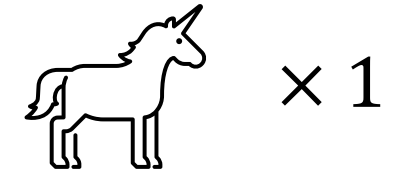
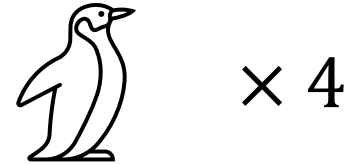
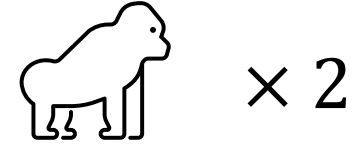
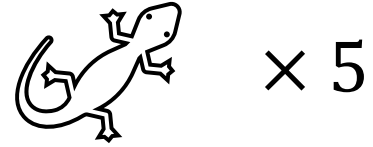
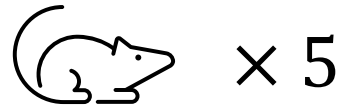
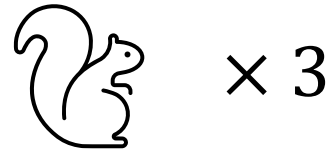
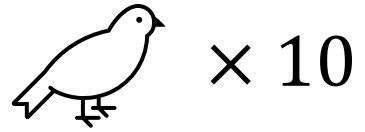


$\times 1$

(5, 3, 5, 2, 4, 1)



Octaves?



Octaves?

- A **species** is in octave n if the abundance a of that species satisfies:

$$2^{n-1} \leq a < 2^n$$

$$\text{i.e., } a \geq 2^{n-1} \text{ AND } a < 2^n$$

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i.e., $a \geq 2^{n-1}$ AND $a < 2^n$

Octave class	$a \geq 2^{n-1}$	$a < 2^n$	Possible abundances a
1			
2			
3			
4			
5			
6			
7			

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1	1		
2			
3			
4			
5			
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7			

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1	1	2	
2			
3			
4			
5			
6			
7			

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1	1	2	1
2			
3			
4			
5			
6			
7			

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1	1	2	1
2	2		
3			
4			
5			
6			
7			

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i.e., $a \geq 2^{n-1}$ AND $a < 2^n$

Octave class	$a \geq 2^{n-1}$	$a < 2^n$	Possible abundances a
1	1	2	1
2	2	4	
3			
4			
5			
6			
7			

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i.e., $a \geq 2^{n-1}$ AND $a < 2^n$

Octave class	$a \geq 2^{n-1}$	$a < 2^n$	Possible abundances a
1	1	2	1
2	2	4	2, 3
3			
4			
5			
6			
7			

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$$2^{n-1} \leq a < 2^n$$

i.e., $a \geq 2^{n-1}$ AND $a < 2^n$

Octave class	$a \geq 2^{n-1}$	$a < 2^n$	Possible abundances a
1	1	2	1
2	2	4	2, 3
3	4	8	4, 5, 6, 7
4			
5			
6			
7			

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$$2^{n-1} \leq a < 2^n$$

i.e., $a \geq 2^{n-1}$ AND $a < 2^n$

Octave class	$a \geq 2^{n-1}$	$a < 2^n$	Possible abundances a
1	1	2	1
2	2	4	2, 3
3	4	8	4, 5, 6, 7
4	8	16	8, 9, 10, 11, 12, 13, 14, 15
5			
6			
7			

Octaves?

- A **species** is in octave n if the abundance a of that species satisfies:

$$2^{n-1} \leq a < 2^n$$

i.e., $a \geq 2^{n-1}$ AND $a < 2^n$

Octave class	$a \geq 2^{n-1}$	$a < 2^n$	Possible abundances a
1	1	2	1
2	2	4	2, 3
3	4	8	4, 5, 6, 7
4	8	16	8, 9, 10, 11, 12, 13, 14, 15
5	16	32	16, 17, ..., 31
6	32	64	32, 33, ..., 63
7	64	128	64, 64, ..., 127

Octaves?

- A **species** is in octave n if the abundance a of that species satisfies:

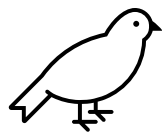
$$2^{n-1} \leq a < 2^n$$

i.e., $a \geq 2^{n-1}$ AND $a < 2^n$

Octave class	$a \geq 2^{n-1}$	$a < 2^n$	Possible abundances a
1	1	2	1
2	2	4	2 – 3
3	4	8	4 – 7
4	8	16	8 – 15
5	16	32	16 – 31
6	32	64	32 – 63
7	64	128	64 – 127



Octaves?

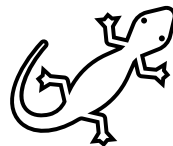


$\times 10$

$$2^3 \leq a < 2^4 \\ \Rightarrow n = 4$$



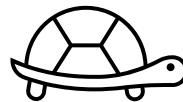
$\times 3$



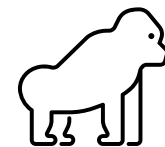
$\times 5$



$\times 3$



$\times 5$



$\times 2$

$$2^1 \leq a < 2^2 \\ \Rightarrow n = 2$$



$\times 5$

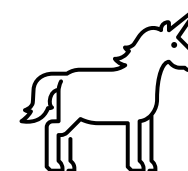
$$2^2 \leq a < 2^3 \\ \Rightarrow n = 3$$



$\times 2$



$\times 4$

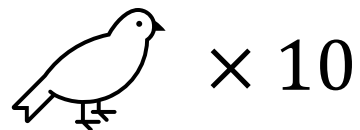


$\times 1$

$$2^0 \leq a < 2^1 \\ \Rightarrow n = 1$$



Octaves?



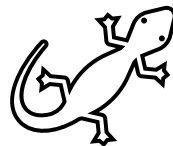
$\times 10$

$$2^3 \leq a < 2^4 \\ \Rightarrow n = 4$$



$\times 3$

$$2^1 \leq a < 2^2 \\ \Rightarrow n = 2$$



$\times 5$

$$2^2 \leq a < 2^3 \\ \Rightarrow n = 3$$



$\times 3$

$$2^1 \leq a < 2^2 \\ \Rightarrow n = 2$$



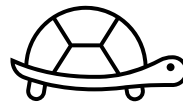
$\times 5$

$$2^2 \leq a < 2^3 \\ \Rightarrow n = 3$$



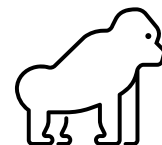
$\times 2$

$$2^1 \leq a < 2^2 \\ \Rightarrow n = 2$$



$\times 5$

$$2^2 \leq a < 2^3 \\ \Rightarrow n = 3$$



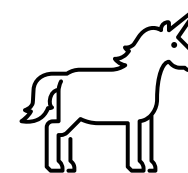
$\times 2$

$$2^1 \leq a < 2^2 \\ \Rightarrow n = 2$$



$\times 4$

$$2^2 \leq a < 2^3 \\ \Rightarrow n = 3$$

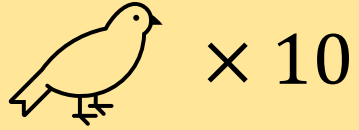


$\times 1$

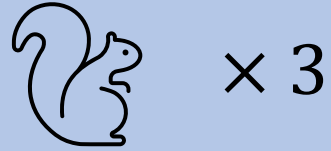
$$2^0 \leq a < 2^1 \\ \Rightarrow n = 1$$



Octaves?



