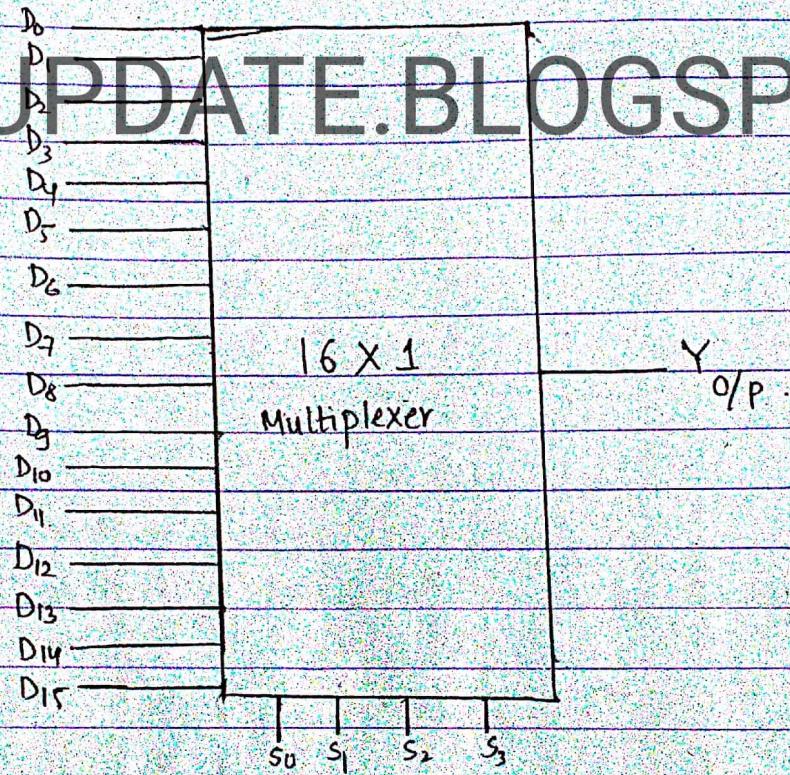


- Gaurav Chauhan  
- Digital Logic

2065

1. Draw a block diagram, truth table and logical circuit of a  $16 \times 1$  multiplexer and explain its working principle.

→ Block diagram:



Working principle:

A multiplexer is a combinational circuit that allows digital information from several sources to be routed on a single line of transmission. It accepts data from any input sources for transmission over a common shared line.

A MUX has several data input lines and a single output line and selection switches which permits digital data on any one of the inputs to be switched to the output lines. A MUX has  $2^n$  inputs and ' $n$ ' select bits.

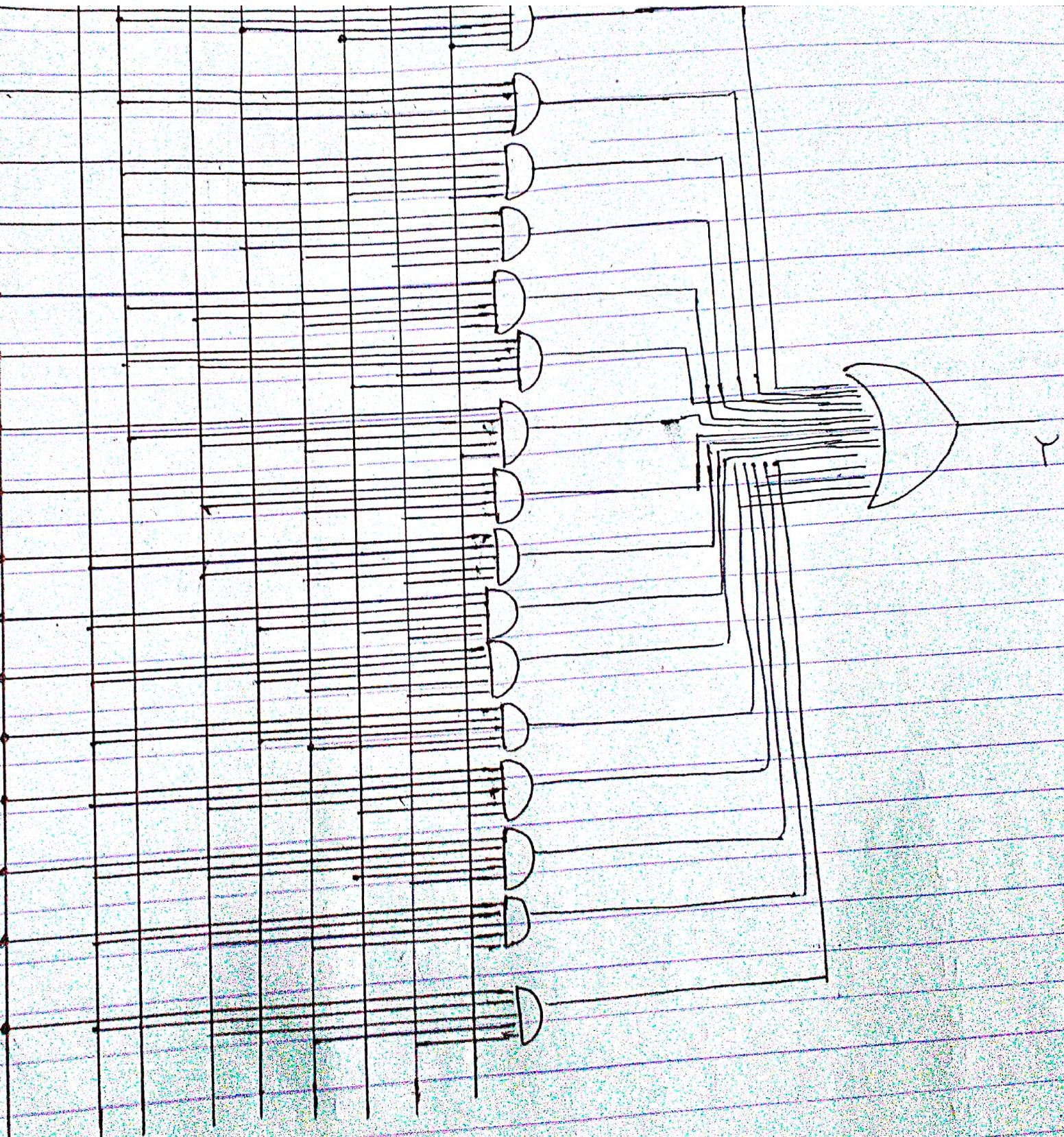
for  $16 \times 1$  MUX,  
 data at inputs =  $2^4 = 16$   
 data output = 1.  
 select bits = 4.

Truth Table :

Data i/p	$S_0$	$S_1$	$S_2$	$S_3$	Y
$D_0$	0	0	0	0	$D_0 \bar{S}_0 \bar{S}_1 \bar{S}_2 \bar{S}_3 \Rightarrow D_0$ selected
$D_1$	0	0	0	1	$D_1 \bar{S}_0 \bar{S}_1 \bar{S}_2 S_3 \Rightarrow D_1$ selected
$D_2$	0	0	1	0	$D_2 \bar{S}_0 \bar{S}_1 S_2 \bar{S}_3 \Rightarrow D_2$ selected
$D_3$	0	0	1	1	$D_3 \bar{S}_0 \bar{S}_1 S_2 S_3 \Rightarrow D_3$ selected
$D_4$	0	1	0	0	$D_4 \bar{S}_0 S_1 \bar{S}_2 \bar{S}_3 \Rightarrow D_4$ selected
$D_5$	0	1	0	1	$D_5 \bar{S}_0 S_1 \bar{S}_2 S_3 \Rightarrow D_5$ selected
$D_6$	0	1	1	0	$D_6 \bar{S}_0 S_1 S_2 \bar{S}_3 \Rightarrow D_6$ selected
$D_7$	0	1	1	1	$D_7 \bar{S}_0 S_1 S_2 S_3 \Rightarrow D_7$ selected
$D_8$	1	0	0	0	$D_8 S_0 \bar{S}_1 \bar{S}_2 \bar{S}_3 \Rightarrow D_8$ selected
$D_9$	1	0	0	1	$D_9 S_0 \bar{S}_1 \bar{S}_2 S_3 \Rightarrow D_9$ selected
$D_{10}$	1	0	1	0	$D_{10} S_0 \bar{S}_1 S_2 \bar{S}_3 \Rightarrow D_{10}$ selected
$D_{11}$	1	0	1	1	$D_{11} S_0 \bar{S}_1 S_2 S_3 \Rightarrow D_{11}$ selected
$D_{12}$	1	1	0	0	$D_{12} S_0 S_1 \bar{S}_2 \bar{S}_3 \Rightarrow D_{12}$ selected
$D_{13}$	1	1	0	1	$D_{13} S_0 S_1 \bar{S}_2 S_3 \Rightarrow D_{13}$ selected
$D_{14}$	1	1	1	0	$D_{14} S_0 S_1 S_2 \bar{S}_3 \Rightarrow D_{14}$ selected
$D_{15}$	1	1	1	1	$D_{15} S_0 S_1 S_2 S_3 \Rightarrow D_{15}$ selected

logic circuit:





2. Explain the 4-bit ripple counter and also draw a timing diagram.

logic high

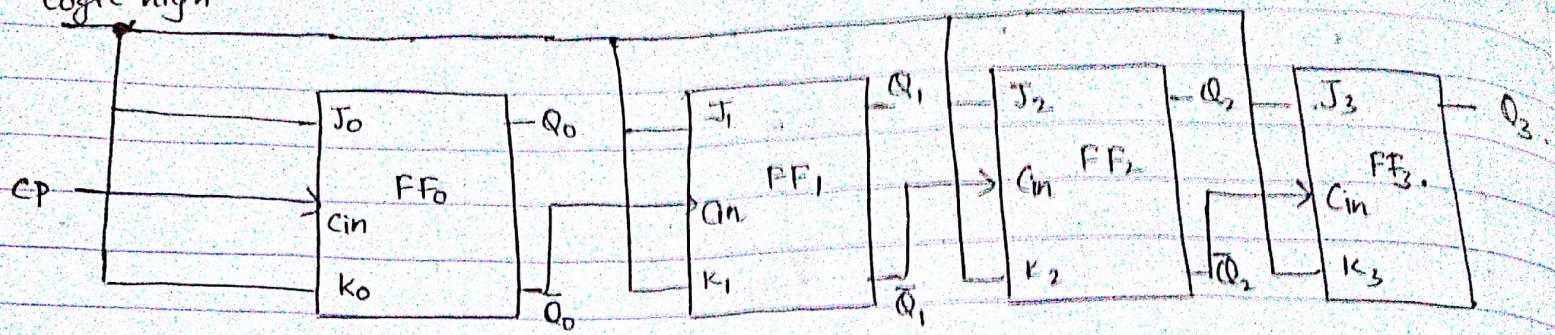
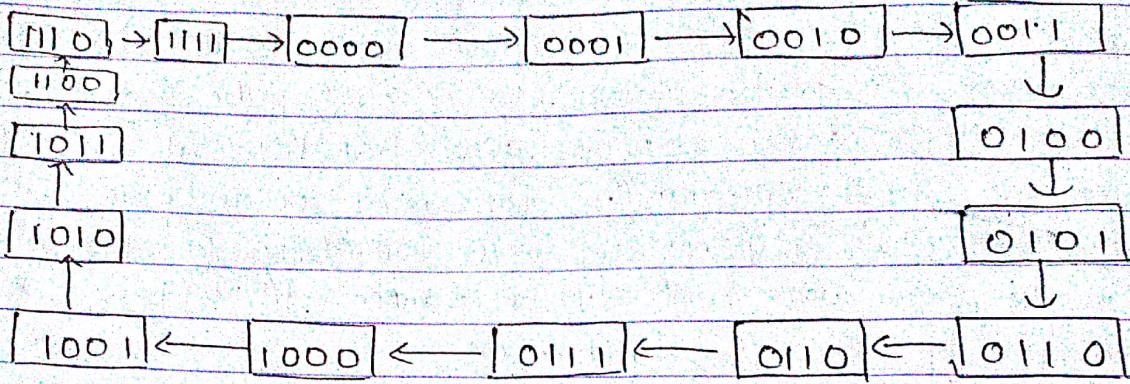


