MR-LDP: a two-sample Mendelian randomization for GWAS summary statistics accounting linkage disequilibrium and horizontal pleiotropy

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Introduction

This vignette provides an introduction to the `MR.LDP` package. R package `MR.LDP` implements MR-LDP, a two-sample Mendelian randomization for GWAS summary statistics accounting linkage disequilibrium and horizontal pleiotropy. The package can be installed with the following commands:

```
library(devtools);
install_github("QingCheng0218/MR.LDP");
```

Load the package using the following command:

```
library(MR.LDP);
```

Fit MR-LDP using simulated data

We first generate genotype data using function *genRawGeno*:

```
library("mvtnorm");
library("PDSCE");

set.seed(2019);

rho = 0.4;L = 1; M = 50; p = M*L; m = p; Alrate = 1;
n1 = 20000; n2 = 20000; n3 = 2500; lam = 0.055;
maf = runif(p, 0.05, 0.5);
G = genRawGeno(maf, L, M, rho, n1 + n2 + n3);

G1 = G[1:n1,];
G2 = G[(n1+1):(n1+n2),];
G12 = G[1:(n1+n2),];
G3 = G[(n1+n2+1):(n1+n2+n3),];
```

Estimate the covariance matrix using function *pdsoft*:

```
R0 = cor(G3);
R = pdsoft(R0, lam)$theta;
diag(R) = rep(1, p);
mask = kronecker(diag(L),matrix(1,M,M));
R = R*mask;
```

Generate the exposure data(y) and outcome data(z) with prespecified indirect(h_y^2) and direct(h_z^2) heritability based on

$$\mathbf{y} = \mathbf{G}_1\gamma + \mathbf{U}_x\eta_x + \mathbf{e}_1, \quad \mathbf{z} = \beta_0\mathbf{x} + \mathbf{G}_2\alpha + \mathbf{U}_y\eta_y + \mathbf{e}_2,$$

```
h2z <- 0.05; h2y <- 0.1; b0 <- 0.1; q <- 50;
u = matrix(rnorm( (n1+n2) * q),ncol=q);

sigma2g <- 0.005;
gamma.nz = rnorm(m)*sqrt(sigma2g);
indx = sample(1:p,m);
gamma = numeric(p);
gamma[indx] = gamma.nz;

Su = matrix(c(1,0.8,0.8,1),nrow=2)
bu = rmvnorm(q,mean=rep(0,2), sigma = Su,method="chol")
by = bu[,1]; bz = bu[,2];
uby = u%*%by; ubz = u%*%bz;
uby = uby/sqrt(as.numeric(var(uby)/0.6));
ubz = ubz/sqrt(as.numeric(var(ubz)/0.2));

G12g = G12%*%gamma;

if(b0!=0){
  h2ga = (h2y *( 1 + b0^2))/(b0^2 * (1 - h2y));
  gamma0 = gamma/sqrt(as.numeric(var(G12g)/h2ga));
  G12g = G12%*%gamma0;
}

yall = G12g + uby + rnorm(n1+n2)*as.numeric(sqrt(1-var(uby)));

# The direct effects on Z
h2yb = var(b0*yall);
h2al = (h2z + h2z*h2yb)/(1 - h2z)

sigma2a <- 0.005;
if(h2z==0){
  alpha0 = rep(0, m);
  G12a = G12%*%alpha0;
}else{
  alno = floor(p*Alrate);
  alpha.nz <- rnorm(alno)*sqrt(sigma2a);
  # sparse setting for pleiotropy
  indxAL = sample(1:p,alno);
  alpha = numeric(p);
  alpha[indxAL] = alpha.nz;

  G12a = G12%*%alpha;
  alpha0 = alpha/sqrt(as.numeric(var(G12a)/(h2al)));
  G12a = G12%*%alpha0;
}

resz = ubz + rnorm(n1+n2)*as.numeric(sqrt(1-var(ubz)));
zall = b0*yall  + G12a +  resz;
H2a.res <- var(G12a)/var(zall);
H2g.res <- var(b0*G12g)/var(zall);

y = yall[1:n1];
```

```
z = zall[(n1+1):(n1+n2)];
```

We then conduct single-variant analysis to obtain the summary statistics.

```
gammah = numeric(p); Gammah = numeric(p);
segamma = numeric(p); seGamma = numeric(p);
pval = numeric(p);
for (i in 1:p){
  fm = lm(y~1+G1[,i]);
  gammah[i] = summary(fm)$coefficients[2,1];
  segamma[i] = summary(fm)$coefficients[2,2];
  pval[i] = summary(fm)$coefficients[2,4];

  fm = lm(z~1+G2[,i]);
  Gammah[i] = summary(fm)$coefficients[2,1];
  seGamma[i] = summary(fm)$coefficients[2,2];
}
```

Until now, we obtain the summary statistics: `gammah` and `segamma` for esposure data, `Gammah` and `seGamma` for outcome data.

