

S. No.		
1	CHAPTER NAME	Pg.No.
2	WAVE OPTICS	01-56
3	WAVES ON STRING	57-96
	SOUND WAVES	97-145

E PHYSICS



hapter	0	1)(
Cont	ent	IS_

WAVE OPTICS

01.	THEORY	03
02.	EXERCISE (S-1)	11
03.	EXERCISE (S-2)	14
04.	EXERCISE (O-1)	18
05.	EXERCISE (O-2)	33
06.	EXERCISE (JM)	37
07.	EXERCISE (JA)	44
08.	ANSWER KEY	54

Important Notes

	_
	_
	_
	_
	_
	_
	_

WAVE OPTICS

KEY CONCEPTS

WAVE THEORY OF LIGHT

This theory was enunciated by Hygen in a hypothetical medium known as luminiferrous ether.

Ether is that imaginary medium which prevails in all space, in isotropic, perfectly elastic and massless.

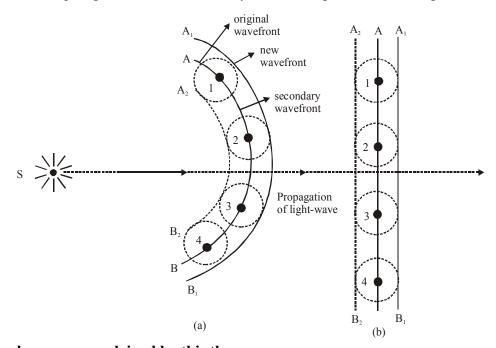
The different colours of light are due to different wave lengths of these waves.

The velocity of light in a medium is constant but changes with change of medium.

This theory is valid for all types of waves.

- (i) The locus of all ether particles vibrating in same phase is known as wavefront.
- (ii) Light travels in the medium in the form of wavefront.
- (iii) When light travels in a medium then the particles of medium start vibrating and consequently a disturbance is created in the medium.
- (iv) Every point on the wave front becomes the source of secondary wavelets. It emits secondary wavelets in all directions which travel with the speed of light (v),

The tangent plane to these secondary wavelets represents the new position of wave front.



The phenomena explained by this theory

- (i) Reflection, refraction, interference, diffraction, polarisation and double refraction.
- (ii) Rectilinear propagation of light.
- (iii) Velocity of light in rarer medium being grater than that in denser medium.

E

Phenomena not explained by this theory

- (i) Photoelectric effect, Compton effect and Raman effect.
- (ii) Backward propagation of light.

WAVE FRONT, VARIOUS TYPES OF WAVE FRONT AND RAYS

Wavefront

The locus of all the particles vibrating in the same phase is known as wavefront.

• Types of wavefront

The shape of wavefront depends upon the shape of the light source originating that wavefront. On the basis of there are three types of wavefront.

Comparative study of three types of wavefront

S.No.	Wavefront	Shape of light source	Diagram of shape of wavefront	Variation of amplitude with distance	Variation of intensity with distance
1.	Spherical	Point source		$A \propto \frac{1}{d}$ or $A \propto \frac{1}{r}$	$I \propto \frac{1}{r^2}$
2.	cylindrical	Linear or slit		$A \propto \frac{1}{\sqrt{d}}$ or $A \propto \frac{1}{\sqrt{r}}$	$I \propto \frac{1}{r}$
3.	Plane	Extended large source situated at very large distance		A = constant	I = constant

CHARACTERISTIC OF WAVEFRONT

- (a) The phase difference between various particles on the wavefront is zero.
- (b) These wavefronts travel with the speed of light in all directions in an isotropic medium.
- (c) A point source of light always gives rise to a spherical wavefront in an isotropic medium.
- (d) In an anisotropic medium it travels with different velocities in different directions.
- (e) Normal to the wavefront represents a ray of light.
- (f) It always travels in the forward direction of the medium.

RAY OF LIGHT

The path of the light energy from one point to another is known as a ray of light.

- (a) A line drawn at right angles to the wavefront is defined as a ray of light, which is shown by arrows in previous diagram of shape of wavefront.
- (b) It represents the direction of propagation of light.

1. INTERFERENCE OF LIGHT

When two light waves of same frequency with zero initial phase difference or constant phase difference superimpose over each other, then the resultant intensity in the region of superposition is different from the sum of intensity of individual waves.

This modification in intensity in the region of superposition is called interference.

(a) Constructive interference

When resultant intensity is greater than the sum of two individual wave intensities $[I > (I_1 + I_2)]$, then the interference is said to be constructive.

(b) Destructive interference

When the resultant intensity is less than the sum of two individual wave intensities $[I < (I_1 + I_2)]$, then the interference is said to destructive. There is no violation of the law of conservation of energy in interference. Here, the energy from the points of minimum energy is shifted to the points of maximum energy.

2. TYPES OF SOURCES

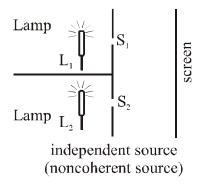
(a) Coherent sources

Two sources are said to be coherent if they emit light waves of the same wave length and start with same phase or have a constant phase difference.

Note: Laser is a source of monochromatic light waves of high degree of coherence.

(b) Incoherent sources

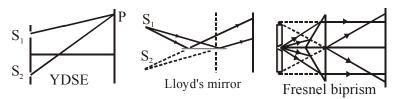
Two independent monochromatic sources, emit waves of same wavelength. But the waves are not in phase. So they are incoherent. This is because, atoms cannot emit light waves in same phase and these sources are said to be incoherent sources.



3. METHOD FOR OBTAINING COHERENT SOURCES

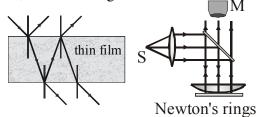
(a) Division of wavefront

In this method, the wavefront is divided into two or more parts by use of mirrors, lenses or prisms. **Example:** Young's double slit experiment. Fresnel's Biprism and Lloyd's single mirror method.



(b) Division of amplitude

The amplitude of incoming beam is divided into two or more parts by partial reflection or refraction. These divided parts travel different paths and are finally brought together to produce interference. Example: The brilliant colour seen in a thin film of transparent material like soap film, oil film, Michelson's Interferro Meter, Newtons' ring etc.



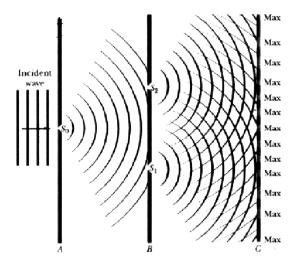
4. If two coherent waves with intensity I_1 and I_2 are superimposed with a phase difference of ϕ , the resulting wave intensity is

$$I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \phi$$

5. The phase difference between two waves at a point will depend upon

- (i) the difference in path lengths of two waves from their respective sources.(geometrical path difference)
- (ii) the refractive index of the medium (media)
- (iii) phase difference at source (if any).
- (iv) In case, the waves suffer reflection, the reflected wave differs in phase by π with respect to the incident wave if the incidence occurs in rarer medium. There would be no phase difference if incidence occurs in denser medium.

6. YOUNG'S DOUBLE SLIT EXPERIMENT



(i) If $d \ll D$

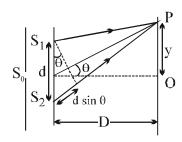
$$\Delta x = S_2 P - S_1 P = d \sin \theta$$

 $\Delta x = S_2 P - S_1 P = d \sin\theta$ If $\lambda \ll d$ then $\sin \theta \approx \theta \approx \tan \theta$ as when P is close to D so θ is small.

$$\Delta x = d\left(\frac{y}{D}\right) = \frac{yd}{D}$$

For maxima $\frac{yd}{D} = n\lambda$ (ii)

or
$$y = 0, \pm \frac{D\lambda}{d}, \pm \frac{2D\lambda}{d}$$

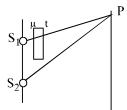


- For minima $\frac{yd}{D} = [n + (1/2)]\lambda$ or $y = \pm \frac{D\lambda}{2d}$, $\pm \frac{3D\lambda}{2d}$, $\pm \frac{5D\lambda}{2d}$, so on (iii)
- Fringe width = the distance between two successive maximas or minima $\beta = \frac{\lambda D}{J}$ (iv)
- (v) **Angular Fringe width**



7. DISPLACEMENT OF FRINGE PATTERN

When a film of thickness t and refractive index μ is introduced in the path of one of the source's of light, then fringe shift occurs as the optical path difference changes.



Optical path difference at P is

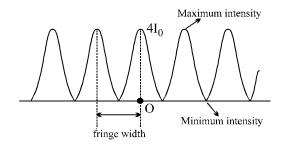
$$\Delta x = S_2 P - [S_1 P + \mu t - t] = S_2 P - S_1 P - (\mu - 1) t = y. (d/D) - (\mu - 1)t$$

 \Rightarrow The fringe shift is given by $\Delta y = \frac{D(\mu - 1)t}{d}$

INTENSITY VARIATION ON SCREEN 8.

If I₀ is the intensity of light beam coming from each slit, the resultant intensity at a point where they

 $I = 4I_0 \cos^2 \frac{\phi}{2}$, where $\phi = \frac{2\pi(d \sin \theta)}{\lambda}$ have a phase difference of $\boldsymbol{\varphi}$ is



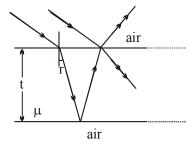
ALLEN

9. INTERFERENCE AT THIN FILM

optical path difference = $2\mu t \cos r$

= $2\mu t$ (in case of near normal incidence)

- (a) For interference in reflected light
 - (i) Condition of minima $2\mu t \cos r = n\lambda$
 - (ii) Condition of maxima $2\mu t \cos r = \left(n + \frac{1}{2}\right)\lambda$



- (b) For interference in transmitted light
 - (i) Condition of maxima $2\mu t \cos r = n\lambda$
 - (ii) Condition of minima $2\mu t \cos r = \left(n + \frac{1}{2}\right)\lambda$

Ampere Law:

The general form of Ampere's law (sometimes called the Ampere-Maxwell law) as

$$\oint \vec{B} \cdot d\vec{\ell} = \mu_0 \left(I + I_0 \right) = \mu_0 \left(I + \in_0 \frac{d\Phi_E}{dt} \right)$$

Hence, the displacement current through any surface is given by

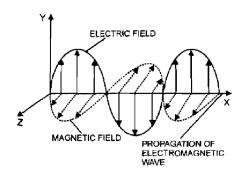
$$I_d = \in_0 \frac{d\Phi_E}{dt}$$

By considering surface S₂, we can identify the displacement current as the source of the magnetic field

ELECTROMAGNETIC WAVES:

In electromagnetic waves, both the field vectors (\vec{E} and \vec{B}) vary with time and space and have the same frequency and same phase. In figure, the electric field vector (\vec{E}) and magnetic field vector

 $\left(\vec{B}\right)$ are vibrating along Y and Z directions and propagation of electromagnetic wave is shown in X-direction.



According to Maxwell the electromagnetic waves are of transverse in nature and they can pass through vacuum with the speed of light (= $3 \times 10^8 \text{ ms}^{-1}$).

The velocity of eletromagnetic wave in a medium is given by

$$v = \frac{1}{\sqrt{\mu_0 \mu_r \in_0 \in_r}}$$

where, μ_0 , μ_r = absolute permeability of space and relative permeability of medium,

 \in_{0} , \in_{r} = absolute permittivity of space and relative permittivity of medium

The velocity of electromagnetic waves of different frequency in vacuum is same but in a medium is different. It is more for red light and less for violet light.

The energy is shared equally between electric field vector and magnetic field vector.

$$U_{av} = \frac{1}{2} \in_{0} E_{0}^{2} = \frac{1}{2} \frac{B_{0}^{2}}{\mu_{0}}$$

It has been found that the velocity (c) of electromagnetic wave in free space is equal to the ratio of amplitude of electric field vector (\mathbf{E}_0) and magnetic field vector (\mathbf{B}_0) i.e $\mathbf{c} = \mathbf{E}_0 / \mathbf{B}_0$.

It was found that the accelerated charge or oscillating charge is a source of electromagnetic waves.

If the plane of electric field is oriented horizontally in respect to the earth, the electromagnetic wave is said to be horizontally polarised. On the other hand, if the plane of electric field vector is oriented vertically the electromagnetic wave is said to be vertically polarised.

The polarisation of electromagnetic wave is mainly the function of the antenna orientation.

Light may be polarized by passing it through a sheet of commercial material called Polaroid

Malus' Law

Suppose we have a second piece of Polaroid whose transmission axis makes an angle θ with that of the first one.

If $I_0 \cong E^2$ is the intensity between the two Polaroids, the intensity transmitted by both of them would be: $I(\theta) = I_0 \cos^2 \theta$.

Brewster's law

$$\tan \theta_{\rm p} = \frac{n_2}{n_1}$$
: Brewster's law

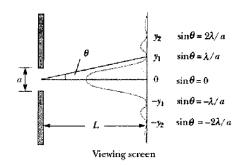
 θ_p is the angle of incidence of unpolarized light which makes the reflected light completely polarized in the perpendicular direction to the plane of incidence (Sir David Brewster, 1812). When the angle of incidence of the initially unpolarized light is θ_p , the reflected and refracted rays are perpendicular to each other.

DIFFRACTION

When light passes through a narrow slit of width comparable to the wavelength of light, the light flares out of the slit; this bending or spreading of waves is called diffraction.

ALLEN

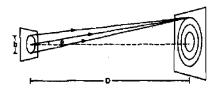
Properties of dark & bright fringes:



- (a) It results from superposition of secondary wavelets originating from various parts of single coherent source.
- (b) Diffraction fringes are never of equal width.
- (c) Intensity of all the bright fringes is not the same.
- (d) Dark fringes are not perfectly dark.

FRAUNHOFER DIFFRACTION BY A CIRCULAR APERTURE

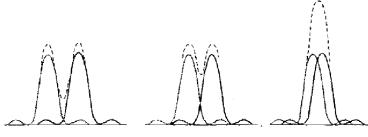
The mathematical analysis shows that the first dark ring is formed by the light diffracted from the hole at an angle θ with the axis $\sin\theta = \frac{1.22\lambda}{b}$.



The radius of the diffraction disc is given by $R = \frac{1.22 \lambda D}{b}$,

LIMIT OF RESOLUTION

The fact that a lens forms a disc image of a point source, puts a limit on resolving two neighboring points imaged by a lens.



well resolved

just resolved

unresolved.

For two objects to be barely resolved, the angular separation between them should be at least:

$$\theta_R = sin^{-1} \left(\frac{1.22\lambda}{b} \right)$$

EXERCISE (S-1)

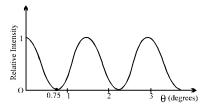
1. In a Young's double slit experiment for interference of light, the slits are 0.2 cm apart and are illuminated by yellow light ($\lambda = 600$ nm). What would be the fringe width on a screen placed 1 m from the plane of slits if the whole system is immersed in water of index 4/3?

WO0001

2. In Young's double slit experiment the slits are 0.5 mm apart and the interference is observed on a screen at a distance of 100 cm from the slit. It is found that the 9th bright fringe is at a distance of 7.5mm from the second dark fringe from the centre of the fringe pattern on same side. Find the wavelength of the light used.

WO0002

3. Light of wavelength 520 nm passing through a double slit, produces interference pattern of relative intensity versus angular position θ as shown in the figure. Find the separation d between the slits.



WO0003

In a Young's double slit experiment, two wavelengths of 500 nm and 700 nm were used. What is the minimum distance from the central maximum where their maximas coincide again? (Take D/d = 10³. Symbols have their usual meanings.)

WO0004

5. In a YDSE apparatus, d = 1mm, $\lambda = 600$ nm and D = 1m. The slits individually produce same intensity on the screen. Find the minimum distance between two points on the screen having 75% intensity of the maximum intensity.

WO0005

6. The distance between two slits in a YDSE apparatus is 3mm. The distance of the screen from the slits is 1m. Microwaves of wavelength 1 mm are incident on the plane of the slits normally. Find the distance of the first maxima on the screen from the central maxima. Also find the total number of maxima on the screen.

WO0006

7. One slit of a double slit experiment is covered by a thin glass plate of refractive index 1.4 and the other by a thin glass plate of refractive index 1.7. The point on the screen, where central bright fringe was formed before the introduction of the glass sheets, is now occupied by the 5th bright fringe. Assuming that both the glass plates have same thickness and wavelength of light used is 4800 Å, find their thickness.

12 JEE-Physics ALLEN

8. A monochromatic light of $\lambda = 5000$ Å is incident on two slits separated by a distance of 5×10^{-4} m. The interference pattern is seen on a screen placed at a distance of 1 m from the slits. A thin glass plate of thickness 1.5×10^{-6} m & refractive index $\mu = 1.5$ is placed between one of the slits & the screen. Find the intensity at the centre of the screen, if the intensity there is I_0 in the absence of the plate. Also find the lateral shift of the central maximum.

WO0008

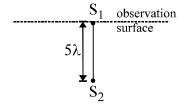
9. In a biprism experiment with sodium light, bands of width 0.0195 cm are observed on screen at 100cm from slit. On introducing a convex lens 30 cm away from the slit between biprism and screen, two images of the slit are seen 0.7 cm apart on screen. Calculate the wavelength of sodium light.

WO0009

10. A long narrow horizontal slit lies 1mm above a plane mirror as in Lloyd's mirror. The interference pattern produced by the slit and its image is viewed on a screen distant 1m from the slit. The wavelength of light is 600nm. Find the distance of first maximum above the mirror.

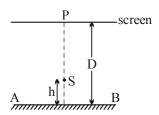
WO0010

11. Two microwave coherent point sources emitting waves of wavelength λ are placed at 5λ distance apart. The interference is being observed on a flat non-reflecting surface along a line passing through one source, in a direction perpendicular to the line joining the two sources (refer figure). Considering λ as 4 mm, calculate the positions of maxima and draw shape of interference pattern. Take initial phase difference between the two sources to be zero.

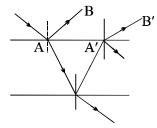


- 12. A point source S emitting light of wavelength 600 nm is placed at a very small height h above the flat reflecting surface AB (see figure). The intensity of the reflected light is 36% of the incident intensity. Interference fringes are observed on a screen placed parallel to the reflecting surface at a very large distance D from it.

 [IIT-JEE 2002]
 - (i) What is the shape of the interference fringes on the screen?
 - (ii) Calculate the ratio of the minimum to the maximum intensities in the interference fringes formed near the point P (shown in the figure).
 - (iii) If the intensities at point P corresponds to a maximum, calculate the minimum distance through which the reflecting surface AB should be shifted so that the intensity at P again becomes max.



13. A ray of light of intensity I is incident on a parallel glass-slab at a point A as shown in figure. It undergoes partial reflection and refraction. At each reflection 20% of incident energy is reflected. The rays AB and A' B'undergo interference. Find the ratio $I_{\rm max}/I_{\rm min}$. [Neglect the absorption of light]



WO0013

Ε

EXERCISE (S-2)

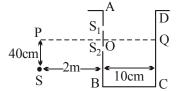
1. A thin glass plate of thickness t and refractive index μ is inserted between screen & one of the slits in a Young's experiment. If the intensity at the centre of the screen is I, what was the intensity at the same point prior to the introduction of the sheet.

WO0014

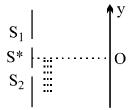
2. In Young's experiment, the source is red light of wavelength 7×10^{-7} m. When a thin glass plate of refractive index 1.5 at this wavelength is put in the path of one of the interfering beams, the central bright fringe shifts by 10^{-3} m to the position which was previously occupied by the 5th bright fringe. Find the thickness of the plate. When the source is now changed to green light of wavelength 5×10^{-7} m, the central fringe shifts to a position initially occupied by the 6th bright fringe due to red light without the plate. Find the refractive index of glass for the green light. Also estimate the change in fringe width due to the change in wavelength.

