

Some Useful Summation Formula:

classmate

Date

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Sum

closed Form

$$\textcircled{1} \sum_{k=0}^n ar^k (r \neq 0) \longrightarrow \frac{ar^{n+1} - a}{r-1}, r \neq 1$$

$$\textcircled{2} \sum_{k=1}^n k \longrightarrow \frac{n(n+1)}{2}$$

$$\textcircled{3} \sum_{k=1}^n k^2 \longrightarrow \frac{n(n+1)(2n+1)}{6}$$

$$\textcircled{4} \sum_{k=1}^n k^3 \longrightarrow \frac{n^2(n+1)^2}{4}$$

$$\textcircled{5} \sum_{k=0}^{\infty} x^k, |x| < 1 \longrightarrow \frac{1}{1-x}$$

$$\textcircled{6} \sum_{k=1}^{\infty} kx^{k-1}, |x| < 1 \longrightarrow \frac{1}{(1-x)^2}$$

Eg: Find $\sum_{k=50}^{100} k^2$

$$\text{Soln } \sum_{k=1}^{100} k^2 = \sum_{k=1}^{49} k^2 + \sum_{k=50}^{100} k^2$$

$$\text{So } \sum_{k=50}^{100} k^2 = \sum_{k=1}^{100} k^2 - \sum_{k=1}^{49} k^2$$

$$\sum_{k=50}^{100} k^2 = \frac{100 \cdot 101 \cdot 201}{6} - \frac{49 \cdot 50 \cdot 99}{6} = 338350 - 49425 = 288925$$

Eg: What is the value of $\sum_{SE(0,2,4)} S$?

81st Because $\sum_{SC(0,2,4)} S$ represents the sum of the values of

S for all the members of the set $\{0,2,4\}$, it follows that

$$\sum_{SC\{0,2,4\}} S = 0+2+4 = 6 //$$