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1 import numpy as np
2 import matplotlib.pyplot as plt
3
4 # Normal Gauss
5 def gauss_elimination(A, b):
6     A = A.astype(float)
7     b = b.astype(float)
8     n = len(b)
9     for k in range(n-1):
10         for i in range(k+1, n):
11             if A[k,k] == 0:
12                 raise ValueError("Zero pivot encountered!")
13         factor = A[i,k]/A[k,k]
14         A[i,k:] -= factor*A[k,k:]
15         b[i] -= factor*b[k]
16     x = np.zeros(n)
17     for i in range(n-1, -1, -1):
18         x[i] = (b[i] - np.dot(A[i,i+1:], x[i+1:])) / A[i,i]
19     return x
20
21 # Selected Gauss
22 def gauss_elimination_pivot(A, b):
23     A = A.astype(float)
24     b = b.astype(float)
25     n = len(b)
26     for k in range(n-1):
27         max_row = np.argmax(abs(A[k:,k])) + k
28         if max_row != k:
29             A[[k,max_row]] = A[[max_row,k]]
30             b[[k,max_row]] = b[[max_row,k]]
31         for i in range(k+1, n):
32             factor = A[i,k]/A[k,k]
33             A[i,k:] -= factor*A[k,k:]
34             b[i] -= factor*b[k]
35     x = np.zeros(n)
36     for i in range(n-1, -1, -1):
37         x[i] = (b[i] - np.dot(A[i,i+1:], x[i+1:])) / A[i,i]
38     return x
39
40 # Equations Define
41 A1 = np.array([[1e-8, 2, 3],
42               [-1, 3.712, 4.623],
43               [-2, 1.072, 5.643]])
44 b1 = np.array([1, 2, 3])
45
46 A2 = np.array([[4, -2, 4],
47               [-2, 17, 10],

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48         [-4, 10, 9]])
49 b2 = np.array([10, 3, 7])
50 x1_gauss = gauss_elimination(A1, b1)
51 x1_pivot = gauss_elimination_pivot(A1, b1)
52 x2_gauss = gauss_elimination(A2, b2)
53 x2_pivot = gauss_elimination_pivot(A2, b2)
54 print("System 1 Gaussian elimination solution:", x1_gauss)
55 print("System 1 Gaussian elimination with partial pivoting
    solution:", x1_pivot)
56 print("System 2 Gaussian elimination solution:", x2_gauss)
57 print("System 2 Gaussian elimination with partial pivoting
    solution:", x2_pivot)
58
59 # Plot
60 fig, ax = plt.subplots(figsize=(10,2))
61 ax.axis('off')
62 text = (
63     "\n"
64     f"          System 1 Gaussian elimination:          {
x1_gauss}\n"
65     f"          System 1 Gaussian elimination w/ pivot:  {
x1_pivot}\n\n\n"
66     f"          System 2 Gaussian elimination:          {
x2_gauss}\n"
67     f"          System 2 Gaussian elimination w/ pivot:  {
x2_pivot}"
68 )
69 ax.text(0.01, 0.99, text, fontsize=12, va='top', ha='left'
    , family='monospace')
70 plt.tight_layout()
71 plt.savefig('Gauss_result.png', dpi=300)
72 plt.show()
73

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