WO0015

3. A vessel ABCD of 10 cm width has two small slits S_1 and S_2 sealed with identical glass plates of equal thickness. The distance between the slits is 0.8 mm. POQ is the line perpendicular to the plane AB and passing through O, the middle point of S_1 and S_2 . A monochromatic light source is kept at S_2 , 40cm below S_3 and 2 m from the vessel, to illuminate the slits as shown in the figure below. Calculate the position of the central bright fringe on the other wall S_4 with respect to the line S_4 Now, a liquid is poured into the vessel and filled up to S_4 . The central bright fringe is found to be at S_4 . Calculate the refractive index of the liquid. [IIT-JEE 2001]



- 4. The Young's double slit experiment is done in a medium of refractive index 4/3. A light of 600 nm wavelength is falling on the slits having 0.45 mm separation. The lower slit S_2 is covered by a thin glass sheet of thickness 10.4 μ m and refractive index 1.5. The interference pattern is observed on a screen placed 1.5 m from the slits as shown [IIT-JEE'99]
 - (i) Find the location of the central maximum (bright fringe with zero path difference) on the y-axis.
 - (ii) Find the light intensity at point O relative to the maximum fringe intensity.
 - (iii) Now, if 600 nm light is replaced by white light of range 400 to 700 nm, find the wavelengths of the light that form maxima exactly at point O. [All wavelengths in this problem are for the given medium of refractive index 4/3. Ignore dispersion]

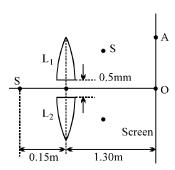


WO0017

5. In a Young's experiment, the upper slit is covered by a thin glass plate of refractive index 1.4 while the lower slit is covered by another glass plate having the same thickness as the first one but having refractive index 1.7. Interference pattern is observed using light of wavelength 5400 Å. It is found that the point P on the screen where the central maximum (n = 0) fell before the glass plates were inserted now has 3/4 the original intensity. It is further observed that what used to be the 5th maximum earlier, lies below the point P while the 6th minimum lies above P. Calculate the thickness of the glass plate. (Absorption of light by glass plate may be neglected). [IIT-JEE 1997]

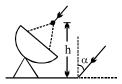
WO0018

6. In the figure shown S is a monochromatic point source emitting light of wavelength $\lambda = 500$ nm. A thin lens of circular shape and focal length 0.10 m is cut into two identical halves L_1 and L_2 by a plane passing through a diameter. The two halves are placed symmetrically about the central axis SO with a gap of 0.5 mm. The distance along the axis from S to L_1 and L_2 is 0.15 m, while that from L_1 & L_2 to O is 1.30 m. The screen at O is normal to SO. [IIT-JEE 1993]



- (i) If the third intensity maximum occurs at the point A on the screen, find the distance OA.
- (ii) If the gap between L_1 & L_2 is reduced from its original value of 0.5 mm, will the distance OA increase, decrease or remain the same ?

7. Radio waves coming at angle α to vertical are recieved by a radar after reflection from a nearby water surface & directly. What should be height of antenna from water surface so that it records a maximum intensity. (wavelength = λ).

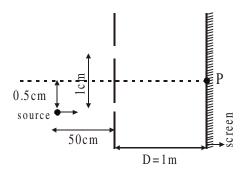


WO0020

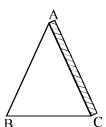
8. One radio transmitter A operating at 60.0 MHz is 10.0 m from another similar transmitter B that is 180° out of phase with transmitter A. How far must an observer move from transmitter A toward transmitter B along the line connecting A and B to reach the nearest point where the two beams are in phase?

WO0021

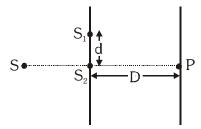
9. In a typical Young's double slit experiment a point source of monochromatic light is kept as shown in the figure. If the source is given an instantaneous velocity v = 1 mm per second towards the screen, then the instantaneous velocity of central maxima is given as $\alpha \times 10^{-\beta}$ m/s upward. Find the value of $\alpha + \beta$.



- 10. A prism $(\mu_p = \sqrt{3})$ has an angle of prism $A = 30^\circ$. A thin film $(\mu_f = 2.2)$ is coated on face AC as shown in the figure. Light of wavelength 550 nm is incident on the face AB at 60° angle of incidence. Find [IIT-JEE 2003]
 - (i) the angle of its emergence from the face AC and
 - (ii) the minimum thickness (in nm) of the film for which the emerging light is of maximum possible intensity.

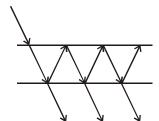


11. In a YDSE experiment two slits S_1 and S_2 have separation of d=2 mm. The distance of the screen is D=8/5 m. Source S starts moving from a very large distance towards S_2 perpendicular to S_1S_2 as shown in figure. The wavelength of monochromatic light is 500 nm. The number of maximas observed on the screen at point P as the source moves towards S_2 is 3995 + n. Find the value of n.



WO0024

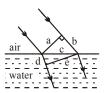
12. A narrow beam of light has entered a large thin glass plate. Each refraction is accompanied by reflection of one third of the beam's energy. What percentage of the light energy is transmitted through the plate?



EXERCISE (0-1)

SINGLE CORRECT TYPE QUESTIONS

1. Figure shows plane waves refracted from air to water using Huygen's principle (where a, b, c, d, e are lengths on the diagram). The refractive index of water wrt air is the ratio:-



(A) a/e

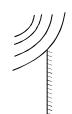
(B) b/e

(C) b/d

(D) d/b

WO0026

2. Spherical wavefronts shown in figure, strike a plane mirror. Reflected wavefronts will be as shown in



(A)

(B)

(C)



WO0027

3. Two beams of light having intensities I and 4I interfere to produce a fringe pattern on a screen. The phase difference between the beams is $\pi/2$ at point A and π at point B. Then the difference between the resultant intensities at A and B is : [IIT-JEE (Scr.) 2001]

(A) 2I

(B) 4I

(C) 5I

(D) 7I

WO0028

4. In a young double slit experiment, 12 fringes are observed to be formed in a certain segment of the screen when light of wavelength 600 nm is used. If the wavelength of light is changed to 400 nm, number of fringes observed in the same segment of the screen is given by [IIT-JEE (Scr.) 2001]

(A) 12

(B) 18

(C) 24

(D) 30

- 5. Two coherent monochromatic light beams of intensities I and 4I are superposed. The maximum and minimum possible intensities in the resulting beam are :
 - (A) 5I and I
- (B) 5I and 3I
- (C) 9I and I
- (D) 9I and 3I

WO0030

- **6.** When light is refracted into a denser medium,
 - (A) its wavelength and frequency both increase
 - (B) its wavelength increases but frequency remains unchanged
 - (C) its wavelength decreases but frequency remains unchanged
 - (D) its wavelength and frequency both decrease.

WO0031

- 7. In YDSE how many maxima can be obtained on the screen if wavelength of light used is 200nm and d = 700 nm:
 - (A) 12
- (B) 7

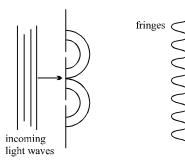
- (C) 18
- (D) none of these

WO0032

- **8.** In a YDSE, the central bright fringe can be identified:
 - (A) as it has greater intensity than the other bright fringes.
 - (B) as it is wider than the other bright fringes.
 - (C) as it is narrower than the other bright fringes.
 - (D) by using white light instead of single wavelength light.

WO0033

9. In a Young's double slit experiment, green light is incident on the two slits. The interference pattern is observed on a screen. Which of the following changes would cause the observed fringes to be more closely spaced?



- (A) Reducing the separation between the slits
- (B) Using blue light instead of green light
- (C) Used red light instead of green light
- (D) Moving the light source further away from the slits.

WO0034

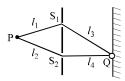
- 10. In Young's double slit experiment, the wavelength of red light is 7800 Å and that of blue light is 5200 Å. The value of n for which nth bright band due to red light coincides with (n + 1)th bright band due to blue light, is:
 - (A) 1

(B)2

(C)3

(D) 4

11. Two identical narrow slits S_1 and S_2 are illuminated by light of wavelength λ from a point source P. If, as shown in the diagram, the light is then allowed to fall on a screen, and if n is a positive integer, the condition for destructive interference at Q is:-



(A)
$$(\ell_1 - \ell_2) = (2n + 1)\lambda/2$$

(C)
$$(\ell_1 + \ell_2) - (\ell_3 + \ell_4) = n\lambda$$

(B)
$$(\ell_3 - \ell_4) = (2n + 1)\lambda/2$$

(D)
$$(\ell_1 + \ell_3) - (\ell_2 + \ell_4) = (2n+1)\lambda/2$$

WO0036

12. In Young's double slit experiment, the two slits act as coherent sources of equal amplitude A and wavelength λ . In another experiment with the same setup the two slits are sources of equal amplitude A and wavelength λ but are incoherent. The ratio of the average intensity of light at the midpoint of the screen in the first case to that in the second case is:-

(D) none of these

WO0037

13. In a Young's double slit experiment, a small detector measures an intensity of illumination of I units at the centre of the fringe pattern. If one of the two (identical) slits is now covered, the measured intensity will be:-

(D) I/2

WO0038

14. In a Young's double slit experiment *D* equals the distance of screen and d is the separation between the slit. The distance of the nearest point to the central maximum where the intensity is same as that due to a single slit, is equal to:-

(A)
$$\frac{D\lambda}{d}$$

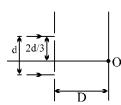
(B)
$$\frac{D\lambda}{2d}$$

(C)
$$\frac{D\lambda}{3d}$$

(D)
$$\frac{2D\lambda}{d}$$

WO0039

15. In the figure shown if a parallel beam of white light is incident on the plane of the slits then the distance of the white spot on the screen from O is [Assume d << D, $\lambda << d$]



(B)
$$d/2$$

(D)
$$d/6$$

WO0040

E

16.	In the above question if the light incident is monochromatic and point O is a maxima, then the
	wavelength of the light incident cannot be :-

- (A) $d^2/3D$
- (B) $d^2/6D$
- (C) $d^2/12D$ (D) $d^2/18D$

WO0041

- 17. In a YDSE bi-chromatic light of wavelengths 400 nm and 560 nm are used. The distance between the slits is 0.1 mm and the distance between the plane of the slits and the screen is 1 m. The minimum distance between two successive regions of complete darkness is :-[IIT-JEE' 2004 (Scr)]
 - (A) 4 mm
- $(B) 5.6 \, \text{mm}$
- (C) 14 mm
- (D) 28 mm

WO0042

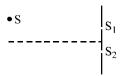
- **18.** In Young's double slit arrangement, water is filled in the space between screen and slits. Then:
 - (A) fringe pattern shifts upwards but fringe width remains unchanged.
 - (B) fringe width decreases and central bright fringe shifts upwards.
 - (C) fringe width increases and central bright fringe does not shift.
 - (D) fringe width decreases and central bright fringe does not shift.

WO0043

- 19. Light of wavelength λ in air enters a medium of refractive index μ . Two points in this medium, lying along the path of this light, are at a distance x apart. The phase difference between these points is:
 - (A) $\frac{2\pi\mu x}{\lambda}$
- (B) $\frac{2\pi x}{\mu \lambda}$
- (C) $\frac{2\pi(\mu-1)x}{\lambda}$ (D) $\frac{2\pi x}{(\mu-1)\lambda}$

WO0044

In YDSE, the source placed symmetrically with respect to the slit is now moved parallel to the plane 20. of the slits so that it is closer to the upper slit, as shown. Then,

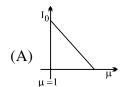


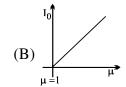
- (A) the fringe width will increase and fringe pattern will shift down.
- (B) the fringe width will remain same but fringe pattern will shift up.
- (C) the fringe width will decrease and fringe pattern will shift down.
- (D) the fringe width will remain same but fringe pattern will shift down.

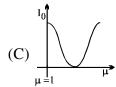
WO0045

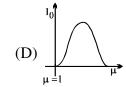
- 21. In the ideal double–slit experiment, when a glass–plate (refractive index 1.5) of thickness t is introduced in the path of one of the interfering beams (wavelength λ), the intensity at the position where the central maximum occurred previously remains unchanged. The minimum thickness of the glassplate is :-[IIT-JEE 2002]
 - $(A) 2\lambda$
- (B) $\frac{2\lambda}{3}$
- (C) $\frac{\lambda}{3}$
- (D) λ

22. In a YDSE experiment if a slab whose refractive index can be varied is placed in front of one of the slits then the variation of resultant intensity at mid-point of screen with μ ($\mu \ge 1$) will be best represented by [Assume slits of equal width and there is no absorption by slab]









WO0047

- 23. In a Young's double-slit experiment, let A and B be the two slits. Films of thicknesses t_A and t_B and refractive indices μ_A and μ_B , are placed in front of A and B respectively. If $\mu_A t_A = \mu_B t_B$, the central maximum will:
 - (A) not shift

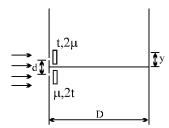
(B) shift towards A

(C) shift towards B

(D) option (B), if $t_B > t_A$; option (C) if $t_B < t_A$

WO0048

24. In the YDSE shown the two slits are covered with thin sheets having thickness t & 2t and refractive index 2μ and μ . Find the position (y) of central maxima

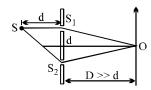


- (A) zero
- (B) $\frac{tD}{d}$
- (C) $-\frac{tD}{d}$
- (D) None

WO0049

- 25. In a double slit experiment, when the width of one slit is made twice as wide as the other in compared to normal YDSE having slits of equal width. Then, in the interference pattern [IIT-JEE(Scr.) 2000]
 - (A) the intensities of both the maxima and the minima increase.
 - (B) the intensity of the maxima increases and the minima has zero intensity.
 - (C) the intensity of the maxima decreases and that of the minima increases.
 - (D) the intensity of the maxima decreases and the minima has zero intensity.

26. To make the central fringe at the centre *O*, a mica sheet of refractive index 1.5 is introduced. Choose the correct statements (s).



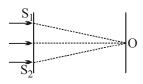
- (A) The thickness of sheet is $2(\sqrt{2}-1)d$ in front of S_1 .
- (B) The thickness of sheet is $(\sqrt{2}-1)d$ in front of S_2 .
- (C) The thickness of sheet is $2\sqrt{2} d$ in front of S_1 .
- (D) The thickness of sheet is $(2\sqrt{2}-1)d$ in front of S_1 .

WO0051

27. Statement-1: In YDSE, as shown in figure, central bright fringe is formed at *O*. If a liquid is filled between plane of slits and screen, the central bright fringe is shifted in upward direction.

and

Statement-2: If path difference at *O* increases, y-coordinate of central bright fringe will change.



- (A) Statement-1 is true, statement-2 is true and statement-2 is correct explanation for statement-1.
- (B) Statement-1 is true, statement-2 is true and statement-2 is NOT the correct explanation for statement-1.
- (C) Statement-1 is true, statement-2 is false.
- (D) Statement-1 is false, statement-2 is true.

WO0052

28. Statement-1: In glass, red light travels faster than blue light.

and

Statement-2: Red light has a wavelength longer than blue.

- (A) Statement-1 is true, statement-2 is true and statement-2 is correct explanation for statement-1.
- (B) Statement-1 is true, statement-2 is true and statement-2 is NOT the correct explanation for statement-1.
- (C) Statement-1 is true, statement-2 is false.
- (D) Statement-1 is false, statement-2 is true.

and

29.

Statement-2: In YDSE set up magnitude of electromagnetic field at central bright fringe is not varying with time.

- (A) Statement-1 is true, statement-2 is true and statement-2 is correct explanation for statement-1.
- (B) Statement-1 is true, statement-2 is true and statement-2 is NOT the correct explanation for statement-1.
- (C) Statement-1 is true, statement-2 is false.
- (D) Statement-1 is false, statement-2 is true.

WO0054

30. Statement-1: In YDSE, the spacing between any two successive points having intensity half of the maximum intensity is same.

and

Statement-2: The intensity on the screen in YDSE varies uniformly with distance from central maximum.

- (A) Statement-1 is true, statement-2 is true and statement-2 is correct explanation for statement-1.
- (B) Statement-1 is true, statement-2 is true and statement-2 is NOT the correct explanation for statement-1.
- (C) Statement-1 is true, statement-2 is false.
- (D) Statement-1 is false, statement-2 is true.

WO0055

In a double slit experiment, the separation between the slits is d = 0.25 cm and the distance of the 31. screen D = 100 cm from the slits. If the wavelength of light used is $\lambda = 6000$ Å and I_0 is the intensity of the central bright fringe, the intensity at a distance $x = 4 \times 10^{-5}$ m from the central maxima is :-

 $(A) I_0$

(B) $I_0/2$

(C) $3I_0/4$

(D) $I_0/3$

WO0056

- Imagine a Young's double slit interference experiment performed with waves associated with fast **32.** moving electrons produced from an electron gun. The distance between successive maxima will decrease the most if :-
 - (A) the accelerating voltage in the electron gun is decreased
 - (B) the accelerating voltage is increased and the distance of the screen from the slits is decreased
 - (C) the distance of the screen from the slits is increased.
 - (D) the distance between the slits is decreased.

33. Two monochromatic and coherent point sources of light are placed at a certain distance from each other in the horizontal plane. The locus of all those points in the horizontal plane which have constructive interference will be

(A) a hyperbola (B) family of hyperbolas

(C) family of straight lines (D) family of parabolas

WO0058

MULTIPLE CORRECT TYPE QUESTIONS

34. To observe a sustained interference pattern formed by two light waves, it is not necessary that they must have :

(A) the same frequency(B) same amplitude(C) a constant phase difference(D) the same intensity

WO0059

35. As a wave propagates,

[IIT-JEE 1999]

- (A) the wave intensity remains constant for a plane wave
- (B) the wave intensity decreases with distance from source and is proportional to inverse of the distance, for a spherical wave.
- (C) the wave intensity decreases with distance from source and proportional to inverse square of the distance, for a spherical wave.
- (D) total average power of the spherical wave over any spherical surface centered at the source remains same.

WO0060

- **36.** In a YDSE apparatus, if we use white light then:
 - (A) the fringe next to the central will be red (B) the central fringe will be white.
 - (C) the fringe next to the central will be violet (D) there will not be a completely dark fringe.

WO0061

- 37. If the source of light used in a Young's Double Slit Experiment is changed from red to blue, then
 - (A) the fringes will become brighter
 - (B) consecutive fringes will come closer
 - (C) the number of maxima formed on the screen increases
 - (D) the central bright fringe will become a dark fringe.

WO0062

- **38.** In a Young's double-slit experiment, let A and B be the two slits. A thin film of thickness t and refractive index μ is placed in front of A. Let β = fringe width. The central maximum will shift:
 - (A) towards A (B) towards B (C) by $t (\mu 1) \frac{\beta}{\lambda}$ (D) by $\mu t \frac{\beta}{\lambda}$

- **39.** If one of the slits of a standard YDSE apparatus is covered by a thin parallel sided glass slab so that it transmit only one half of the light intensity of the other, then:
 - (A) the fringe pattern will get shifted towards the covered slit.
 - (B) the fringe pattern will get shifted away from the covered slit.
 - (C) the bright fringes will be less bright and the dark ones will be more bright.
 - (D) the fringe width will remain unchanged.

WO0064

40. In an interference arrangement similar to Young's double-slit experiment, the slits S₁ & S₂ are illuminated with coherent microwave sources, each of frequency 10⁶ Hz. The sources are synchronized to have zero phase difference. The slits are separated by a distance d = 150.0 m. The intensity $I(\theta)$ is measured as a function of θ at a large distance from S_1 & S_2 , where θ is defined as shown. If I_0 is the maximum intensity then $I(\theta)$ for $0 \le \theta \le 90^{\circ}$ is given by :

(A)
$$I(\theta) = \frac{I_0}{2}$$
 for $\theta = 30^{\circ}$

(B)
$$I(\theta) = \frac{I_0}{4}$$
 for $\theta = 90^{\circ}$

(C)
$$I(\theta) = I_0$$
 for $\theta = 0^\circ$

(D) $I(\theta)$ is constant for all values of θ .

WO0065

- 41. In a standard YDSE apparatus, a thin film ($\mu = 1.5$, $t = 2.1 \mu m$) is placed in front of upper slit. How far above or below the centre point of the screen are two nearest maxima located? Take D = 1 m, d = 1mm, $\lambda = 4500$ Å. (Symbols have usual meaning)
 - (A) 1.5 mm
- $(B) 0.6 \, mm$
- $(C) 0.15 \, \text{mm}$
- (D) $0.3 \, \text{mm}$

WO0066

- 42. In a YDSE with two identical slits, when the upper slit is covered with a thin, perfectly transparent sheet of mica, the intensity at the centre of screen reduces to 75% of the initial value. Second minima is observed to be above this point and third maxima below it. Which of the following can be a possible value of phase difference caused by the mica sheet
 - (A) $\frac{\pi}{3}$
- (B) $\frac{13\pi}{3}$
- (C) $\frac{17\pi}{3}$
- (D) $\frac{11\pi}{3}$

WO0067

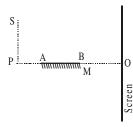
- 43. A beam of 2000 eV electrons are incident normally on the surface of crystal whose inter atomic separation is 0.11 nm. The mass of the electron can be taken as 9×10^{-31} kg. At what angle to the normal can we observe a diffraction maxima.

- (A) $\sin^{-1}\left(\frac{1}{4}\right)$ (B) $2\cos^{-1}\left(\frac{1}{4}\right)$ (C) $\sin^{-1}\left(\frac{1}{2}\right)$ (D) $2\cos^{-1}\left(\frac{1}{2}\right)$

COMPREHENSION TYPE QUESTIONS

Paragraph for Question No. 44 and 45

In an experiment on interference due to single mirror, a light wave emitted directly by the source S (narrow slit) interferes with the wave reflected from the mirror M of length 2 mm. Source and screen are separated by distance 90 cm. Source S is at the height of 3 mm, from the point P and the middle point of mirror is at distance of 2mm from point P. Point P and mirror are in the same plane of screen is perpendicular to this plane.



