

NECESSARY LIBERAL PRECONDITIONS: A PROOF SYSTEM

MASTER'S THESIS IN INFORMATICS

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SCHOOL OF COMPUTATION, INFORMATION AND TECHNOLOGY - INFORMATICS
TECHNICAL UNIVERSITY OF MUNICH



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SYSTEM
NOTWENDIGE LIBERALE VORBEDINGUNGEN: EIN
BEWEISSYSTEM**

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Submission date: 15. September 2023



DECLARATION

Ich versichere, dass ich diese Masterarbeit selbstständig verfasst und nur die angegebenen Quellen und Hilfsmittel verwendet habe.

I confirm that this master's thesis is my own work and I have documented all sources and material used.

Munich, 15. September 2023

Anran Wang

ABSTRACT

This is where the abstract goes.

ZUSAMMENFASSUNG

Kurze Zusammenfassung des Inhaltes in deutscher Sprache...

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ACRONYMS

Part I

HOARE TRIPLES, WEAKEST PRECONDITIONS, WEAKEST LIBERAL PRECONDITIONS

Some text about this part.

BACKGROUND

In 1739, the Scottish philosopher David Hume questioned why we know that the sun will rise tomorrow, “tho’ ’tis plain we have no further assurance of these facts, than what experience affords us” [7]. Hume’s question about causality is daunting, yet most of us are not in crisis because we doubt if the sun rises tomorrow. The reason is probably that we believe in physics, astrology, and the rules and formulas that assure us the universe works in a certain way, hence the sun rises tomorrow. It is exactly the rules and formulas this thesis attempts to investigate, in the realm of computer programs, with which we are certain that the equivalent version of the sun in a program will rise tomorrow.

Computer programs are ubiquitous in almost every aspect of human life. We want them to solve our problem efficiently, and correctly. Imagine being driven by an autonomous car. It is desirable that it delivers us to the correct destination, and never get stuck driving around the same block without making progress. Delivering the correct result and stopping eventually is called **total correctness**. Once we know that a program is totally correct, then we are sure that the sun rises tomorrow.

To know “for sure”, we could verify programs using formal methods. One famous method is **Hoare Triples** [6]. A Hoare Triple contains three parts: a precondition, a program, and a postcondition. They are written as such: $G \{C\} F$. It states that if the system is in a state that satisfies the precondition, then the state after the execution of the program will satisfy the postcondition, provided that the program terminates. Hoare Triples is elegant in that once we have appropriate preconditions, it works well syntactically and sequentially. But with Hoare Triples in its original form, we know the program is correct, but we are not sure of its termination. This is called **partial correctness**.

To prove a program totally correct, Dijkstra presented the **weakest precondition transformer** [2] (wp): starting with a postcondition, it works backwards and calculates what the precondition can be that guarantees both correctness and termination. While in Hoare Triples, the precondition is a **sufficient** condition where the program will be correct in that the final state will satisfy the desired postcondition, with wp we obtain a **necessary and sufficient** precondition.

Since then, a plethora of research projects blossomed and yielded fruitful results. This thesis aims to follow the steps of the predecessors and investigate **weakest liberal precondition transformer** [4] (wlp), which gives preconditions that are necessary and sufficient so that the program either terminates correctly or never terminates.

We first introduce Hoare Triples, wp transformer, and wlp transformer, using **Guarded Command Language** [2] to present programs in **Chapter 2**. We also explain their connections and differences.

Then we proceed to **Chapter 3** [fill in content of this chapter]

1

¹ TODO: Decide on all the colors in the end.

PRELIMINARIES

2.1 HOARE LOGIC

Since the beginning of the 1960s, scholars have been researching the establishment of mathematics in computation [5, 10] to have a formal understanding and reasoning of programs. One of the most known methods is [Hoare logic](#).

In 1969, C.A.R. Hoare wrote *An Axiomatic Basis for Computer Programming* [6] to explore the logic of computer programs using axioms and inference rules to prove the properties of programs. He introduced **sufficient** preconditions that guarantee correct results but do not rule out non-termination. A selection of the axioms and rules are shown in [Table 1](#).¹² $\{F[x/e]\}$ is obtained by substituting occurrences of x by e .

