# Momentum Library

Minified

Competitive Programming Library

Of

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# Data Structures

# **Sparse Table**

```
int n, a[N], ST[LOG_N][N], LOG[N];
void buildST() {
    LOG[0] = -1;
    for (int i = 0; i < n; ++i) {
        ST[0][i] = i;
        LOG[i + 1] = LOG[i] + !(i & (i + 1));
    }
    for (int j = 1; (1 << j) <= n; ++j) {
        for (int i = 0; (i + (1 << j)) <= n; ++i) {
            int x = ST[j - 1][i];
            int y = ST[j - 1][i + (1 << (j - 1))];
            ST[j][i] = (a[x] <= a[y] ? x : y);
        }
    }
}
int query(int 1, int r) {
    int g = LOG[r - l + 1];
    int x = ST[g][1];
    int y = ST[g][r - (1 << g) + 1];
    return (a[x] \leftarrow a[y] ? x : y);
}
```

## **Monotonic Queue**

```
template<class T>
class monotonic_queue {
    queue<T> qu;
    deque<T> mx;
public:
    void push(T v) {
        qu.push(v);
        while (mx.size() && mx.back() < v) mx.pop_back();</pre>
        mx.push_back(v);
    }
    void pop() {
        if (mx.front() == qu.front()) mx.pop_front();
        qu.pop();
    }
    T front() {
        return qu.front();
    }
    T max() {
        return mx.front();
    }
    T size() {
        return qu.size();
    }
};
```

# **Disjoint-Sets Union (DSU)**

```
int setsCount;
int par[N], siz[N];
void init(int n) {
       setsCount = n;
       for (int i = 0; i < n; ++i) {
               par[i] = i;
               siz[i] = 1;
       }
}
int findSet(int u) {
       return u == par[u] ? u : par[u] = findSet(par[u]);
}
bool sameSet(int u, int v) {
       return findSet(u) == findSet(v);
}
bool unionSets(int u, int v) {
       u = findSet(u);
       v = findSet(v);
       if (u == v) {
               return false;
       }
       setsCount--;
       siz[v] += siz[u];
       par[u] = v;
       return true;
}
int getSetSize(int u) {
       return siz[findSet(u)];
}
```

#### **Fenwick Tree**

```
class fenwick tree {
    int BIT[N];
public:
    fenwick_tree() {
        memset(BIT, 0, sizeof(BIT));
    }
    void update(int idx, int val) {
        while (idx < N) {
            BIT[idx] += val;
            idx += idx \& -idx;
        }
    }
    int operator[](int idx) {
        int res = 0;
        while (idx > 0) {
            res += BIT[idx];
            idx -= idx & -idx;
        }
        return res;
    }
};
class range_fenwick_tree {
    fenwick_tree M, C;
public:
    void update(int 1, int r, int val) {
        M.update(1, val);
        M.update(r + 1, -val);
        C.update(l, -val * (l - 1));
        C.update(r + 1, val * r);
    }
    int operator[](int idx) {
        return idx * M[idx] + C[idx];
    }
};
```

