Exercise Sheet 1

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1 Exercise 1: What is SLAM

1.1 Why would a SLAM system need a map?

- can inform path planning

- provides intuitive visualization for humans

1.2 How can we apply SLAM technology into real-world applications?

- we need SLAM in applications where a prior map is not available but the robot needs to be aware of its surroundings and relative position

- SLAM is useful for military applications, agriculture, autonmous driving, cleaning/service robots

- to apply SLAM you need a set of sensors (LIDAR, depth, RGB, DVS, etc.) which are the processed by the system's fron-end. This front-end interprets the sensor information (fusion, segmentation, filtering, feature tracking, etc.). It is also responsible for loop closure. The processed sensory data is then sent to the back-end part of the system that usually performs MAP estimation resulting in a SLAM estimate.

1.3 Describe the history of SLAM

1.3.1 The classical age (1984-2004)

- introduction of probabilistic SLAM formulations: MAP, Extended Kalman Filter, Rao-Blackwellised Particle Filters

- decoupling of main challenges: efficiency and robust data association

1.3.2 Algorithmic analysis age (2004-2015)

- study of SLAM fundamentals: observability, convergence, and consistency

- development of main open source libraries for SLAM (Ceres, GTSAM, g2o, iSAM, SLAM++)

- using sparsity to create efficient SLAM solvers

1.3.3 Robust perception age (2015-present)

- SLAM "solved" for specific conditions (e.g. using LIDAR to map an indoor 2D non-dynamic environment with a slow-moving robot)

- actively researched/unsolved problems:

  - robust performance (in the face of outliers, changing maps, non-rigid world, degredation of sensors)
  - high-level understanding (semantic maps, dynamic vs static parts)
  - resource awareness (dealing with influx in CPU stress, taking advantage of idle processor)
  - task-driven perception (filter non-relevant perceptual information, produce adaptive map representations)

2   Exercise 2: git, cmake, gcc, merge-requests

- Prepends the path where cmake will look for modules with the **include** and **find_package** commands with the current dir (.) and the subdirectory **cmake_modules**

- CMAKE_CXX_STANDARD

  - sets the optional property for the build to use the appropriate compiler and linker flags for the C++11 standard to use the appropriate flags for C++ 11. If a newer compiler/linker is available it will be used (i.e. 14 or 17). If only older versions are available, it will fallback to those.
  - Disables the decay to older C++ standards. If C++11 or newer is not available, compilation will fail.

– Forces the build to use standard C++11 dialect and not an extended variant of this (such as gnu++11). Having the property set to ON (default) may result in cross-platform build bugs

- CMAKE_ CXX_ FLAGS Sets global flags and specific flags for specific build targets (specified through e.g. `cmake -DCMAKE_TYPE=DEBUG ..`)

  – O0: compiles without optimization

  – O3: compiles with full optimization

  – g: compiles with GDB debugging enabled

  – EIGEN_INITIALIZE_MATRICES_BY_NAN: initializes matrices with NaN values, makes it easier to find uninitialized matrices when debugging

  – NDEBUG: disables assert statements in code

  – ftemplate-backtrace-limit=0: disables the limit of instantiation notes for a single error (default is 10)

  – Wall: enables all warnings during build time

  – EXTRA_WARNING_FLAGS: set of flags defined previously to account for different compilers (gcc and clang) e.g.: Wsign-compare (warning generated when signed and unsigned values are compared), Wno-exceptions (disables clang enabled exception warnings)

  – march: is set to native so that compiler generates instructions for the build system's CPU

3 Exercise 3: SO(3) and SE(3) Lie groups

Theorem:

Show that

$$exp(\xi^\wedge) = \begin{pmatrix} \sum_{n=0}^{\infty} \frac{1}{n!}(\phi^\wedge)^n & \sum_{n=0}^{\infty} \frac{1}{(n+1)!}(\phi^\wedge)^n \rho \\ 0^T & 1 \end{pmatrix}$$

where

$$\xi^\wedge = \begin{pmatrix} \phi^\wedge & \rho \\ 0^T & 0 \end{pmatrix}$$

is a 4x4 matrix.

Proof:

$$exp(\xi^\wedge) = \sum_{n=0}^{\infty} \frac{1}{n!}(\xi^\wedge)^n$$

$$= \sum_{n=0}^{\infty} \frac{1}{n!} \begin{pmatrix} \phi^\wedge & \rho \\ 0^T & 0 \end{pmatrix}^n$$

$$= I_{(4,4)} + \begin{pmatrix} \phi^\wedge & \rho \\ 0^T & 0 \end{pmatrix}$$

$$+ \frac{1}{2} \begin{pmatrix} \phi^\wedge & \rho \\ 0^T & 0 \end{pmatrix} \begin{pmatrix} \phi^\wedge & \rho \\ 0^T & 0 \end{pmatrix}$$

$$+ \frac{1}{6} \begin{pmatrix} \phi^\wedge & \rho \\ 0^T & 0 \end{pmatrix} \begin{pmatrix} \phi^\wedge & \rho \\ 0^T & 0 \end{pmatrix} \begin{pmatrix} \phi^\wedge & \rho \\ 0^T & 0 \end{pmatrix}$$

$$+ ...$$

$$= I_{(4,4)} + \begin{pmatrix} \phi^\wedge & \rho \\ 0^T & 0 \end{pmatrix}$$

$$+ \frac{1}{2} \begin{pmatrix} (\phi^\wedge)^2 & \phi^\wedge \rho \\ 0^T & 0 \end{pmatrix}$$

$$+ \frac{1}{6} \begin{pmatrix} (\phi^\wedge)^3 & (\phi^\wedge)^2 \rho \\ 0^T & 0 \end{pmatrix}$$

$$+ ...$$

$$= I_{(4,4)} + \sum_{n=1}^{\infty} \frac{1}{n!} \begin{pmatrix} (\phi^\wedge)^n & (\phi^\wedge)^{(n-1)} \rho \\ 0^T & 0 \end{pmatrix}$$

$$= I_{(4,4)} + \begin{pmatrix} \sum_{n=1}^{\infty} \frac{1}{n!}(\phi^\wedge)^n & \sum_{n=1}^{\infty} \frac{1}{n!}(\phi^\wedge)^{(n-1)} \rho \\ 0^T & 0 \end{pmatrix}$$

$$= \begin{pmatrix} I_{(3,3)} + \sum_{n=1}^{\infty} \frac{1}{n!}(\phi^\wedge)^n & \sum_{n=1}^{\infty} \frac{1}{n!}(\phi^\wedge)^{(n-1)} \rho \\ 0^T & 1 \end{pmatrix}$$

$$= \begin{pmatrix} \sum_{n=0}^{\infty} \frac{1}{n!}(\phi^\wedge)^n & \sum_{n=0}^{\infty} \frac{1}{(n+1)!}(\phi^\wedge)^n \rho \\ 0^T & 1 \end{pmatrix}$$

q.e.d.