Initilize the parameters for MR-LDP algorithm. `epsStopLogLik` is the convergence tolerance, `maxIter` is the iteration number. `beta0, gamma, alpha, sgga2, sgal2` are the initial values for the PX-VBEM algorithm.

```
epsStopLogLik <- 1e-7; maxIter <- 10000;
beta0 <- 0;
gamma <- rep(0, p);
alpha <- rep(0, p);
sgga2 <- 0.01;
sgal2 <- 0.01;
```

We conduct the simulation study using `MRLDP_SimPXvb`, `model = 1` and `model = 2` represent MR-LD and MR-LDP, respectively.

Fit MR-LD w/ (`constr = 1`) and w/o (`constr = 0`) constraint that $\beta = 0$ as:

```
SimMRLD_Hb = MRLDP_SimPXvb(gammah, Gammah, segamma, seGamma,
                      gamma, alpha,  beta0, sgga2, sgal2, R,
                      constr = 0, epsStopLogLik, maxIter, model = 1);

SimMRLD_H0 = MRLDP_SimPXvb(gammah, Gammah, segamma, seGamma,
                      gamma, alpha,  beta0, sgga2, sgal2, R,
                      constr = 1, epsStopLogLik, maxIter, model = 1);

tstat = 2*(SimMRLD_Hb$tstat - SimMRLD_H0$tstat);
pval = pchisq(tstat, 1, lower.tail = F);
beta_hat = SimMRLD_Hb$beta0;
se_hat = abs(beta_hat/sqrt(tstat));
```

Fit MR-LDP w/ (`constr = 1`) and w/o (`constr = 0`) constraint that $\beta = 0$ as:

```
SimMRLDP_Hb = MRLDP_SimPXvb(gammah, Gammah, segamma, seGamma,
                      gamma, alpha,  beta0, sgga2, sgal2, R,
                      constr = 0, epsStopLogLik, maxIter, model = 2);

SimMRLDP_H0 = MRLDP_SimPXvb(gammah, Gammah, segamma, seGamma,
                      gamma, alpha,  beta0, sgga2, sgal2, R,
                      constr = 1, epsStopLogLik, maxIter, model = 2);
```

```
tstat = 2*(SimMRLDP_Hb$tstat - SimMRLDP_H0$tstat);
pval = pchisq(tstat, 1, lower.tail = F);
beta_hat = SimMRLDP_Hb$beta0;
se_hat = abs(beta_hat/sqrt(tstat));
```

beta_hat, se_hat, pval are estimated causal effect, corresponding standard error and p-value of beta_hat.

Fit MR-LDP using CAD-CAD study.

Furthermore, we give an example to illustrate the implements of MR.LDP for real data analysis. The following datasets('heart attack_myocardial infarction.txt', 'c4d.txt', 'cardiogram.txt', 'all_chr_1000G.bed', 'all_chr_1000G.fam', 'all_chr_1000G.bim', 'fourier_ls-all.bed') should be prepared. Download here https://drive.google.com/drive/folders/1IAs3daG9TIvjnneR32j1pfV0niz8PHyu.

```
filescreen= "heart attack_myocardial infarction.txt";
fileexposure = "c4d.txt";
fileoutcome = "cardiogram.txt";
stringname3 = "all_chr_1000G";
block_file = "fourier_ls-all.bed"
```

'filescreen', 'fileexposure', 'fileoutcome' are the datasets names for screen, exposure and outcome, respectively. These three datasets must have the following format(note that it must be tab delimited):

SNP	chr	BP	A1	A2	beta	se	pvalue
rs3094315	1	752566	A	C	0.00012546	0.00042437	0.76750
rs3131969	1	754182	G	A	0.00033099	0.00045415	0.46611
rs3131972	1	752721	G	A	0.00010445	0.00042414	0.80548
rs1048488	1	760912	T	C	0.00017441	0.00042195	0.67935
rs12562034	1	768448	A	C	-0.00003632	0.00049399	0.94138

'stringname3' is the name of reference panel data. Here we use samples from '1000 Genome Project Phase 1' which is in plink binary format. 'block_file' is used to partition the whole genome into blocks.