## **Segment Tree as Multiset**

```
const int MAX_RANGE = 1e9;
struct node {
    int size;
    node *childL, *childR;
   node() {
        size = 0;
        childL = childR = this;
    }
    node(int s, node* l, node* r) {
        size = s;
        childL = 1;
        childR = r;
    }
    void update() {
        size = childL->size + childR->size;
    }
};
class segment_multiset {
    node *nil, *root;
public:
    segment_multiset() {
        root = nil = new node();
    }
    ~segment_multiset() {
        clear();
        delete nil;
    }
    void clear() {
        destroy(root);
        root = nil;
    }
    int size() {
        return root->size;
    }
    int count(int val) {
        node* cur = root;
        int l = - MAX_RANGE, r = MAX_RANGE;
        while (l < r) {
            int mid = 1 + (r - 1) / 2;
```

```
if (val <= mid) {</pre>
            cur = cur->childL;
            r = mid;
        } else {
            cur = cur->childR;
            l = mid + 1;
        }
    }
    return cur->size;
}
void insert(int val, int cnt = 1) {
    assert(cnt > 0);
    insert(root, val, cnt, -MAX_RANGE, MAX_RANGE);
}
int erase(int val, int cnt = 1) {
    assert(cnt > 0);
    return erase(root, val, cnt, -MAX RANGE, MAX RANGE);
}
// Returns integer from the multiset by its index (0-indexed).
int operator[](int idx) {
    if (idx < 0 \mid \mid idx >= root->size) {
        throw out_of_range("ERROR :: trying to access an out of range element");
    }
    node* cur = root;
    int 1 = -MAX_RANGE, r = MAX_RANGE;
    while (1 < r) {
        int mid = 1 + (r - 1) / 2;
        if (idx < cur->childL->size) {
            cur = cur->childL;
            r = mid;
        } else {
            idx -= cur->childL->size;
            cur = cur->childR;
            l = mid + 1;
        }
    }
    return r;
}
int lower_bound(int val) {
    int ret = 0;
    node* cur = root;
    int 1 = -MAX RANGE, r = MAX RANGE;
```

```
while (1 < val) {
            int mid = 1 + (r - 1) / 2;
            if (val <= mid) {</pre>
                cur = cur->childL;
                r = mid;
            } else {
                ret += cur->childL->size;
                cur = cur->childR;
                l = mid + 1;
            }
        }
        return ret;
    }
    int upper_bound(int val) {
        return lower_bound(val + 1);
    }
private:
    void insert(node*& root, int val, int cnt, int l, int r) {
        if (val < l || val > r) {
            return;
        }
        if (root == nil) {
            root = new node(0, nil, nil);
        }
        root->size += cnt;
        if (1 == r) {
            return;
        }
        int mid = 1 + (r - 1) / 2;
        insert(root->childL, val, cnt, 1, mid);
        insert(root->childR, val, cnt, mid + 1, r);
    }
    int erase(node*& root, int val, int cnt, int l, int r) {
        if (val < l || val > r) {
            return 0;
        }
        if (root == nil) {
            return 0;
        }
        if (1 == r) {
```

```
return remove(root, cnt);
    }
    int mid = 1 + (r - 1) / 2;
    int ret = 0;
    ret += erase(root->childL, val, cnt, 1, mid);
    ret += erase(root->childR, val, cnt, mid + 1, r);
    return remove(root, ret);
}
int remove(node*& root, int cnt) {
    int ret = min(cnt, root->size);
    root->size -= cnt;
    if (root->size <= 0) {</pre>
        destroy(root);
        root = nil;
    }
    return ret;
}
void destroy(node* root) {
    if (root == nil) {
        return;
    }
    destroy(root->childL);
    destroy(root->childR);
    delete root;
}
```

**};** 

# Strings

#### **KMP**

```
int F[N];
int failure(const char* pat, char c, int len) {
    while (len > 0 && c != pat[l]) {
        len = F[l - 1];
    }
    return len + (c == pat[l]);
}

void KMP(const char* str) {
    F[0] = 0;
    for (int i = 1; str[i]; ++i) {
        F[i] = failure(str, str[i], F[i - 1]);
    }
}
```

# **Z-Algorithm**

```
int z[N];

void z_function(const char* str) {
    for (int i = 1, l = 0, r = 0; str[i]; ++i) {
        if (i <= r)
            z[i] = min(r - i + 1, z[i - l]);

    while (str[i + z[i]] && str[z[i]] == str[i + z[i]])
        z[i]++;

    if (i + z[i] - 1 > r)
        l = i,
        r = i + z[i] - 1;
    }
}
```