$$2^3 \leq a < 2^4 \\ \Rightarrow n = 4$$



$$2^1 \leq a < 2^2 \\ \Rightarrow n = 2$$



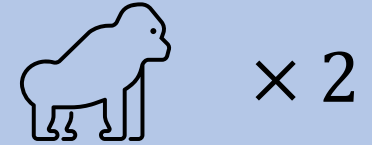
$$2^2 \leq a < 2^3 \\ \Rightarrow n = 3$$



$$2^1 \leq a < 2^2 \\ \Rightarrow n = 2$$



$$2^2 \leq a < 2^3 \\ \Rightarrow n = 3$$



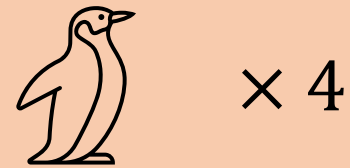
$$2^1 \leq a < 2^2 \\ \Rightarrow n = 2$$



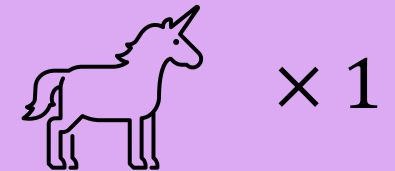
$$2^2 \leq a < 2^3 \\ \Rightarrow n = 3$$



$$2^1 \leq a < 2^2 \\ \Rightarrow n = 2$$



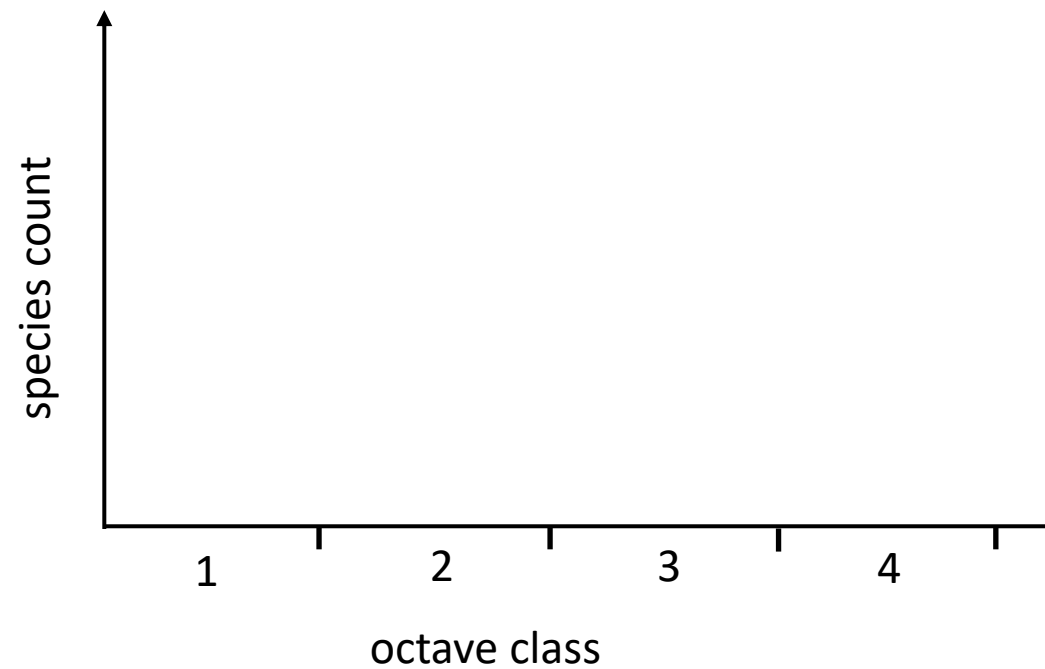
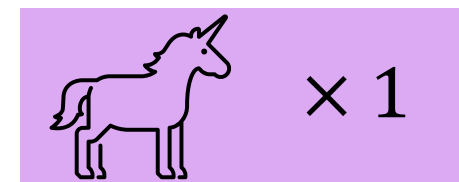
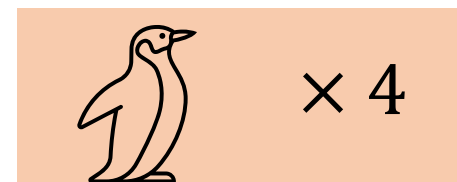
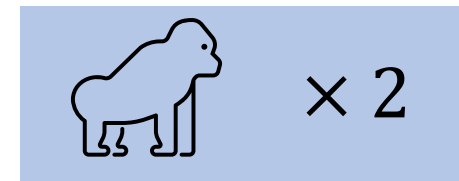
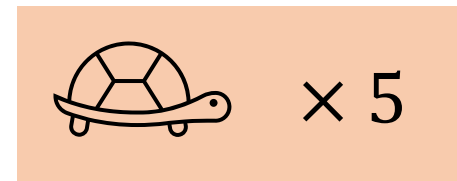
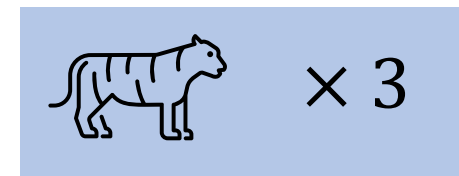
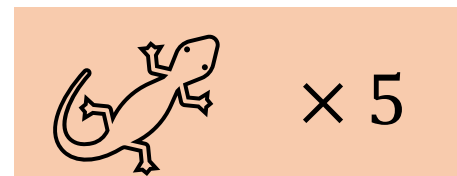
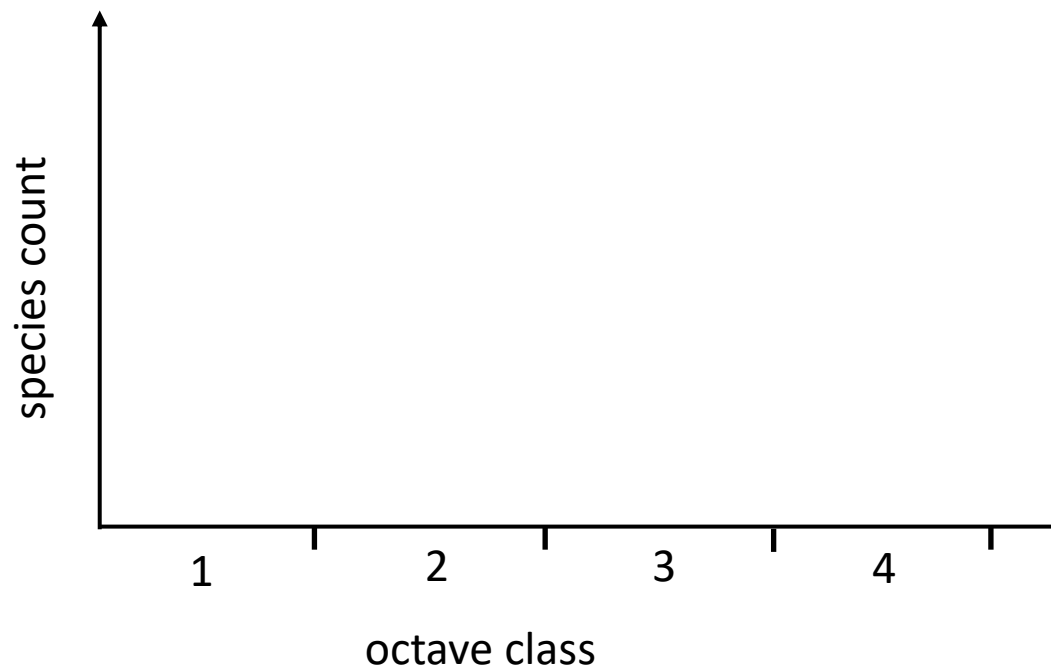
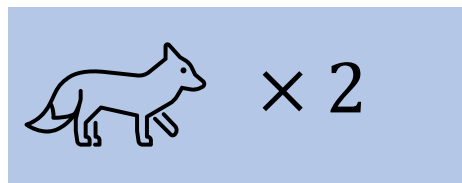
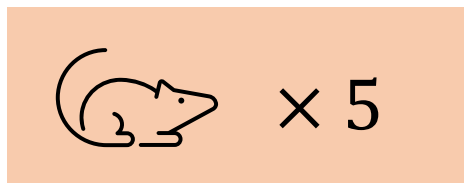
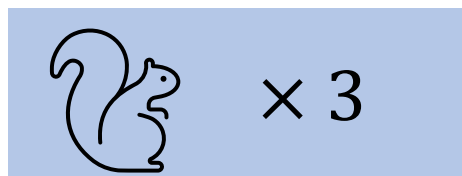
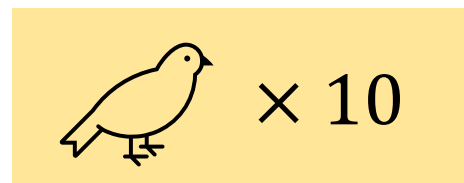
$$2^2 \leq a < 2^3 \\ \Rightarrow n = 3$$