fig. 4-bit ripple Counter

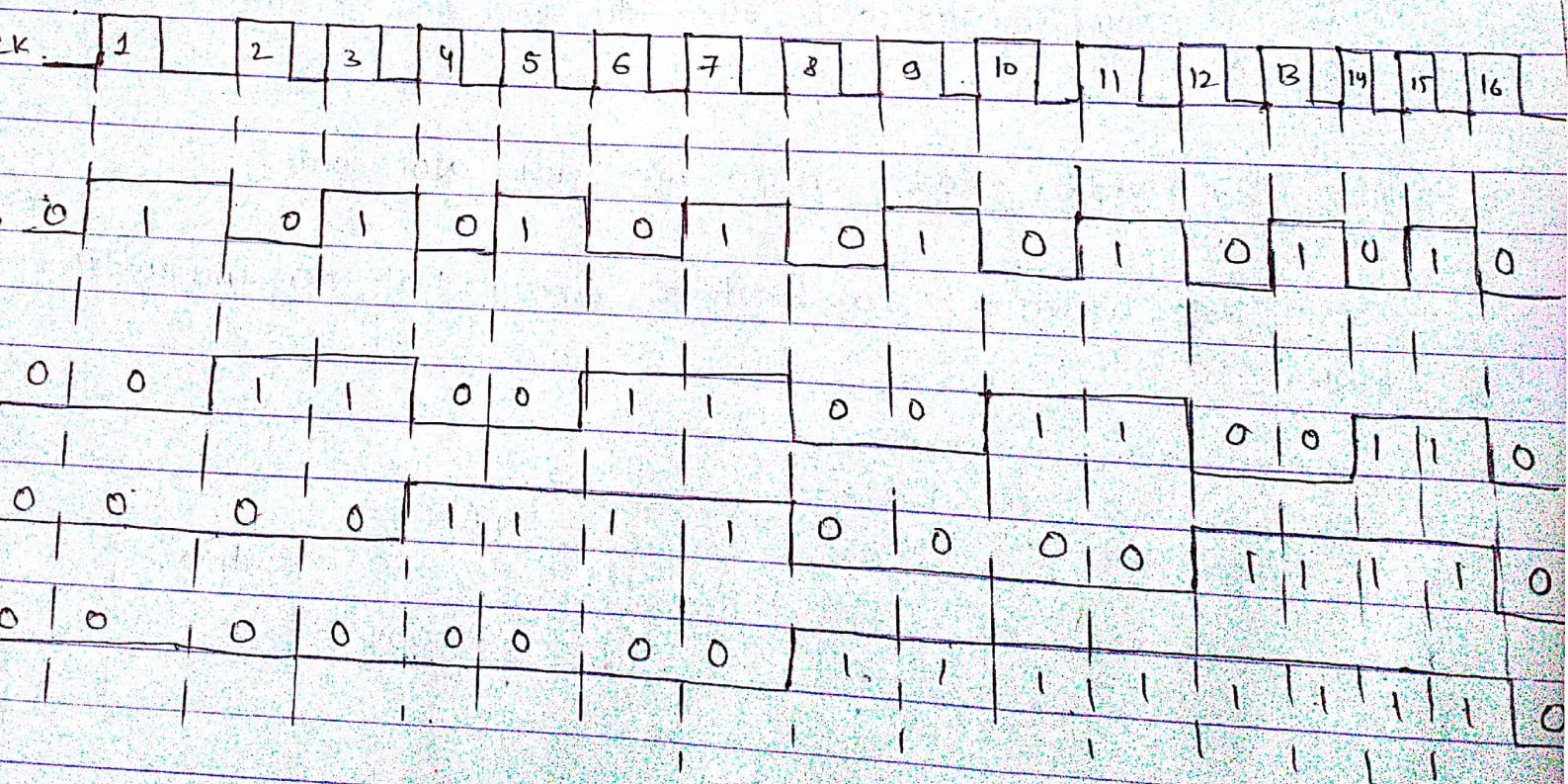
state sequence:

clock pulse	$Q_3$	$Q_2$	$Q_1$	$Q_0$
Initially	0	0	0	0
1	0	0	0	1
2	0	0	1	0
3	0	0	1	1
4	0	1	0	0
5	0	1	0	1
6	0	1	1	0
7	0	1	1	1
8	1	0	0	0
9	1	0	0	1
10	1	0	1	0
11	1	0	1	1
12	1	1	0	0
13	1	1	0	1
14	1	1	1	0
15	1	1	1	1
(Recycler) 16	0	0	0	0

state diagram:



timing diagram:



Here, 4 flipflops are connected with CP applied to Cinput of the first flipflop ( $FF_0$ ) which is always the least significant bit. The second flipflop ( $FF_1$ ) is triggered by  $\bar{Q}_0$  [output of  $FF_0$ ].  $FF_0$  changes state at positive going edge of clock pulse but  $FF_1$  changes only when triggered by positive going transition of  $\bar{Q}_0$ . Since, transition of input CP and  $\bar{Q}_0$  can never occur exactly at the same time, The two flipflops are never simultaneously triggered. Likewise, in the same way with similar manner  $FF_2, FF_3$  are triggered and the counter operation is asynchronous.

The 4-bit ripple counter has 16 states because of 4-flips. This is an up-counter which counts from 0 to 15 - where,

- $Q_0$  is complemented at every count pulse
- $Q_1$  is complemented only when  $Q_0$  goes from 1 to 0.
- $Q_2$  is complemented only when  $Q_1$  goes from 1 to 0.
- $Q_3$  is

Design Half adder logic circuit only using NOR gate.

Half adder is a combinational circuit that performs addition of 2 binary bits.



fig. Block diagram

Truth table:

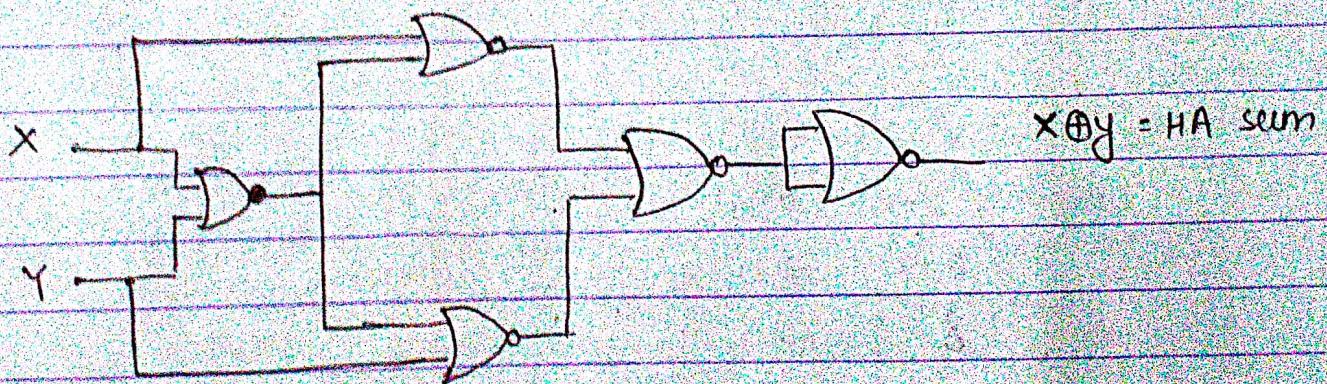
Inputs		Outputs	
X	Y	HA sum	HA carry
0	0	0	0
0	1	1	0
1	1	0	1

$$\text{HA sum} = \bar{x}y' + \bar{y}x' = x \oplus y$$

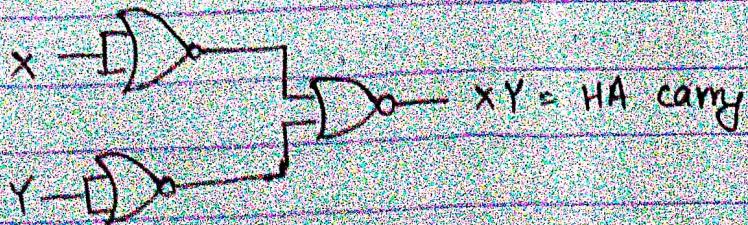
$$\text{HA carry} = xy$$

only using Nor gates, [logic circuit].

HA sum:



HA carry:



5. Convert the following decimal numbers into hexadecimal and octal number.

(a) 304

Converting into octal:

$$\begin{array}{r} 8 \mid 304 \rightarrow 0 \\ 8 \mid 38 \rightarrow 6 \\ 4 \rightarrow 4 \end{array}$$

$$\therefore (304)_{10} = (460)_8.$$

Converting into hexadecimal:

$$\begin{array}{r} 16 \mid 304 \rightarrow 0 \\ 16 \mid 19 \rightarrow 3 \\ 1 \rightarrow 1 \end{array}$$

$$\therefore (304)_{10} = (130)_{16}$$

(b) 224

Converting into octal:

$$\begin{array}{r} 8 \mid 224 \rightarrow 0 \\ 8 \mid 28 \rightarrow 4 \\ 3 \rightarrow 3 \end{array}$$

$$\therefore (224)_{10} = (340)_8$$

Converting into hexadecimal:

$$\begin{array}{r} 16 \mid 224 \rightarrow 0 \\ 14 \rightarrow 14 \end{array}$$

$$\therefore (224)_{10} = (140)_{16}$$

6) Describe the three variable K-map with example:

The Karnaugh map or K-map is a graphical technique for simplifying boolean function. The K-map is two dimensional representation of truth table. It provides a simpler method for minimizing logic expressions. The map method is ideally suited for four or less variables. A K-map is diagram consisting of squares. Each square representing either min term or max term. Any logic expression can be written either in sum of product term or product of sum term.