44. If fringe width is 0.1 mm then what is the wavelength of light used?

(A)
$$3.3 \times 10^{-7}$$
 m

(B)
$$6.7 \times 10^{-7}$$
 m

(C)
$$1.0 \times 10^{-7}$$
 m

(D)
$$4 \times 10^{-7}$$
 m

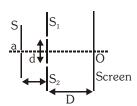
WO0069

- **45.** If the mirror is shifted towards left then how does the fringe pattern on screen change?
 - (A) Fringe width decreases and the region in which interference is formed shifts downward.
 - (B) Fringe width decreases and region in which inteference is formed shifts upwards
 - (C) Fringe width does not change and region in which interference is formed shifts upwards
 - (D) Fringe width does not change and region in which inteference is formed shifts downwards

WO0069

Paragraph for Question No. 46 to 48

The figure shows a schematic diagram showing the arrangement of Young's Double Slit Experiment



- **46.** Choose the correct statement(s) related to the wavelength of light used
 - (A) Larger the wavelength of light larger the fringe width
 - (B) The position of central maxima depends on the wavelength of light used
 - (C) If white light is used in YDSE, then the violet colour forms its first maxima closest to the central maxima
 - (D) The central maxima of all the wavelengths coincide

- 47. If the distance D is varied, then choose the correct statement(s)
 - (A) The angular fringe width does not change
 - (B) The fringe width changes in direct proportion
 - (C) The change in fringe width is same for all wavelengths
 - (D) The position of central maxima remains unchanged

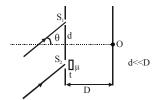
WO0070

- 48. If the distance d is varied, then identify the correct statement(s)
 - (A) The angular width does not change
- (B) The fringe width changes in inverse proportion
- (C) The positions of all maxima change
- (D) The positions of all minima change

WO0070

Paragraph for Question No. 49 to 51

A monochromatic beam of light falls on Young's double slit experiment apparatus as shown in figure. A thin sheet of glass is inserted in front of lower slit S_2 .



- 49. The central bright fringe can be obtained
 - (A) at O only

(B) at O or below O only

(C) at O or above O only

(D) Anywhere on the screen

WO0071

50. If central bright fringe is obtained on screen at O:-

(A)
$$(\mu-1) t = dsin\theta$$

(B)
$$(\mu-1) t = dcos\theta$$

(B)
$$(\mu-1) t = d\cos\theta$$
 (C) $(\mu-1)t + d\sin\theta = 0$ (D) $\frac{t}{\mu-1} = \frac{d}{\sin\theta}$

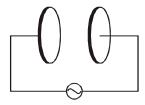
$$D) \frac{\iota}{\mu - 1} = \frac{a}{\sin \theta}$$

WO0071

- 51. The phase difference between the waves interfering at fifth minima is
 - (A) 5π
- (B) 7π
- (C) 9π
- (D) 11π

SUPPLEMENT FOR JEE-MAINS

- 52. A parallel plate capacitor (fig.) made of circular plates each of radius R = 6.0 cm has a capacitance $C = 100 \mu F$. The capacitor is connected to a 230 V ac supply with a (angular) frequency of 300 rad s^{-1} .
 - (a) What is the rms value of the conduction current?
 - (b) Is the conduction current equal to the displacement current?
 - (c) Determine the amplitude of B at a point 3.0 cm from the axis between the plates.



WO0072

53. The amplitude of the magnetic field part of a harmonic electromagnetic wave in vacuum is $B_0 = 510$ nT. What is the amplitude of the electric field part of the wave?

WO0073

- **54.** In a plane electromagnetic wave, the electric field oscillates sinusoidally at a frequency of 2.0×10^{10} Hz and amplitude 48 V m⁻¹.
 - (a) What is the wavelength of the wave?
 - (b) What is the amplitude of the oscillating magnetic field?
 - (c) Show that the average energy density of the E field equals the average energy density of the B field. [$c = 3 \times 10^8 \text{ m s}^{-1}$]

WO0074

55. Suppose that the electric field part of an electromagnetic wave in vaccum is

E = $\{(3.1 \text{ N/C}) \cos [(1.8 \text{ rad/m}) \text{ y} + (5.4 \times 10^8 \text{ rad/s})t] \hat{i}$.

- (a) What is the direction of propagation?
- (b) What is the wavelength λ ?
- (c) What is the frequency v?
- (d) What is the amplitude of the magnetic field part of the wave?
- (e) Write an expression for the magnetic field part of the wave.

WO0075

56. Two coherent waves are described by the following expressions.

$$E_1 = E_0 \sin \left(\frac{2\pi x_1}{\lambda} - 2\pi f t + \frac{\pi}{6}\right); E_2 = E_0 \sin \left(\frac{2\pi x_2}{\lambda} - 2\pi f t + \frac{\pi}{8}\right)$$

Determine the relationship between x_1 and x_2 that produces constructive interference when the two waves are superposed.

A nickel crystal is used as a diffraction grating for x-rays. Then the same crystal is used to diffract 57. electrons. If the two diffraction patterns are identical, and the energy of each x-ray photon is E = 20.0keY. What is the kinetic energy of each electron?

WO0079

- Which of these statements correctly describes the orientation of the electric field (\vec{E}) , the magnetic **58.**
 - field (\vec{B}) , and and velocity of propagation (\vec{v}) of an electromagnetic wave?
 - (A) \vec{E} is perpendicular to \vec{R} ; \vec{v} may have any orientation relative to \vec{E} .
 - (B) \vec{E} is perpendicular to \vec{R} ; \vec{v} may have any orientation perpendicular to \vec{E}
 - (C) \vec{E} is parallel to \vec{B} : \vec{v} is perpendicular to both \vec{B} and \vec{E} .
 - (D) Each of the three vectors is perpendicular to the other two.

WO0081

- **59.** The amplitude of electric field in a parallel light beam of intensity 4Wm⁻² is:
 - (A) 35.5 NC^{-1}
- (B) 45.5 NC⁻¹
- (C) 49.5 NC^{-1}
- (D) 54.8 NC^{-1}

WO0082

- Instantaneous displacement current of 1.0A in the space between the parallel plates of 1µF capacitor **60.** can be established by changing potential difference of:
 - (A) 10^{-6} V/s
- (B) 10^6 V/s
- (C) 10^{-8} V/s
- (D) 10^8 V/s

WO0083

A plane electromagnetic wave, 61.

> $E_z = 100 \cos (6 \times 10^8 t + 4x) \text{ V/m}$ propagates in a medium of dielectric constant:

- (A) 1.5
- (B) 2.0
- (C) 2.4
- (D) 4.0

WO0084

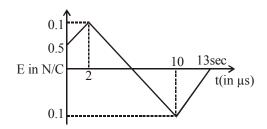
- **62.** The rms value of the electric field of the light coming from the sun is 720 N/c. The average total energy density of the electromagnetic wave is:
 - (A) $4.58 \times 10^{-6} \text{ J/m}^3$
- (B) $6.37 \times 10^{-9} \text{ J/m}^3$ (C) $81.35 \times 10^{-12} \text{ J/m}^3$ (D) $3.3 \times 10^{-3} \text{ J/m}^3$

WO0086

- A plane electromagnertic wave travels in free space along x-axis. At a particular point in space, the **63.** electric field along y-axis is 9.3 Vm⁻¹. The magnetic induction is:
 - (A) 3.1×10^{-8} T
- (B) $3 \times 10^{-5} \,\mathrm{T}$
- (C) 3.1×10^{-6} T
- (D) 9.3×10^{-6} T

WO0088

The electric field through an area of 2m² varies with time as shown in the graph. The greatest 64. displacement current through the area is at :-



- (A) t = 1 sec.
- (B) t = 4 sec.
- (C) t = 8 sec.
- (D) t = 12 sec.

(A)
$$E_y = 33 \cos \pi \times 10^{11} \left(t - \frac{x}{c} \right)$$
; $B_z = 1.1 \times 10^{-7} \cos \pi \times 10^{11} \left(t - \frac{x}{c} \right)$

(B)
$$E_y = 11 \cos 2\pi \times 10^{11} \left(t - \frac{x}{c} \right)$$
; $B_y = 1.1 \times 10^{-7} \cos 2\pi \times 10^{11} \left(t - \frac{x}{c} \right)$

(C)
$$E_x = 33 \cos \pi \times 10^{11} \left(t - \frac{x}{c} \right)$$
; $B_x = 1.1 \times 10^{-7} \cos \pi \times 10^{11} \left(t - \frac{x}{c} \right)$

(D)
$$E_y = 66 \cos 2\pi \times 10^{11} \left(t - \frac{x}{c} \right)$$
; $B_z = 2.2 \times 10^{-7} \cos 2\pi \times 10^{11} \left(t - \frac{x}{c} \right)$

WO0090

- 66. In a stack of three polarizing sheets the first and third are crossed while the middle one has its axis at 45° to the axes of the other two. The fraction of the intensity of an incident unpolarized beam of light that is transmitted by the stack is:
 - (A) 1/2
- (B) 1/3
- (C) 1/4
- (D) 1/8

WO0091

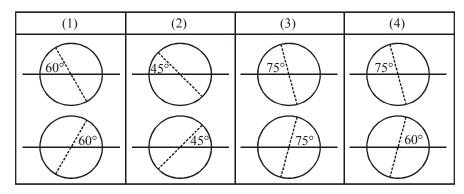
- 67. A beam of light strikes a piece of glass at an angle of incidence of 60° and the reflected beam is completely plane polarised. The refractive index of the glass is:-
 - (A) 1.5
- (B) $\sqrt{3}$
- (C) $\sqrt{2}$
- (D)(3/2)

WO0092

- **68.** The Sun is directly overhead and you are facing toward the north. Light coming to your eyes from the sky just above the horizon is:-
 - (A) Partially polarized north-south
- (B) Partially polarized east, west
- (C) Partially polarized up-down
- (D) Randomly polarized

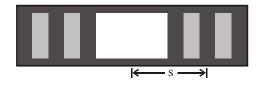
WO0093

69. The diagrams show four pairs of polarizing sheets, with the polarizing directions indicated by dashed lines. The two 'sheets of each pair are placed one behind the other and the front sheet is illuminated by unpolarized light. The incident intensity is the same for all pairs of sheets. Rank the pairs according to the intensity of the transmitted light, least to greatest.



- (A) 1,2, 3, 4
- (B) 4, 2, 1, 3
- (C) 2, 4, 3, 1
- (D) 2, 1,4, 3

70. Light of wavelength 600 nm is incident upon a single slit with width 4×10^{-4} m. The figure shows the pattern observed on a screen positioned 2 m from the slits. Determine the distance s.



(A) 0.002 m

(B) 0.003 m

(C) 0.004 m

(D) 0.006 m

WO0095

71. The image of a star (effectively a point source) is made by a convergent lens of focal length 1m and diameter of aperture 5.0 cm. If the lens is ideal and the effective wavelength in image formation is taken as 5×10^{-5} cm, the diameter of the image formed will be nearest to:

(A) zero

(B) 10^{-6} cm

(C) 10^{-5} cm

(D) 10^{-3} cm

WO0096

- 72. In a single slit diffraction pattern, as the width of the slit is increased,
 - (A) the peak intensity of central maxima increases and its width also increases
 - (B) the peak intensity of central maxima increases and its width decreases.
 - (C) the peak intensity of central maxima decreases and its width increases
 - (D) the peak intensity of central maxima decreases and its width also decreases.

WO0097

73. A beam of electrons with de-broglie wavelength of 10^{-4} m pass through a slit 10^{-3} m wide. Calculate the angular spread introduced because of diffraction by slit.

(A) $\frac{9^{\circ}}{\pi}$

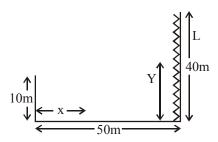
(B) $\frac{18^{\circ}}{\pi}$

(C) $\frac{36^{\circ}}{\pi}$

(D) $\frac{4.5^{\circ}}{\pi}$

WO0098

74. A person lives in a high-rise building on the bank of a river 50m wide. Across the river is a well lit tower of height 40 m. When the person, who is at a height of 10m, looks through a polarizer at an appropriate angle at light of the tower reflecting from the river surface, he notes that intensity of light coming from distance X from his building is the least and this corresponds to the light coming from light bulbs at height 'Y' on the tower. The values of X and Y are respectively close to (refractive index of water $\approx 4/3$)



(A) 13 m, 27 m

(B) 22 m, 13 m

(C) 25 m, 10 m

(D) 17 m, 29 m

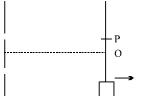
WO0099

E

EXERCISE (0-2)

SINGLE CORRECT TYPE QUESTIONS

- 1. In a Young's Double slit experiment, first maxima is observed at a fixed point P on the screen. Now the screen is continuously moved away from the plane of slits. The ratio of intensity at point P to the intensity at point O (centre of the screen)
 - (A) remains constant
 - (B) keeps on decreasing
 - (C) first decreases and then increases
 - (D) First decreases and then becomes constant



WO0100

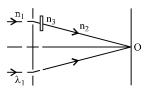
2. Two slits are separated by 0.3 mm. A beam of 500 nm light strikes the slits producing an interference pattern. The number of maxima observed in the angular range $-30^{\circ} < \theta < 30^{\circ}$.



- (A) 300
- (B) 150
- (C)599
- (D) 601

WO0101

3. In the figure shown in YDSE, a parallel beam of light is incident on the slit from a medium of refractive index n_1 . The wavelength of light in this medium is λ_1 . A transparent slab of thickness t and refractive index n_3 is put in front of one slit. The medium between the screen and the plane of the slits is n_2 . The phase difference between the light waves reaching point 'O' (symmetrical, relative to the slits) is:



- (A) $\frac{2\pi}{n_1\lambda_1}(n_3-n_2)$ t (B) $\frac{2\pi}{\lambda_1}(n_3-n_2)$ t (C) $\frac{2\pi n_1}{n_2\lambda_1}\left(\frac{n_3}{n_2}-1\right)$ t (D) $\frac{2\pi n_1}{\lambda_1}(n_3-n_1)$ t

WO0102

- 4. A thin slice is cut out of a glass cylinder along a plane parallel to its axis. The slice is placed on a flat glass plate as shown. The observed interference fringes from this combination shall be [IIT-JEE '99]
 - (A) straight
 - (B) circular
 - (C) equally spaced
 - (D) having fringe spacing which increases as we go outwards.

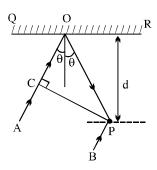


E

ode06 180BA-8B\Kota\EE[Advanced]\ENTHUSE\Phy\Woodule\Wave Optics, Wave on Shing & Sound Wave\eng\1-Wave Optics\01_Theay+Ex p65

5. In the adjacent diagram, CP represents a wavefront and AO and BP, the corresponding two rays. Find the condition on θ for constructive interference at P between the ray BP and reflected ray OP.

[JEE (Scr.) 2003]

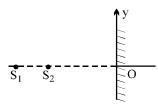


- (A) $\cos\theta = \frac{3\lambda}{2d}$ (B) $\cos\theta = \frac{\lambda}{4d}$ (C) $\sec\theta \cos\theta = \frac{\lambda}{d}$ (D) $\sec\theta \cos\theta = \frac{4\lambda}{d}$

WO0104

- 6. Two point monochromatic and coherent sources of light of wavelength λ are placed on the dotted line in front of a large screen. The sources emit waves in phase with each other. The distance between S_1 and S_2 is d while their distance from the screen is much larger.
 - (1) If $d = 7 \lambda/2$, O will be a minima
 - (2) If $d = 4.3 \lambda$, there will be a total of 8 minima on y-axis.
 - (3) If $d = 7 \lambda$, O will be a maxima.
 - (4) If $d = \lambda$, there will be only one maxima on the screen.

Which is the set of correct statement:



- (A) 1, 2 & 3
- (B) 2, 3 & 4
- (C) 1, 2, 3 & 4
- (D) 1, 3 & 4

WO0105

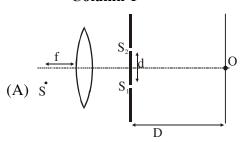
- 7. A parallel coherent beam of light falls on Fresnel biprism of refractive index μ and angle α . The fringe width on a screen at a distance D from biprism will be (wavelength = λ)
 - (A) $\frac{\lambda}{2(\mu-1)\alpha}$ (B) $\frac{\lambda D}{2(\mu-1)\alpha}$ (C) $\frac{D}{2(\mu-1)\alpha}$

- (D) none

MATRIX MATCH TYPE QUESTIONS

8. Column-I shows some modifications in a standard YDSE setup. Column-II shows the associated characteristics.

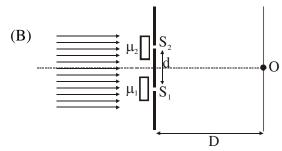
Column-I



monochromatic point source S placed in focal plane.

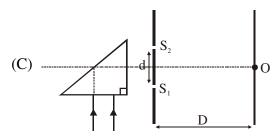
Column-II

(P) Zero order maxima lies above O.

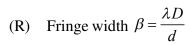


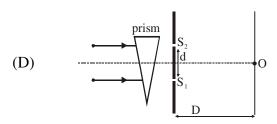
monochromatic parallel beam incident on S_1S_2 through transparent slabs of same thickness but $\mu_1 > \mu_2$

(Q) If a transparent mica sheet is introduced infront of S₂ central bright fringe can be obtained at O.



monochromatic parallel beam incident on a right angled isosceles prism of refractive index 1.50





monochromatic parallel beam incident on thin prism

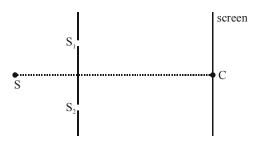
(S) Point O can be a minima

(T) Point O can be a least order minima.

36

9. In a YDSE setup, light of wavelength 4000 Å is used. Distance of screen from the slits is 2m and distance between slits is 1mm. There are three slabs slab 1(thickness 2mm, $\mu = 2$), slab 2

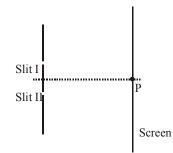
(thickness 1mm, $\mu = 3$), slab 3(thickness 4mm $\mu = \frac{3}{2}$)



- (A) If slab 1 is placed in front of slit S₁
- (P) Central maxima at C
- (B) If the slab 2 is placed in front of slit S, along with condition (A)
- (Q) Central maxima above C
- (C) If slab 3 is placed in front of slab 1 along with condition (B)
- (R) Fringe width is equal to 0.8 mm
- (S) No. of fringes crossing centre as a result of slab placing is 5000

WO0108

10. A double slit interference pattern is produced on a screen, as shown in the figure, using monochromatic light of wavelength 500nm. Point P is the location of the central bright fringe, that is produced when light waves arrive in phase without any path difference. A choice of three strips A, B and C of transparent materials with different thicknesses and refractive indices is available, as shown in the table. These are placed over one or both of the slits, singularly or in conjunction, causing the interference pattern to be shifted across the screen from the original pattern. In the column–I, how the strips have been placed, is mentioned whereas in the column–II, order of the fringe at point P on the screen that will be produced due to the placement of the strips(s), is shown. Correctly match both the column.



Film	A	В	С
Thickness (in µm)	5	1.5	0.25
Refractive index	1.5	2.5	2

Column I

Column II

Fifth Dark

(A) Only strip B is placed over slit–I

- (P) First Bright
- (B) Strip A is placed over slit–I and strip C is placed over slit–II
- (Q) Fourth Dark

(C) Strip A is placed over the slit–I and strip B and strip C are placed over the slit–II in conjunction

(R)

- (D) Strip A and strip C are placed over slit–I (in conjuction) and strip B is placed over Slit–II
- (S) Central Bright

EXERCISE-(J-M)

1.	A mixture of light, consisting of wavelength 590 nm and an unknown wavelength, illuminates Young's
	double slit and gives rise to two overlapping interference patterns on the screen. The central maximum
	of both lights coincide. Further, it is observed that the third bright fringe of known light coincides
	with the 4th bright fringe of the unknown light. From this data, the wavelength of the unknown light
	is:- [AIEEE-2009]

(1) 442.5 nm

(2) 776.8 nm

(3) 393.4 nm

(4) 885.0 nm

WO0110

Direction: Questions number 2 to 4 are based on the following paragraph.

An initially parallel cylindrical beam travels in a medium of refractive index $\mu(I) = \mu_0 + \mu_2 I$, where μ_0 and μ_2 are positive constants and I is the intensity of the light beam. The intensity of the beam is decreasing with increasing radius.