$$2^0 \leq a < 2^1 \\ \Rightarrow n = 1$$

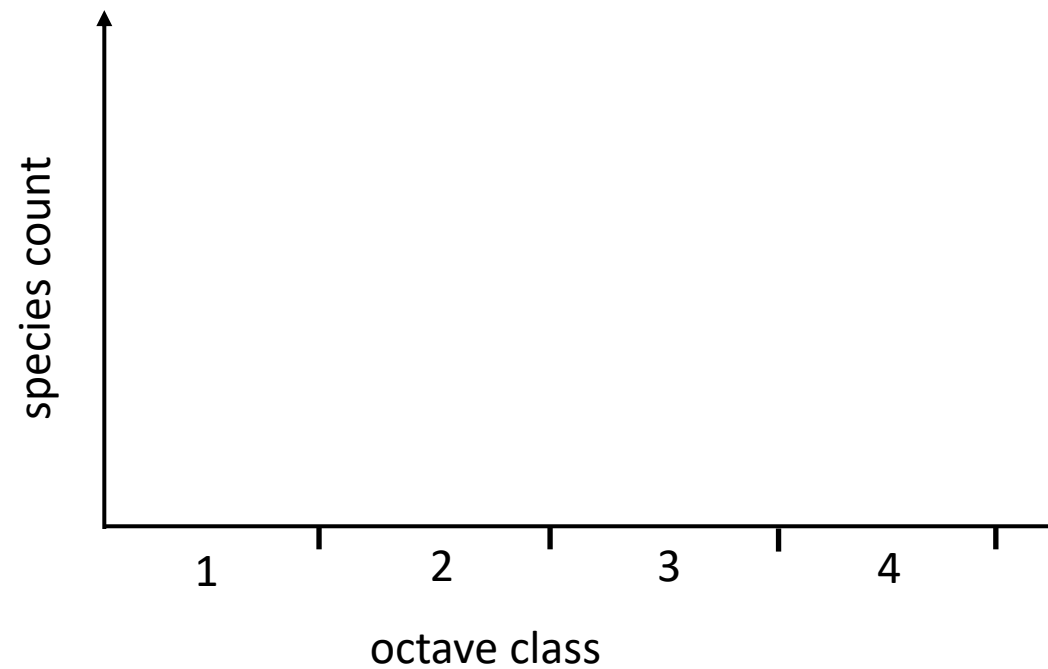
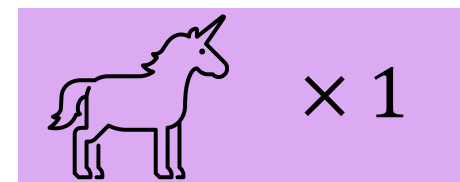
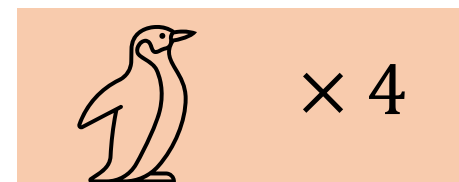
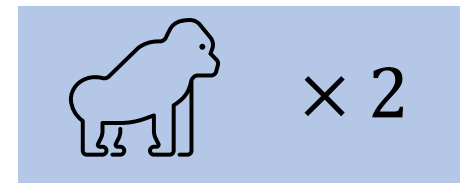
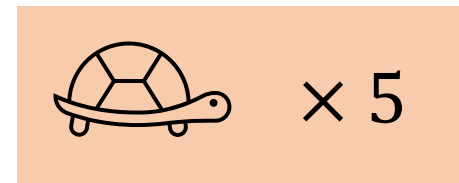
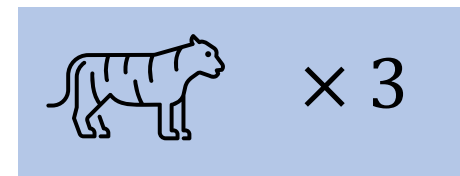
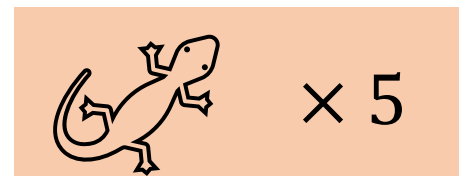
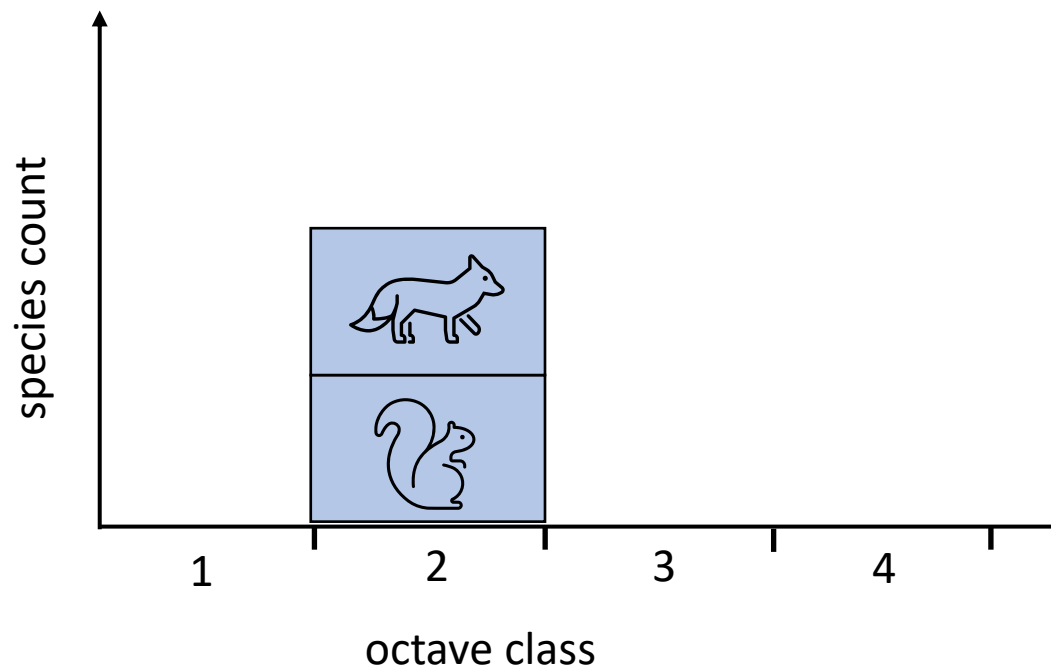
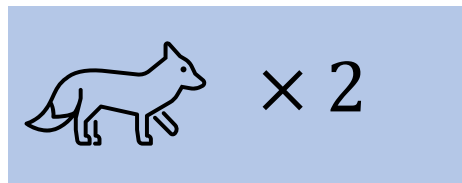
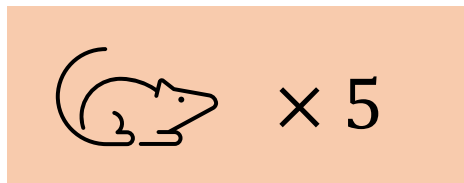
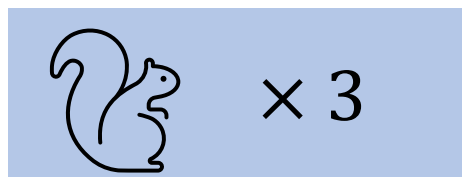
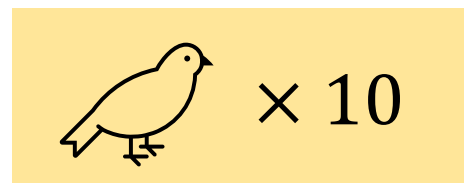