A Karnaugh map for n variables are made up of  $2^n$  squares. Each square designates a product term in Boolean expression. For three variable Karnaugh-map, there are 3 variables i.e. the K-map consists of 8 squares. Each square for product for any boolean function,

$$F(W, X, Y) = \sum(0, 1, 3, 4)$$

K-map is written as,

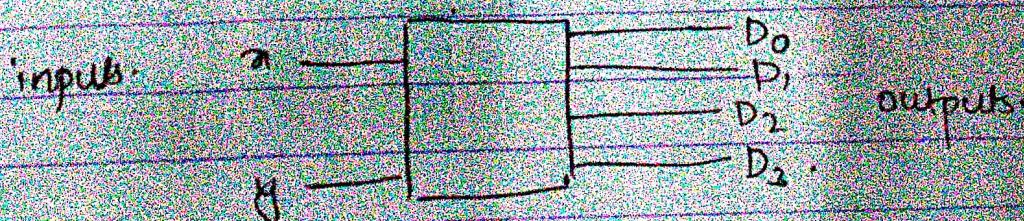
W	XY	X'Y	X'Y'	XY'
W'	1	1	1	
W	1			

The reduced boolean expression is

$$F = X'Y' + Y$$

7) Design the Decoder using universal gates:

2x4 decoder:



Truth table:

inputs		outputs			
X	Y	D <sub>0</sub>	D <sub>1</sub>	D <sub>2</sub>	D <sub>3</sub>
0	0	1	0	0	0
0	1	0	1	0	0
1	0	0	0	1	0
1	1	0	0	0	1

Boolean expression:

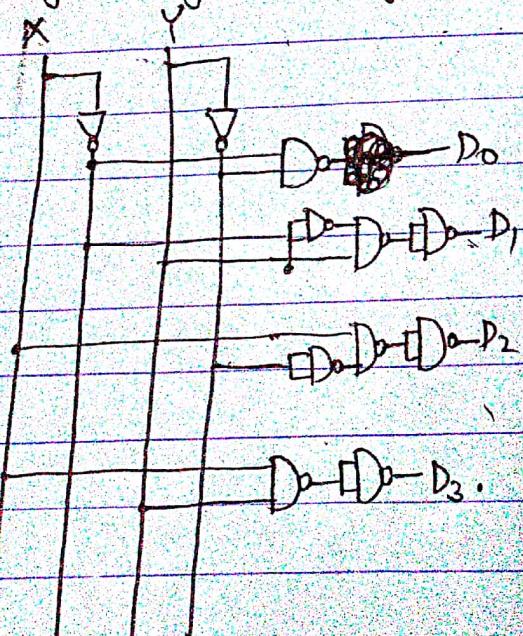
$$D_0 = \bar{x}y'$$

$$D_1 = \bar{x}'y$$

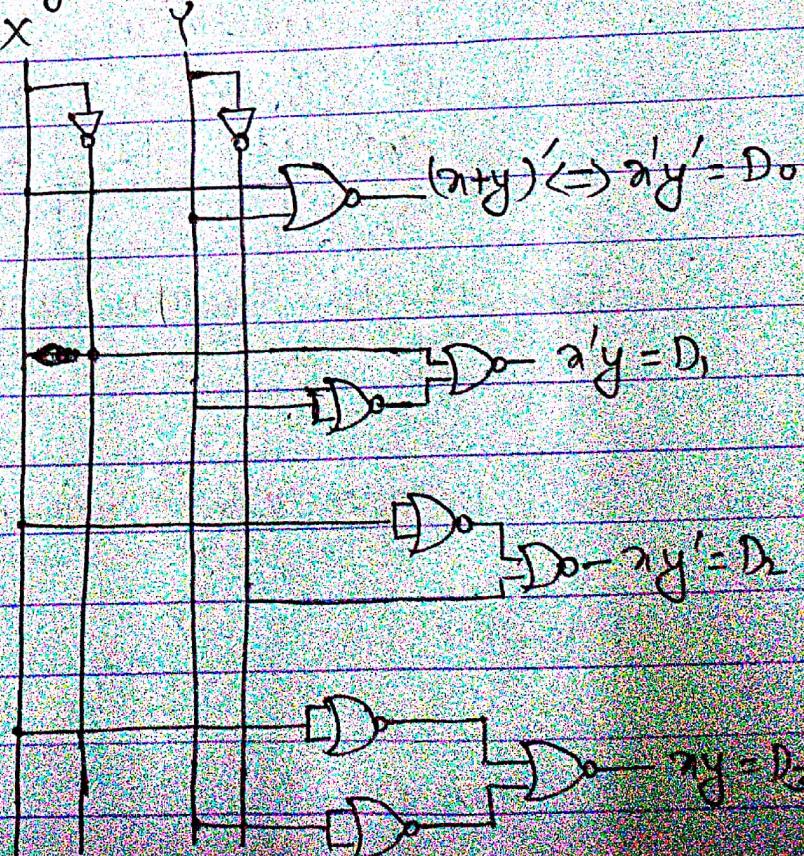
$$D_2 = xy'$$

$$D_3 = xy$$

logic diagram using NAND gate

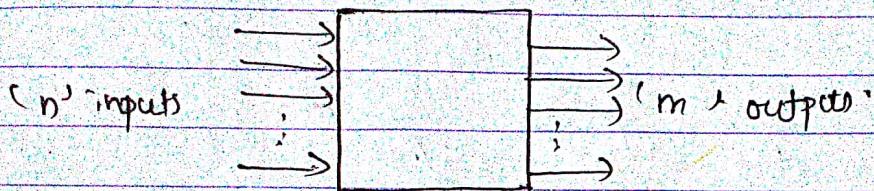


logic diagram using NOR



8. What is combinational circuit? What are its important features?

→ Combinational circuit consists of logic gates whose output at any time is determined by combining the values of the applied inputs using logic operators. Performs an operation that can be specified logically by a set of boolean expressions. It consists of input variables, output variables, logic gates and interconnections which accepts signals from the input and generates signals at the output. For 'n' input variables, there are  $2^n$  possible input combinations.



Characteristics:

- i) The output of combinational circuit at any instant of time, depends only on the levels present at input terminals.
- ii) The combinational circuit does not use any memory. The previous state of input does not have any effect on present state of the output.
- iii) A combinational circuit can have 'n' number of inputs and 'm' no. of outputs.

9. Describe the Clocked RS flip flop

→ A basic flip flop is an asynchronous sequential circuit which has no clock pulse. & by adding gates to the input of the basic circuits, the flip flop can be made to respond to the input levels during the occurrence of a clock pulse. A clocked RS flip flop consists of basic NOR flip flop and two NAND gates or basic NAND flip flop and two NOR gates.

The outputs of two AND gates remain at 0 as long as CP is 0 regardless of S and R input values. When CP goes 1, information from S and R inputs is allowed to reach the basic flip flop. The SET state is reached with S=1, R=0 and CP=1. CLEAR state is reached with S=0, R=1 and CP=1. If S=1 and R=1, the occurrence of clockpulse causes both outputs to momentarily go 0. This is called indeterminate state and has to be practically avoided. If S=0 and R=0, the flip flop retains the previous state.

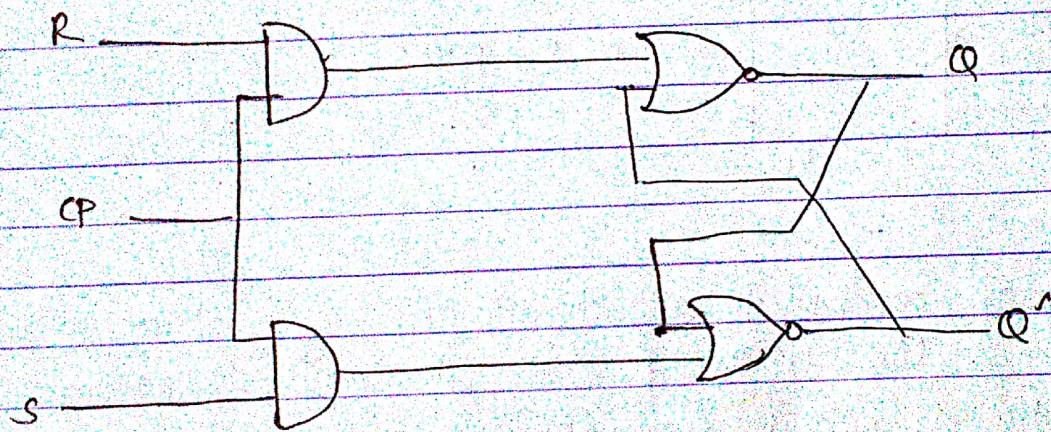


Fig. clocked R-S flip using basic flipflop and AND gate

11. What are shift register operations?

→

shift register is a register capable of shifting its binary information either to the right or to the left. The logical configuration of a shift register consists of a chain of flipflops connected in a cascade with the output of one flipflop connected to the input of another flipflop. All flipflops receives on common clock pulse.



fig. Block diagram of serial transfer using shift registers.

The serial transfer of information from register-A to register-B is done using shift registers. The serial output, SO of register-A goes to the serial <sup>input</sup> of register-'B'. To prevent the loss of information stored in the source register, the values of register-A is made to circulate by connecting the SO to its SI terminal. The initial content of register-B is shifted out through the serial output and is lost unless it is transferred to a third shift register.

- Gaurav Chauhan  
- Digital logic

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1. Design the 4-bit Synchronous up/down counter with timing diagram, logic diagram and truth table.

→ It is a counter that is capable of processing in other directions through a certain sequence which is also called bi-directional counter.

A 4-bit counter that advances upward through its sequence 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15 & then downwards till 0.

Up/down counter can be reversed at any point in their sequence.

For example:

0, 1, 2, 3, 4, 5, 4, 3, 2, 1, 0, 3, 4, 5, 6, 7, 6, 5, 4, 3, 2, 5, 6, 7, up, down, up.

Binary sequence:

C.P	UP	$Q_3$	$Q_2$	$\bar{Q}_1$	$Q_0$	Down
0		0	0	0	0	
1		0	0	1	0	
2		0	1	0	0	
3		0	1	1	1	

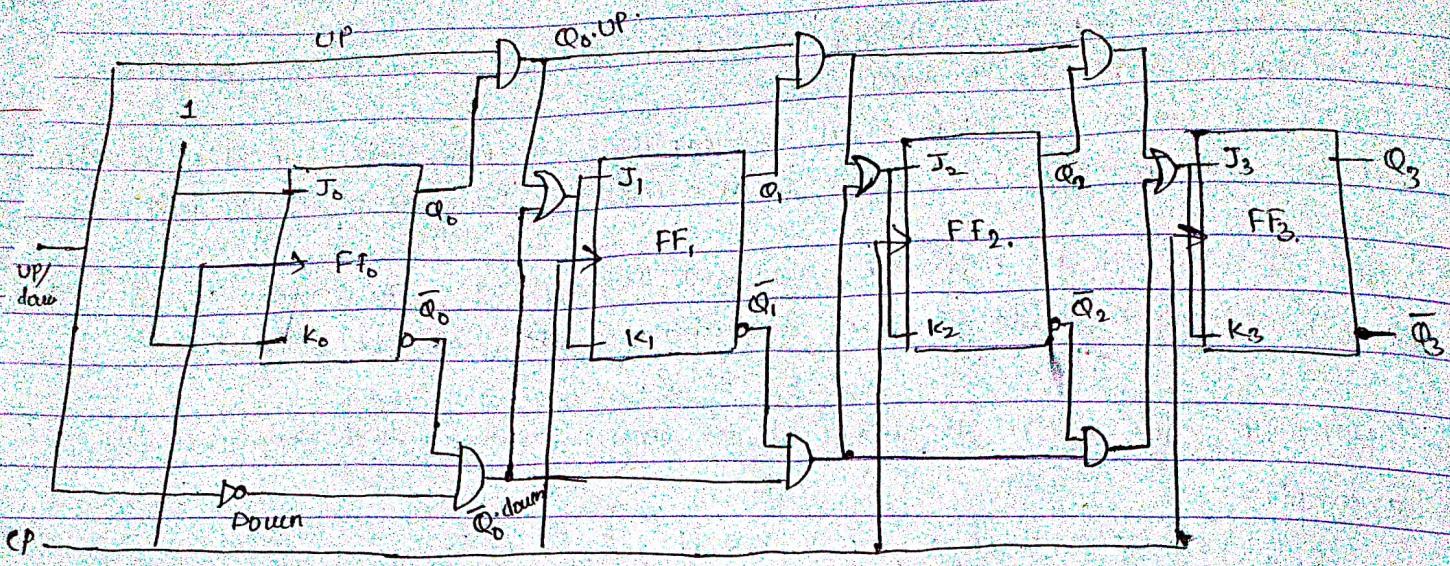


fig. logic diagram of UP/DOWN synchronous counter (4-bit)

Here,

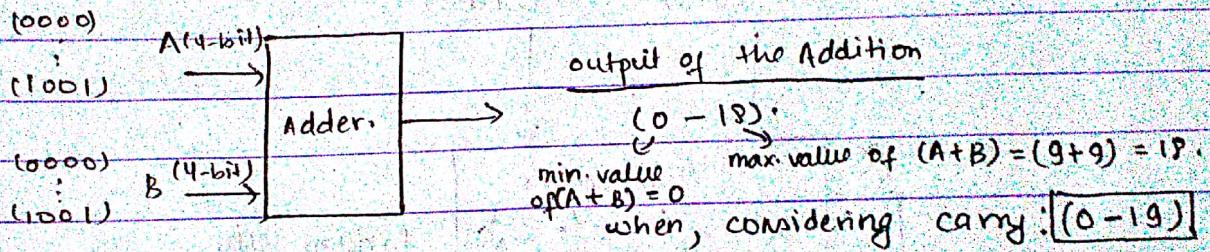
- $Q_0$  changes on its CP i.e.  $J_0 = K_0 = 1$ .
- for UP sequence,  $Q_1$  changes state when  $Q_0 = 1$  and for down sequence,  $Q_1$  changes state when  $Q_0 = 0$  i.e.  $J_1 = K_1 = Q_0 \cdot \text{UP} + Q_0' \cdot \text{down}$
- For UP sequence,  $Q_2$  changes state when  $Q_0 = Q_1 = 1$  and for down sequence,  $Q_2$  changes state when  $Q_0 = Q_1 = 0$  i.e.  $J_2 = K_2 = Q_0 \cdot Q_1 \cdot \text{UP} + Q_0' \cdot Q_1' \cdot \text{down}$
- For UP sequence,  $Q_3$  changes state when  $Q_0 = Q_1 = Q_2 = 1$  and for down sequence,  $Q_3$  changes state when  $Q_0 = Q_1 = Q_2 = 0$  i.e.  $J_3 = K_3 = Q_0 \cdot Q_1 \cdot Q_2 \cdot \text{UP} + Q_0' \cdot Q_1' \cdot Q_2' \cdot \text{down}$

3. Design a decimal adder with logic diagram and truth table.

A BCD adder is a circuit that adds two BCD digits in parallel and produces a sum of digits also in BCD upto 9 i.e. 0 to 9. The corresponding BCD is identical to the binary so no correction is required.