2. The initial shape of the wavefront of the beam is:-

[AIEEE-2010]

- (1) planar
- (2) convex
- (3) concave
- (4) convex near the axis and concave near the periphery

WO0112

3. The speed of the light in the medium is :-

[AIEEE-2010]

- (1) maximum on the axis of the beam
- (2) minimum on the axis of the beam
- (3) the same everywhere in the beam
- (4) directly proportional to the intensity I

WO0112

4. As the beam enters the medium, it will:

[AIEEE-2010]

- (1) travel as a cylindrical beam
- (2) diverge
- (3) converge
- (4) diverge near the axis and converge near the periphery

WO0112

5. At two points P and Q on screen in Young's double slit experiment, waves from slits S_1 and S_2 have a path difference of 0 and $\frac{\lambda}{4}$ respectively. the ratio of intensities at P and Q will be : [AIEEE-2011]

(1)3:2

(2) 2:1

 $(3) \sqrt{2} : 1$

(4)4:1

6. Statement-1: On viewing the clear blue portion of the sky through a Calcite Crystal, the intensity of transmitted light varies as the crystal is rotated.

Statement-1: The light coming from the sky is polarized due to scattering of sun light by particles in the atmosphere. The scattering is largest for blue light. [AIEEE-2011]

- (1) Statement-1 is false, statement-2 is true
- (2) Statement-1 is true, statement-2 is false
- (3) Statement-1 is true, statement-2 true; statement-2 is the correct explanation of statement-1
- (4) Statement-1 is true, statement-2 is true; statement -2 is not correct explanation of statement-1.

WO0114

7. In a Young's double slit experiment, the two slits act as coherent sources of waves of equal amplitude A and wavelength λ . In another experiment with the same arrangement the two slits are made to act as incoherent sources of waves of same amplitude and wavelength. If the intensity at the middle point

of the screen in the first case is I_1 and in the second case I_2 , then the ratio $\frac{I_1}{I_2}$ is:- [AIEEE-2011]

(1)4

(2) 2

(3)1

(4)0.5

WO0115

8. Direction:

> The question has a paragraph followed by two statement, Statement-1 and statement-2. Of the given four alternatives after the statements, choose the one that describes the statements.

> A thin air film is formed by putting the convex surface of a plane-convex lens over a plane glass plate. With monochromatic light, this film gives an interference pattern due to light reflected from the top (convex) surface and the bottom (glass plate) surface of the film [AIEEE-2011]

Statement-1:

When light reflects from the air-glass plate interface, the reflected wave suffers a phase change of π . **Statement-2:** The centre of the interference pattern is dark:

- (1) Statement-1 is true, Statement-2 is true and Statement-2 is not the correct explanation of Statement-1.
- (2) Statement-1 is false, Statement-2 is true
- (3) Statement-1 is true, Statement-2 is false
- (4) Statement-1 is true, Statement-2 is true and Statement-2 is the correct explanation of statement-1.

WO0116

- 9. In Young's double slit experiment, one of the slit is wider than other, so that the amplitude of the light from one slit is double of that from other slit. If I_m be the maximum intensity, the resultant intensity I when they interfere at phase difference ϕ is given by : [AIEEE-2012]
 - $(1) \frac{I_{m}}{9} (1 + 8\cos^{2}\frac{\phi}{2}) \qquad (2) \frac{I_{m}}{9} (4 + 5\cos\phi) \qquad (3) \frac{I_{m}}{3} (1 + 2\cos^{2}\frac{\phi}{2}) \qquad (4) \frac{I_{m}}{5} (1 + 4\cos^{2}\frac{\phi}{2})$

- 10. An electromagnetic wave in vacuum has the electric and magnetic fields \vec{E} and \vec{B} , which are always perpendicular to each other. The direction of polarization is given by \vec{X} and that ofwave propagation by \vec{k} . Then [AIEEE-2012]
 - (1) $\vec{X} \parallel \vec{B}$ and $\vec{k} \parallel \vec{E} \times \vec{B}$

(2) $\vec{X} \parallel \vec{E}$ and $\vec{k} \parallel \vec{B} \times \vec{E}$

(3) $\vec{X} \parallel \vec{B}$ and $\vec{k} \parallel \vec{B} \times \vec{E}$

(4) $\vec{X} \parallel \vec{E}$ and $\vec{k} \parallel \vec{E} \times \vec{B}$

WO0118

11. This question has Statement-1 and statement-2. Of the four choices given after the Statements, choose the one that best describes the two statements.

[AIEEE - 2012]

Statement-1: Davisson - Germer experiment established the wave nature of electrons.

Statement-2: If electrons have wave nature, they can interfere and show diffraction.

- (1) Statement-1 is true, Statement-2 is true and Statement-2 is the correct explanation for Statement-1.
- (2) Statement-1 is true, Statement-2 is true and Statement-2 is not the correct explanation of Statement-I
- (3) Statement-1 is false, Statement-2 is true.
- (4) Statement-1 is true, Statement-2 is false

WO0119

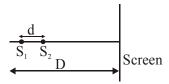
- 12. A beam of unpolarised light of intensity I₀ is passed through a polaroid A and then through another polaroid B which is oriented so that its principal plane makes an angle of 45° relative to that of A. The intensity of the emergent light is:[JEE-Mains 2013]
 - $(1) I_0$

- $(2) I_0/2$
- $(3) I_0/4$
- $(4) I_0/8$

WO0120

13. Two coherent point sources S_1 and S_2 are separated by a small distance 'd' as shown. The fringes obtained on the screen will be:

[JEE-Mains 2013]



- (1) points
- (2) straight lines
- (3) semicircles
- (4) concentric circles

WO0121

14. During the propagation of electromagnetic waves in a medium :

[JEE-Mains 2014]

- (1) Electric energy density is equal to the magnetic energy density
- (2) Both electric magnetic energy densities are zero
- (3) Electric energy density is double of the magnetic energy density
- (4) Electric energy density is half of the magnetic energy density.

the initial intensitites of the two beams are I_A and I_B respectively, then $\frac{I_A}{I_B}$ equals :[JEE-Mains 2014]

(1) 1

(2) $\frac{1}{3}$

(3) 3

 $(4) \frac{3}{2}$

WO0124

16. A red LED emits light at 0.1 watt uniformly around it. The amplitude of the electric field of the light at a distance of 1 m from the diode is:- [JEE-Mains 2015]

(1) 5.48 V/m

(2) 7.75 V/m

(3) 1.73 V/m

(4) 2.45 V/m

WO0125

17. Assuming human pupil to have a radius of 0.25cm and a comfortable viewing distance of 25cm, the minimum separation between two objects that human eye can resolve at 500 nm wavelength is:-

[JEE-Mains 2015]

 $(1) 100 \, \mu m$

 $(2) 300 \mu m$

 $(3) 1 \mu m$

 $(4) 30 \mu m$

WO0126

18. On a hot summer night, the refractive index of air is smallest near the ground and increases with height from the ground. When a light beam is directed horizontally, the Huygens' principle leads us to conclude that as it travels, the light beam:

[JEE-Mains 2015]

(1) bends downwards

(2) bends upwards

(3) becomes narrower

(4) goes horizontally without any deflection

WO0127

19. The box of a pin hole camera, of length L, has a hole of radius a. It is assumed that when the hole is illuminated by a parallel beam of light of wavelength λ the spread of the spot (obtained on the opposite wall of the camera) is the sum of its geometrical spread and the spread due to diffraction. The spot would then have its minimum size (say b_{min}) when:-

(1)
$$a = \frac{\lambda^2}{L}$$
 and $b_{min} = \sqrt{4\lambda L}$

(2)
$$a = \frac{\lambda^2}{L}$$
 and $b_{min} = \left(\frac{2\lambda^2}{L}\right)$

(3)
$$a = \sqrt{\lambda L}$$
 and $b_{min} = \left(\frac{2\lambda^2}{L}\right)$

(4)
$$a = \sqrt{\lambda L}$$
 and $b_{min} = \sqrt{4\lambda L}$

WO0128

20. In a Young's double slit experiment, slits are separated by 0.5 mm, and the screen is placed 150 cm away. A beam of light consisting of two wavelengths, 650 nm and 520 nm, is used to obtain interference fringes on the screen. The least distance from the common central maximum to the point where the bright fringes due to both the wavelengths coincide is:
[JEE-Main 2017]

(1) 9.75 mm

(2) 15.6 mm

(3) 1.56 mm

 $(4) 7.8 \, \text{mm}$

WO0130

E

21.	The angular width of the central maximum in a single slit diffraction pattern is 60° . The width of the
	slit is 1 μm . The slit is illuminated by monochromatic plane waves. If another slit of same width is
	made near it, Young's fringes can be observed on a screen placed at a distance 50 cm from the slits.
	If the observed fringe width is 1 cm, what is slit separation distance? (i.e. distance between the centres
	of each slit.) [JEE-Main 2018]

- (1) $50 \mu m$
- (2) $75 \mu m$
- $(3)\ 100\ \mu m$
- (4) $25 \mu m$

WO0131

An EM wave from air enters a medium. The electric fields are $\vec{E}_1 = E_{01} \hat{x} \cos \left[2\pi v \left(\frac{z}{c} - t \right) \right]$ in air and 22.

 $\vec{E}_2 = E_{02}\hat{x}\cos\left[k\left(2z-ct\right)\right]$ in medium, where the wave number k and frequency v refer to their values in air. The medium is non-magnetic. If \in_{r_1} and \in_{r_2} refer to relative permittivity of air and medium respectively, which of the following options is correct? [**JEE-Main 2018**]

- $(1) \frac{\epsilon_{r_1}}{\epsilon_{r_1}} = 2$
- $(2) \frac{\epsilon_{r_i}}{\epsilon_r} = \frac{1}{4} \qquad (3) \frac{\epsilon_{r_i}}{\epsilon_r} = \frac{1}{2} \qquad (4) \frac{\epsilon_{r_i}}{\epsilon_r} = 4$

WO0132

SELECTED PROBLEMS FROM JEE-MAINS ONLINE PAPERS

In a Young's double slit experiment, the slits are placed 0.320 mm apart. Light of wavelength 23. $\lambda = 500$ nm is incident on the slits. The total number of bright fringes that are observed in the angular range $-30^{\circ} \le \theta \le 30^{\circ}$ is: [JEE Main-2019 Jan]

- (1)320
- (2)641
- (3)321
- (4)640

24. In a double-slit experiment, green light (5303 Å) falls on a double slit having a separation of 19.44 μm and a width of 4.05 μm. The number of bright fringes between the first and the second diffraction minima is :-[JEE Main-2019 Jan]

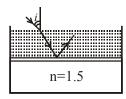
- (1)09
- (2) 10
- (3) 04
- (4)05

25. A light wave is incident normally on a glass slab of refractive index 1.5. If 4% of light gets reflected and the amplitude of the electric field of the incident light is 30V/m, then the amplitude of the electric field for the wave propogating in the glass medium will be: [JEE Main-2019 Jan]

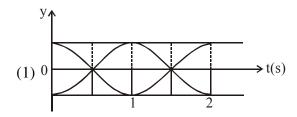
- (1) 10 V/m
- (2) 24 V/m
- (3) 30 V/m
- (4) 6 V/m

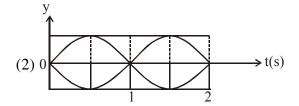
26. Consider a tank made of glass(reiractive index 1.5) with a thick bottom. It is filled with a liquid of refractive index μ ,. A student finds that, irrespective of what the incident angle i (see figure) is for a beam of light entering the liquid, the light reflected from the liquid glass interface is never completely polarized. For this to happen, the minimum value of μ is:

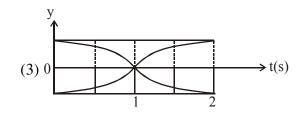
[JEE Main-2019 Jan]

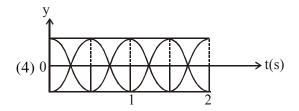


- $(1) \frac{3}{\sqrt{5}}$
- (2) $\frac{5}{\sqrt{3}}$
- $(4) \frac{4}{3}$
- 27. The correct figure that shows, schematically, the wave pattern produced by superposition of two [JEE Main-2019 April] waves of frequencies 9 Hz and 11 Hz is:









- 28. Calculate the limit of resolution of a telescope objective having a diameter of 200 cm, if it has to detect light of wavelength 500 nm coming from a star :-[JEE Main-2019 April]

 - (1) 305×10^{-9} radian (2) 152.5×10^{-9} radian (3) 610×10^{-9} radian
- $(4) 457.5 \times 10^{-9}$ radian
- 29. Diameter of the objective lens of a telescope is 250 cm. For light of wavelength 600nm. coming from a distant object, the limit of resolution of the telescope is close to :-[JEE Main-2019_April]
 - (1) 1.5×10^{-7} rad
- $(2) 2.0 \times 10^{-7} \text{ rad}$
- $(3) 3.0 \times 10^{-7} \text{ rad}$
- $(4) 4.5 \times 10^{-7} \text{ rad}$
- **30.** The value of numerical aperature of the objective lens of a microscope is 1.25. If light of wavelength 5000 Å is used, the minimum separation between two points, to be seen as distinct, will be :

[JEE Main-2019 April]

- $(1) 0.24 \mu m$
- $(2) 0.48 \mu m$
- $(3) 0.12 \mu m$
- $(4) 0.38 \mu m$
- The aperture diameter of a telescope is 5m. The separation between the moon and the earth is 31. 4×10^5 km. With light of wavelength of 5500 Å, the minimum separation between objects on the surface of moon, so that they are just resolved, is close to: [JEE Main-2020 Jan]
 - $(1) 20 \, \text{m}$
- $(2)600 \,\mathrm{m}$
- (3) 60 m
- (4) 200 m

A plane electromagnetic wave is propagating along the direction $\frac{\hat{i} + \hat{j}}{\sqrt{2}}$, with its polarization along 32.

the direction \hat{k} . The correct form of the magnetic field of the wave would be (here B_0 is an appropriate constant): [JEE Main-2020 Jan]

(1) $B_0 \frac{\hat{i} - \hat{j}}{\sqrt{2}} \cos \left(\omega t - k \frac{\hat{i} + \hat{j}}{\sqrt{2}} \right)$

(2) $B_0 \frac{\hat{i} + \hat{j}}{\sqrt{2}} \cos \left(\omega t - k \frac{\hat{i} + \hat{j}}{\sqrt{2}} \right)$

(3) $B_0 \hat{k} \cos \left(\omega t - k \frac{\hat{i} + \hat{j}}{\sqrt{2}} \right)$

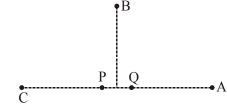
- (4) $B_0 \frac{\hat{j} \hat{i}}{\sqrt{2}} \cos \left(\omega t + k \frac{\hat{i} + \hat{j}}{\sqrt{2}} \right)$
- 33. In a Young's double slit experiment, 16 fringes are observed in a certain segment of the screen when light of wavelength 700 nm is used. If the wavelength of light is changed to 400 nm, the number of fringes observed in the same segment of the screen would be: [JEE Main-2020 Sep]
 - (2)24
- 34. A beam of plane polarised light of large cross sectional area and uniform intensity of 3.3 Wm⁻² falls normally on a polariser (cross sectional area 3×10^{-4} m²) which rotates about its axis with an angular speed of 31.4 rad/s. The energy of light passing through the polariser per revolution, is close to:

[JEE Main-2020 Sep]

- $(1) 1.0 \times 10^{-5} J$
- $(2) 5.0 \times 10^{-4} \text{ J}$
- $(3) 1.0 \times 10^{-4} J$
- $(4) 1.5 \times 10^{-4} \text{ J}$
- 35. A beam of electrons of energy E scatters from a target having atomic spacing of 1Å. The first maximum intensity occurs at $\theta = 60^{\circ}$. Then E (in eV) is _____. (Planck constant $h = 6.64 \times 10^{-34}$ Js, 10^{-34} Js, 10^{-19} J, electron mass $m = 9.1 \times 10^{-31}$ kg)

[JEE Main-2020 Sep]

In the figure below, P and Q are two equally intense coherent sources emitting radiation of wavelength **36.** 20 m. The separation between P and Q is 5 m and the phase of P is ahead of that of Q by 90°. A, B and C are three distinct points of observation, each equidistant from the midpoint of PQ. The intensities of radiation at A, B, C will be in the ratio: [JEE Main-2020 Sep]



- (1) 0:1:2
- (2) 4:1:0
- (3) 0:1:4
- (4) 2:1:0

EXERCISE-(J-A)

1. Column I shows four situations of standard Young's double slit arrangement with the screen placed far away from the slits S_1 and S_2 . In each of these cases $S_1P_0 = S_2P_0$, $S_1P_1 - S_2P_1 = \lambda/4$ and $S_1P_2 - S_2P_2 = \lambda/3$,, where λ is the wavelength of the light used. In the cases B, C and D, a transparent sheet of refractive index μ and thickness t is pasted on slit S_2 . The thicknesses of the sheets are different in different cases. The phase difference between the light waves reaching a point P on the screen from the two slits is denoted by $\delta(P)$ and the intensity by I(P). Match each situation given in **Column I** with the statement(s) in **Column II** valid for that situation. [IIT-JEE-2009]

> Column-I Column-II

$$\begin{array}{c|c}
S_2 & & P_2 \\
P_1 & & P_0 \\
S_1 & & P_0
\end{array}$$

$$(p) \quad \delta(P_0) = 0$$

(B)
$$(\mu - 1) t = \lambda/4$$

$$S_{2}$$

$$P_{2}$$

$$P_{3}$$

$$S_{1}$$

(q)
$$\delta(P_1) = 0$$

(C)
$$(\mu - 1) t = \lambda/2$$
 S_2 P_2 P_1 P_0

(r)
$$I(P_1) = 0$$

(D)
$$(\mu - 1) t = 3\lambda/4$$

$$S_2$$

$$P$$

$$P$$

$$P$$

$$S_1$$

(s)
$$I(P_0) > I(P_1)$$

(t)
$$I(P_2) > I(P_1)$$

WO0133

Young's double slit experiment is carried out by using green, red and blue light, one color at a time. 2. The fringe widths recorded are β_G , β_R and β_B , respectively. Then

[IIT-JEE-2012]

(A) $\beta_G > \beta_R > \beta_R$

(B) $\beta_B > \beta_G > \beta_R$

(C) $\beta_R > \beta_R > \beta_G$

(D) $\beta_R > \beta_G > \beta_R$

WO0134

3. In the Young's double slit experiment using a monochromatic light of wavelength λ , the path difference (in terms of an integer n) corresponding to any point having half the peak intensity is:-

[JEE Advanced 2013]

(A) $(2n+1)\frac{\lambda}{2}$

(B) $(2n+1)\frac{\lambda}{4}$

(C) $(2n+1)\frac{\lambda}{8}$

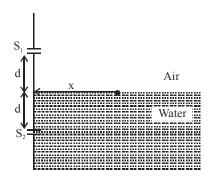
(D) $(2n+1)\frac{\lambda}{16}$

WO0135

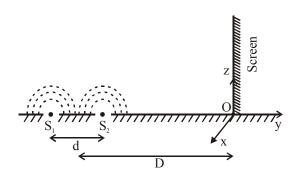
- 4. A light source, which emits two wavelengths $\lambda_1 = 400$ nm and $\lambda_2 = 600$ nm, is used in a Young's double slit experiment. If recorded fringe widths for λ_1 and λ_2 are β_1 and β_2 and the number of fringes for them within a distance y on one side of the central maximum are m₁ and m₂, respectively, then:-[JEE Advanced 2014]
 - (A) $\beta_2 > \beta_1$
 - (B) $m_1 > m_2$
 - (C) From the central maximum, 3^{rd} maximum of λ_2 overlaps with 5^{th} minimum of λ_1
 - (D) The angular separation of fringes of λ_1 is greater than λ_2

WO0136

A Young's double slit interference arrangement with slits S₁ and S₂ is immersed in water (refractive 5. index = 4/3) as shown in the figure. The positions of maxima on the surface of water are given by x^2 = $p^2m^2\lambda^2 - d^2$, where λ is the wavelength of light in air (refractive index = 1), 2d is the separation between the slits and m is an integer. The value of p is. [JEE Advanced 2015]



While conducting the Young's double slit experiment, a student replaced the two slits with a large opaque plate in the x-y plane containing two small holes that act as two coherent point sources (S_1, S_2) emitting light of wavelength 600 nm. The student mistakenly placed the screen parallel to the x-z plane (for z > 0) at a distance D = 3m from the mid-point of S_1S_2 , as shown schematically in the figure. The distance between the sources d = 0.6003 mm. The origin O is at the intersection of the screen and the line joining S_1S_2 . Which of the following is (are) true of the intensity pattern on the screen?