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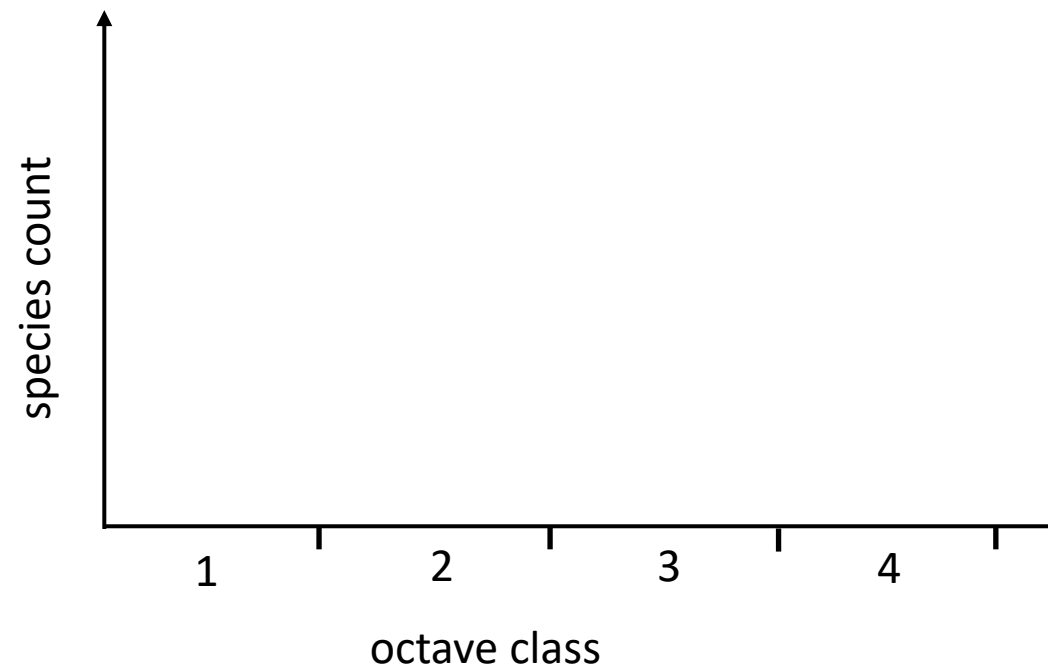
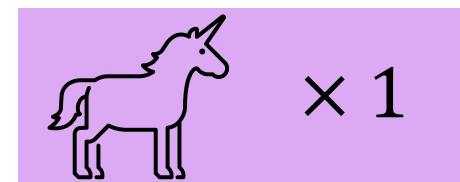
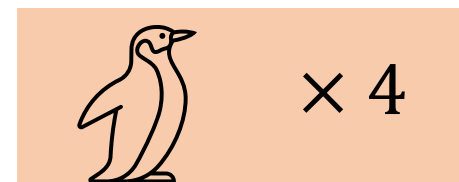
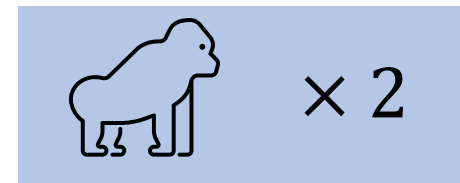
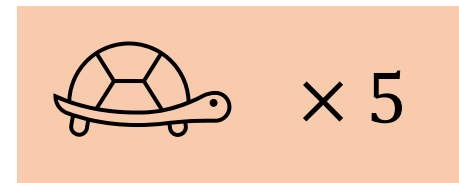
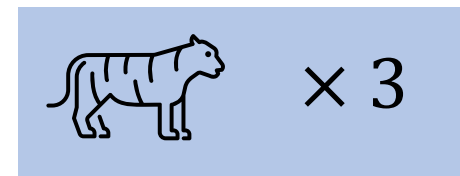
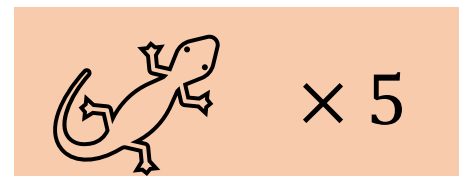
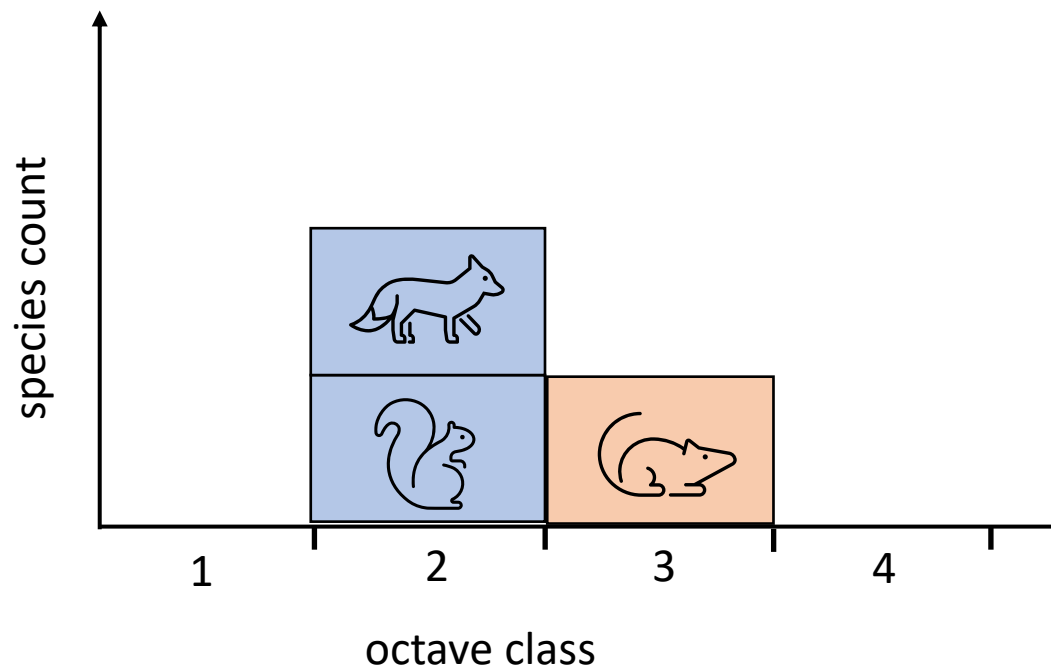
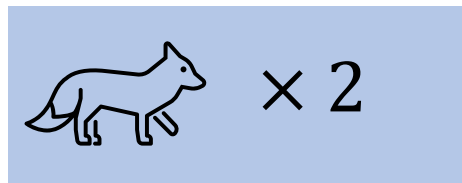
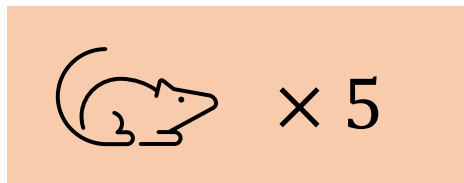
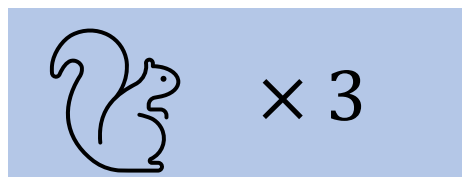
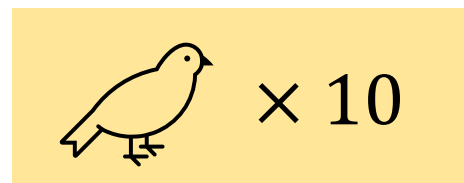