matchscreen function is used to match the three datasets with a cutoff named 'pva_cutoff'. 'matchExp = TRUE' means we fix the direction of exposure data. Since MR-LDP is invariant to the orientation of genetic variants, 'matchExp' does not affect the results. Default is FALSE.

```
pva_cutoff = 1e-4;
scrres = matchscreen(filescreen, fileexposure, fileoutcome, stringname3,
                     pva_cutoff, matchExp = FALSE)
bh1 = as.numeric(scrres$bh1);
bh2 = as.numeric(scrres$bh2);
s12 = as.numeric(scrres$s12);
s22 = as.numeric(scrres$s22);
chr = as.numeric(scrres$chr);
bp = scrres$bp;
rsname = scrres$rsname
avbIndex = scrres$idxin;
idx4panel = scrres$idx4panel;
```

`bh1`and `s12` are the SNP effects and corresponding standard errors on the exposure variable, `bh2`and `s22` are the SNP effects and corresponding standard errors on the outcome variable. After matching the three datasets, we obtain 'chr'(chromosome number) , 'bp'(base position),'rsname'(rs number).'avbIndex'(location) and 'idx4panel'(Indicators to be adjusted in reference panel data).

One can using the following function *summaryQC* to remove the MHC region(QCindex = 1), or skip the procedure(QCindex = 0).

```
QCindex = 1;
if(QCindex){
  QCresult = summaryQC(mhcstart, mhcend, bh1, bh2, s12, s22, bp,
                       chr, rsname, avbIndex, idx4panel, Inf, Inf)
  bh1new = QCresult$bh1new;
  bh2new = QCresult$bh2new;
  s12new = QCresult$s12new;
  s22new = QCresult$s22new;
  bpnew = QCresult$bpnew;
  chrnew = QCresult$chrnew;
  avbIndexnew = QCresult$avbIndexnew;
  idx4panelnew = QCresult$idx4panel
  rsnamenew = QCresult$rsnamenew;
}else{
  bh1new = bh1;
  bh2new = bh2;
  s12new = s12;
  s22new = s22;
  bpnew = bp;
  chrnew = chr;
  rsnamenew = rsname;
  idx4panelnew = idx4panel;
  avbIndexnew = avbIndex;
}

p = length(avbIndexnew);
```

Initilize the parameters for MR-LDP algorithm. CoreNum is the number of cores in your CPU.

```
gamma = rep(0.01, p);
alpha = rep(0.01, p);
sgga2 =  0.01;
sgal2 =  0.01;
beta0 = 0;
maxIter = 10000
coreNum = 24;
lam = 0.1;
epsStopLogLik = 1e-7;
```

Fit MR-LD w/ (`constr = 1`) and w/o (`constr = 0`) constraint that $\beta = 0$ as:

```
RealMRLD_Hb = MRLDP_RealPXvb_block(bpnew, chrnew, avbIndexnew-1, idx4panelnew, block_file,
                                   stringname3, bh1new, bh2new, s12new, s22new,
                                   gamma, alpha, beta0, sgga2, sgal2, coreNum,
                                   lam, 0, epsStopLogLik, maxIter, model = 1);
RealMRLD_H0 = MRLDP_RealPXvb_block(bpnew, chrnew, avbIndex-1, idx4panelnew, block_file,
                                   stringname3, bh1new, bh2new, s12new, s22new,
                                   gamma, alpha, beta0, sgga2, sgal2, coreNum,
                                   lam, 1, epsStopLogLik, maxIter, model = 1);

beta0_MRLD = RealMRLD_Hb$beta0;
Tstat_LD <- 2*(RealMRLD_Hb$tstat - RealMRLD_H0$tstat);
MRLD_se = abs(RealMRLD_Hb$beta0/sqrt(Tstat_LD));
```

beta0_MRLD is the estimated effect of exposure on outcome and MRLD_se is corresponding standard error using MRLD model.

Fit MR-LDP w/ (`constr = 1`) and w/o (`constr = 0`) constraint that $\beta = 0$ as:

```
RealMRLDP_Hb = MRLDP_RealPXvb_block(bp, chr, avbIndex-1, idx4panel, block_file,
                                    stringname3, bh1, bh2, s12, s22,
                                    gamma, alpha, beta0, sgga2, sgal2, coreNum,
                                    lam, 0, epsStopLogLik, maxIter, model = 2);
RealMRLDP_H0 = MRLDP_RealPXvb_block(bp, chr, avbIndex-1, idx4panel, block_file,
                                    stringname3, bh1, bh2, s12, s22,
                                    gamma, alpha, beta0, sgga2, sgal2, coreNum,
                                    lam, 1, epsStopLogLik, maxIter, model = 2);
beta0_MRLDP = RealMRLDP_Hb$beta0;
Tstat_MRLDP <- 2*(RealMRLDP_Hb$tstat - RealMRLDP_H0$tstat);
MRLDP_se = abs(RealMRLDP_Hb$beta0/sqrt(Tstat_MRLDP));
```

beta0_MRLDP is the estimated effect of exposure on outcome and MRLDP_se is the corresponding standard error using MRLD model.