#### Trie

```
const int N = 100100, ALPA = 255; // N: total length of all strings
int nodesCount;
int distinctWordsCount;
int trie[N][A];
int wordsCount[N];
                                    // Number of words sharing node "i"
                                    // Number of words ending at node "i"
int wordsEndCount[N];
void init() {
    nodesCount = 0;
    memset(trie, -1, sizeof(trie));
}
int addEdge(int id, char c) {
    int& nxt = trie[id][c];
    if (nxt == -1) {
        nxt = ++nodesCount;
    }
    return nxt;
}
void insert(const char* str) {
    int cur = 0;
    for (int i = 0; str[i]; ++i) {
        wordsCount[cur]++;
        cur = addEdge(cur, str[i]);
    }
    wordsCount[cur]++;
    distinctWordsCount += (++wordsEndCount[cur] == 1);
}
void erase(const char* str) {
    int cur = 0;
    for (int i = 0; str[i]; ++i) {
        int nxt = trie[cur][str[i]];
        if (wordsCount[cur]-- == 1) {
            trie[cur][str[i]] = -1;
        }
        cur = nxt;
    }
    wordsCount[cur]--;
    distinctWordsCount -= (--wordsEndCount[cur] == 0);
}
```

```
bool search(const char* str) {
    int cur = 0;

    for (int i = 0; str[i]; ++i) {
        int nxt = trie[cur][str[i]];

        if (nxt == -1) {
            return 0;
        }

        cur = nxt;
    }

    return wordsEndCount[cur];
}
```

### **Suffix Array (N.log(N))**

```
const int N = 1e5 + 5;
                the number of suffixes (length of the string + 1)
// n:
                the suffix array, holding all the suffixes in lexicographical order.
// SA:
// suffixRank:
                the order of the i-th suffix after sorting.
// LCP:
                the length of the longest common prefix between SA[i] and SA[i - 1].
int n, SA[N], suffixRank[N], LCP[N];
// Temporary arrays needed while computing the suffix array
int sortedSA[N], sortedRanks[N], rankStart[N];
struct comparator {
    int h;
    comparator(int h) : h(h) {}
    bool operator()(int i, int j) const {
        if (suffixRank[i] != suffixRank[j])
            return suffixRank[i] < suffixRank[j];</pre>
        return suffixRank[i + h] < suffixRank[j + h];</pre>
    }
};
void computeSuffixRanks(int h) {
    comparator comp(h);
    for (int i = 1; i < n; ++i) {
        int& r = sortedRanks[i] = sortedRanks[i - 1];
        if (comp(sortedSA[i - 1], sortedSA[i])) {
            rankStart[++r] = i;
        }
    }
    for (int i = 0; i < n; ++i) {
        SA[i] = sortedSA[i];
        suffixRank[SA[i]] = sortedRanks[i];
    }
}
```

```
void buildSuffixArray(const string& str) {
    n = str.size() + 1;
    for (int i = 0; i < n; ++i) {
        sortedSA[i] = i;
        suffixRank[i] = str[i];
    }
    sort(sortedSA, sortedSA + n, comparator(0));
    computeSuffixRanks(0);
    for (int h = 1; sortedRanks[n - 1] != n - 1; h <<= 1) {
        for (int i = 0; i < n; ++i) {
            int k = SA[i] - h;
            if (k >= 0) {
                sortedSA[rankStart[suffixRank[k]]++] = k;
            }
        }
        computeSuffixRanks(h);
    }
}
void buildLCP(const string& str) {
    int cnt = 0;
    for (int i = 0, k = 0; i < str.size(); ++i) {
        int j = SA[suffixRank[i] - 1];
        while (str[i + cnt] == str[j + cnt]) ++cnt;
        LCP[suffixRank[i]] = cnt;
        if (cnt > 0) --cnt;
    }
}
```

# Graphs

# **Topological Sort**

```
bool vis[N];
                       // Graph adjacency list
vector<int> edges[N];
vector<int> sortedNodes;
                            // List of topologically sorted nodes
void topoSortDFS(int u) {
    vis[u] = true;
    for (int v : edges[u]) {
        if (!vis[v]) {
            topoSortDFS(v);
        }
    }
    sortedNodes.push_back(u);
}
void topoSortBFS() {
    queue<int> q;
    vector<int> inDeg(n + 1, 0);
    for (int i = 1; i <= n; ++i) {
        for (int v : edges[i]) {
            ++inDeg[v];
        }
    }
    for (int i = 1; i <= n; ++i) {
        if (inDeg[i] == 0) {
            q.push(i);
        }
    }
    while (!q.empty()) {
        int u = q.front();
        q.pop();
        sortedNodes.push_back(u);
        for (int v : edges[u]) {
            if (--inDeg[v] == 0) {
                q.push(v);
            }
        }
    }
}
```