- (A) Hyperbolic bright and dark bands with foci symmetrically placed about O in the x-direction
- (B) Semi circular bright and dark bands centered at point O
- (C) The region very close to the point O will be dark
- (D) Straight bright and dark bands parallel to the x-axis

WO0138

- 7. Two coherent monochromatic point sources S_1 and S_2 of wavelength $\lambda = 600$ nm are placed symmetrically on either side of the center of the circle as shown. The sources are separated by a distance d = 1.8mm. This arrangement produces interference fringes visible as alternate bright and dark spots on the circumference of the circle. The angular separation between two consecutive bright spots is $\Delta\theta$. Which of the following options is/are correct?

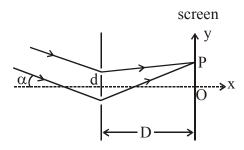
 [JEE Advanced 2017]
 - (A) A dark spot will be formed at the point P₂
 - (B) The angular separation between two consecutive bright spots decreases as we move from P_1 to P_2 along the first quadrant
- $\Delta\theta$ S_{\downarrow} d S_{2} d

- (C) At P₂ the order of the fringe will be maximum
- (D) The total number of fringes produced between P₁ and P₂ in the first quadrant is close to 3000

WO0139

8. In a Young's double slit experiment, the slit separation d is 0.3 mm and the screen distance D is 1m. A parallel beam of light of wavelength 600nm is incident on the slits at angle α as shown in figure. On the screen, the point O is equidistant from the slits and distance PO is 11.0 mm. Which of the following statement(s) is/are correct?

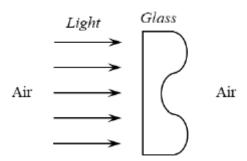
[JEE Advanced 2019]

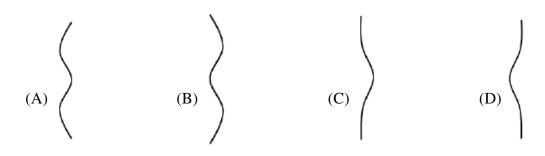


- (1) For $\alpha = \frac{0.36}{\pi}$ degree, there will be destructive interference at point O.
- (2) Fringe spacing depends on α
- (3) For $\alpha = \frac{0.36}{\pi}$ degree, there will be destructive interference at point P
- (4) For $\alpha = 0$, there will be constructive interference at point P.

WO0140

9. A parallel beam of light strikes a piece of transparent glass having cross section as shown in the figure below. Correct shape of the emergent wavefront will be (figures are schematic and not drawn to scale)[JEE Advanced 2020]





WAVE OPTICS

CBSE Previous Year's Questions

- 1. Two narrow slits are illuminated by a single monochromatic source. Name the pattern obtained on the screen. One of the slits is now completely covered. What is the name of the pattern now obtained on the screen? Draw Intensity pattern obtained in the two cases. Also write two differences between the patterns obtained in the above two cases.

 [3; CBSE-2004]
- **2.** Using Huygen's principle, draw a diagram to show propagation of a wave-front originating from a monochromatic point source.
 - Describe diffraction of light due to a single slit. Explain formation of a pattern of fringes obtained on the screen and plot showing variation of intensity with angle θ in single slit diffraction.

[5; CBSE-2005]

3. What is meant by a linearly polarized light? Which type of waves can be polarised? Briefly explain a method for producing polarised light. "Two Polaroids are placed at 90° to each other and the intensity of transmitted light is zero. What will be the intensity of transmitted light when one more Polaroid is placed between these two bisecting the angle between them? Take intensity of unpolarised light as λ .

[5; CBSE-2005]

- 4. Name the constituent radiation of electromagnetic spectrum which
- [3; CBSE-2005]

- (a) Is used in satellite communication.
- (b) Is used for studying crystal structure.
- (c) Is similar to the radiations emitted during decay of radioactive nuclei?
- (d) Has its wavelength range between 390 nm and 770 nm.
- (e) Is absorbed from sunlight by ozone layer.
- (f) Produces intense heating effect.
- 5. Mention the significance of Davisson-Germer experiment. An α particle and a proton are accelerated from rest through the same potential difference V. Find the ratio of de-Broglie wavelengths associated with them.

 [3; CBSE-2005]
- What are coherent sources of light? State two conditions for two light sources to be coherent.Derive a mathematical expression for the width of interference fringes obtained in Young's double slit experiment with the help of a suitable diagram.[5; CBSE-2006]
- 7. State Huygens' principle. Using the geometrical construction of secondary wave-lets, explain the refraction of a plane wave front incident at a plane surface. Hence verify Snell's law of refraction. Illustrate with the help of diagrams the action of (i) convex lens and (ii) concave mirror on a plane wave front incident on it.

 [5; CBSE-2006]
- 8. State the essential condition for diffraction of light to take place. Use Huygen's principle to explain diffraction of light due to a narrow single slit and the formation of a pattern of fringes obtained on the screen. Sketch the pattern of fringes formed due to diffraction at a single slit showing variation of intensity with angle θ.[3; CBSE-2007]
- 9. What are coherent sources of light? Why are coherent sources required to obtain sustained interference pattern? State three characteristic features which distinguish the interference pattern due to two coherently illuminated sources as compared to that observed in a diffraction pattern due to a single slit

[3; CBSE-2007]

- Name the following constituent radiations of electromagnetic spectrum which 10.
 - (i) produce intense heating effect,
 - (ii) is absorbed by the ozone layer in the atmosphere.
 - (iii) is used for studying crystal structure.

Write one more application for each of these radiations.

[2; CBSE-2007]

- 11. Draw a schematic diagram of the experimental arrangement used by Davisson and Germer to establish the wave nature of electrons. Explain briefly how the de-Broglie relation was experimentally verified in case of electrons. [3; CBSE-2007]
- **12.** How is a wavefront defined? Using Huygen's construction draw a figure showing the propagation of a plane wave refraction at a plane surface separating two media. Hence verify Snell's law of refraction.

[2; CBSE-2008]

- 13. (a) What is plane polarised light? Two polaroids are placed at 90° to each other and the transmitted intensity is zero. What happens when one more Polaroid is placed between these two, bisecting the angle between them? How will the intensity of transmitted light vary on further rotating the third Polaroid?
 - (b) If a light beam shows no intensity variation when transmitted through a polaroid which is rotated, does it mean that the light is unpolarised? Explain briefly, [5; CBSE-2008]
- Name the part of the electromagnetic spectrum of wavelength 10^{-2} m and mention its one application. 14. [1; CBSE-2008]
- **15.** The oscillating magnetic field in a plane electromagnetic wave is given by

By = $(8 \times 10^{-6}) \sin [2 \times 10^{11} t + 300 \pi x] T$

- (i) Calculate the wavelength of the electromagnetic wave.
- (ii) Write down the expression for the oscillating electric field.

[2; CBSE-2008]

16. Unpolarized light is incident on a plane surface of glass of refractive index µ at angle i. If the reflected light gets totally polarized, write the relation between the angle i and refractive index μ .

[1; CBSE-2009]

- Draw a diagram to show refraction of a plane wavefront incident in a convex lens and hence draw the 17. refracted wave front. [1; CBSE-2009]
- 18. In a single slit diffraction experiment, when a tiny circular obstacle is placed in the path of light from distant source, a bright spot is seen at the centre of the shadow of the obstacle. Explain why?

[3; CBSE-2009]

- 19. State two points of difference between the interference patterns obtained in Young's double slit experiment and the diffraction pattern due to a single slit. [3; CBSE-2009]
- Name the electromagnetic radiation to which waves of wavelength in the range of 10^{-2} m belong. **20.** Give on use of this part of EM spectrum. [l;CBSE-2009]
- 21. How does a charge q oscillating at certain frequency produce electromagnetic waves? Sketch a schematic diagram depicting electric and magnetic field for an electromagnetic wave propagating along the Z-direction. [2; CBSE-2009]
- In Young's double slit experiment, the two slits 0.15 mm apart are illuminated by monochromatic 22. [3; CBSE-2010] light of wavelength 450 nm. the screen is 1.0 m away from the slits.
 - (a) Find the distance of the second (i) bright fringe, (ii) dark fringe from the central maximum.
 - (b) How will the fringe pattern change if the screen is moved away from the slits?

ode06 180BA-8B\Kota\EE[Advanced]\ENTHUSE\Phy\Woodule\Wave Optics, Wave on Shing & Sound Wave\eng\1-Wave Optics\01_Theay+Ex p65

50 JEE-Physics ALLEN

23. How does an unpolarised light get polarised when passed through a polaroid?

Two polaroids are set in crossed positions. A third polaroid is placed between the two making an angle θ with the pass axis of the first polaroid. Write the expression for the intensity of light transmitted from the second polaroid. In what orientations will the transmitted intensity be (i) minimum and (ii) maximum?

[3; CBSE-2010]

- 24. Name the part of electromagnetic spectrum whose wavelength lies in the rage of 10^{-10} m. Give its one use. [1; CBSE-2010]
- 25. Draw a sketch of a plane electromagnetic wave propagating along the z-direction. Depict clearly the directions of electric and magnetic field varying sinusoidally with z. [2; CBSE-2010]
- **26.** State the importance of coherent sources in the phenomenon of interference.
 - In Young's double slit experiment to produce interference pattern, obtain the conditions for constructive and destructive interference. Hence deduce the expression for the fringe width. How does the fringes width get affected, if the entire experimental apparatus of Young is immersed in water?

[5; CBSE-2011]

- **27.** (a) State Huygens' principle. Using this principle explain how a diffraction pattern is obtained on a screen due to a narrow slit on which a narrow beam coming from a monochromatic source of light is incident normally.
 - (b) show that the angular width of the first diffraction fringe is half of that of the central fringe.
 - (c) If a monochromatic source of light is replaced by white light, what change would you observe in the diffraction pattern? [5; CBSE-2011]
- 28. How does the angular separation between fringes in single-slit diffraction experiment change when the distance of separation between the slit screens is doubled? [1; CBSE-2012]
- **29.** (a) In Young's double slit experiment, derive the condition for
 - (i) constructive interference and
 - (ii) destructive interference at a point on the screen
 - (b) A beam of light consisting of two wavelengths, 800 nm and 600 nm is used to obtain the interference fringes in a Young's double slit experiment on a screen placed 1.4m away. If the two slits are separated by 0.2 8 mm, calculate the least distance from the central bright maximum where the bright fringes of the two wavelength coincide.

OR

- (a) How does an unpolarized light incident on a polaroid get polarized? Describe briefly, with the help of a necessary diagram, the polarization of light by reflection from a transparent medium.
- (b) Two polaroids 'A' and 'B' are kept in crossed position. How should a third polaroid 'C' be placed between them so that the intensity of polarized light transmitted by polaroid B reduces to 1/8th of the intensity of unpolarized light incident on A? (5; CBSE-2012]
- 30. What are the directions of electric and magnetic field vectors relative to each other and relative to the direction of propagation of electromagnetic waves? [1; CBSE-2012]
- 31. A parallel beam of light of 500 nm falls on a narrow slit and the resulting diffraction pattern is observed on a screen 1 m away. It is observed that the first minimum is at a distance of 2-5 mm from the centre of the screen. Calculate the width of the slit. [CBSE-2013]

- (a) What is linearly polarized light? Describe briefly using a diagram how sunlight is polarised. **32.**
 - (b) Unpolarised light is incident on a polaroid. How would the intensity of transmitted light change when the polaroid is rotated? [CBSE-2013]
- 33. Welders wear special goggles or face masks with glass windows to protect their eyes from electromagnetic radiations. Name the radiations and write the range of their frequency.

[1; CBSE-2013]

- A capacitor, made of two parallel plates each of plate area A and separation d, is being charged by an 34. external ac source. Show that the displacement current inside the capacitor is the same as the current charging the capacitor. [3; CBSE-2013]
- **35.** Name the type of waves which are used for line of sight (LOS) communication. What is the range of their frequencies?
 - A transmitting antenna at the top of a tower has a height of 20 m and the height of the receiving antenna is 45 m. Calculate the maximum distance between them for satisfactory communication in LOS mode. (Radius of the Earth = 6.4×10^6 m) [3; CBSE-2013]
- To which part of the electromagnetic spectrum does a wave of frequency 3×10^{13} Hz belong? **36.**

[CBSE-2014]

- 37. Considering the case of a parallel plate capacitor being charged, show how one is required to generalize Ampere's circuital law to include the term due to displacement current. [CBSE-2014]
- 38. (1) Show, with the help of a diagram, how unpolarised sunlight gets polarised due to scattering,
 - (2) Two polaroids P₁ and P₂ are placed with their pass axes perpendicular to each other. Unpolarised light of intensity I_0 is incident on P_1 . A third polaroid P_3 is kept in between P_1 and P_2 such that its pass axis makes an angle of 45° with that of P_1 . Determine the intensity of light transmitted through P_1 , P_2 [CBSE-2014] and P_3 .
- **39.** (a) In Young's double slit experiment, describe briefly how bright and dark fringes are obtained on the screen kept in front of a double slit. Hence obtain the expression for the fringe width. (b) The ratio of the intensities at minima to the maxima in the Young's double slit experiment is 9:25. Find the ratio of the widths of the two slits. [CBSE-2014]

OR

- (a) Describe briefly how a diffraction pattern is obtained on a screen due to a single narrow slit illuminated by a monochromatic source of light. Hence obtain the conditions for the angular width of secondary maxima and secondary minima.
- (b) Two wavelengths of sodium light of 590nm and 596 nm are used in turn to study the diffraction taking place at a single slit of aperture 2×10^6 m. The distance between the slit and the screen is 1.5m. Calculate the separation between the positions of first maxima of the diffraction pattern obtained in the two cases.
- 40. An electron microscope uses electrons accelerated by a voltage of 50 kV. Determine the de-Broglie wavelength associated with the electrons. Taking other factors, such as numerical aperture etc. to be same, how does the resolving power of an electron microscope compare with that of an optical microscope which uses yellow light? [CBSE-2014]

OR

- (a) When a wave is propagating from a rarer to a denser medium, which characteristic of the wave does not change and why?
- (b) What is the ratio of the velocity of the wave in the two media of refractive indices μ_1 and μ_2 ?
- 42. In Young's double slit experiment, the two slits are separated by a distance of 1.5 mm and the screen is placed 1 m away from the plane of the slits. A beam of light consisting of two wavelengths 650nm and 520 nm is used to obtain interference fringes. Find

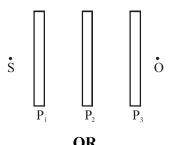
 [CBSE-2015]
 - (a) the distance of the third bright fringe for $\lambda = 520$ nm on the screen from the central maximum.
 - (b) the least distance from the central maximum where the bright fringes due to both the wavelengths coincide.
- 43. How are electromagnetic waves produced? What is the source of the energy carried by a propagating electromagnetic wave? [CBSE-2015]

Identify the electromagnetic radiations used

- (i) in remote switches of household electronic devices; and
- (ii) as diagnostic tool in medicine.
- 44. Why can't we see clearly through fog? Name the phenomenon responsible for it.

[1; CBSE-2016]

- **45.** (i) Derive Snell's law on the basis of Huygen's wave theory when light is travelling from a denser to a rarer medium. [3; CBSE-2016]
 - (ii) Draw the sketches to differentiate between plane wavefront and spherical wavefront.
- 46. How are electromagnetic waves produced? What is the source of energy of these waves? Write mathematical expressions for electric and magnetic fields of an electromagnetic wave propagating along the z-axis. Write any two important properties of electromagnetic waves. [3; CBSE-2016]
- 47. (a) Why does unpolarised light from a source show a variation in intensity when viewed through a polaroid which is rotated? Show with the help of a diagram, how unpolarised light from sun gets linearly polarised by scattering. [5; CBSE-2016]
 - (b) Three identical polaroid sheets P_1 , P_2 and P_3 are oriented so that the pass axis of P_2 and P_3 are inclined at angles of 60° and 90° respectively with the pass axis of P_1 . A monochromatic source S of unpolarized light of intensity I_0 is kept in front of the polaroid sheet P_1 as shown in the figure. Determine the intensities of light as observed by the observer at O, when polaroid P_3 is rotated with respect to P_2 at angles $\theta = 30^\circ$ and 60° .



- (a) Derive an expression for path difference in Young's double slit experiment and obtain the conditions for constructive and destructive interference at a point on the screen.
- (b) The intensity at the central maxima in Young's double slit experiment is I_0 . Find out the intensity

at a point where the path difference is $\frac{\lambda}{6}$, $\frac{\lambda}{4}$ and $\frac{\lambda}{3}$.

[CBSE-2017]

49. Draw the intensity pattern for single slit diffraction and double slit interference. Hence, state two differences between interference and diffraction patterns. [CBSE-2017]

OR

Unpolarised light is passed through a polaroid P_1 . When this polarised beam passes through another polaroid P_2 and if the pass axis of P_2 makes angle θ with the pass axis of P_1 , then write the expression for the polarised beam passing through P_2 . Draw a plot showing the variation of intensity when θ varies from 0 to 2π .

50. Identify the electromagnetic waves whose wavelengths vary as

[CBSE-2017]

- (a) $10^{-12} \text{ m} < \lambda < 10^{-8} \text{ m}$
- (b) $10^{-3} \text{ m} < \lambda < 10^{-1} \text{ m}$

Write one use for each.

- **51.** (a) Define wavefront. Use Huygens' principle to verify the laws of refraction.
 - (b) How is linearly polarised light obtained by the process of scattering of light? Find the Brewster angle for air glass interface, when the refractive index of glass = 1.5. [CBSE-2017]
- **52.** Name the electromagnetic radiations used for (a) water purification, and (b) eye surgery.

[CBSE-2018]

53. (a) Why are infra-red waves often called heat waves? Explain.

- [CBSE-2018]
- (b) What do you understand by the statement, "Electromagnetic waves transport momentum"?
- 54. (a) If one of two identical slits producing interference in Young's experiment is covered with glass, so that the light intensity passing through it is reduced to 50%, find the ratio of the maximum and minimum intensity of the fringe in the interference pattern. [CBSE-2018]
 - (b) What kind of fringes do you expect to observe if white light is used instead of monochromatic light?
- 55. (a) Define a wavefront. Using Huygen's principle, verify the laws of reflection at a plane surface.
 - (b) In a single slit diffraction experiment, the width of the slit is made double the original width. How does this affect the size and intensity of the central diffraction band? Explain.
 - (c) When a tiny circular obstacle is placed in the path of light from a distant source, a bright spot is seen at the centre of the obstacle. Explain why.