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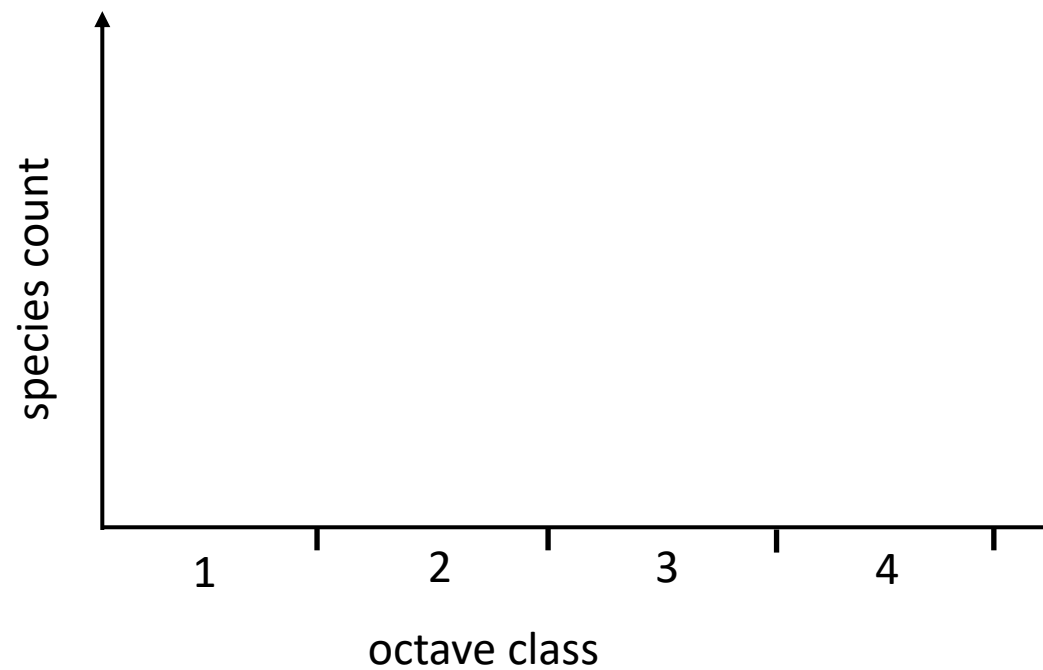
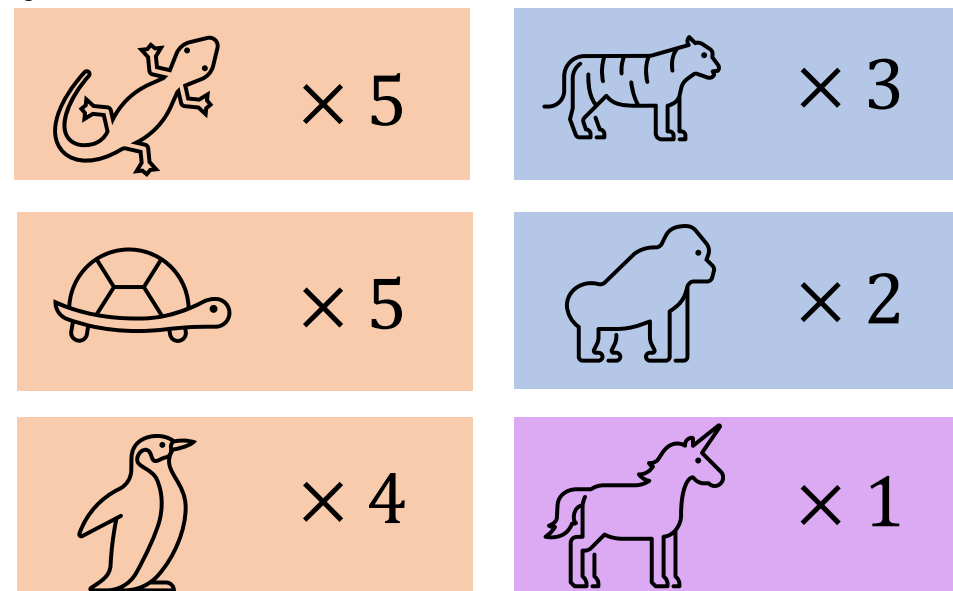
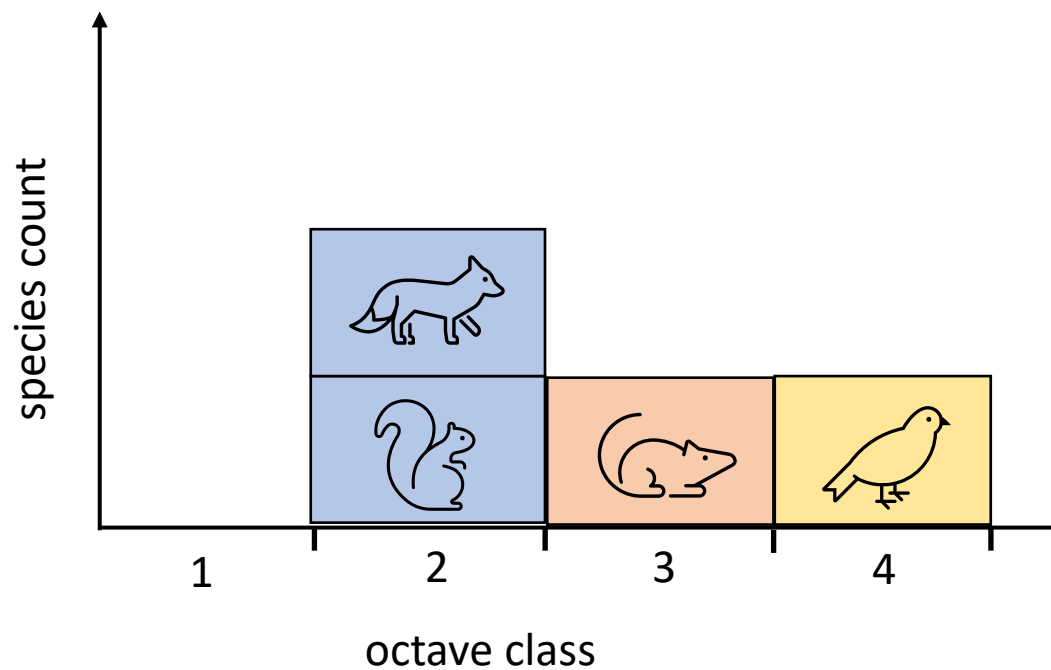
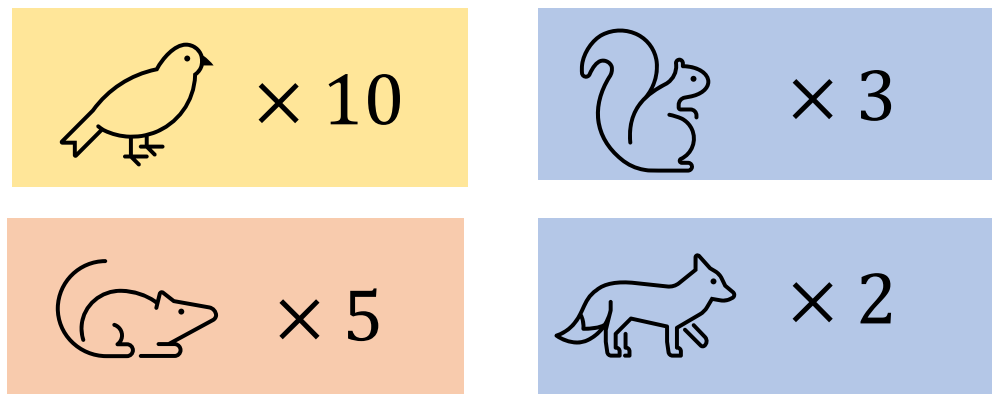