# **Bellman Ford**

```
vector<pair<int, int>> edges[N];
bool bellmanFord(int src) {
    memset(par, -1, sizeof(par));
    memset(dis, 0x3F, sizeof(dis));
    dis[src] = 0;
    bool updated = 1;
    for (int k = 0; k < n \&\& updated; ++k) {
        updated = 0;
        for (int u = 1; u <= n; ++u) {
            for (auto& e : edges[u]) {
                int v = e.first;
                int w = e.second;
                if (dis[v] > dis[u] + w) {
                    dis[v] = dis[u] + w;
                    par[v] = u;
                    updated = 1;
                }
            }
        }
    }
    return updated; // Whether a negative cycle exist or not
}
```

#### **Floyd Warshal**

```
// Note that:
// -----
// adj[u][u] = 0
// adj[u][v] = cost(u, v) when direct edge exists from u to v with cost (u, v)
// adj[u][v] = INF otherwise
// -----
// par[u][v] = u
int n, adj[N][N], par[N][N];
void init() {
   for (int i = 0; i < n; ++i)
       for (int j = 0; j < n; ++j)
           adj[i][j] = (i == j ? 0 : 1e9),
           par[i][j] = i;
}
void floyd() {
   for (int k = 0; k < n; ++k)
       for (int i = 0; i < n; ++i)
           for (int j = 0; j < n; ++j)
               if (adj[i][j] > adj[i][k] + adj[k][j])
                  adj[i][j] = adj[i][k] + adj[k][j],
                  par[i][j] = par[k][j];
}
bool checkNegativeCycle() {
   bool ret = false;
   for (int i = 0; i < n; ++i) {
       ret = ret || (adj[i][i] < 0);
   return ret;
}
```

# **BFS on Complement Graph**

```
void bfs(int u) {
    queue<int> q;
    q.push(u);
    memset(dis, -1, sizeof(dis));
    dis[u] = 0;
    int id = 0;
    list<int> 11, 12;
    memset(vis, 0, sizeof(vis));
    for (int i = 1; i <= n; ++i) {
        if (i != u) {
            11.push_back(i);
        }
    }
    while (!q.empty()) {
        u = q.front();
        q.pop();
        id++;
        for (int v : edges[u]) {
            if (dis[v] == -1) {
                vis[v] = id;
            }
        }
        for (int v : l1) {
            if (vis[v] == id) {
                12.push_back(v);
                continue;
            }
            dis[v] = dis[s] + 1;
            q.push(v);
        }
        11.clear();
        11.swap(12);
    }
}
```

## Dijkstra

```
struct edge {
    int from, to, weight;
    edge() {}
    edge(int f, int t, int w) : from(f), to(t), weight(w) {}
    bool operator<(const edge& rhs) const {</pre>
        return weight > rhs.weight;
    }
};
void dijkstra(int src) {
    priority_queue<edge> q;
    q.push(edge(-1, src, 0));
    memset(par, -1, sizeof(par));
    memset(dis, 0x3F, sizeof(dis));
    while (!q.empty()) {
        int u = q.top().from;
        int v = q.top().to;
        int w = q.top().weight;
        q.pop();
        if (dis[v] <= w) {
            continue;
        }
        dis[v] = w;
        par[v] = u;
        for (edge& e : edges[v]) {
            if (w + e.weight < dis[e.to]) {</pre>
                q.push(edge(v, e.to, w + e.weight));
            }
        }
    }
}
```