 [CBSE-2018]
- 56. Show using a proper diagram how unpolarised light can be linearly polarised by reflection from a transparent glass surface. [CBSE-2018]

ANSWER KEY

EXERCISE (S-1)

- 1. Ans. 0.225 mm
- 2. Ans. 5000Å
- 3. Ans. 1.99×10^{-2} mm

- 4. Ans. 3.5 mm
- 5. Ans. 0.2 mm
- **6. Ans.** 35.35 cm approximate, 5

- 7. Ans. 8 µm
- 8. Ans. 0, 1.5 mm
- **9. Ans.** $\lambda = 5850 \text{ Å}$

- **10. Ans.** 0.15 mm
- **11. Ans.** 48, 21, $\frac{32}{3}$, $\frac{9}{2}$, 0 m.m.;
- **12. Ans.** (i) circular, (ii) $\frac{1}{16}$, (C) 3000Å
- 13. Ans. 81:1

EXERCISE (S-2)

1. Ans. $I_0 = I \sec^2 \left[\frac{\pi(\mu - 1) t}{\lambda} \right]$

- **2. Ans.** 7 µm, 1.6, $\frac{400}{7}$ µm (decrease)
- **3. Ans.** (i) y = 2 cm, (ii) m = 1.0016
- **4. Ans.** (i) y = -13/3 mm, (ii) intensity at $O = 0.75I_{max}$ (iii) 650 nm, 433.33 nm
- **5. Ans.** 9.3 μm
- **6. Ans.** (i) 1 mm (ii) increase
- 7. Ans. $\frac{\lambda}{4\cos\alpha}$

- 8. Ans. 1.25 m
- 9. Ans. 7
- **10. Ans.** 0, 125 nm
- 11. Ans. 5

12. Ans. 50

EXERCISE (0-1)

- 1. Ans. (C) 2. Ans. (C)
- 3. Ans. (B)
- 4. Ans. (B)
- 5. Ans. (C)
- 6. Ans. (C)

- 7. Ans. (B)

- 10. Ans. (B)
- 11. Ans. (D)
- 12. Ans. (B)

- 8. Ans. (D)
- 9. Ans. (B)

- 13. Ans. (C) 14. Ans. (C)
- 15. Ans. (D)
- 16. Ans. (A)
- 17. Ans. (D)
- 18. Ans. (D)

- 19. Ans. (A) 20. Ans. (D)
- 21. Ans. (A)
- 22. Ans. (C)
- 23. Ans. (D)
- 24. Ans. (B)

- 25. Ans. (A) 26. Ans. (A)
- 27. Ans. (D)
- 28. Ans. (A)
- 29. Ans. (C)
- 30. Ans. (C)

- 31. Ans. (C) 32. Ans. (B)
- 33. Ans. (B)
- 34. Ans. (B,D)
- 35. Ans. (A,C,D)

- 36. Ans. (A,B,D)
- 37. Ans. (B,C)
- 38. Ans. (A,C)
- 39. Ans. (A,C,D)

- 40. Ans. (A,C)
- 41. Ans. (C,D)
- 42. Ans. (B,C,D)
- 43. Ans. (B,D)

44. Ans. (B)

- 45. Ans. (C)
- 46. Ans. (A,C,D)
- 47. Ans. (A,B,D)

- 48. Ans. (B,D)
- 49. Ans. (D)
- 50. Ans. (A)
- 51. Ans. (C)

52. Ans. (a)
$$I_{rms} = V_{rms} \omega C = 6.9 \text{ A}$$
 (b) Yes (c) $B_0 = \frac{\mu_0}{2\pi} \frac{r}{R^2} i_0$, $B_0 = 1.63 \times 10^{-5} \text{ T}$

53. Ans. 153 N/C

54. Ans. (a)
$$\lambda = (c/v) = 1.5 \times 10^{-2} \text{ m}$$

(b)
$$B_0 = (E_0/c) = 1.6 \times 10^{-7} \text{ T}$$

(c) Energy density in E field: $u_E = (1/2)\varepsilon_0 E^2$

Energy density in B field: $uB = (1/2 \mu) B^2$

Using E = cB, and c =
$$\frac{1}{\sqrt{\mu_0 \epsilon_0}}$$
, $u_E = u_B$

55. Ans.(a) $-\hat{j}$ (b) 3.5 m (b) 86 MHz (c) 10.3 nT (e) {(10.3 nT) cos [(1.8 rad/m) y + (5.4 × 10⁸ rad/s)t]} \hat{k}

56. Ans.
$$\left(n - \frac{1}{48}\right)\lambda = x_1 - x_2$$
 57. Ans. 391 eV **58.** Ans. (D) **59.** An

73. Ans. (C) 74. Ans. (A)

EXERCISE (O-2)

- 1. Ans. (C) 2. Ans. (C)
- 3. Ans. (A)
- 4. Ans. (A)
- 5. Ans. (B)
- 6. Ans. (C)
- 7. Ans. (A) 8. Ans. (A) (PRST); (B) (QRST); (C) (R); (D) (PRST)
- 9.Ans. (A)-R,S; (B)-P,R; (C)-R,S
- 10. Ans. (A) (R); (B) (R); (C) (S); (D) (P)

EXERCISE-(J-M)

- 1. Ans. (1)
- 2. Ans. (1)
- 3. Ans. (2)
- 4. Ans. (3)
- 5. Ans. (2)

- 6. Ans. (3)
- 7. Ans. (2)
- 8. Ans. (1)
- 9. Ans. (1)
- 10. Ans. (4)

- 11. Ans. (1)
- 12. Ans. (3)
- 13. Ans. (4)
- 14. Ans. (1)
- 15. Ans. (2)

- 16. Ans. (4)
- 17. Ans. (4)
- 18. Ans. (2)
- 19. Ans. (4)
- 20. Ans. (4)

- 21. Ans. (4)
- 22. Ans. (2)
- SELECTED PROBLEMS FROM JEE-MAINS ONLINE PAPERS
- 23. Ans. (2)
- 24. Ans. (4) or (3) 25. Ans. (2)
- 26. Ans. (1)
- 27. Ans. (4)

- 28. Ans. (1)
- 29. Ans. (3)
- 30. Ans. (1)
- 31. Ans. (3)
- 32. Ans. (1)

- 33. Ans. (1)
- 34. Ans. (3)

35. Ans. (50.00)

- 36. Ans. (4)

EXERCISE-(J-A)

- 1. Ans. (A) p, s; (B) q; (C) t; (D) r,s,t 2. Ans. (D)
- 3. Ans. (B)
- 4. Ans. (A,B,C)

- 5. Ans. 3
- 6. Ans. (B, C)
- 7. Ans. (C), (D)
- 8. Ans. (3)
- 9. Ans. (A)

56 JEE-Physics ALLEN

Important Notes



hapter	02)
	tents₋

WAVES ON STRING

01.	THEORY	59
02.	EXERCISE (S-1)	75
03.	EXERCISE (S-2)	77
04.	EXERCISE (O-1)	79
05.	EXERCISE (O-2)	86
06.	EXERCISE (JM)	91
07.	EXERCISE (JA)	93
08.	ANSWER KEY	95

Important Notes

WAVES ON STRING

KEY CONCEPTS

INTRODUCTION OF WAVES

What is wave motion?

- When a particle moves through space, it carries KE with itself. Wherever the particle goes, the energy goes with it. (One way of transport energy from one place to another place)
- There is another way (wave motion) to transport energy from one part of space to other without any bulk motion of material together with it. Sound is transmitted in air in this manner.
 - Ex. You (Kota) want to communicate your friend (Delhi)



1st option involves the concept of particle & the second choice involves the concept of wave.

Ex. When you say "Namaste" to your friend no material particle is ejected from your lips to fall on your friends ear. Basically you create some disturbance in the part of the air close to your lips. Energy is transferred to these air particles either by pushing them ahead or pulling them back. The density of the air in this part temporarily increases or decreases. These disturbed particles exert force on the next layer of air, transferring the disturbance to that layer. In this way, the disturbance proceeds in air and finally the air near the ear of the listener gets disturbed.

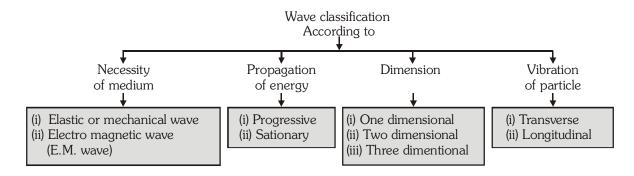
Note :- In the above example air itself does not move.

A **wave** is a disturbance that propagates in space, transports energy and momentum from one point to another without the transport of matter.

Few examples of waves:

The ripples on a pond (water waves), the sound we hear, visible light, radio and TV signals etc.

CLASSIFICATION OF WAVES



1. Based on medium necessity: A wave may or may not require a medium for its propagation. The waves which do not require medium for their propagation are called non-mechanical, e.g. light, heat (infrared), radio waves etc. On the other hand the waves which require medium for their propagation are called mechanical waves. In the propagation of mechanical waves elasticity and density of the medium play an important role therefore mechanical waves are also known as elastic waves.

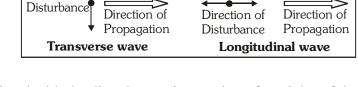
Example: Sound waves in water, seismic waves in earth's crust.

- **2. Based on energy propagation :-** Waves can be divided into two parts on the basis of energy propagation (i) Progressive wave (ii) Stationary waves. The progressive wave propagates with fixed velocity in a medium. In stationary waves particles of the medium vibrate with different amplitude but energy does not propagate.
- **3. Based on direction of propagation**: Waves can be one, two or three dimensional according to the number of dimensions in which they propagate energy. Waves moving along strings are one-dimensional. Surface waves or ripples on water are two dimensional, while sound or light waves from a point source are three dimensional.
- 4. Based on the motion of particles of

medium:

Waves are of two types on the basis of motion of particles of the medium.

- (i) Longitudinal waves
- (ii) Transverse waves



In the transverse wave the direction associated with the disturbance (i.e. motion of particles of the medium) is at right angle to the direction of propagation of wave while in the longitudinal wave the direction of disturbance is along the direction of propagation.

Direction of

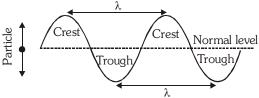
TRANSVERSE WAVE MOTION

Mechanical transverse waves produce in such type of medium which have shearing property, so they are known as shear wave or S-wave

Note:- Shearing is the property of a body by which it changes its shape on application of force.

⇒ Mechanical transverse waves are generated only in solids & surface of liquid.

In this individual particles of the medium execute SHM about their mean position in direction \perp^{r} to the direction of propagation of wave motion.



A **crest** is a portion of the medium, which is raised temporarily above the normal position of rest of particles of the medium, when a transverse wave passes.

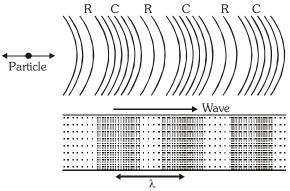
A **trough** is a portion of the medium, which is depressed temporarily below the normal position of rest of particles of the medium, when a transverse wave passes.

LONGITUDINAL WAVE MOTION

In this type of waves, oscillatory motion of the medium particles produces regions of compression (high pressure) and rarefaction (low pressure) which propagated in space with time (see figure).

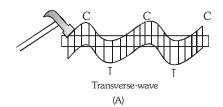
Note: The regions of high particle density are called compressions and regions of low particle density are called rarefactions.

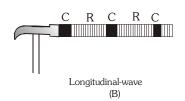
• The propagation of sound waves in air is visualized as the propagation of pressure or density fluctuations. The pressure fluctuations are of the order of 1 Pa, whereas atmospheric pressure is 10⁵ Pa.



Mechanical Waves in Different Media

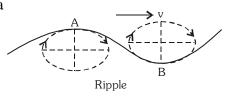
- A mechanical wave will be transverse or longitudinal depends on the nature of medium and mode of excitation.
- In strings mechanical waves are always transverse when string is under a tension. In gases and liquids mechanical waves are always longitudinal e.g. sound waves in air or water. This is because fluids cannot sustain shear.
- In solids, mechanical waves (may be sound) can be either transverse or longitudinal depending on the mode of excitation. The speed of the two waves in the same solid are different. (Longitudinal waves travels faster than transverse waves). e.g., if we struck a rod at an angle as shown in fig. (A) the waves in the rod will be transverse while if the rod is struck at the side as shown in fig. (B) or is rubbed with a cloth the waves in the rod will be longitudinal. In case of vibrating tuning fork waves in the prongs are transverse while in the stem are longitudinal.





Further more in case of seismic waves produced by Earthquakes both S (shear) and P (pressure) waves are produced simultaneously which travel through the rock in the crust at different speeds $[v_s \cong 5 \text{ km/s while } v_p \cong 9 \text{ km/s}]$ S—waves are transverse while P—waves longitudinal.

Some waves in nature are neither transverse nor longitudinal but a combination of the two. These waves are called 'ripple' and waves on the surface of a liquid are of this type. In these waves particles of the medium vibrate up and down and back and forth simultaneously describing ellipses in a vertical plane [Fig.]



CHARACTERISTICS OF WAVE MOTION

Some of the important characteristics of wave motion are as follows:

- In a wave motion, the disturbance travels through the medium due to repeated periodic oscillations of the particles of the medium about their mean positions.
- The energy is transferred from place to another without any actual transfer of the particles of the medium.
- Each particle receives disturbance a little later than its preceding particle i.e., there is a regular phase difference between one particle and the next.
- The velocity with which a wave travels is different from the velocity of the particles with which they vibrate about their mean positions.
- The wave velocity remains constant in a given medium while the particle velocity changes continuously during its vibration about the mean position. It is maximum at the mean position and zero at the extreme position.
- For the propagation of a mechanical wave, the medium must possess the properties of inertia, elasticity and minimum friction amongst its particles.

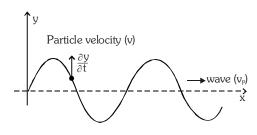
• Wavelength (λ) [length of one wave]

Distance travelled by the wave during the time, any one particle of the medium completes one vibration about its mean position. We may also define wavelength as the distance between any two nearest particles of the medium, vibrating in the same phase.

- **Frequency (n)**: Number of vibrations (Number of complete wavelengths) complete by a particle in one second.
- Time period (T): Time taken by wave to travel a distance equal to one wavelength.
- Amplitude (A): Maximum displacement of vibrating particle from its equilibrium position.
- Angular frequency (ω): It is defined as $\omega = \frac{2\pi}{T} = 2\pi n$
- **Phase :** Phase is a quantity which contains all information related to any vibrating particle in a wave. For equation $y = A \sin(\omega t kx)$; $(\omega t kx) = \text{phase}$.
- Angular wave number (k): It is defined as $k = \frac{2\pi}{\lambda}$
- Wave number (\vec{v}) : It is defined as $\vec{v} = \frac{1}{\lambda} = \frac{k}{2\pi} = \text{number of waves in a unit length of the wave pattern.}$
- Particle velocity, wave velocity and particle's acceleration: In plane progressive harmonic wave particles of the medium oscillate simple harmonically about their mean position. Therefore, all the formulae what we have read in SHM apply to the particles here also. For example, maximum particle velocity is $\pm A\omega$ at mean position and it is zero at extreme positions etc. Similarly maximum particle acceleration is $\pm \omega^2 A$ at extreme positions and zero at mean position. However the wave velocity is different from the particle velocity. This depends on certain characteristics of the medium. Unlike the particle velocity which oscillates simple harmonically (between $+ A\omega$ and $A\omega$) the wave velocity is constant for given characteristics of the medium.

• Particle velocity in wave motion :

The individual particles which make up the medium do not travel through the medium with the waves. They simply oscillate about their equilibrium positions. The instantaneous velocity of an oscillating particle of the medium, through which a wave is travelling, is known as "Particle velocity".



- Wave velocity: The velocity with which the disturbance, or planes of equal phase (wave front), travel through the medium is called wave (or phase) velocity.
- Relation between particle velocity and wave velocity:

Wave equation :- y = A sin (ωt - kx), Particle velocity $v = \frac{\partial y}{\partial t} = A\omega \cos(\omega t - kx)$.

Wave velocity =
$$v_p = \frac{\lambda}{T} = \lambda \frac{\omega}{2\pi} = \frac{\omega}{k}$$
, $\frac{\partial y}{\partial x} = -Ak \cos(\omega t - kx) = -\frac{A}{\omega}\omega k \cos(\omega k - kx) = -\frac{1}{v_p} \frac{\partial y}{\partial t}$

$$\Rightarrow \frac{\partial y}{\partial x} = -\frac{1}{v_P} \frac{\partial y}{\partial t}$$

Note: $\frac{\partial y}{\partial x}$ represent the slope of the string (wave) at the point x.

Particle velocity at a given position and time is equal to negative of the product of wave velocity with slope of the wave at that point at that instant.

• Differential equation of harmonic progressive waves :

$$\frac{\partial^2 y}{\partial t^2} = -A\omega^2 \sin(\omega t - kx) \Rightarrow \frac{\partial^2 y}{\partial x^2} = -Ak^2 \sin(\omega t - kx) \Rightarrow \frac{\partial^2 y}{\partial x^2} = \frac{1}{v_p^2} \frac{\partial^2 y}{\partial t^2}$$

• Particle velocity (v_p) and acceleration (a_p) in a sinusoidal wave :

The acceleration of the particle is the second particle is the second partial derivative of y(x, t) with respect to t,

$$\therefore a_{\rm P} = \frac{\partial^2 y(x,t)}{\partial t^2} = \omega^2 A \sin(kx - \omega t) = -\omega^2 y(x,t)$$

i.e., the acceleration of the particle equals $-\omega^2$ times its displacement, which is the result we obtained for SHM. Thus, $a_p = -w2$ (displacement)

• Relation between Phase difference,

Path difference & Time difference

**Phase (
$$\phi$$
)** $0 \quad \frac{\pi}{2} \quad \pi \quad \frac{3\pi}{2} \quad 2\pi \quad \frac{5\pi}{2} \quad 3\pi$

Wave length (
$$\lambda$$
) 0 $\frac{\lambda}{4}$ $\frac{\lambda}{2}$ $\frac{3\lambda}{4}$ λ $\frac{5\lambda}{4}$ $\frac{3}{2}\lambda$

Time-period (T)
$$0 \quad \frac{T}{4} \quad \frac{T}{2} \quad \frac{3T}{4} \quad T \quad \frac{5T}{4} \quad \frac{3T}{2}$$

$$\Rightarrow \frac{\Delta \phi}{2\pi} = \frac{\Delta \lambda}{\lambda} = \frac{\Delta T}{T} \Rightarrow \text{Path difference} = \left(\frac{\lambda}{2\pi}\right) \text{ Phase difference}$$

Ex. A progressive wave of frequency 500 Hz is travelling with a velocity of 360 m/s. How far apart are two points 60° out of phase.

Sol. We know that for a wave $v = f \lambda$ So $\lambda = \frac{v}{f} = \frac{360}{500} = 0.72 \text{ m}$

Phase difference $\Delta \phi = 60^{\circ} = (\pi/180) \times 60 = (\pi/3) \text{ rad}$,

so path difference
$$\Delta x = \frac{\lambda}{2\pi} (\Delta \phi) = \frac{0.72}{2\pi} x \frac{\pi}{3} = 0.12 \text{ m}$$

THE GENERAL EQUATION OF WAVE MOTION

Some physical quantity (say y) is made to oscillate at one place and these oscillations of y propagate to other places. The y may be,

- (i) displacement of particles from their mean position in case of transverse wave in a rope or longitudinal sound wave in a gas.
- (ii) pressure difference (dP) or density difference (dp) in case of sound wave or
- (iii) electric and magnetic fields in case of electromagnetic waves.

64

The oscillations of y may or may not be simple harmonic in nature. Consider one-dimensional wave travelling along x-axis. In this case y is a function of x and t. i.e. y = f(x, t) But only those function of

x & t, represent a wave motion which satisfy the differential equation. $\frac{\partial^2 y}{\partial t^2} = v^2 \frac{\partial^2 y}{\partial v^2}$...(i)

The general solution of this equation is of the form $y(x, t) = f(ax \pm bt)$

Thus, any function of x and t and which satisfies equation (i) or which can be written as equation (ii) represents a wave. The only condition is that it should be finite everywhere and at all times, Further,

if these conditions are satisfied, then speed of wave (v) is given by $v = \frac{\text{coefficient of t}}{\text{coefficient of x}} = \frac{b}{a}$

Which of the following functions represent a travelling wave? Ex.

(a)
$$(x - vt)^2$$

(b)
$$\ell n(x + vt)$$

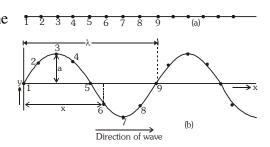
(c)
$$e^{-(x-vt)^2}$$

(d)
$$\frac{1}{x + vt}$$

Sol. Although all the four functions are written in the form $f(ax \pm bt)$, only (c) among the four functions is finite everywhere at all times. Hence only (c) represents a travelling wave.

Equation of a Plane Progressive Wave

If, on the propagation of wave in a medium, the particles of the medium perform simple harmonic motion then the wave is called a 'simple harmonic progressive wave'. Suppose, a simple harmonic progressive wave is propagating in a medium along the positive direction of the x-axis (from left to right). In fig. (a) are shown the equilibrium positions of the particles 1, 2, 3



When the wave propagates, these particles oscillate about their equilibrium positions. In Fig. (b) are shown the instantaneous positions of these particles at a particular instant. The curve joining these positions represents the wave. Let the time be counted from the instant when the particle 1 situated at the origin starts oscillating. If y be the displacement of this particle after t seconds, then $y = a \sin \omega t...(i)$

where a is the amplitude of oscillation and $\omega = 2\pi$ n, where n is the frequency. As the wave reaches the particles beyond the particle 1, the particles start oscillating. If the speed of the wave be v, then it will reach particle 6, distant x from the particle 1, in x/v sec. Therefore, the particle 6 will start oscillating x/v sec after the particle 1. It means that the displacement of the particle 6 at a time t will be the same as that of the particle 1 at a time x/v sec earlier i.e. at time t-(x/v). The displacement of particle 1 at time t - (x/v) can be the particle 6, distant x from the origin (particle 1), at time t is given by

$$y = a \sin \omega \left(t - \frac{x}{v}\right)$$

$$y = a \sin \omega \left(t - \frac{x}{v}\right)$$
 But $\omega = 2\pi n$, $y = a \sin (\omega t - kx) \left(k = \frac{\omega}{v}\right)$...(ii)

$$y = a \sin \left[\frac{2\pi}{T} t - \frac{2\pi}{\lambda} x \right]$$

Also
$$k = \frac{2\pi}{\lambda}$$

$$y = a \sin \left[\frac{2\pi}{T} t - \frac{2\pi}{\lambda} x \right] \qquad \text{Also } k = \frac{2\pi}{\lambda} \qquad ...(iii) \qquad \qquad y = a \sin 2\pi \quad \left[\frac{t}{T} - \frac{x}{\lambda} \right] ...(iv)$$

This is the equation of a simple harmonic wave travelling along +x direction. If the wave is travelling along the -x direction then inside the brackets in the above equations, instead of minus sign there will

be plus sign. For example, equation (iv) will be of the following form : $y = a \sin 2\pi \left(\frac{t}{T} + \frac{x}{\lambda}\right)$. If ϕ be

the phase difference between the above wave travelling along the +x direction and an other wave, then the equation of that wave will be

$$y = a sin \left\{ 2\pi \left(\frac{t}{T} - \frac{x}{\lambda} \right) \pm \phi \right\}$$

Ex. The equation of a wave is, $y(x,t) = 0.05 \sin \left[\frac{\pi}{2} (10x - 40t) - \frac{\pi}{4} \right] m$

Find:(a) The wavelength, the frequency and the wave velocity

(b) The particle velocity and acceleration at x=0.5 m and t=0.05 s.