But, when the input binary sum is greater than  $10_1$  i.e. 1001, the BCD sum is not equivalent to the binary sum. So, correction is required i.e. the addition of binary '6' [0110] to the binary sum converts it to the BCD representation and also produces required carry.

The correction can be derived from the truth table.



Decimal	Binary Sum					BCD sum				
	C*	S <sub>3</sub> *	S <sub>2</sub> *	S <sub>1</sub> *	S <sub>0</sub> *	C	S <sub>3</sub>	S <sub>2</sub>	S <sub>1</sub>	S <sub>0</sub>
0	0	0	0	0	0	0	0	0	0	0
1	0	0	0	0	1	0	0	0	1	0
2	0	0	0	1	0	0	0	0	1	1
3	0	0	0	1	1	0	0	0	1	0
4	0	0	1	0	0	0	0	1	0	0
5	0	0	1	0	1	0	0	1	0	1
6	0	0	1	1	0	0	0	1	1	0
7	0	0	1	1	1	0	0	1	0	0
8	0	1	0	0	0	0	1	0	0	1
9	0	1	0	0	1	0	0	1	1	0
10	0	1	0	1	0	1	0	0	0	0
11	0	1	0	1	1	1	0	0	0	1
12	0	1	1	0	0	1	0	0	0	1
13	0	1	1	0	1	1	0	0	1	0
14	0	1	1	1	0	1	0	1	0	1
15	0	1	1	1	1	1	0	1	1	0
16	1	0	0	0	0	1	0	1	0	1
17	1	0	0	0	1	1	1	0	0	0
18	1	0	0	1	0	1	1	0	0	1
19	1	0	0	1	1	1	1	0	0	0

Analyzing the truth table, we can clearly see that the binary sum and BCD sum are not equivalent from 10 to 19. So, we have to apply correction i.e. adding "0110" when :

- (i)  $C^* = 1$
- (ii)  $S_3^* \cdot (S_2^* + S_1^*)$
- (iii)  $S_3^* \cdot S_1^*$

Now,

The condition for correction and output carry can be expressed by boolean formula,  $C = C^* + S_3^* \cdot (S_2^* + S_1^*) + S_3^* \cdot S_1^*$   
 $= C^* + S_3^* \cdot S_2^* + S_3^* \cdot S_1^*$

When,  $C=1$ , it is necessary to add 0110 to the binary sum.

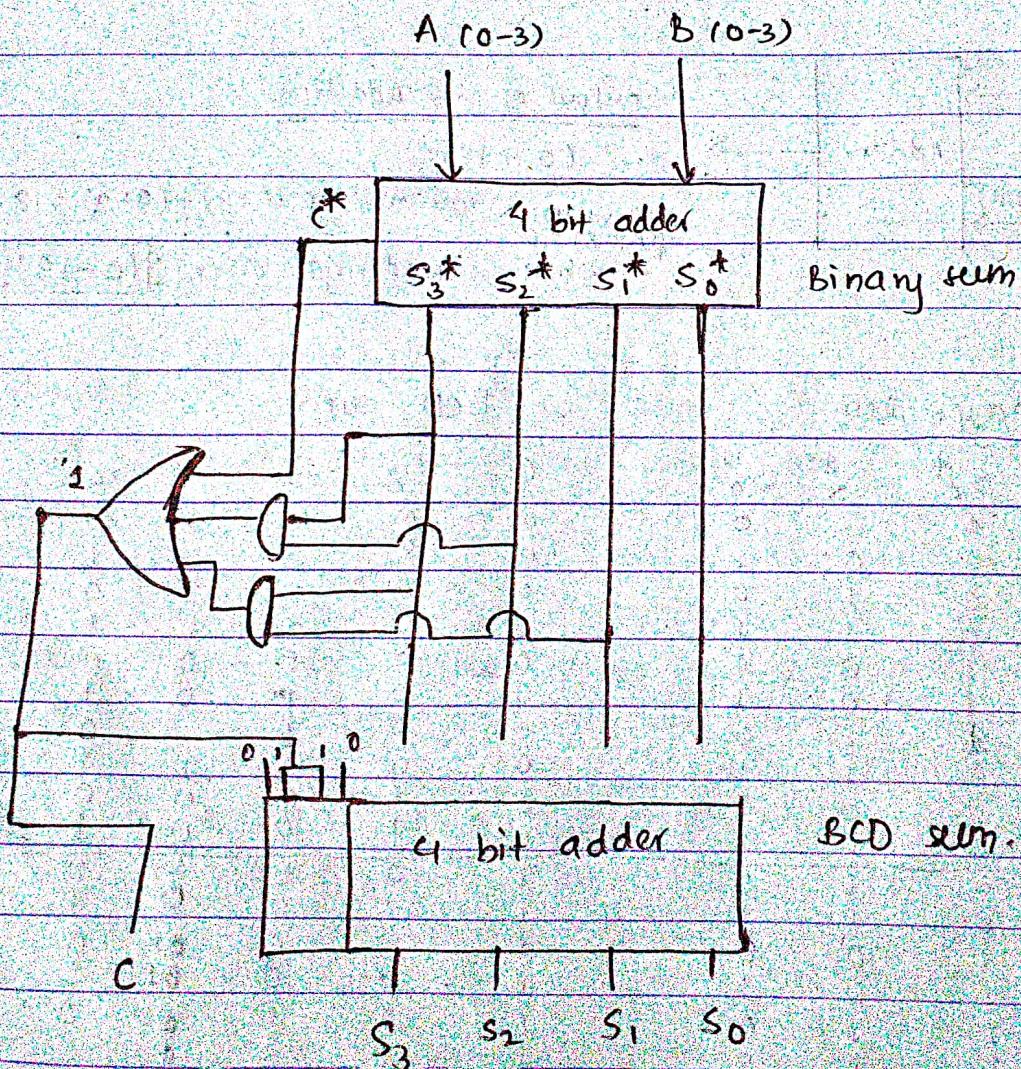


Fig. logic diagram of BCD adder

5. Convert the following octal numbers to hexadecimal.

a) 1760.46.

Solution:

$$(1760.46)_8 = (?)_{16}.$$

First:

changing octal into binary:

$$\begin{array}{ccccccccc} 1 & 7 & 6 & 0 & . & 4 & 6 \\ 001 & 111 & 110 & 000 & . & 100 & 110 \end{array}$$

$$(1760.46)_8 = (111\ 110\ 000.\ 100110).$$

Now,

changing binary into hexadecimal:

$$\begin{array}{ccccccccc} 0001 & 1111 & 0000 & . & 1001 & 1000 \\ 1 & F & 0 & . & 9 & 8 \end{array}$$

$$\therefore (1760.46)_8 = (1F0.98)_{16}.$$

b) 6055.263.

Solution:

$$(6055.263)_8 = (?)_{16}.$$

• changing octal to binary:

$$\begin{array}{ccccccccc} 6 & 0 & 5 & 5 & . & 2 & 6 & 3 \\ 110 & 000 & 101 & 101 & . & 010 & 110 & 011 \end{array}$$

$$\therefore (6055.263)_8 = (110000101101.010110011)_2$$

Now,

changing binary into hexadecimal:

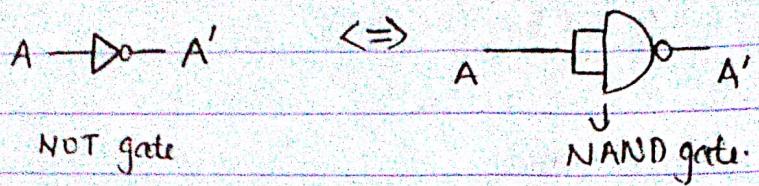
$$\begin{array}{ccccccccc} 1100 & 0010 & 1101 & . & 0101 & 1001 & 1000 \\ C & 2 & D & . & 5 & 9 & 8 \end{array}$$

$$\therefore (6055.263)_8 = (C2D.598)_{16}$$

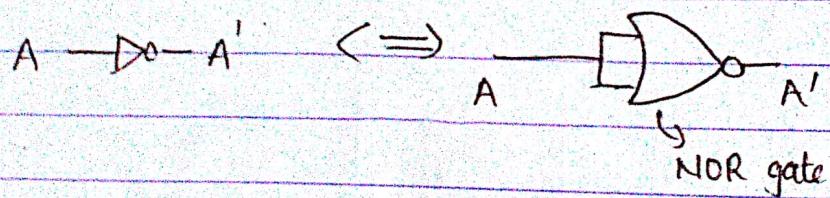
6. Which gates can be used as inverters in addition to the NOT gate and how?