#### Kosaraju's SCC Algorithm

```
int n, m;
                            // Number of nodes and edges
                            // Whether node u has been visited before or not
bool vis[N];
                            // Graph adjacency list
vector<int> edges[N];
                            // Transposed graph adjacency list (i.e. with reversed edges)
vector<int> edgesT[N];
vector<int> sortedNodes;
                            // List of topologically sorted nodes
vector<vector<int>> scc;
                            // Strongly connected components
void topoSortDFS(int u, vector<int>* edges, vector<int>& nodes) {
       vis[u] = 1;
       for (int v : edges[u]) {
               if (!vis[v]) {
                       topoSortDFS(v, edges, nodes);
               }
       }
       nodes.push_back(u);
}
void kosaraju() {
       memset(vis, 0, sizeof(vis));
       for (int i = 1; i <= n; ++i) {
               if (!vis[i]) {
                       topoSortDFS(i, edges, sortedNodes);
               }
       }
       memset(vis, 0, sizeof(vis));
       for (int i = sortedNodes.size() - 1; i >= 0; --i) {
               int u = sortedNodes[i];
               if (!vis[u]) {
                       scc.push_back(vector<int>());
                       topoSortDFS(u, edgesT, scc.back());
               }
       }
}
```

#### LCA (Eular walk + RMQ)

```
int n, m, u, v, dep[N];
int F[N], ST[LOG_N][N << 1], LOG[N << 1];</pre>
vector<int> E, edges[N];
void dfs(int u = 1, int p = 0, int d = 0) {
    dep[u] = d;
    F[u] = E.size();
    E.push_back(u);
    for (int v : edges[u]) {
        if (v != p) {
            dfs(v, u, d + 1);
            E.push back(u);
        }
    }
}
void buildRMQ() {
    int i, j, x, y;
    for (i = 0, LOG[0] = -1; i < E.size(); ++i) {
        ST[0][i] = i;
        LOG[i + 1] = LOG[i] + !(i & (i + 1));
    for (j = 1; (1 << j) <= E.size(); ++j) {
        for (i = 0; (i + (1 << j)) <= E.size(); ++i) {
            x = ST[j - 1][i];
            y = ST[j - 1][i + (1 << (j - 1))];
            ST[j][i] = (dep[E[x]] < dep[E[y]]) ? x : y;
        }
    }
}
int query(int 1, int r) {
    if (1 > r) swap(1, r);
    int g = LOG[r - l + 1];
    int x = ST[g][1];
    int y = ST[g][r - (1 << g) + 1];
    return (dep[E[x]] < dep[E[y]]) ? x : y;
}
int getLCA(int u, int v) {
    return E[query(F[u], F[v])];
}
int getDistance(int u, int v) {
    return dep[u] + dep[v] - 2 * dep[getLCA(u, v)];
}
```

#### **LCA (Parent Sparse Table)**

```
int n, m, u, v, dep[N];
int LOG[N], par[LOG_N][N];
                              // par[j][i] : the (2^j)-th ancestor of node number i.
vector<int> edges[N];
void dfs(int u = 1, int p = 0, int d = 0) {
    dep[u] = d;
    par[0][u] = p;
    for (int i = 1; (1 << i) <= d; ++i) {
        par[i][u] = par[i - 1][par[i - 1][u]];
    }
    for (int v : edges[u]) {
        if (v != p) {
            dfs(v, u, d + 1);
        }
    }
}
int getAncestor(int u, int k) {
    while (k > 0) {
        int x = k \& -k;
        k -= x;
        u = par[LOG[x]][u];
    }
    return u;
}
int getLCA(int u, int v) {
    if (dep[u] > dep[v]) {
        swap(u, v);
    }
    v = getAncestor(v, dep[v] - dep[u]);
    if (u == v) {
        return u;
    }
    for (int i = LOG[dep[u]]; i >= 0; --i) {
        if (par[i][u] != par[i][v]) {
            u = par[i][u];
            v = par[i][v];
        }
    }
    return par[0][u];
}
```

```
int getDistance(int u, int v) {
    return dep[u] + dep[v] - 2 * dep[getLCA(u, v)];
}

void computeLog() {
    LOG[0] = -1;
    for (int i = 1; i <= n; ++i) {
        LOG[i] = LOG[i - 1] + !(i & (i - 1));
    }
}</pre>
```