Axiom of Assignment	$F[x/e] \{x := e\} F$
Rules of Consequence	$\text{If } G \{C\} F \text{ and } F \Rightarrow P \text{ then } G \{C\} P$ $\text{If } G \{C\} F \text{ and } P \Rightarrow G \text{ then } P \{C\} F$
Rule of Composition	$\text{If } G \{C_1\} F_1 \text{ and } F_1 \{C_2\} F \text{ then } G \{C_1; C_2\} F$
Rule of Iteration	$\text{If } (F \wedge B) \{C\} F \text{ then } F \{\text{while } B \text{ do } C\} \neg B \wedge F$

Table 1: Valid Hoare Triple

Semantically, a Hoare triple $G \{C\} F$ is said to be valid for (partial) correctness, if the execution of the program C with an initial state satisfying the precondition G leads to a final state that satisfies the postcondition F , provided that the program terminates. The definitions in [Table 1](#) indeed correspond to this intended semantics. Formal soundness proofs can be found in Krzysztof R. Apt's survey [1] in 1981. As an example, consider the rule of composition: if the execution of program C_1 changes the state from G to F_1 , and C_2 changes the state from F_1 to F , then executing them consecutively should bring the program state from G to F , with the intermediate state F_1 .

The missing guarantee of termination can be seen in the rule of iteration: consider the triple $x \leq 2 \{\text{while } x \leq 1 \text{ do } x := x * 2\} 1 < x \leq 2$, it is provable in Hoare logic with the following proof tree. However, this while-loop will not terminate in case $x \leq 0$ in the initial state.

¹ We omit the symbol \vdash in front of a Hoare triple, which denotes “valid/provable”, for better readability.

² Non-determinism was not considered in the original paper, so we treat the programs here as deterministic. With deterministic programs, one initial state corresponds to one final state, and in case of non-termination we assign a final state \perp .³

$\frac{x \leq 1 \{x := x * 2\} x \leq 2}{x \leq 2 \{\text{while } x \leq 1 \text{ do } x := x * 2\} 1 < x \leq 2}$	
$\frac{}{x \leq 1 \{x := x * 2\} x \leq 2}$	Axiom of Assignment
$\frac{}{x \leq 2 \{\text{while } x \leq 1 \text{ do } x := x * 2\} 1 < x \leq 2}$	Rule of Iteration

Using style taken from Benjamin L. Kaminski's dissertation [8], Figure 1 illustrates a valid Hoare triple: Σ represents the set of all states, the section denoted with G includes the states that satisfy the predicate G . The arrow from left to right denotes the execution of the program C .

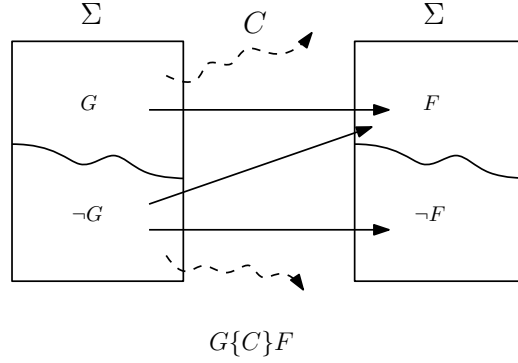


Figure 1: Valid Hoare Triple (Deterministic)

A sensible advancement of Hoare logic would be to also prove termination, i.e. to eliminate the arrows from G to the abyss. Supplementing Hoare logic with a termination proof is done by Zohar Manna and Amir Pnueli in 1974 [9], where they introduced what we call a **loop variant**, a value that decreases with each iteration. The name is in contrast to **loop invariant**, concretely the F in **Rule of Iteration** in Table 1, which is constant before and after the loop.

Another advancement would be to find the **necessary and sufficient** preconditions that grant us the post-properties, i.e. to eliminate the arrows from $\neg G$ to F in Figure 1, which is what Edsger W. Dijkstra accomplished with his **weakest precondition** transformer in 1975 [2], among other things.