→ NAND and NOR gates can be used as NOT gate.  
They can be made into NOT gate by manipulating the single input as numerous inputs as shown in the figure:

(i) NOT using NAND:



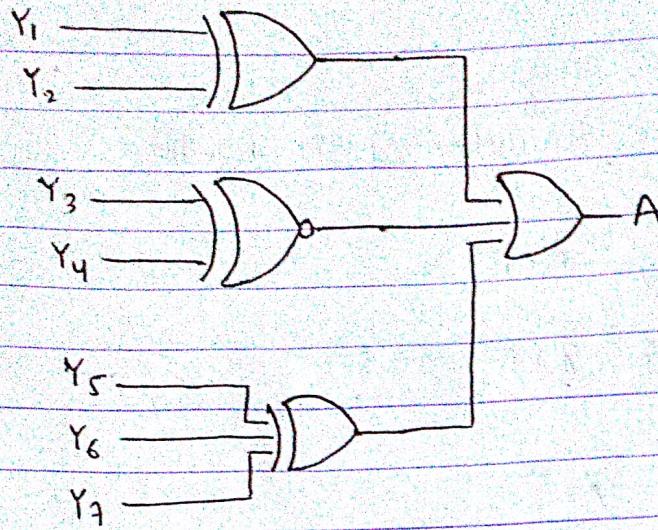
(ii) NOR as NOT:



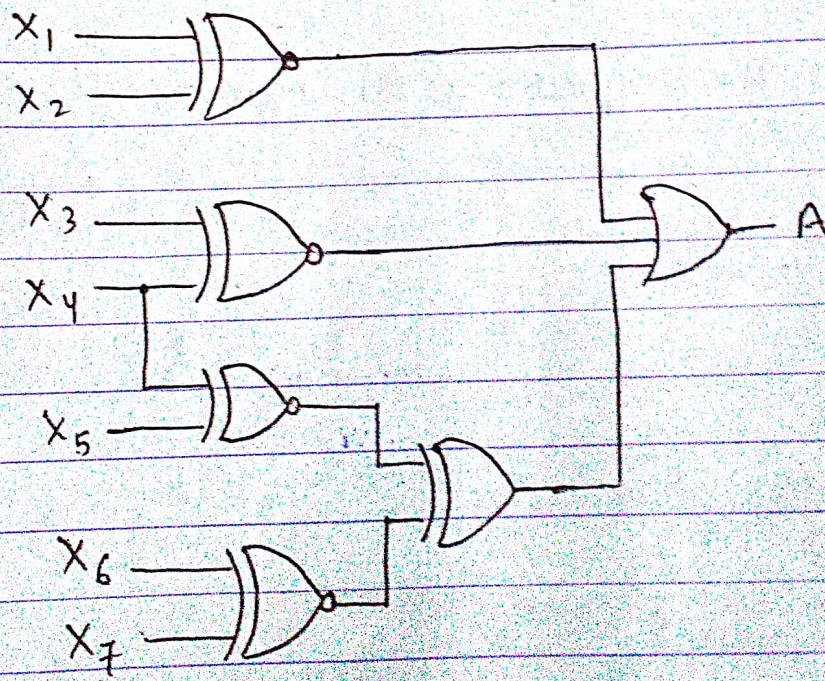
7. Draw a logic gates that implements the following:

$$9) \quad A = (Y_1 \oplus Y_2)(Y_3 \odot Y_4) + Y_5 \oplus Y_6 \oplus Y_7.$$

2



$$b) A = (x_1 \odot x_2) + (x_3 \odot x_4) + (x_4 \odot x_5) \oplus (x_6 \odot x_7)$$



8. State and prove De-Morgan's theorem 1<sup>st</sup> and 2<sup>nd</sup> with logic gates and

truth table:

→ There are two De-Morgan's theorem. They are:

i) The negation of a conjunction is the disjunction of the negations.

$$\overline{A \cdot B} = \overline{A} + \overline{B}$$

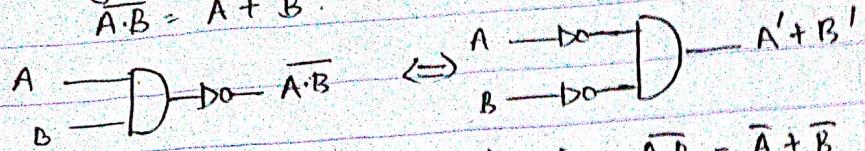


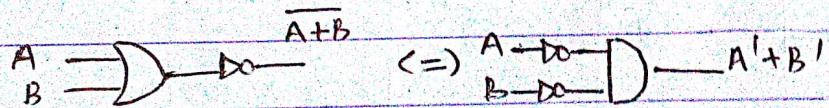
fig. logic gates showing  $\overline{A \cdot B} = \overline{A} + \overline{B}$

Truth table:

A	B	$\overline{A}$	$\overline{B}$	$A \cdot B$	$\overline{A \cdot B}$	$\overline{A} + \overline{B}$
0	0	1	1	0	1	1
0	1	1	0	0	1	1
1	0	0	1	0	1	1
1	1	0	0	1	0	0

ii) The negation of a disjunction is the conjunction of the negations.

$$\overline{A+B} = \overline{A} \cdot \overline{B}$$



Truth table:

A	B	$\overline{A}$	$\overline{B}$	$\overline{A} \cdot \overline{B}$	$A+B$	$\overline{A+B}$
0	0	1	1	1	0	1
0	1	1	0	0	1	0
1	0	0	1	0	1	0
1	1	0	0	0	1	0

9. Reduce the following expression using K-map.

$$\begin{aligned}
 F &= \bar{A} + B(A + \bar{B} + D)(\bar{B} + C)(B + C + D) \\
 &= \bar{A} + (AB + BD)(\bar{B} + C)(B + C + D) \\
 &= \bar{A} + (AB + BD)(\bar{B}C + \bar{B}D + BC + C + CD) \\
 &= \bar{A} + \cancel{AB\bar{B}C^0} + \cancel{AB\bar{B}D^0} + ABC + ABCD + \cancel{B\bar{B}CD^0} + \cancel{B\bar{B}DD^0} \\
 &\quad B\bar{B}CD + BCD + BCDD \\
 &= \bar{A} + ABC + ABC + ABCD + BCD + BCD + BC \\
 &= \bar{A} + ABC + BCD + ABCD \\
 &= A'B'C'D' + A'BCD + ABCD' + ABCD + ABCD + A'BCD + ABCD
 \end{aligned}$$

using K-Map,

	$C'D'$	$C'D$	$CD$	$CD'$
$A'B'$	1			
$A'B$		1		
$AB$			1	1
$AB'$				

$$F = A'B'C'D' + BCD + ABC.$$

11. Explain the operation of Decoder!

10. Difference between a MUX and DEMUX

→

Multiplexer (MUX):

- i) Many inputs & one output
- ii) Data select lines
- iii) Parallel to serial conversion
- iv) When we design MUX, we don't need additional gates.

v) Example: 8:1; 16:1; 32:1.

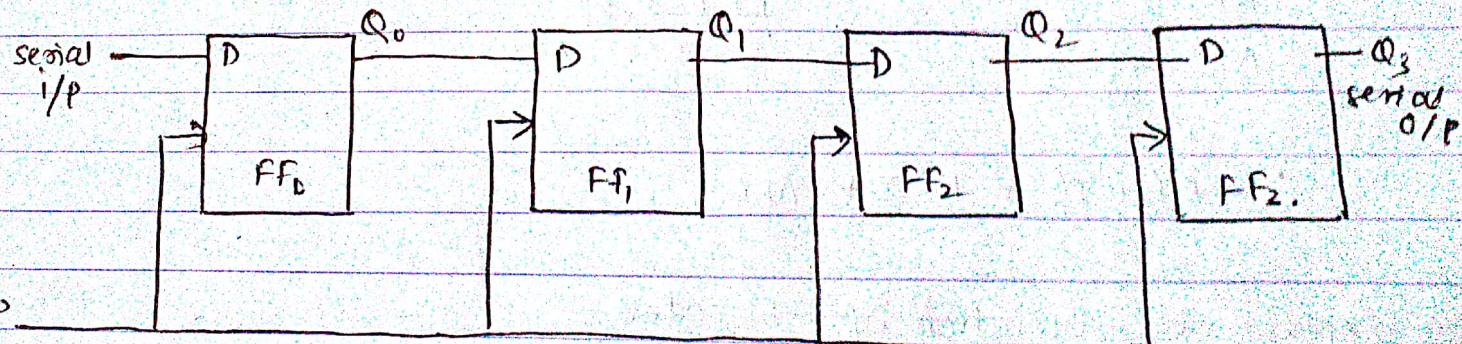
Demultiplexer:-

- i) one input and many outputs
- ii) Data distributor
- iii) serial to parallel conversion
- iv) When we design demultiplexer, we need additional gates.
- v) Example: 1:8, 1:16, 1:32.

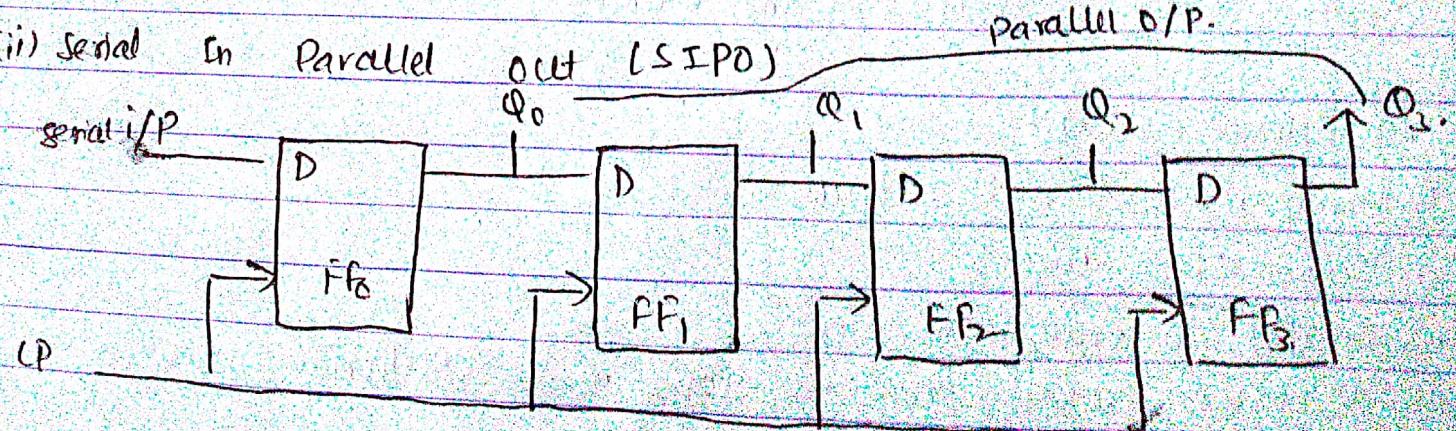
12. What are the various types of shift registers:

→ There are four types of shift registers. They are:

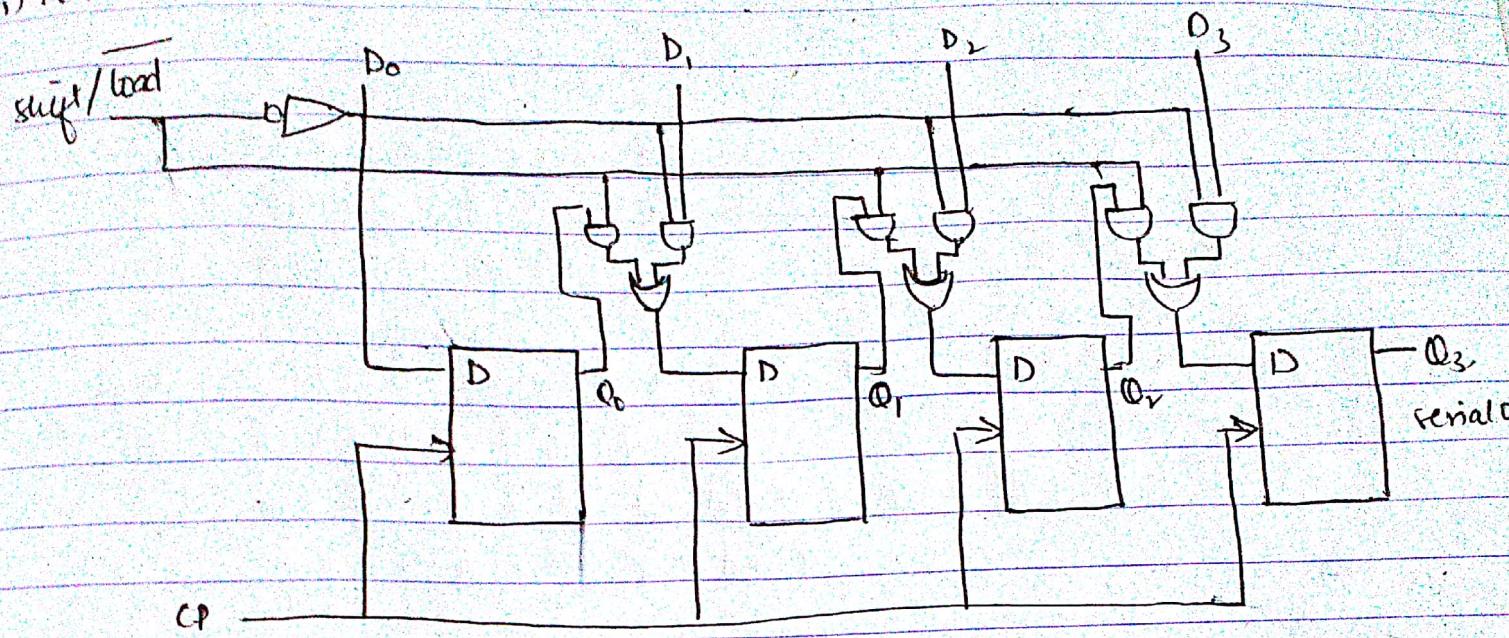
(i) Serial In Serial Out (SISO)