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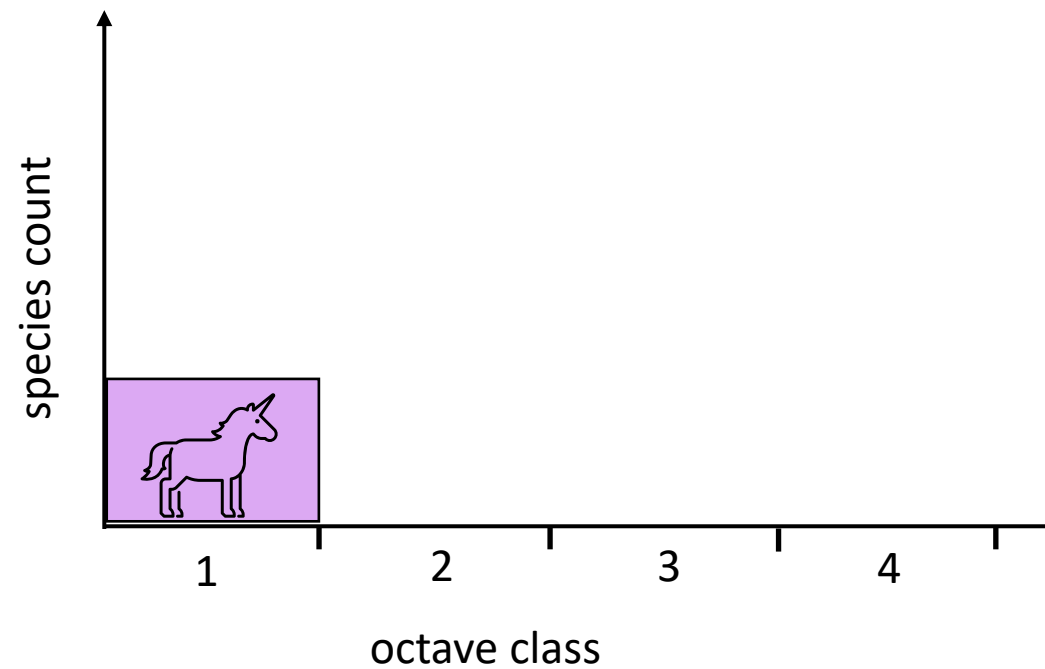
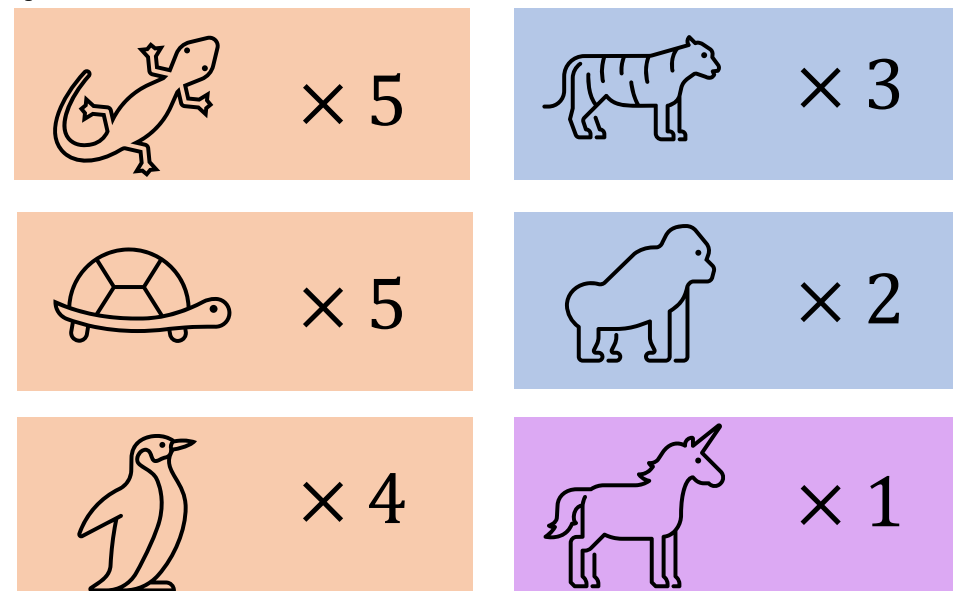
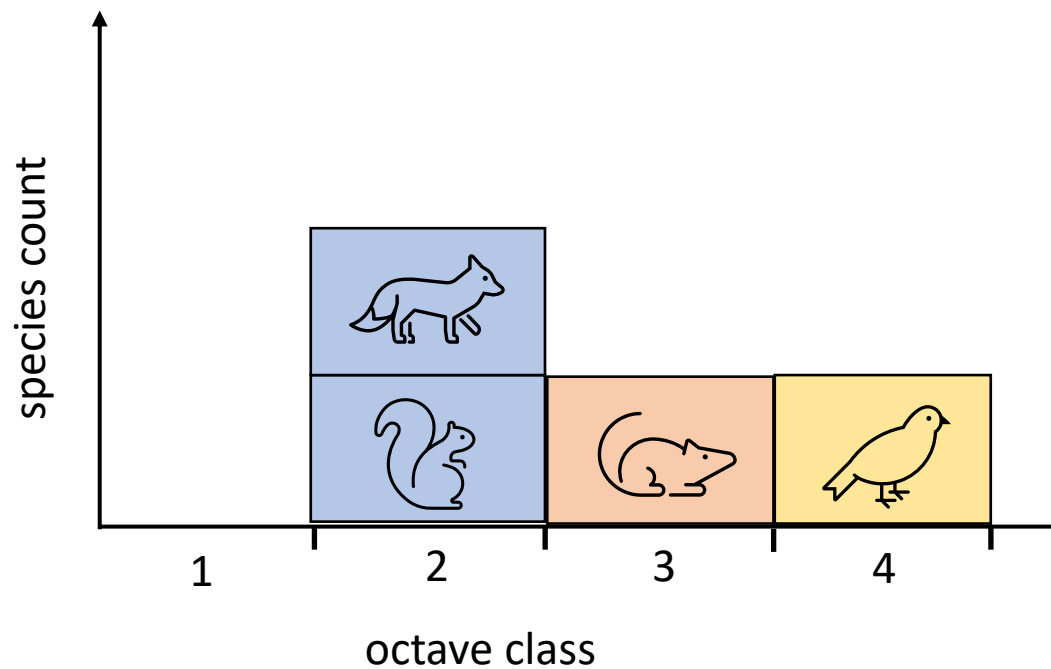
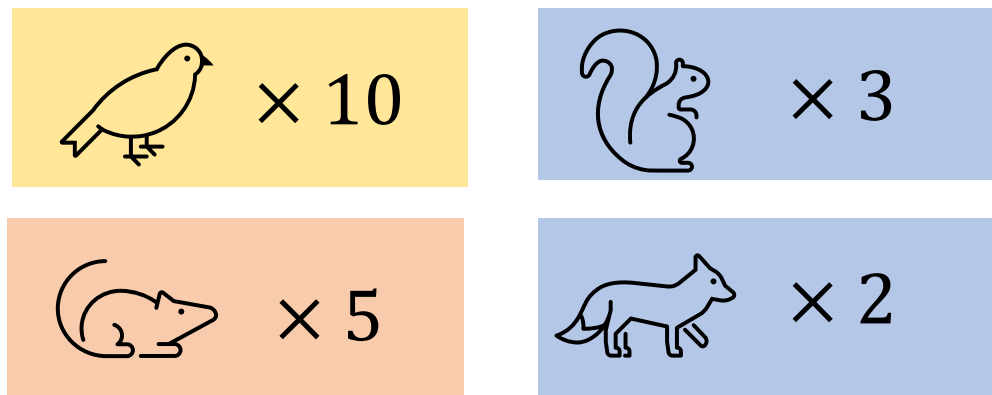