2.2 GUARDED COMMAND LANGUAGE

From now on we will use Dijkstra's (non-deterministic) **guarded command language (GCL)** [2] to represent programs and to include non-determinism (starting from Section 2.3.3). For better readability, we use an equivalent⁴ form of GCL that is similar to modern pseudo-code as shown in Table 2.

The **assignment**, **sequential composition**, **conditional choice**, **while-loop** commands conform to their usual meaning. The **non-deterministic choice** $\{C_1\} \square \{C_2\}$ chooses from two programs randomly. It is however not **probabilistic**, meaning we do not know the probabilistic distribution of the outcome of the choice.

When **skip** is executed, the program state does not change and the consecutive part is executed. When **diverge** is executed, the program goes to a state symbolizing non-termination, and the execution stops.

⁴ Specifically, if $(\varphi) \{C_1\} \text{ else } \{C_2\}$ is equivalent to $\text{if } \varphi \rightarrow C_1 \square \neg\varphi \rightarrow C_2 \text{ fi}$ in Dijkstra's original style [2]; $\{C_1\} \square \{C_2\}$ is equivalent to $\text{if true} \rightarrow C_1 \square \text{true} \rightarrow C_2 \text{ fi}$.

$C ::=$	$x := e$	$ C; C$	$ \{C\} \square \{C\}$
	assignment	sequential composition	non-deterministic choice
	$ \text{if } (\varphi) \{C\} \text{ else } \{C\}$	$ \text{while } (\varphi) \{C\}$	$ \text{skip} \quad \text{diverge}$
	conditional choice	while-loop	

Table 2: Guarded Command Language

In our representation of GCL, non-determinism is explicitly constructed via the infix operator \square , whereas in its original definition, non-determinism occurs when the guards within the `if` and `while` commands are not mutually exclusive [4]. Additionally, the `if` statement in Dijkstra’s GCL is equivalent to divergence in case non of its guards are true, but in our version this can no longer happen because of the Law of Excluded Middle: the predicate φ must be either true or false, so either the “then” branch or the “else” branch is activated. Consequently, non-termination can only originate from either the `diverge` or the `while` command.

2.3 WEAKEST PRECONDITION

2.3.1 The Deterministic Case

To better relate Hoare triples and Dijkstra’s weakest precondition transformer, we first focus on deterministic programs. The goal is to find the **necessary and sufficient** precondition such that the program is guaranteed to **terminate** in a state that satisfies the postcondition. Figure 2 shows it graphically alongside the figure for valid Hoare triples. We can see that on the right side, the arrows from G to non-termination and from $\neg G$ to F are absent.

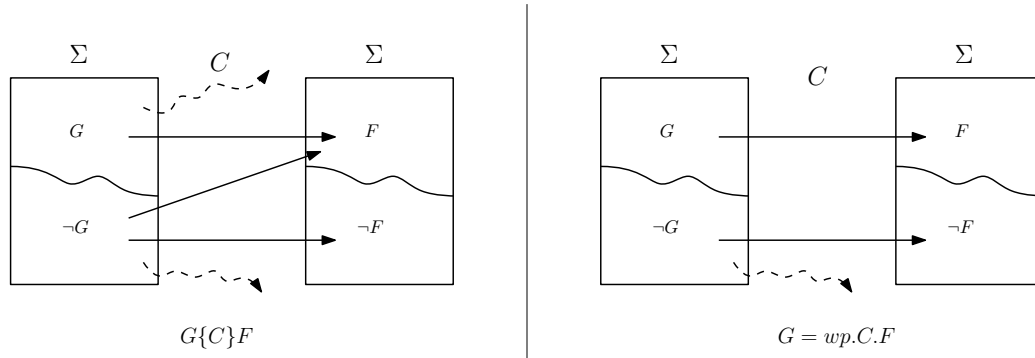


Figure 2: Valid Hoare Triple vs. Weakest Precondition (Deterministic)

We define the **weakest precondition** transformer inductively over the program structure in lambda-calculus style⁵ as in Table 3:

$F[x/e]$ is F where every occurrence of x is syntactically replaced by e .