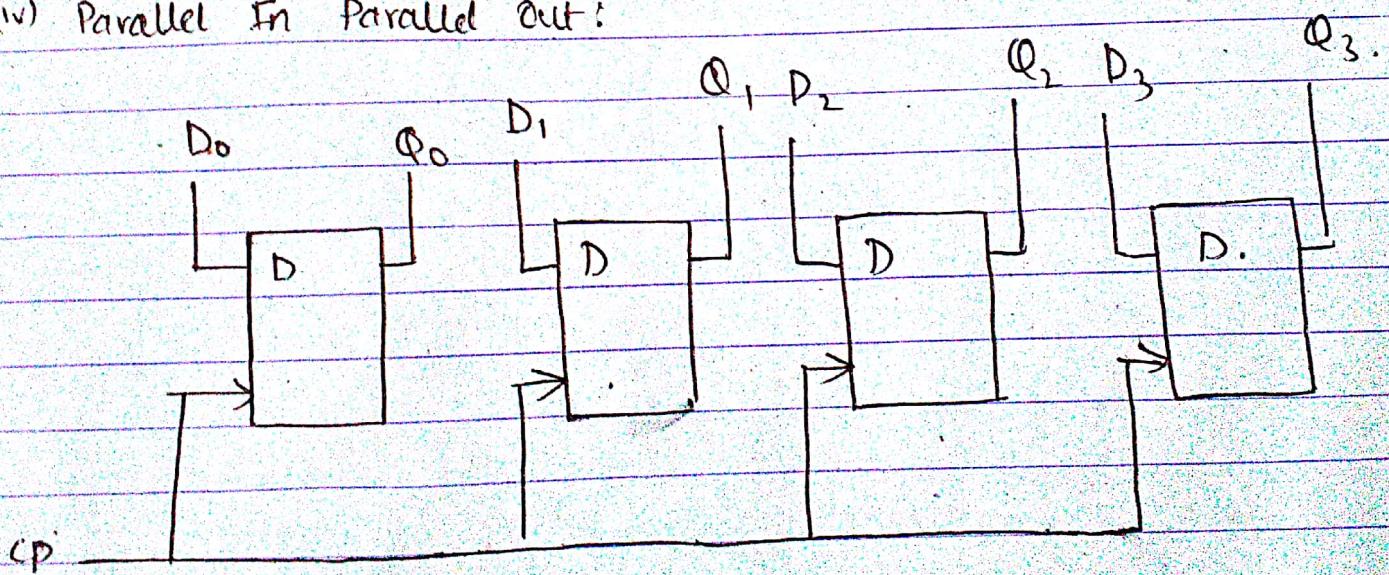
(ii) Serial In Parallel Out (SIPO)



(iii) Parallel In serial Out



(iv) Parallel In Parallel Out:



- Gaurav Chauhan  
- Digital Logic

2070

1. Explain magnitude comparator and also design a logic diagram for a 4-bit magnitude comparator.

→

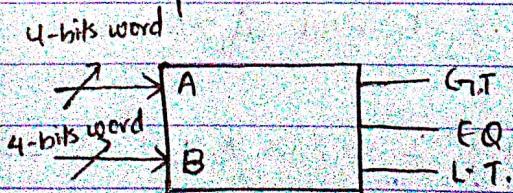
A Magnitude comparator is a digital comparator which has three output terminals, one for each : equality;  $A=B$ , greater than;  $A>B$ , and less than  $A<B$ .

The purpose of digital comparator is to compare a set of variables are unknown numbers. for example ; a magnitude comparator of two 1-bits, (A and B) inputs would produce the following three output conditions compared to each other.

$$A>B, A=B, A<B.$$

This is useful if we want to compare two variables and want to produce an output when any of the above three conditions are achieved.

4-bit magnitude comparator:



Since,  $A = 4$  bits

$B = 4$  bits

let,  $A = A_3 \ A_2 \ A_1 \ A_0$

$B = B_3 \ B_2 \ B_1 \ B_0$

Firstly, we try to verify equality comparison.

for that,

let us suppose,  $X_i = A_i \oplus B_i = A_i B_i + A_i' B_i'$

∴

In order to verify equality comparison,  
 $x_3$  should be equal to 1 i.e.  $x_3 = 1$ .  
 But,  $x_i = 1$  if and only if  $A_i = B_i$  for all  $i = 0, 1, 2, 3$ . Therefore, the condition for  $A = B$  or Equality ( $EQ = 1$ ) if and only if:

- $A_3 = B_3 \Rightarrow (x_3 = 1)$ , and
- $A_2 = B_2 \Rightarrow (x_2 = 1)$ , and
- $A_1 = B_1 \Rightarrow (x_1 = 1)$ , and
- $A_0 = B_0 \Rightarrow (x_0 = 1)$

Then the boolean expression for equality to be equal to '1' will be  
 $EQ = x_3 x_2 x_1 x_0$  — (ii)

Then, we try to verify greater than comparison,  
 $GT$  (Greater than) = 1 if  $A > B$ .

So, the condition for  $A > B$  or  $GT = 1$  if and only if:

$$\rightarrow A_3 > B_3 \Rightarrow A_3 = 1 \text{ and } B_3 = 0 ; \text{ or}$$

$$\rightarrow A_3 = B_3 \text{ and } A_2 > B_2 \text{ or}$$

$$\rightarrow A_3 = B_3 \text{ and } A_2 = B_2 \text{ and } A_1 > B_1 \text{ , or}$$

$$\rightarrow A_3 = B_3 \text{ and } A_2 = B_2 \text{ and } A_1 = B_1 \text{ and } A_0 > B_0$$

Therefore,

$$GT = A_3 B_3' + x_3 A_2 B_2' + x_3 x_2 A_1 B_1' + x_3 x_2 x_1 A_0 B_0' — (ii)$$

$x_3$  is written when  $A_3 = B_3$  as derived in equality similarly  $x_2$  and  $x_1$  are written.

for less than comparison,

$$LT = A_3' B_3 + x_3 A_2' B_2 + x_3 x_2 A_1' B_1 + x_3 x_2 x_1 A_0' B_0 — (iii)$$

Circuit Diagram:

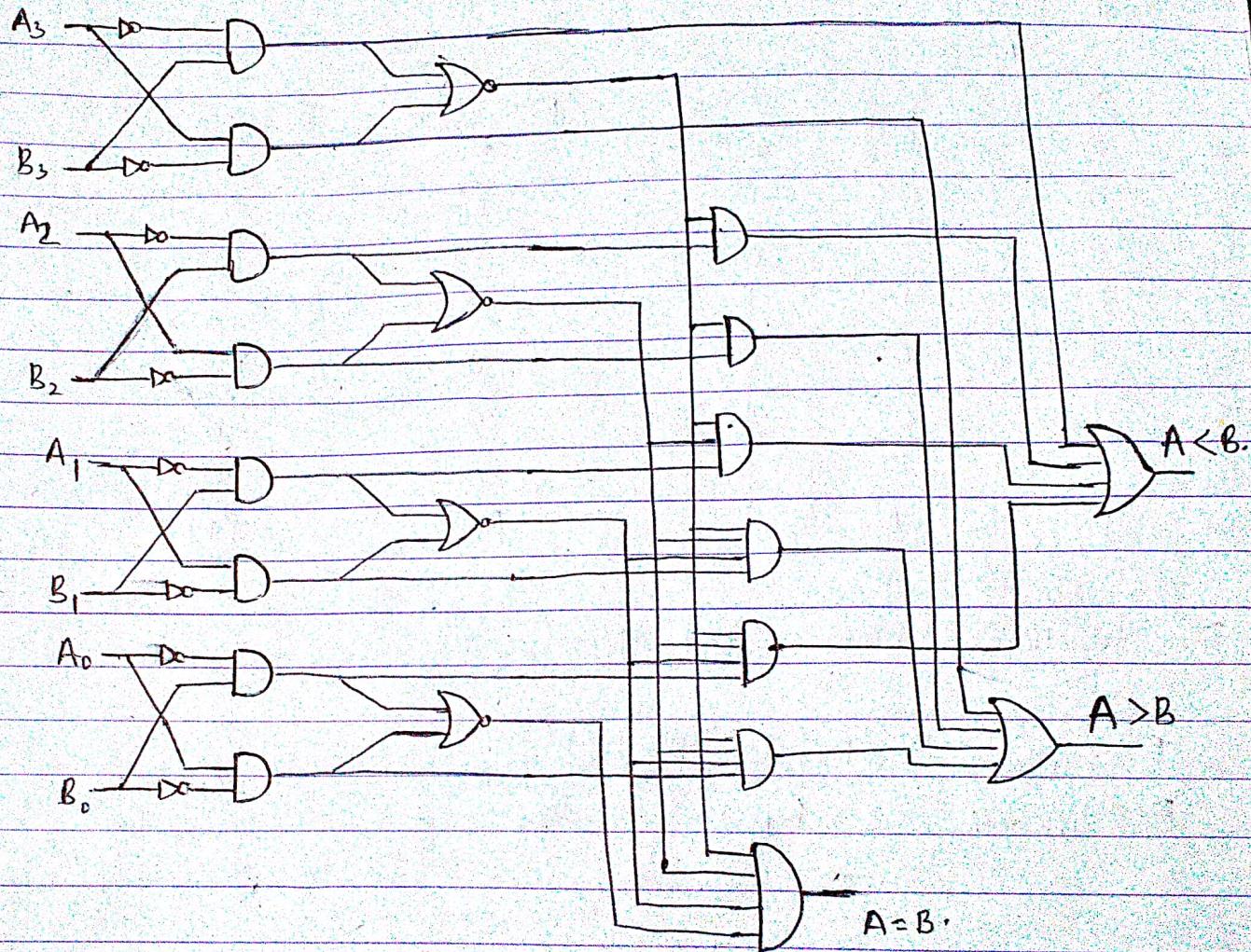


fig. 4-bit Magnitude comparator.

3. Explain full subtractor using decoder.

→ It is a combinational circuit that performs a subtraction bet" two bits taking into account that 1 may have been borrowed by a lower significant stage. The circuit has three inputs and

two outputs. The 1's and 0's for output variables are determined from subtraction of  $(x-y) - z$ .