Sol.: (a) The equation may be rewritten as, $y(x,t) = 0.05 \sin \left(5\pi x - 20\pi t - \frac{\pi}{4} \right) m$

Comparing this with equation of plane progressive harmonic wave,

 $y(x, t) = A \sin(kx - \omega t + \phi)$ we have, wave number $k = \frac{2\pi}{\lambda} = 5\pi \text{ rad/m}$ $\therefore \lambda = 0.4\text{m}$

The angular frequency is, $\omega = 2\pi f = 20\pi \, \text{rad/s}$ $\therefore f = 10 \, \text{Hz}$

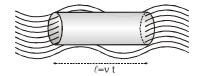
The wave velocity is, v = f $\lambda = \frac{\omega}{k} = 4 \text{ms}^{-1} \text{ in} + x \text{ direction}$

(b) The particle velocity and acceleration are, $v_p = \frac{\partial y}{\partial t} = -(20\pi)(0.05)\cos\left(\frac{5\pi}{2} - \pi - \frac{\pi}{4}\right) = 2.22 \text{m/s}$

$$a_p = \frac{\partial^2 y}{\partial t^2} = -(20\pi)^2 (0.05) \sin\left(\frac{5\pi}{2} - \pi - \frac{\pi}{4}\right) = 140 \text{ m/s}^2$$

INTENSITY OF WAVE

The amount of energy flowing per unit area and per unit time is called the intensity of wave. It is represented by I. Its units are J/m^2s or watt/metre². $I = 2\pi^2f^2A^2\rho v$ i.e. $I \propto A^2$ and $I \propto A^2$. If P is the power of an isotropic point source, then intensity at a distance r is given by,



$$I = \frac{P}{4\pi r^2}$$
 or $I \propto \frac{1}{r^2}$ (for a point source)

If P is the power of a line source, then intensity at a distance r is given by,

$$I = \frac{P}{2\pi r\ell} \ or \ I \propto \frac{1}{r} \ \ (for a \ line \ source) \ As, \ I \propto A^2$$

Therefore, $A \propto \frac{1}{r}$ (for a point source) and $A \propto \frac{1}{\sqrt{r}}$ (for a line source)

SUPERPOSITION PRINCIPLE

Two or more waves can propagate in the same medium without affecting the motion of one another. If several waves propagate in a medium simultaneously, then the resultant displacement of any particle of the medium at any instant is equal to the vector sum of the displacements produced by individual wave. The phenomenon of intermixing of two or more waves to produce a new wave is called Superposition of waves. Therefore according to superposition principle.

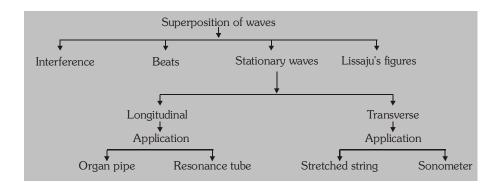
The resultant displacement of a particle at any point of the medium, at any instant of time is the vector sum of the displacements caused to the particle by the individual waves.

If $\vec{y}_1, \vec{y}_2, \vec{y}_3, ...$ are the displacement of particle at a particular time due to individual waves, then the resultant displacement is given by $\vec{y} = \vec{y}_1 + \vec{y}_2 + \vec{y}_3 + ...$

Principle of superposition holds for all types of waves, i.e., mechanical as well as electromagnetic waves. But this principle is not applicable to the waves of very large amplitude.

Due to superposition of waves the following phenomenon can be seen

- Interference: Superposition of two waves having equal frequency and nearly equal amplitude.
- **Beats**: Superposition of two waves of nearly equal frequency in same direction.
- Stationary waves: Superposition of equal wave from opposite direction.
- **Lissajous' figure:** Superposition of perpendicular waves.



INTERFERENCE OF WAVES:

When two waves of equal frequency and nearly equal amplitude travelling in same direction having same state of polarisation in medium superimpose, then intensity is different at different points. At some points intensity is large, whereas at other points it is nearly zero.

$$y_1 = A_1 \sin (\omega t - kx)$$
 and $y_2 = A_2 \sin (\omega t - kx + \phi)$

By principle of superposition $y = y_1 + y_2 = A \sin(\omega t - kx + \delta)$

where
$$A^2 = A_1^2 + A_2^2 + 2A_1A_2 \cos \phi$$
 and $\tan \delta = \frac{A_2 \sin \phi}{A_1 + A_2 \cos \phi}$

As intensity
$$I \propto A^2$$
 so $I = I_1 + I_2 + 2\sqrt{I_1I_2} \cos \phi$

• Constructive interference (maximum intensity):

Phase difference $\phi = 2n\pi$ or path difference = $n\lambda$ where n = 0, 1, 2, 3, ...

$$\Rightarrow$$
 $A_{max} = A_1 + A_2$ and $I_{max} = I_1 + I_2 + 2\sqrt{I_1I_2}$

• Destructive interference (minimum intensity):

Phase difference $\phi = (2n+1)\pi$, or path difference $= (2n-1) \frac{\lambda}{2}$ where n = 0, 1, 2, 3, ...

$$\Rightarrow$$
 $A_{min} = A_1 - A_2$ and $I_{min} = I_1 + I_2 - 2\sqrt{I_1I_2}$

KEY POINTS

- Maximum and minimum intensities in any interference wave form. $\frac{I_{Max}}{I_{Min}} = \left(\frac{\sqrt{I_1} + \sqrt{I_2}}{\sqrt{I_1} \sqrt{I_2}}\right)^2 = \left(\frac{a_1 + a_2}{a_1 a_2}\right)^2$
- Average intensity of interference wave form :- < I > or $I_{av} = \frac{I_{max} + I_{min}}{2} = I_1 + I_2$

if $a = a_1 = a_2$ and $I_1 = I_2 = I$ then $I_{max} = 4I$, $I_{min} = 0$ and $I_{AV} = 2I$

• Degree of interference Pattern (f): Degree of hearing (Sound Wave) or

Degree of visibility (Light Wave) $f = \frac{I_{max} - I_{min}}{I_{max} + I_{min}} \times 100$

In condition of perfect interference degree of interference pattern is maximum $f_{max} = 1$ or 100%

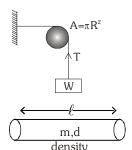
• Condition of maximum contrast in interference wave form $a_1 = a_2$ and $I_1 = I_2$ then $I_{max} = 4I$ and $I_{min} = 0$

For perfect destructive interference we have a maximum contrast in interference wave form.

VELOCITY OF TRANSVERSE WAVE

Mass of per unit length $m = \frac{\pi r^2 \ell \times d}{\ell}$, $m = \pi r^2 d$, where d = Density of matter

Velocity of transverse wave in any wire $v = \sqrt{\frac{T}{m}}$ or $\sqrt{\frac{T}{\pi r^2 d}} = \sqrt{\frac{T}{Ad}} : \pi r^2 = A$



- If m is constant then, $v \propto \sqrt{T}$ it is called tension law.
- If tension is constant then $\ v \propto \sqrt{\frac{1}{m}} \ \leftarrow$ it is called law of mass
- If T is constant & take wire of different radius for same material then $v \propto \frac{1}{r} \leftarrow$ it is called law of radius
- If T is constant & take wire of same radius for different material. Then $v \propto \sqrt{\frac{1}{d}} \leftarrow law$ of density

REFLECTION FROM RIGID END

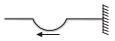
When the pulse reaches the right end which is clamped at the wall, the element at the right end exerts a force on the clamp and the clamp exerts equal and opposite force on the element. The element at the right end is thus acted upon by the force from the clamp. As this end remains fixed, the two forces are opposite to each other. The force from the left part of the string transmits the forward wave pulse and hence, the force exerted by the clamp sends a return pulse on the string whose shape is similar to a return pulse but is inverted. The original pulse tries to pull the element at the fixed end up and the return pulse sent by the clamp tries to pull it down, so the resultant displacement is zero. Thus, the wave is reflected from the fixed end and the reflected wave is inverted with respect to the original wave. The shape of the string at any time, while the pulse is being reflected, can be found by adding an inverted image pulse to the incident pulse.

Equation of wave propagating in +ve x-axis

Incident wave
$$y_1 = a \sin(\omega t - kx)$$

$$y_2 = a \sin(\omega t + kx + \pi)$$

or
$$y_2 = -a \sin(\omega t + kx)$$



REFLECTION FROM FREE END

The right end of the string is attached to a light frictionless ring which can freely move on a vertical rod. A wave pulse is sent on the string from left. When the wave reaches the right end, the element at this end is acted on by the force from the left to go up. However, there is no corresponding restoring force from the right as the rod does not exert a vertical force on the ring. As a result, the right end is displaced in upward direction more than the height of the pulse i.e., it overshoots the normal maximum displacement. The lack of restoring force from right can be equivalent described in the following way. An extra force acts from right which sends a wave from right to left with its shape identical to the original one. The element at the end is acted upon by both the incident and the reflected wave and the displacements add. Thus, a wave is reflected by the free end without inversion.

Incident wave
$$y_1 = a \sin(\omega t - kx)$$
 Reflected wave $y_2 = a \sin(\omega t + kx)$

STATIONARY WAVES

* **Definition:** The wave propagating in such a medium will be reflected at the boundary and produce a wave of the same kind travelling in the opposite direction. The superposition of the two waves will give rise to a stationary wave. Formation of stationary wave is possible only and only in bounded medium.

ANALYTICAL METHOD FOR STATIONARY WAVES

• From rigid end: We know equation for progressive wave in positive x-direction $y_1 = a \sin(\omega t - kx)$ After reflection from rigid end $y_2 = a \sin(\omega t + kx + \pi) = -a \sin(\omega t + kx)$ By principle of super position. $y = y_1 + y_2 = a \sin(\omega t - kx) - a \sin(\omega t + kx) = -2a \sin kx \cos \omega t$ This is equation of stationary wave reflected from rigid end

Amplitude =
$$2a \sin kx$$
 Velocity of particle $\mathbf{v}_{pa} = \frac{dy}{dt} = 2a \omega \sin kx \sin \omega t$

Strain
$$\frac{dy}{dx} = -2ak \cos kx \cos \omega t$$
 Elasticity $E = \frac{stress}{strain} = \frac{dp}{\frac{dy}{dx}}$ Change in pressure $dp = E \frac{dy}{dx}$

• Node
$$x = 0, \frac{\lambda}{2}, \lambda$$
...... $A = 0, V_{pa} = 0, strain \rightarrow max$ Change in pressure $\rightarrow max$

• Antinode
$$x = \frac{\lambda}{4}$$
, $\frac{3\lambda}{4}$ $A \rightarrow max$, $-V_{pa} \rightarrow max$. strain = 0 Change in pressure = 0

• From free end: we know equation for progressive wave in positive x-direction $y_1 = a \sin(\omega t - kx)$ After reflection from free end $y_2 = a \sin(\omega t + kx)$ **Amplitude** = $2a \cos kx$,

Velocity of particle = $v_{Pa} = \frac{dy}{dt} = 2a \omega \cos \omega t \cos kx$

 $\frac{dy}{dx} = -2ak \sin \omega t \sin kx$ Change in pressure $dp = E \frac{dy}{dx}$

• Antinode: x = 0, $\frac{\lambda}{2}$, λ $A \rightarrow Max$, $V_{pa} = \frac{dy}{dt} \rightarrow max$.

Strain = 0, dp = 0

• Node: $x = \frac{\lambda}{4}, \frac{3\lambda}{4}, \frac{5\lambda}{4}$ $A = 0, V_{pa} = \frac{dy}{dt} = 0, \text{ strain} \rightarrow \text{max}, dp \rightarrow \text{max}$

PROPERTIES OF STATIONARY WAVES

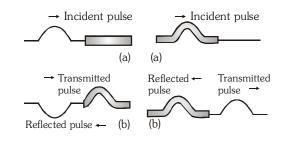
The stationary waves are formed due to the superposition of two identical simple harmonic waves travelling in opposite direction with the same speed.

Important characteristics of stationary waves are:-

- Stationary waves are produced in the bounded medium and the boundaries of bounded medium (i) may be rigid or free.
- In stationary waves nodes and antinodes are formed alternately. Nodes are the points which are (ii) always in rest having maximum strain. Antinodes are the points where the particles vibrate with maximum amplitude having minimum strain.
- All the particles except at the nodes vibrate simple harmonically with the same period. (iii)
- The distance between any two successive nodes or antinodes is $\lambda/2$. (iv)
- The amplitude of vibration gradually increases from zero to maximum value from node to (v) antinode.
- All the particles in one particular segment vibrate in the same phase, but the particle of two adjacent segments differ in phase by 180°
- (vii) All points of the medium pass through their mean position simultaneously twice in each period.
- (viii) Velocity of the particles while crossing mean position varies from maximum at antinodes to zero at nodes.
- (ix) In a stationary wave the medium is splitted into segments and each segment is vibrating up and down as a whole.
- (x) In longitudinal stationary waves, condensation (compression) and refraction do not travel forward as in progressive waves but they appear and disappear alternately at the same place.
- These waves do not transfer energy in the medium. Transmission of energy is not possible in a stationary wave.

TRANSMISSION OF WAVES

We may have a situation in which the boundary is intermediate between these two extreme cases, that is, one in which the boundary is neither rigid nor free. In this case, part of the incident energy is transmitted and part is reflected. For instance, suppose a light string is attached to a heavier string as in (figure). When a pulse travelling on the light reaches the knot, same part of it is reflected and inverted and same part of it is transmitted to the heavier string.



As one would expect, the reflected pulse has a smaller amplitude than the incident pulse, since part of the incident energy is transferred to the pulse in the heavier string. The inversion in the reflected wave is similar to the behaviour of a pulse meeting a rigid boundary, when it is totally reflected. When a pulse travelling on a heavy string strikes the boundary of a lighter string, as in (figure), again part is reflected and part is transmitted. However, in this case the reflected pulse is not inverted. In either case, the relative height of the reflected and transmitted pulses depend on the relative densities of the two string. In the previous section, we found that the speed of a wave on a string increases as the density of the string decreases. That is, a pulse travels more slowly on a heavy string than on a light string, if both are under the same tension. The following general rules apply to reflected waves. When a wave pulse travels from medium A to medium B and $v_A > v_B$ (that is, when B is denser than A), the pulse will be inverted upon reflection. When a wave pulse travels from medium A to medium B and $v_A < v_B$ (A is denser than B), it will not be inverted upon reflection.

KEY POINTS

Phenomenon of reflection and transmission of waves obeys the laws of reflection and refraction.

The frequency of these wave remains constant i.e. does not change. $\omega_i = \omega_r = \omega_r = \omega$

From rarer to denser medium $y_i = a_i \sin(\omega t - k_1 x)$ $y_r = -a_i \sin(\omega t + k_1 x)$ $y_t = a_t \sin(\omega t - k_2 x)$ From denser to rarer medium $y_i = a_i \sin(\omega t - k_1 x)$ $y_r = a_i \sin(\omega t + k_1 x)$ $y_t = a_t \sin(\omega t - k_2 x)$

STATIONARY WAVE ARE OF TWO TYPES:

(i) Transverse st. wave (stretched string) (ii) Longitudinal st. wave (organ pipes)

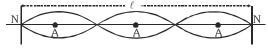
(i) **Transverse Stationary wave**

$$\frac{\lambda}{2} = \ell \implies \lambda = 2\ell$$

Second Harmonic - N

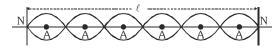
$$\frac{2\lambda}{2} = \ell \implies \lambda = \ell$$

Third Harmonic



$$\frac{3\lambda}{2} = \ell \implies \lambda = \frac{2\ell}{3}$$

p th harmonic



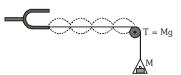
$$\frac{p\lambda}{2} = \ell \implies \lambda = \frac{2\ell}{p}$$

- Law of length: For a given string, under a given tension, the fundamental frequency of vibration is inversely proportional to the length of the string, i.e, $n \propto \frac{1}{\ell}$ (T and m are constant)
- **Law of tension:** The fundamental frequency of vibration of stretched string is directly proportional to the square root of the tension in the string, provided that length and mass per unit length of the string are kept constant. $n \propto \sqrt{T}$ (ℓ and m are constant)

- Law of mass: The fundamental frequency of vibration of a stretched string is inversely proportional to the square root of its mass per unit length provided that length of the string and tension in the string are kept constant, i.e., $n \propto \frac{1}{\sqrt{m}}$ (ℓ and T are constant)
- **Melde's experiment :** In Melde's experiment, one end of a flexible piece of thread is tied to the end of a tuning fork. The other end passed over a smooth pulley carries a pan which can be loaded. There are two arrangements to vibrate the tied fork with thread.

Transverse arrangement:

Case 1. In a vibrating string of fixed length, the product of number of loops and square root of tension are constant or p \sqrt{T} = constant.



Case 2. When the tuning fork is set vibrating as shown in fig. then the prong vibrates at right angles to the thread. As a result the thread is set into motion. The frequency of vibration of the thread (string) is equal to the frequency of the tuning fork. If length and tension are properly adjusted then, standing waves are formed in the string. (This happens when frequency of one of the normal modes of the string matched with the frequency of the tuning fork). Then, if p loops

are formed in the thread, then the frequency of the tuning fork is given by $n = \frac{p}{2\ell} \sqrt{\frac{T}{m}}$

Case 3. If the tuning fork is turned through a right angle, so that the prong vibrates along the length of the thread, then the string performs only a half oscillation for each complete vibrations of the prong. This is because the thread only makes node at the midpoint when the prong moves towards the pulley i.e. only once in a vibration.

Longitudinal arrangement:

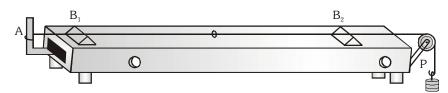
The thread performs sustained oscillations when the natural frequency of the given length of the thread under tension is half that of the fork.



Thus if p loops are formed in the thread, then the frequency of the tuning fork is $n = \frac{2p}{2\ell} \sqrt{\frac{T}{m}}$

SONOMETER:

Sonometer consists of a hollow rectangular box of light wood. One end of the experimental wire is fastened to one end of the box. The wire passes over a frictionless pulley P at the other end of the box. The wire is stretched by a tension T.



The box serves the purpose of increasing the loudness of the sound produced by the vibrating wire. If the length the wire between the two bridges is ℓ , then the frequency of vibration is $n=\frac{1}{2\ell}\sqrt{\frac{T}{m}}$

To test the tension of a tuning fork and string, a small paper rider is placed on the string. When a vibrating tuning fork is placed on the box, and if the length between the bridges is properly adjusted, then when the two frequencies are exactly equal, the string quickly picks up the vibrations of the fork and the rider is thrown off the wire. There are three laws of vibration of a wire.

COMPARISON OF PROGRESSIVE AND STATIONARY WAVES

Progressive waves

- 1. These waves travels in a medium with definite velocity.
- 2. These waves transmit energy in the medium.
- 3. The phase of vibration varies continuously from particle to particle.
- 4. No particle of medium is Permanently at rest.
- 5. All particles of the medium vibrate and amplitude of vibration is same.
- 6. All the particles do not attain the maximum displacement position simultaneously.

Stationary waves

These waves do not travel and remain confined between two boundaries in the medium.

These waves do not transmit energy in the medium. The phase of all the particles in between two nodes is always same. But particles of two Adjacent nodes differ in phase by 180° Particles at nodes are permanently at rest.

The amplitude of vibration changes from particle to particle. The amplitude is zero for all at nodes and maximum at antinodes.