⁵ For example, $wp.C.F$ can be seen as $wp(C, F)$ in “typical” style, where wp is treated as a function that has two parameters. The advantage of lambda-calculus style is scalability, we can simply extend the aforementioned function to $wp.C.F.\sigma$ where σ means the initial state. Here wp is treated

C	wp.C.F
skip	F
diverge	false
$x := e$	$F[x/e]$
$C_1; C_2$	$\text{wp}.C_1.(\text{wp}.C_2.F)$
if (φ) { C_1 } else { C_2 }	$(\varphi \wedge \text{wp}.C_1.F) \vee (\neg\varphi \wedge \text{wp}.C_2.F)$
while (φ) { C' }	$\text{lfp } X.(\neg\varphi \wedge F) \vee (\varphi \wedge \text{wp}.C'.X)$

Table 3: The Weakest Precondition Transformer for Deterministic Programs [8]

$\text{lfp } X.f$ is the least fixed point of function f with variable X .

Let

$$\Phi(X) := (\neg\varphi \wedge F) \vee (\varphi \wedge \text{wp}.C'.X)$$

be the characteristic function, then wp for while-loop can be defined as:

$$\text{wp}.\text{while}(\varphi)\{C'\}.F = \text{lfp } X.\Phi(X)$$

Most of the definitions in Table 3 are intuitive and correspond to their counterparts in Hoare logic, while those for *diverge* and *while* deserve special attention. Since wp aims for total correctness, a program starting in an initial state satisfying the precondition $\text{wp}.\text{diverge}.F$ should terminate in a final state satisfying the postcondition F . Because *diverge* does not terminate, there is no such precondition and wp for *diverge* should be *false*.

The definition for the while-loop [8] is trickier, but we can verify its correctness by recalling Dijkstra's original definition in the following section.

2.3.2 Defining Loops

In Dijkstra's original paper [2], he defined wp for while-loops based on its (intended) semantics, i.e. the precondition that guarantees loop termination with the required postcondition within a certain number of iterations.

Let

$$\text{WHILE} = \text{while}(\varphi)\{C'\} \quad \text{and} \quad \text{IF} = \text{if } (\varphi)\{C'\} \text{ else } \{\text{diverge}\}.$$

Rewriting Dijkstra's definition in a form conforming to our style, he defines

$$H_0(F) = (\neg\varphi \wedge F) \quad \text{and} \quad H_k(F) = \text{wp}.\text{IF}.H_{k-1}(F) \vee H_0(F).$$

IF is defined in such way that $\text{wp}.\text{IF}.X$ is the weakest precondition that makes sure the guard of IF discharges and C' is executed once, leaving the program in a state satisfying X . As a result, $H_k(F)$ corresponds to the weakest precondition such that the program terminates in a final state satisfying F after **at most** k iterations.

as a function that has three parameters, if we were to write it in the "typical" style. It is then questionable whether we changed the type of wp.

Then by definition:

$$\text{wp.WHILE.F} = (\exists k \geq 0 : H_k(F)) \quad (1)$$

We state that the definition in Table 3 coincides with this definition. Without going too deep into domain theory, we only use one of its theorem that yields a computation for least fixed points, provided they exist.

Theorem 1. *[Insert theorem]*

Coincidentally, $H_k(F)$ is the $(k + 1)$ –th iteration of the characteristic function Φ from the bottom element, denoted by $\Phi^{k+1}(\text{false})$. For all predicates F and all programs C' :

Lemma 1. $\forall k \geq 0 : H_k(F) = \Phi^{k+1}(\text{false})$

Proof. Proof by induction.

BASE CASE:

$$\begin{aligned} \Phi(\text{false}) &= (\neg\varphi \wedge F) \vee (\varphi \wedge \text{wp.C'.false}) \\ &= (\neg\varphi \wedge F) \vee (\varphi \wedge \text{false}) && | (*) \\ &= \neg\varphi \wedge F && | \text{predicate calculus} \\ &= H_0(F) \end{aligned}$$

The equation (*) is supported by the Law of Excluded Miracle [3, p.18]: for all programs C , $\text{wp.C.false} = \text{false}$. It states that it is impossible for a program to terminate in a state satisfying no postcondition.