### Max Flow (Edmonds-Karp's Algorithm)

```
const int N = 105; // Max number of nodes
const int M = 105; // Max number of edges
                    // Number of nodes and number of edges
int n, m;
int edgeId;
                    // The next edge id to be inserted
int head[N];
                    // head[u]
                                : id of the last edge added from node u
                  // nxt[e] : next edge id pointed from the san
// to[e] : id of the node pointed by edge e
int nxt[M];
                                    : next edge id pointed from the same node as e
int to[M];
int capacity[M];
                    // capacity[e] : maximum capacity of edge e
int flow[M];
                    // flow[u]
                                 : current flow of edge e
int src, snk;
                    // id of source and sink nodes
int dist[N];
                    // dist[u]
                                   : shortest distance between the source and node u
                    // from[u]
int from[N];
                                     : id of the edge that leads to node u in the path
                                       from source to sink nodes
                    //
void init() {
    edgeId = 0;
    memset(head, -1, sizeof(head));
}
void addEdge(int f, int t, int c) {
    int e = edgeId++;
    to[e] = t;
    capacity[e] = c;
    flow[e] = 0;
    nxt[e] = head[f];
    head[f] = e;
}
void addAugEdge(int f, int t, int c) {
    addEdge(f, t, c);
    addEdge(t, f, 0);
}
bool findPath() {
    queue<int> q;
    q.push(src);
    memset(dist, -1, sizeof(dist));
    dist[src] = 0;
    while (!q.empty()) {
        int u = q.front();
        q.pop();
        for (int e = head[u]; \sim e; e = nxt[e]) {
                                             24
```

```
int v = to[e];
            int c = capacity[e];
            int f = flow[e];
            if (c <= f) {
                continue;
            }
            if (dist[v] == -1) {
                dist[v] = dist[u] + 1;
                from[v] = e;
                q.push(v);
            }
            if (v == snk) {
                return 1;
            }
        }
    }
    return 0;
}
int augmentPath() {
    int f = INT_MAX;
    for (int u = snk, e, r; u != src; u = to[r]) {
        e = from[u]; // x ---e--> u
        r = e ^ 1;
                       // x <--r-- u
        f = min(f, capacity[e] - flow[e]);
    }
    for (int u = snk, e, r; u != src; u = to[r]) {
        e = from[u]; // x ---e--> u
        r = e ^ 1;
                       // x <--r-- u
        flow[e] += f;
        flow[r] -= f;
                       // Reversed edge for flow cancelation
    }
    return f;
}
int maxFlow() {
    int f = 0;
    while (findPath()) {
        f += augmentPath();
    }
    return f;
}
```

# **Tree Diameter**

```
int bfs(int u) {
    queue<int> q;
    q.push(u);
   memset(dis, -1, sizeof(dis));
   dis[u] = 0;
   while (!q.empty()) {
        u = q.front();
        q.pop();
        for (auto v : edges[u]) {
            if (dis[v] == -1) {
                dis[v] = dis[u] + 1;
                q.push(v);
            }
        }
    }
    return u;
}
int calcTreeDiameter(int root) {
    int u = bfs(root);
    int v = bfs(u);
   return dis[v];
}
```

# **Bipartite Graph Check**

```
int color[N];
vector<int> edges[N];
bool dfs(int u = 0) {
    for (int v : edges[u]) {
        if (color[v] == -1) {
            color[v] = color[u] ^ 1;
            if (!dfs(v)) {
                return false;
            }
        }
        else if (color[v] == color[u]) {
            return false;
        }
    }
    return true;
}
bool isBipartiteGraph() {
    memset(color, -1, sizeof(color));
    color[1] = 0;
    return dfs();
}
```