Truth Table:

	Inputs			output		
	X	Y	Z	F-S bumen	FS difference.	
D <sub>0</sub>	0	0	0	1	1	0
D <sub>1</sub>	0	0	1	1	1	1
D <sub>2</sub>	0	1	0	1	0	0
D <sub>3</sub>	0	1	1	0	1	1
D <sub>4</sub>	1	0	0	0	0	0
D <sub>5</sub>	1	0	1	0	0	0
D <sub>6</sub>	1	1	0	0	0	0
D <sub>7</sub>	1	1	1	1	1	1

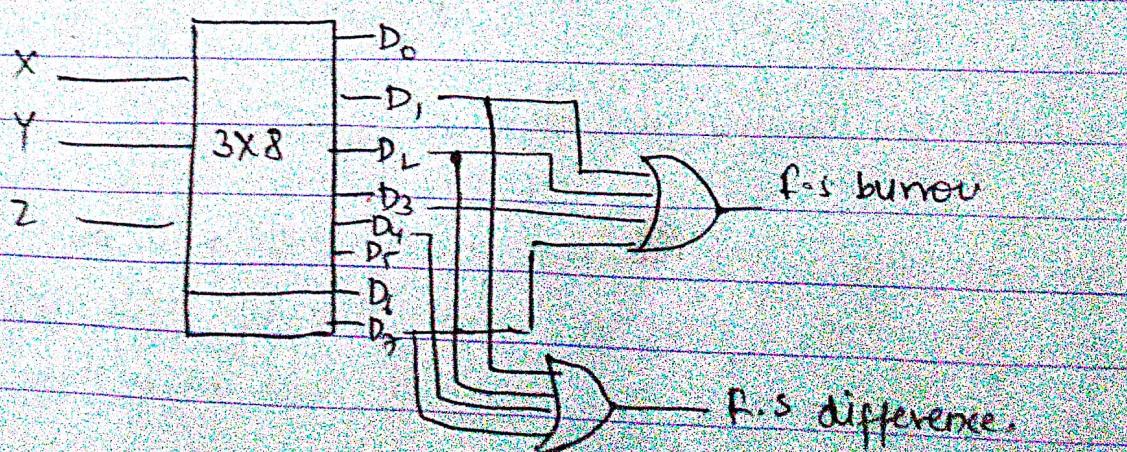
boolean of

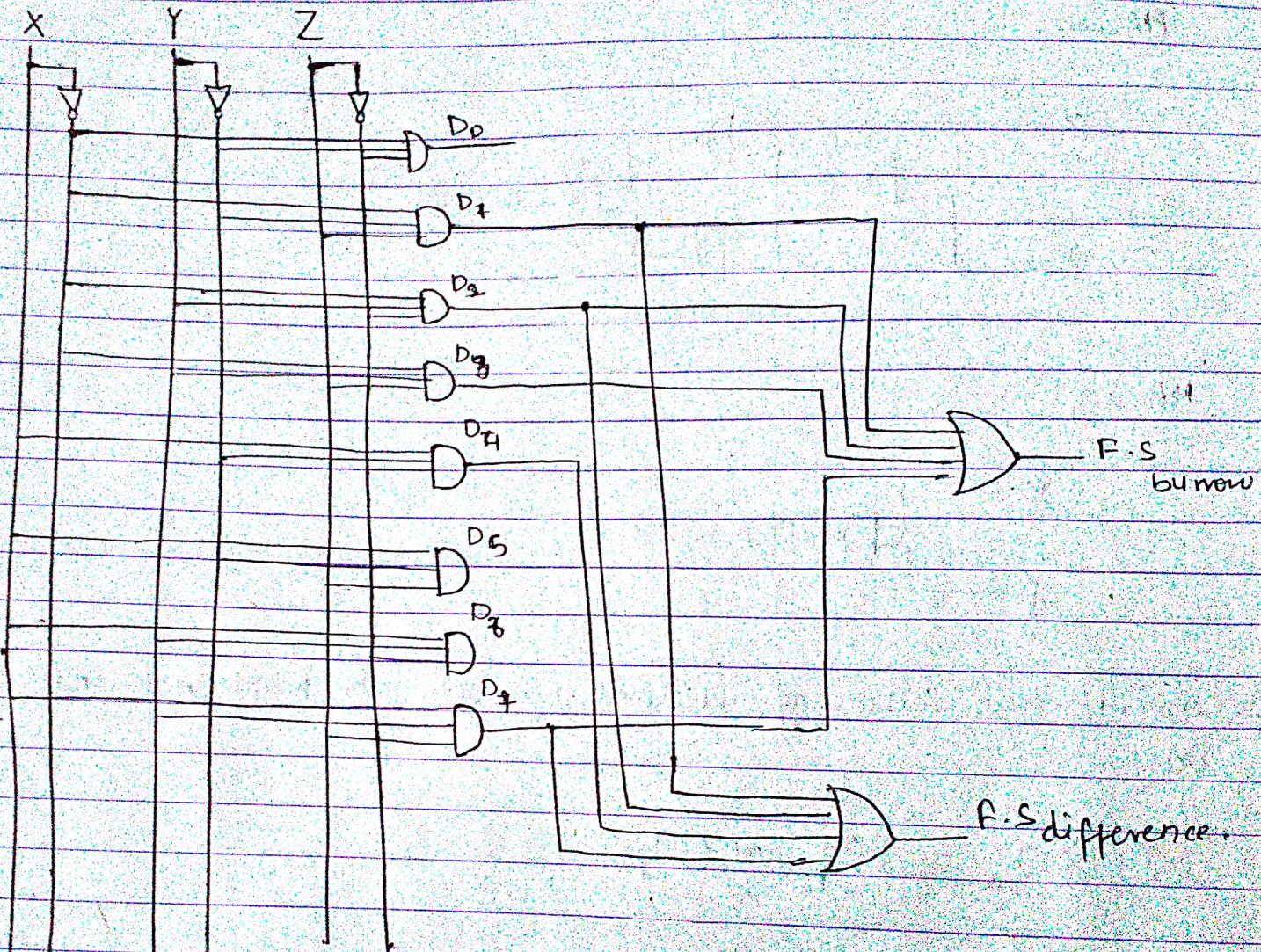
The function : bumen : and difference is:

$$F.S \text{ bumen} = \sum(D_1, D_2, D_3, D_7)$$

$$F.S \text{ difference} = \sum(D_1, D_2, D_4, D_7)$$

Since, there are three inputs and 8 outputs, we can implement 3x8 decoders.





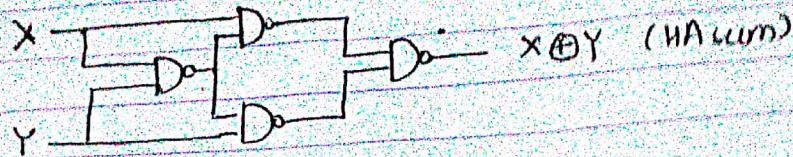
4. Design Half adder logic only using NAND gates.

We have,

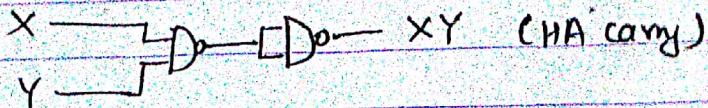
$$HA_{\text{sum}} = xy' + \bar{x}y = x \oplus y$$

$$HA_{\text{carry}} = xy$$

HA sum:



HA carry:



5. Convert the following decimal numbers into hexadecimal and octal.

(a) 334.

$$(i) (334)_{10} \rightarrow (?)_{16}.$$

$$\begin{array}{r} 16 \boxed{334} \rightarrow 14 \\ 16 \boxed{20} \rightarrow 4 \\ \quad \quad \quad \boxed{1} \rightarrow 1 \end{array}$$

$$\therefore (334)_{10} \Rightarrow (14E)_{16}$$

$$(ii) (334)_{10} \rightarrow (?)_8$$

$$\begin{array}{r} 8 \boxed{334} \rightarrow 6 \\ 8 \boxed{41} \rightarrow 1 \\ \quad \quad \quad \boxed{5} \rightarrow 5 \end{array}$$

$$\therefore (334)_{10} \Rightarrow (516)_8$$

b) 225

(i)  $(225)_{10} \rightarrow (?)_{16}$

$$\begin{array}{r} 16 \mid 225 \rightarrow 1 \\ 14 \rightarrow 14 \end{array}$$

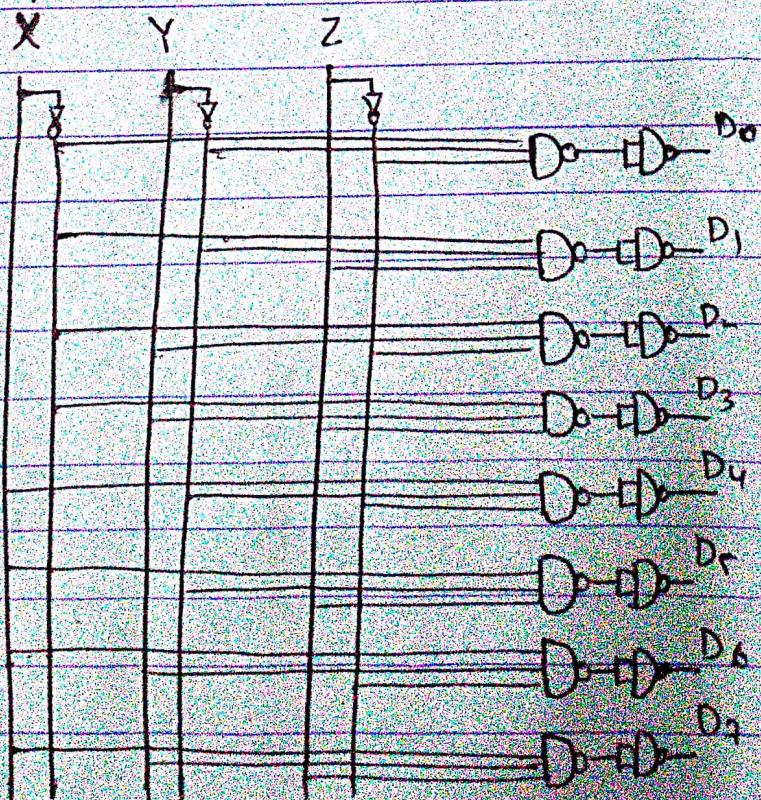
$$\therefore (225)_{10} \Rightarrow (E1)_{16}$$

(ii)  $(225)_{10} \rightarrow (?)_8$

$$\begin{array}{r} 8 \mid 225 \rightarrow 1 \\ 8 \mid 28 \rightarrow 4 \\ 3 \rightarrow 3 \end{array}$$

$$\therefore (225)_{10} \Rightarrow (341)_8$$

11. Explain and design decoder with universal gates.  
→ for 3x8 decoder,

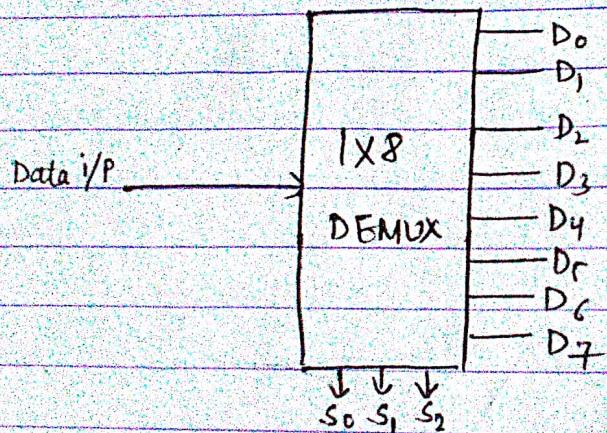


- Gaurav Chaulagain  
- Digital logic

2071.