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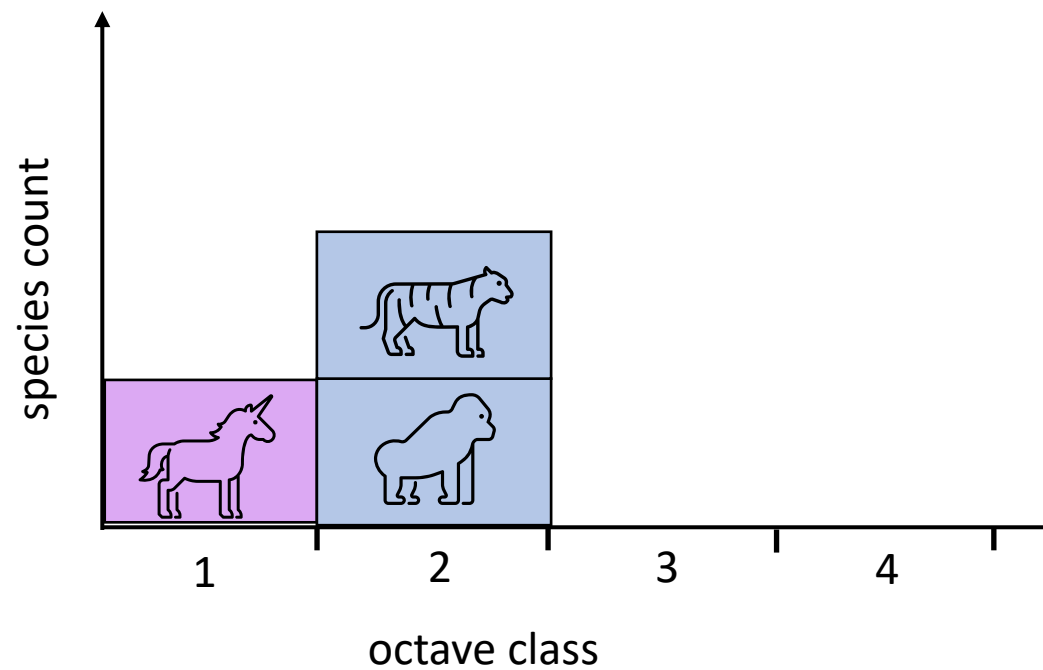
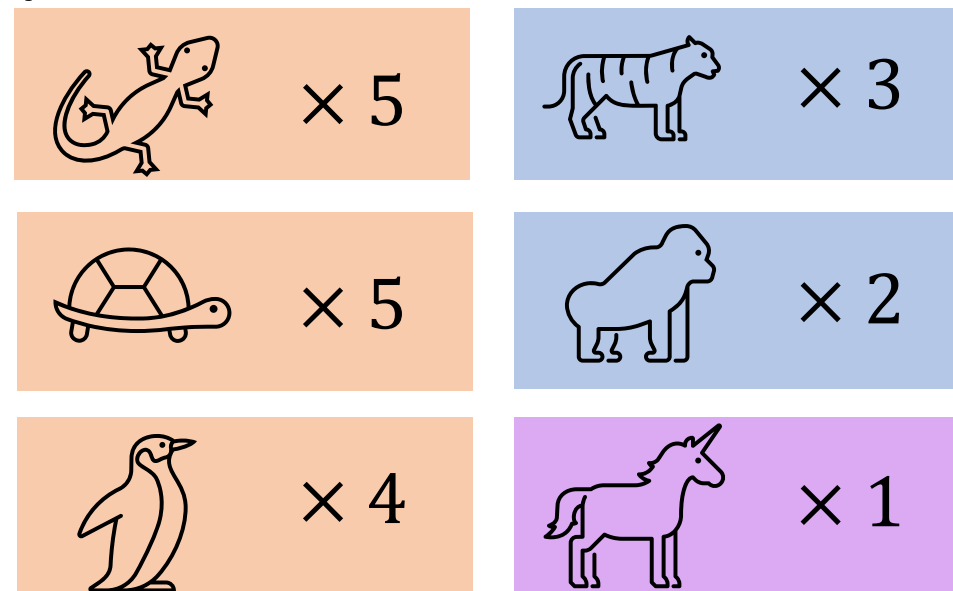
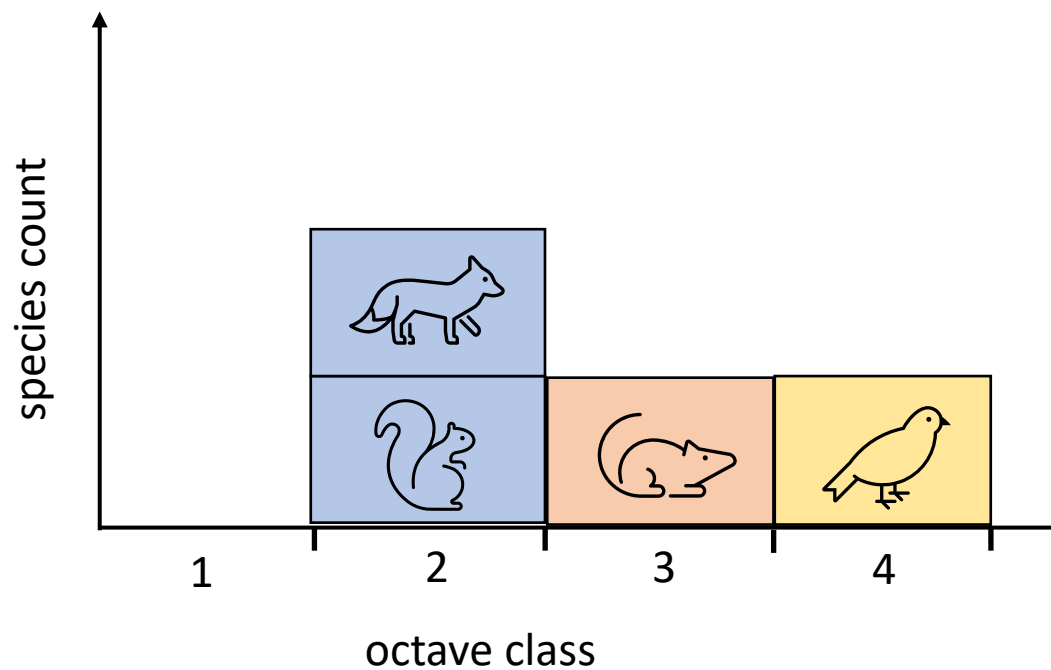
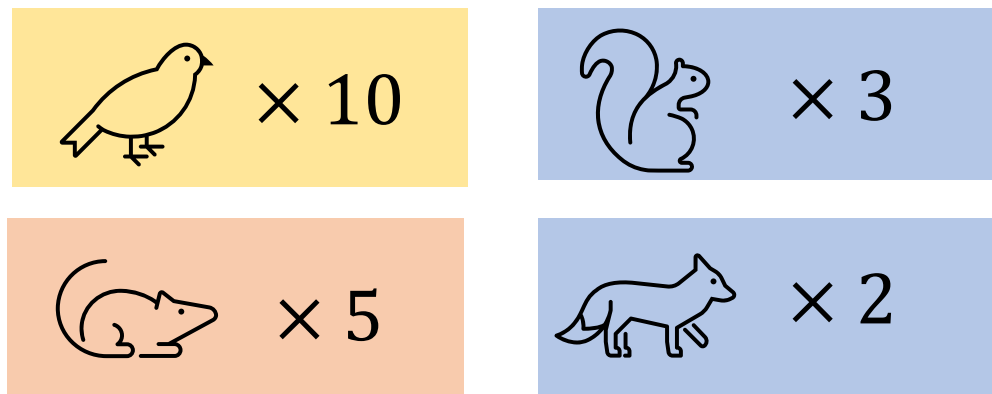