#### **Bridge Tree**

```
// n:
                total number of vertices in the graph.
// T:
                counter represents time.
                node id in the built bridge tree after calling buildBridgeTree().
// root:
                the parent array of the DSU data structure.
// par[u]:
// tin[u]:
                visiting (discovery) time of node u.
// Low[u]:
                earliest visiting time of a vertex that node u is reachable from.
                list of out edges of node u in the graph.
// edges[u]:
// tree[u]:
                list of out edges of node u in the built bridge tree after calling
//
                buildBridgeTree().
                list contains all bridge edges of the graph after calling findBridges().
// bridges:
int n;
int T, root, par[N], tin[N], low[N];
vector<int> edges[N], tree[N];
vector<pair<int, int>> bridges;
int findSet(int u) {
    return (par[u] == u ? u : par[u] = findSet(par[u]));
}
void unionSets(int u, int v) {
    par[findSet(u)] = findSet(v);
}
void findBridges(int u = 1, int p = -1) {
    tin[u] = low[u] = ++T;
    for (auto v : edges[u]) {
        if (v == p) {
            continue;
        }
        if (tin[v] == 0) {
            findBridges(v, u);
            if (low[v] > tin[u]) {
                bridges.push_back({ u, v });
            } else {
                unionSets(u, v);
            }
        }
        low[u] = min(low[u], low[v]);
    }
}
```

```
void buildBridgeTree() {
    for (int i = 1; i <= n; ++i) {
        par[i] = i;
    }

    findBridges();

    for (auto& b : bridges) {
        int u = findSet(b.first);
        int v = findSet(b.second);

        tree[u].push_back(v);
        tree[v].push_back(u);

        root = u;
    }
}</pre>
```

# Math

```
int gcd (int a, int b) {
    return b == 0 ? a : gcd (b, a % b);
}
int lcm(int a, int b) {
    return a / gcd(a, b) * b;
}
pair<int, int> extendedEuclid(int a, int b) {
    if (b == 0) {
        return { 1, 0 };
    }
    pair<int, int> p = extendedEuclid(b, a % b);
    int s = p.first;
    int t = p.second;
    return { t, s - t * (a / b) };
}
int power(int base, int exp, int mod) {
    int ans = 1;
    base %= mod;
    while (exp > 0) {
        if (exp & 1) ans = (ans * base) % mod;
        exp >>= 1;
        base = (base * base) % mod;
    }
    return ans;
}
int modInverse(int a, int m) {
    return power(a, m - 2, m);
}
int nCr(int n, int r) {
    if (n < r)
        return 0;
    if (r == 0)
        return 1;
    return n * nCr(n - 1, r - 1) / r;
}
```

```
int comb[N][N];
void buildPT(int n) {
    for (int i = comb[0][0] = 1; i <= n; ++i)
        for (int j = comb[i][0] = 1; j <= i; ++j)
            comb[i][j] = (comb[i - 1][j] + comb[i - 1][j - 1]) % MOD;
}
bool isPrime(int n) {
    if (n < 2)
        return 0;
    if (n \% 2 == 0)
        return (n == 2);
    for (int i = 3; i * i <= n; i += 2)
        if (n \% i == 0)
            return 0;
    return 1;
}
bool prime[N];
void generatePrimes(int n) {
    memset(prime, true, sizeof(prime));
    prime[0] = prime[1] = false;
    for (int i = 2; i * i <= n; ++i) {
        if (!prime[i]) continue;
        for (int j = i * i; j <= n; j += i) {
            prime[j] = false;
        }
    }
}
vector<int> primeDivs[N];
void generatePrimeDivisors(int n) {
    for (int i = 2; i <= n; ++i) {
        if (primeDivs[i].size()) continue;
        for (int j = i; j <= n; j += i) {
            primeDivs[j].push_back(i);
        }
    }
}
```

```
vector<int> getDivisors(int n) {
    vector<int> divs;
    for (int i = 1; i * i <= n; ++i) {
        if (n % i == 0) {
            divs.push_back(i);
            if (i * i != n) {
                divs.push_back(n / i);
            }
        }
    }
    sort(divs.begin(), divs.end());
    return divs;
}
vector<int> divs[N];
void generateDivisors(int n) {
    for (int i = 1; i <= n; ++i)
        for (int j = i; j <= n; j += i)
            divs[j].push_back(i);
}
```

# Others

# **Longest Increasing Sub-sequence**

```
int n, a[N];
int getLIS() {
    if (n < 1) return 0;

    int len = 0;
    vector<int> LIS(n, INT_MAX);

    for (int i = 0; i < n; ++i) {
        // To get the Length of the Longest non decreasing subsequence
        // replace function "Lower_bound" with "upper_bound"
        int idx = lower_bound(LIS.begin(), LIS.end(), a[i]) - LIS.begin();
        LIS[idx] = a[i];
        len = max(len, idx);
    }

    return len + 1;
}</pre>
```