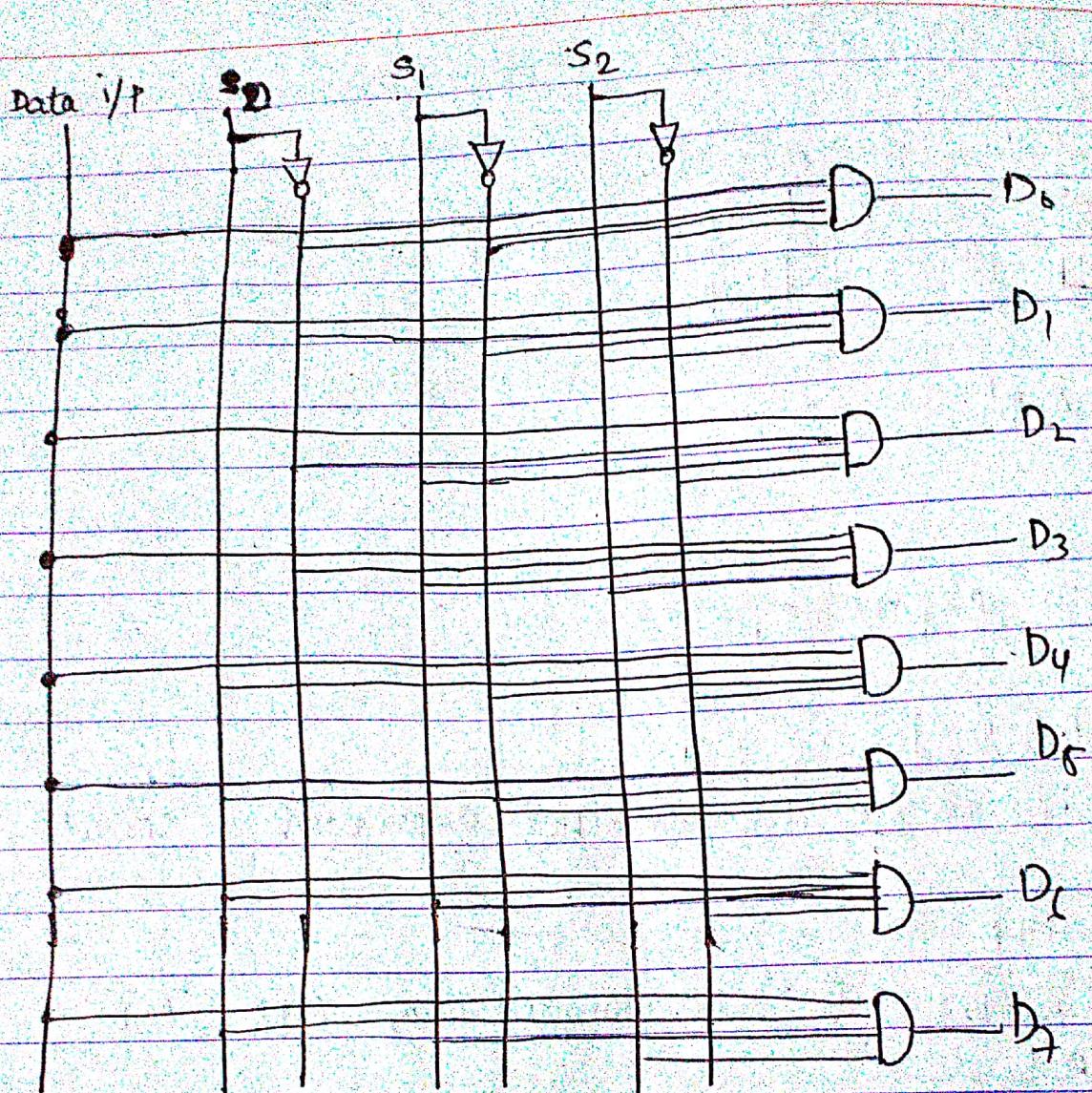
3. What is demultiplexer? Draw its block diagram and explain its working principle.

→ Demultiplexer is a data distributor which reverses the multiplexer function by taking digital information from 1 line & distributing it to a given number of output lines. It receives information on a single line and transmitted information are of  $2^n$  possible output lines. The selection of a specific output lines is controlled by the bit value of selection switches.



Truth table:

Data I/P	S <sub>0</sub> S <sub>1</sub> S <sub>2</sub>			Output	output							
	D <sub>0</sub>	D <sub>1</sub>	D <sub>2</sub>		D <sub>0</sub>	D <sub>1</sub>	D <sub>2</sub>	D <sub>3</sub>	D <sub>4</sub>	D <sub>5</sub>	D <sub>6</sub>	D <sub>7</sub>
D <sub>0</sub>	0	0	0	.	1	0	0	0	0	0	0	0
D <sub>1</sub>	0	0	1		0	1	0	0	0	0	0	0
D <sub>2</sub>	0	1	0		0	0	1	0	0	0	0	0
D <sub>3</sub>	0	1	1		0	0	0	1	0	0	0	0
D <sub>4</sub>	1	0	0		0	0	0	0	1	0	0	0
D <sub>5</sub>	1	0	1		0	0	0	0	0	1	0	0
D <sub>6</sub>	1	1	0		0	0	0	0	0	0	1	0
D <sub>7</sub>	1	1	1		0	0	0	0	0	0	0	1



simplify the boolean function using 3-variable K-Map.

$$(a) f(x, y, z) = \Sigma(0, 3, 2, 5)$$

	$x'z'$	$y'z'$	$y'z$	$yz'$	$yz$
$x'$	1	.	1	1	.
$x$	.	1	.	.	.

$$f = x'y'z' + y + xy'z$$

$$(b) F(A, B, C) = \sum(0, 2, 4, 5, 6)$$

	$BC$	$B'C'$	$B'C$	$BC'$	$B'C'$
$A'$	1	1	1	1	1
$A$	1	1	0	0	1

$$F = C' + AB'$$

7. Simplify the boolean expression:

$$Y = \overline{A \cdot B} + \overline{A} + \overline{B}$$

Prepare truth table to check that simplified expression is correct or not.

$$\rightarrow Y = \overline{A \cdot B} + \overline{A} + \overline{B}$$

$$= \overline{A \cdot B} + (\overline{A} \cdot \overline{B}) \quad [ \because \text{De Morgan's law, } \overline{A+B} = \overline{A} \cdot \overline{B}. ]$$

$$= \overline{A \cdot B} + A \cdot B$$

$$= 1 \quad [ \because A + A' = 1 ]$$

$$A + A' = 0.$$

Truth table.

A	B	$\overline{A}$	$\overline{B}$	$A \cdot B$	$\overline{A \cdot B}$	$\overline{A} + \overline{B}$	$\overline{\overline{A} + \overline{B}}$	$\overline{A \cdot B} + \overline{A} + \overline{B}$
0	0	1	1	0	1	1	0	1
0	1	1	0	0	1	1	0	1
1	0	0	1	0	1	1	0	1
1	1	0	0	1	0	0	1	1.

Hence, verified

Q. Explain the PLA (Programmable Logic Array).

A combinational circuit may have Don't care conditions and when implemented with a ROM, a Don't care condition becomes an address input that will never occur. The words at the don't care address need not be programmed and maybe left in the original state. The result is that, not all the bit patterns available in the ROM are used, which maybe considered a waste of available equipments. Thus, for cases where no. of Don't care conditions are excessive it is more economical to use a component called programmable logic array (PLA).

A PLA is similar to ROM in concept. However, the PLA does not provide full decoding of the variables and does not generate all the minterms as in the ROM. In PLA, the decoder is replaced by a group of AND gates, each of which can be programmed to generate a product term of the input variable.

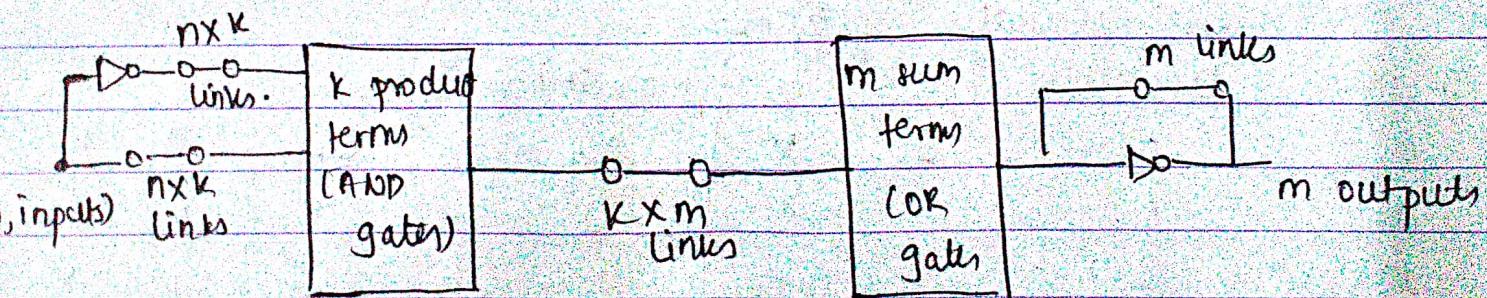


fig. PLA block diagram.

Q. How JK flip flop can be converted into a D flip flop? Explain.

- steps:
1. Identify available and required flip flop.
  2. Make characteristic table for required flip flop.
  3. Make excitation table for available flip flop.
  4. Write boolean expression for available ff.
  5. Draw the circuit.

Here,

available flip flop = JK flip flop  
 required flip flop = D flip flop

Characteristic Table for D flip flop:

$Q(t)$	D	$Q(t+1)$
0	0	0
0	1	1
1	0	0
1	1	1

Excitation table for available flip flop:

Now we have, $Q(t)$	$Q(t+1)$	J	K
0	0	0	X
0	1	1	X
1	0	X	1
1	1	X	0

Excitation table:

$Q_n$	D	$Q_{n+1}$	J	K
0	0	0	0	X
0	1	1	1	X
1	0	0	X	1
1	1	1	1	X

Boolean expression:

for J,

$Q_t$	D	$D'$	D
$Q'_t$	0	1	
$Q_t$	X	X	

$$J = D$$

for K,

$Q_t$	D	$D'$	$D''$
$Q'_t$	X	X	
$Q_t$	1	0	

$$K = D'$$

Circuit:

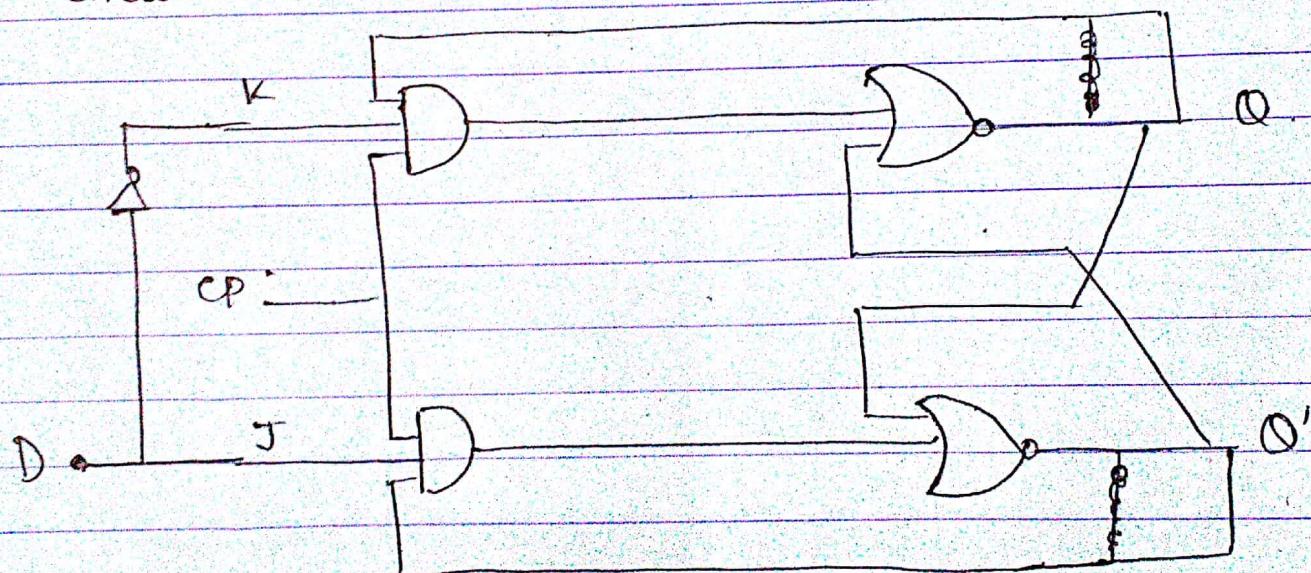


Fig. D-flipflop using J-K flipflop.