STEP CASE:

$$\begin{aligned} H_{k+1}(F) &= \text{wp.IF.H}_k(F) \vee H_0(F) \\ &= (\varphi \wedge \text{wp.C'.H}_k(F)) \vee (\neg\varphi \wedge \text{wp.diverge.H}_k(F)) \vee H_0(F) \\ &&& | \text{unfold IF; definition of wp} \\ &= (\varphi \wedge \text{wp.C'.H}_k(F)) \vee (\neg\varphi \wedge \text{false}) \vee H_0(F) \\ &&& | \text{definition of wp} \\ &= (\varphi \wedge \text{wp.C'.}\Phi^{k+1}(\text{false})) \vee H_0(F) \\ &&& | \text{induction hypothesis; predicate calculus} \\ &= (\varphi \wedge \text{wp.C'.}\Phi^{k+1}(\text{false})) \vee (\neg\varphi \wedge F) \\ &= \Phi^{k+2}(\text{false}) \end{aligned}$$

□

Thus by identifying the least fixed point, we find a k that satisfies Equation 1. The advantage of using least fixed point to define wp is that there are heuristics to find it, whereas Equation 1 excels at giving intuitions for the preconditions that guarantee loop termination. Essentially, they express the same predicate, i.e. the “weakest” precondition for while-loops which is unique. Consequently, it means that we can not use other fixed points to define wp.WHILE , which are weaker than the least fixed point. For the same reason, we will see that greatest fixed point is necessary to define weakest liberal precondition.

2.3.3 The Non-deterministic Case: Angelic vs. Demonic

Now we bring the non-deterministic choice back into the picture and add its wp to Table 4. Here we assume a setting with **angelic non-determinism**, where we think that whenever non-determinism occurs, it will resolve in our favor. This results in the weakest precondition for our non-deterministic choice being a disjunction of the wp for its subprograms. We are hopeful that a precondition satisfying the wp of one of the subprograms can also lead to termination in our desired postcondition. This is a design choice that is different from Dijkstra's [2], where the wp for non-deterministic choice would be a conjunction, hinting at a demonic setting. Both choices are justifiable, we choose to follow Zhang and Kaminski's work, favoring the resulting Galois connection between the weakest (liberal) precondition transformers and the strongest (liberal) postcondition transformers [11].

C	$\text{wp}.C.F$
skip	F
diverge	false
$x := e$	$F[x/e]$
$C_1; C_2$	$\text{wp}.C_1.(\text{wp}.C_2.F)$
if $(\varphi) \{C_1\}$ else $\{C_2\}$	$(\varphi \wedge \text{wp}.C_1.F) \vee (\neg\varphi \wedge \text{wp}.C_2.F)$
$\{C_1\} \sqcap \{C_2\}$	$\text{wp}.C_1.F \vee \text{wp}.C_2.F$
while $(\varphi) \{C'\}$	$\text{lfp } X.(\neg\varphi \wedge F) \vee (\varphi \wedge \text{wp}.C'.X)$

Table 4: The Weakest Precondition Transformer for Non-deterministic Programs [8]

The left side of Figure 3 shows wp with non-deterministic programs. Each arrow from left to right shows a **possible** execution of program C .

