

Walking Through My Thesis

Necessary Liberal Preconditions: A Proof System

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Agenda

1 Thesis Structure

2 Contribution

3 Current TODOs

Overview: 3 Parts, 30 Pages, N Images

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Currently divided into three parts:

Part I Definitions, explanations, illustrations.

Part II Proposals, proofs, examples.

Part III Tables, figures, acronyms.

Part I: Hoare Triples, Weakest Preconditions, Weakest Liberal Preconditions

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Chapter 1: Background

- Convince that proof systems are important
- Show the structure of the thesis

Chapter 2: Preliminaries

- Table of Notations
- Definitions of Hoare Triples, GCL, wp, wlp, sp
 - Explain the use of lfp and gfp
- Soundness: semantics of wp, wlp, sp
- Properties of wp and wlp that will be used in part II (forthcoming)

Part II: Necessary Liberal Preconditions

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Chapter 3: A Proof System

- (Forthcoming) Literature review: the similar triples that have been studied
- Studying a special G such that $w/p.C.F \implies G$: establish wlp with angelic non-determinism using G and sp .
- Studying G in general: proving things negatively

Chapter 4: Conclusion

- Conclusion (forthcoming)
- Future work (forthcoming)

Part III: Appendix

III APPENDIX

A SYMBOLS AND ACRONYMS

B GRAPHICAL ILLUSTRATION OF PREDICATE TRANSFORMERS

BIBLIOGRAPHY

- 22 ■ Symbols and Acronyms (delete?)
- 23
- 24 ■ Graphical illustration of predicate
26 transformers (all combinations)

Contribution of My Thesis

- (Re-)Explanation of the use of least and greatest fixed points while defining predicate transformers, might be of pedagogic value.
- Establish wlp in angelic setting using wlp_d and sp , which might shed light on angelic and demonic views on non-determinism.
- A proof system that proves programs when negation is hard or impossible.

Current TODOs

Thank you!

Link to Repository

[1] <https://github.com/AnranW/wlp/blob/main/thesis/main-anran-ma.pdf>.