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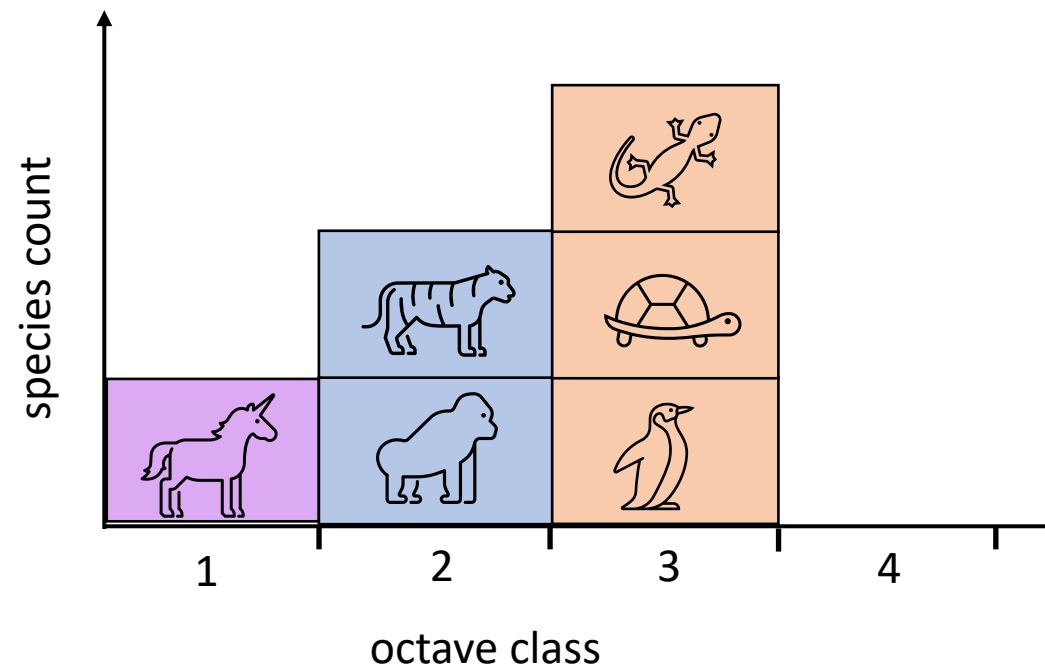
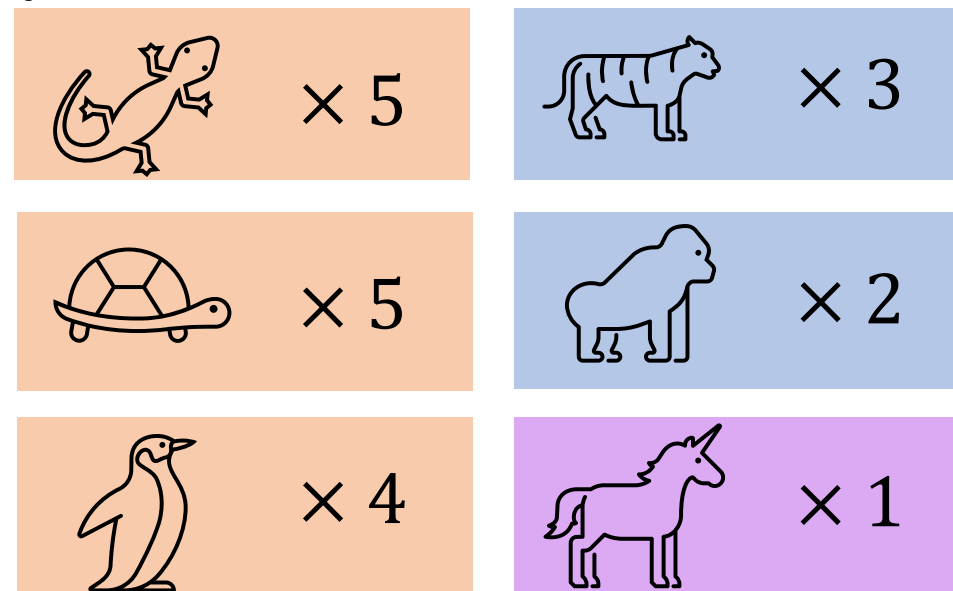
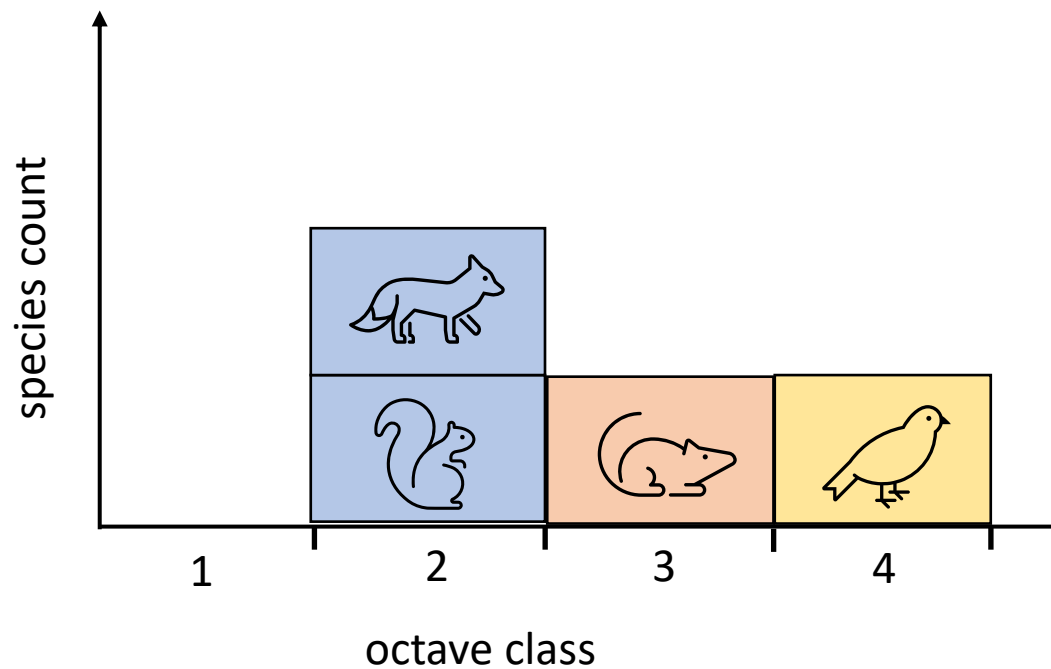
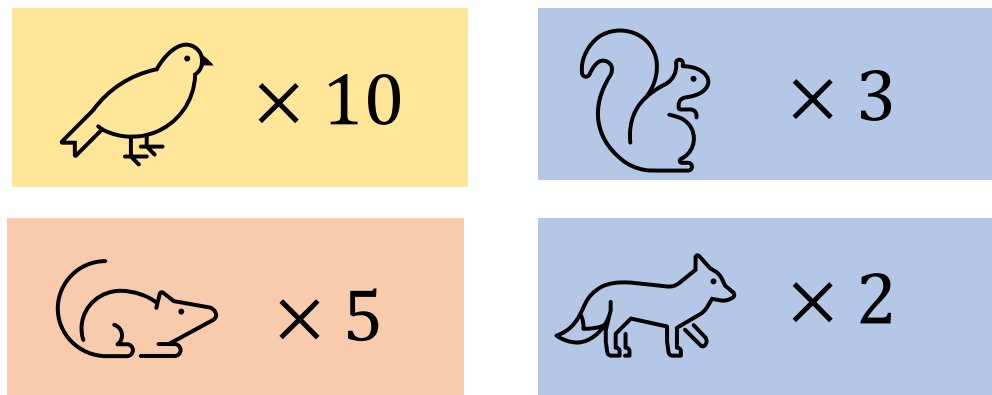


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