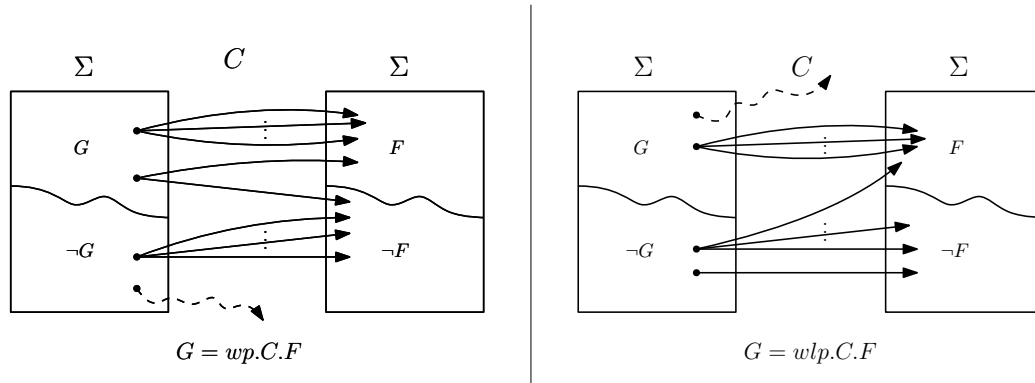


Figure 3: Weakest Precondition (Angelic Non-determinism), Weakest Liberal Precondition (Demonic Non-determinism)

2.4 WEAKEST LIBERAL PRECONDITION

While wp-transformer excludes non-termination, wlp-transformer takes a more liberal approach. The weakest precondition delivers a precondition so that the program terminates and the postcondition is **reachable**. The weakest liberal precondition, however, delivers a precondition so that the program either terminates satisfying the postcondition, or diverges. The postcondition in the wlp setting is not only reachable, but also guaranteed upon termination, because we regard the non-deterministic choice as demonic, again favoring to establish Galois connection [11].

We define the weakest liberal precondition transformer in Table 5. A graphical representation can be found in the right side of Figure 3.

C	wlp.C.F
skip	F
diverge	true
$x := e$	$F[x/e]$
$C_1; C_2$	$\text{wlp}.C_1.(\text{wlp}.C_2.F)$
if (φ) { C_1 } else { C_2 }	$(\varphi \wedge \text{wlp}.C_1.F) \vee (\neg\varphi \wedge \text{wlp}.C_2.F)$
$\{C_1\} \Box \{C_2\}$	$\text{wlp}.C_1.F \wedge \text{wlp}.C_2.F$
while (φ) { C' }	$\text{gfp } X.(\neg\varphi \wedge F) \vee (\varphi \wedge \text{wlp}.C'.X)$

Table 5: The Weakest Liberal Precondition Transformer

As preluded earlier, greatest fixed points are used to define wlp for while-loops.

6

2.5 PROPERTIES OF WP AND WLP

wp and wlp are each other's conjugate:

$$\text{wp}.C.F = \neg \text{wlp}.C.\neg F$$

[TO BE CONTINUED]

6 TODO: Explain the use of gfp. Possibly relate to page 185 of Dijkstra and Scholten 1990 book.

Part II

NECESSARY LIBERAL PRECONDITIONS

Some text about this part.

A PROOF SYSTEM

3.1 A PROOF SYSTEM

In this section we study the necessary liberal precondition:

$$\text{wlp}.C.F \implies G$$

3.2 SKETCHES

Note for readers: In this section are informal sketches of my thoughts.

POSSIBLE WAYS TO APPROACH THIS

1. $\text{wlp}.C.F \implies G$ but restrict G by requiring that the postcondition F is always reachable. Effectively this transfers wlp in demonic setting to wlp in angelic setting, the postcondition being “guaranteed” changes into “reachable”. Remember: both Dijkstra’s wp and wlp are in demonic setting, and they are related by $\text{wp}_d.C.X = \text{wp}_d.C.\text{true} \wedge \text{wlp}_d.C.X$. Explore the relationship between $\text{wp}_{\text{angelic}}$, $\text{wp}_{\text{demonic}}$, $\text{wlp}_{\text{angelic}}$, $\text{wlp}_{\text{demonic}}$? Then the results in [11] and [4] can be linked. But then who uses angelic wlp? Also, does it even make sense to investigate this, since they are both extrema, specially in a quantitative setting.

2.

$$\text{wlp}.C.F \implies G \equiv \neg G \implies \neg \text{wlp}.C.F \equiv \neg G \implies \text{wp}.C.\neg F$$

This corresponds to total correctness, but negatively. $\neg G \{C\} \neg F$ would be a valid Hoare Triple. But negative is not pretty.

CONCLUSIONS

4.1 CONCLUSIONS

4.2 FUTURE WORK

Part III

APPENDIX

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COLOPHON

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