All the particles attain the maximum displacement

WORKED OUT EXAMPLES

- **Ex.1** A wave is propagating along x-axis. The displacement of particles of the medium in z-direction at t = 0 is given by: $z = \exp[-(x + 2)^2]$, where 'x' is in meters. At t = 1s, the same wave disturbance is given by: $z = \exp[-(2-x)^2]$. Then, the wave propagation velocity is
 - (A) 4 m/s in + x direction

(B) 4 m/s in -x direction

(C) 2 m/s in + x direction

(D) 2 m/s in - x direction

Ans. (D)

Ex.2 A transverse wave is propagating along +x direction. At t = 2 sec, the particle at x = 4m is at y = 2 mm. With the passage of time its y coordinate increases and reaches to a maximum of 4 mm. The wave equation may be (using ω and k with their usual meanings)

(A)
$$y = 4\sin(\omega(t+2) + k(x-2) + \frac{\pi}{6})$$

(B)
$$y = 4\sin(\omega(t+2) + k(x) + \frac{\pi}{6})$$

(C)
$$y = 4\sin(\omega(t-2) - k(x-4) + \frac{5\pi}{6})$$
 (D) $y = 4\sin(\omega(t-2) - k(x-4) + \frac{\pi}{6})$

(D)
$$y = 4\sin(\omega(t-2) - k(x-4) + \frac{\pi}{6})$$

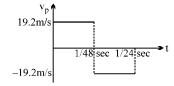
Ans. (D)

- $Y(x,t) = 0.05 / [(4x + 2t)^2 + 5]$ represents a moving wave pulse, where x and y are in meters and t is Ex.3in seconds. Then which statement(s) are **CORRECT**:
 - (A) Pulse is moving in -x direction
- (B) Wave speed is 0.5 m/s
- (C) Maximum particle displacement is 1 cm (D) It is a symmetric pulse

Ans. (A,B,C,D)

Ex.4 A symmetrical triangular pulse of maximum height 0.4 m and total length 1 m is moving in the positive x-direction on a string on which the wave speed is 24 m/s. At t = 0 the pulse is entirely located between x = 0 and x = 1 m. Draw a graph of the transverse velocity of particle of string versus time at x = +1m.

Ans.



A transverse harmonic disturbance is produced in a string. The maximum transverse velocity is 3 m/s and maximum transverse acceleration is 90 m/s². If the wave velocity is 20 m/s then find the waveform. [IIT-JEE 2005]

Ans.
$$y = (10 \text{ cm}) \sin (30 \text{ t} \pm \frac{3}{2} x + \text{f})$$

- **Ex.6** A non-uniform rope of mass M and length L has a variable linear mass density given by μ =kx where x is the distance from one end of the wire and k is a constant.
 - (a) Show that $M = kL^2/2$
 - (b) Show that the time required for a pulse generated at one end of the wire to travel to the other end is given by $t = \sqrt{8ML/9F}$ where F (constant) is the tension in the wire.
- Ex.7 One end of a long string of linear mass density 10⁻² kg m⁻¹ is connected to an electrically driven tuning fork of frequency 150 Hz. The other end passes over a pulley and is tied to a pan containing a mass of 90 kg. The pulley end absorbs all the incoming energy so that reflected waves from this end have negligible amplitude. At t = 0, the left end (fork end) of the string is at x = 0 has a transverse displacement of 2.5 cm and is moving along positive y-direction. The amplitude of the wave is 5 cm. Write down the transverse displacement y (in cm) as function of x (in m) and t (in sec) that describes the wave on the string.

Ans.
$$y = 5\sin\left\{\pi(300t - x) + \frac{\pi}{6}\right\}$$

- **Ex.8** If the tension in a stretched string fixed at both ends is changed by 20%, the fundamental frequency is found to increase by 15Hz. then the
 - (A) original frequency is 157 Hz
 - (B) velocity of propagation of the transverse wave along the string changes by 5%
 - (C) velocity of propagation of the transverse wave along the string changes by 10%.
 - (D) fundamental wave length on the string does not change.

Ans. (A,C,D)

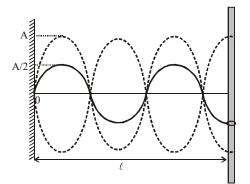
Ex.9 Here given snap shot at $t = \frac{T}{12}$ of a standing wave. Then the equations of the wave will be when particles are moving towards their extreme and when particles are moving towards the mean position respectively $\left(\text{Here, } T = \frac{2\pi}{\omega}\right)$.

(A)
$$y = A \sin kx \sin \omega t$$
, $y = A \sin \left(\omega t + \frac{2\pi}{3}\right) \sin kx$

(B)
$$y = A \sin kx \cos \omega t$$
, $y = A \sin \left(\omega t + \frac{2\pi}{3}\right) \sin kx$

(C)
$$y = A \cos kx \cos \omega t$$
, $y = A \cos \left(\omega t + \frac{2\pi}{3}\right) \sin kx$

(D)
$$y = A \cos kx \sin \omega t$$
, $y = A \cos \left(\omega t + \frac{2\pi}{3}\right) \cos kx$



Ans. (A)

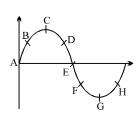
- **Ex.10** A standing wave of time period T is set up in a string clamped between two rigid supports. At t = 0 antinode is at its maximum displacement 2A.
 - (A) The energy density of a node is equal to energy density of an antinode for the first time at t = T/4.
 - (B) The energy density of node and antinode becomes equal after T/2 second.
 - (C) The displacement of the particle at antinode at $t = \frac{T}{8}$ is $\sqrt{2}A$
 - (D) The displacement of the particle at node is zero

Ans. (C,D)

EXERCISE (S-1)

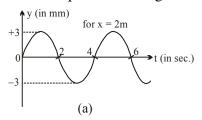
Wave equation

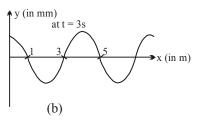
1. A transverse wave is travelling along a string from left to right. The figure represents the shape of the string (snap-shot) at a given instant. At this instant (a) which points have an upward velocity (b) which points will have downward velocity (c) which points have zero velocity (d) which points have maximum magnitude of velocity.



WA0001

- 2. A sinusoidal wave propagates along a string. In figure (a) and (b) 'y' represents displacement of particle from the mean position. 'x' & 't' have usual meanings. Find:
 - (a) wavelength, frequency and speed of the wave.
 - (b) maximum velocity and maximum acceleration of the particles
 - (c) the magnitude of slope of the string for x = 2 m at t = 4 sec.

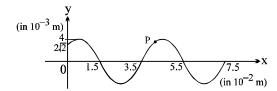




WA0002

- 3. A light pointer fixed to one prong of a tuning fork touches a vertical plate. The fork is set vibrating and plate is allowed to fall freely. 8 complete oscillations are counted when the plate falls through 10 cm. What is the frequency of the tuning fork?

 WA0003
- 4. A long uniform string of mass density 0.1 kg/m is stretched with a force of 40 N. One end of the string (x = 0) is oscillated transversely (sinusoidally) with an amplitude of 0.02 m and a period of 0.1 sec, so that travelling waves in the +x direction are set up.
 - (a) What is the velocity of the waves?
 - (b) What is their wavelength?
 - (c) If at the driving end (x = 0) the displacement (y) at t = 0 is 0.01 m with dy/dt negative, what is the equation of the travelling waves? **WA0004**
- 5. The figure shows a snap photograph of a vibrating string at t = 0. The particle P is observed moving up with velocity 20π cm/s. The angle made by string with x-axis at P is 6° .
 - (a) Find the direction in which the wave is moving
 - (b) the equation of the wave
 - (c) the total energy carried by the wave per cycle of the string, assuming that μ , the mass per unit length of the string = 50 gm/m.



Velocity of wave

6. The extension in a string, obeying Hooke's law is x. The speed of wave in the stretched string is v. If the extension in the string is increased to $1.5 \,\mathrm{x}$ find the new speed of wave.

WA0006

7. A uniform rope of length L and mass m is held at one end and whirled in a horizontal circle with angular velocity ω. Ignore gravity. Find the time required for a transverse wave to travel from one end of the rope to the other.

WA0007

8. A copper wire is held at the two ends by rigid supports. At 30°C, the wire is just taut, with negligible. Find the speed of transverse waves in this wire at 10°C.

Given : Young modulus of copper = $1.3 \times 10^{11} \text{ N/m}^2$.

Coefficient of linear expansion of copper = 1.7×10^{-5} °C⁻¹.

Density of copper = 9×10^3 kg/m³.

[IIT-1979]

WA0008

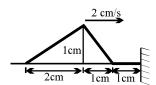
Energy of wave

9. A steel wire has a mass of 5g/m and is under tension 450 N. Find the maximum average power that can be carried by the transverse wave in the wire if the amplitude is not to exceed 20% of the wavelength.

WA0009

Superposition of waves

- 10. The figure shown a triangular pulse on a rope at t = 0. It is approaching a fixed end at 2 cm/s
 - (a) Draw the pulse at t = 2 sec.
 - (b) The particle speed on the leading edge at the instant depicted is _____.



WA0010

11. A 40 cm long wire having a mass 3.2 gm and area of cross-section 1 mm² is stretched between the supports 40.05 cm apart. In its fundamental mode it vibrate with a frequency 1000/64 Hz. Find the young's modulus of the wire.

WA0011

12. A plane wave given by equation $y = 0.04 \sin (0.5\pi x - 100\pi t)$, where x and y are in meter and t in sec is incident normally on a boundary between two media beyond which wave speed becomes doubled. State boundary condition and find the equation of the reflected and transmitted waves. Take x = 0 as the boundary between two media.

WA0012

13. A string between x = 0 and x = l vibrates in fundamental mode. The amplitude A, tension T and mass per unit length μ is given. Find the total energy of the string. [IIT-JEE 2003(Scr)]

$$x=0$$
 $x=l$

EXERCISE (S-2)

1. A long string under tension of 100 N has one end at x = 0. A sinusoidal wave is generated at x = 0

whose equation is given by $y = (0.01 \text{ cm}) \sin \left[\left(\frac{\pi x}{10} \text{ m} \right) - 50 \pi t \text{ (sec)} \right]$

- (i) Sketch the shape of the string at $t = \frac{1}{50}$ sec.
- (ii) Find the average power transmitted by the wave.
- (iii) Draw velocity time graph of particle at x = 5 m.

WA0014

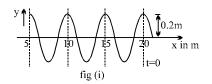
2. A string fixed at both ends is vibrating in the lowest mode of vibration for which a point at quarter of its length from one end is a point of maximum displacement. The frequency of vibration in this mode is 100 Hz. What will be the frequency emitted when it vibrates in the next mode such that this point is again a point of maximum displacement?

WA0015

3. A uniform string of length L and total mass M is suspended vertically and a transverse pulse is given at the top end of it. At the same moment a body is released from rest and falls freely from the top of the string. How far from the bottom does the body pass the pulse.

WA0016

- 4. A sinusoidal wave is moving along the positive x-direction as shown in figure (i) and (ii).
 - (i) Write the complete expression for the wave $y\left(x,t\right)$
 - (ii) Find the possible values of x_0 for which figure (ii) refers.





WA0017

5. A plane progressive wave of frequency 25 Hz, amplitude 2.5×10^{-5} m and initial phase zero propagates along the negative x-direction with a velocity of 300 m/s. At any instant, the phase difference between the oscillations at two points 6m apart along the line of propagation is, and the corresponding amplitude difference is m. [IIT-1997C]

78 JEE-Physics ALLEN

A steel wire 8×10^{-4} m in diameter is fixed to a support at one end and is wrapped round a cylindrical tuning peg 5 mm in diameter at the other end. The length of the wire between the peg and the support is 0.06 m. The wire is initially kept taut but without any tension. What will be the fundamental frequency of vibration of the wire if it is tightened by giving the peg a quarter of a turn? Density of steel = 7800 kg/m^3 , Y of steel = $20 \times 10^{10} \text{ N/m}^2$.

WA0020

7. A steel of wire of length 25 cm is fixed at its ends to rigid walls. Young's modulus of steel = $200 \,\text{GPa}$, coefficient of linear thermal expansion = 10^{-5} /°C. Initially, the wire is just taut at 20° C temperature. The density of steel = $8.0 \,\text{g/cc}$. A tuning fork of frequency $200 \,\text{Hz}$ is touched to the wire, to execute oscillations. Simultaneously, the temperature is slowly lowered. At what temperature will resonance occur corresponding to the third overtone?

WA0021

- 8. A non-uniform rope of mass M and length L has a variable linear mass density given by μ =kx where x is the distance from one end of the wire and k is a constant.
 - (a) Show that $M = kL^2/2$
 - (b) Show that the time required for a pulse generated at one end of the wire to travel to the other end is given by $t = \sqrt{8ML/9F}$ where F (constant) is the tension in the wire.

EXERCISE (O-1)

Wave equation

The function of x and t that does not represent a progressive wave is :-

(A) $y = 2 \sin(4t - 3x)$ (B) $y = e^{(4+(4t-3x))}$

- (C) $y = [4t 3x]^{-1}$ (D) y = [4t-3x]

WA0023

- At x = 0 particle oscillate by law $y = \frac{3}{2t^2 + 1}$. If wave is propagating along –ve x axis with velocity 2. 2m/s. Find equation of wave
 - (A) $y = \frac{3}{2\left(t \frac{x}{2}\right)^2 + 1}$ (B) $y = \frac{3}{2\left(t + \frac{x}{2}\right)^2 + 1}$ (C) $y = \frac{3}{2\left(t \frac{z}{2}\right)^2 + 1}$ (D) $y = \frac{3}{2\left(t + \frac{z}{2}\right)^2 + 1}$

WA0024

The shape of a wave propagating in the positive x or negative x-direction is given $y = \frac{1}{\sqrt{1 - x^2}}$ at 3.

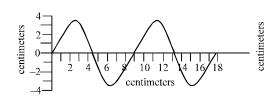
t = 0 and $y = \frac{1}{\sqrt{2 - 2x + x^2}}$ at t = 1s where x and y are in meters. The shape the wave disturbance

does not change during propagation. Find the velocity of the wave.

- (A) 1 m/s in positive x direction
- (B) 1 m/s in negative x direction
- (C) $\frac{1}{2}$ m/s in positive x direction
- (D) $\frac{1}{2}$ m/s in negative x direction

WA0025

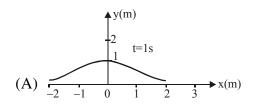
A transverse wave is travelling along a horizontal string. The first picture shows the shape of the string at an instant of time. This picture is superimposed on a coordinate system to help you make any necessary measurements. The second picture is a graph of the vertical displacement of one point along the string as a function of time. How far does this wave travel along the string in one second?

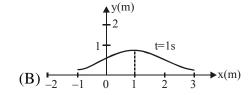


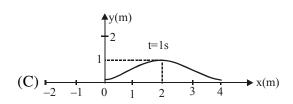
(A) 0.3 cm

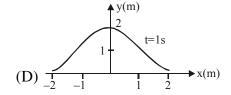
- (B) 3.0 cm
- - (C) 9.0 cm
- (D) 27 cm

A wave pulse is given by the equation $y = f(x, t) = A \exp(-B(x-vt)^2)$. Given $A = 1.0 \text{ m}^{-2}$ 5. and v = +2.0 m/s, which of the following graph shows the correct wave profile at the instant t = 1 s?









WA0027

6. The displacement from the position of equilibrium of a point 4 cm from a source of sinusoidal oscillations is half the amplitude at the moment t = T/6 (T is the time period). Assume that the source was at mean position at t = 0. The wavelength of the running wave is

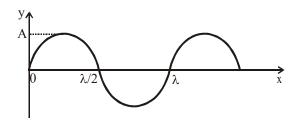
(A) 0.96 m

- (B) 0.48 m
- (C) 0.24 m
- (D) 0.12 m

WA0028

7. Here given snap shot of a progressive wave at t = 0 with time period = T. Then the equation of the wave if wave is going in +ve x-direction and if wave is going in -ve x-direction will be respectively.

$$\left(\text{Here, T} = \frac{2\pi}{\omega}\right)$$



- (A) $y = A \sin(kx + \omega t)$, $y = A \sin(kx \omega t)$
- (B) $y = A \cos(kx + \omega t)$, $y = A \cos(kx \omega t)$
- (C) $y = A \sin(\omega t kx)$, $y = A \sin(\omega t + kx)$
- (D) $y = A \sin(kx \omega t)$, $y = A \sin(kx + \omega t)$

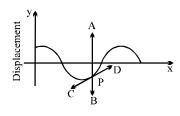
WA0029

8. A sinusoidal wave travelling in the positive direction of x on a stretched string has amplitude 2.0 cm, wavelength 1 m and wave velocity 5.0 m/s. At x = 0 and t = 0, it is given that displacement y = 0 and

 $\frac{\partial y}{\partial t}$ < 0. Express the wave function correctly in the form y = f(x, t):-

- (A) $y = (0.02 \text{ m}) \sin 2\pi (x-5t)$
- (B) $y = (0.02 \text{ cm}) \cos 2\pi (x-5t)$
- (C) $y = (0.02 \text{ m}) \sin 2\pi \left(x 5t + \frac{1}{4}\right)$ (D) $y = (0.02 \text{ cm}) \cos 2\pi \left(x 5t + \frac{1}{4}\right)$

9. The figure below shows a snap photograph of a simple harmonic progressive wave, progressing in the negative X-axis, at a given instant. The direction of the velocity of the particle at the stage P on the figure is best represented by the arrow.

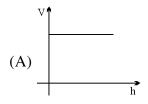


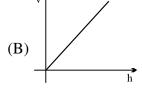
- (A) \overrightarrow{PA}
- (B) \overrightarrow{PB}
- (C) \overrightarrow{PC}
- (D) \overrightarrow{PD}

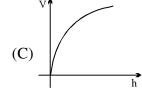
WA0031

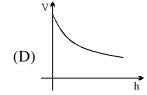
Velocity of wave

10. A uniform rope having some mass hanges vertically from a rigid support. A transverse wave pulse is produced at the lower end. The speed (v) of the wave pulse varies with height (h) from the lower end as:





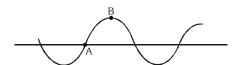




WA0032

Energy of wave

11. A progressive wave is travelling in a string as shown. Then which of the following statement about KE and potential energy of the elements A and B is true?



- (A) For point A: kinetic energy is maximum and potential energy is min.
- (B) For point B: kinetic energy is minimum and potential energy is min.
- (C) For point A: kinetic energy is minimum and potential energy is max.
- (D) For point B: kinetic energy is minimum and potential energy is max.

WA0033

12. The prong of a electrically operated tuning fork is connected to a long string of $\mu = 1$ kg/m and tension 25N. The maximum velocity of the prong is 1 cm/s, then the average power needed to drive the prong is:

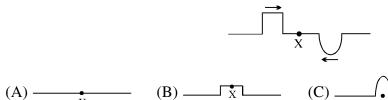


(B)
$$2.5 \times 10^{-4}$$
 W

(C)
$$1 \times 10^{-4} \text{ W}$$

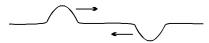
Superposition of waves

13. The diagram below shows two pulses traveling towards each other in a uniform medium with same speed. Pulses in the figure are at the same distance from X and has same height & width. Which diagram best represents the medium when the pulses meet at point X?



WA0035

14. Two symmetric, identical pulses of opposite amplitude travel along a stretched string in opposite directions as shown in the figure below. Which one of the following statements most fully describes



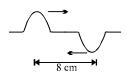
- (A) There is an instant when the string is straight
- (B) When the two pulses interfere completely, the energy of the wave is zero
- (C) There is a point on the string that does not move up or down
- (D) Both A and C

the situation?

(E) Both A and B

WA0036

15. Two pulses in a stretched string whose centres are initially 8 cm apart are moving towards each other as shown in figure. The speed of each pulse is 2 cm/s. After 2 seconds, the total energy of the pulses will be:-



(A) zero

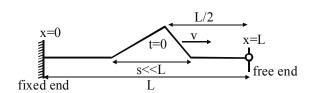
(B) purely kinetic

(C) purely potential

(D) partly kinetic and partly potential

WA0037

16. A small pulse travelling with speed v in a string is shown at t=0, moving towards free end. Which of these is not **CORRECTLY** matched.



- (i) $t = \frac{L}{v}$
- (P)
- (ii) $t = \frac{2L}{v}$
- (Q)
- (iii) $t = \frac{3L}{v}$
- (R)
- (A) (i)
- (B) (ii) (C) (iii)
- (D) None of these

$$\rightarrow$$
 μ_l μ_r

(A) 1 (B)
$$\frac{2}{1 + \sqrt{\mu_l / \mu_r}}$$
 (C) $\frac{2\sqrt{\mu_l / \mu_r}}{1 + \sqrt{\mu_l / \mu_r}}$ (D) $\frac{\sqrt{\mu_l / \mu_r} - 1}{\sqrt{\mu_l / \mu_r} + 1}$

WA0039

- A wave travels on a light string . The equation of the wave is $Y = A\sin(kx wt + 30^\circ)$. It is reflected 18. from a heavy string tied to an end of the light string at x = 0. If 64% of the incident energy is reflected the equation of the reflected wave is
 - $(A)Y = 0.8A\sin(kx wt + 30^{\circ} + 180^{\circ})$
- (B)Y = 0.8Asin(kx+wt+ 30° + 180°)

 $(C)Y = 0.8A\sin(kx+wt-30^{\circ})$

(D)Y = 0.8Asin(kx+wt+30°)

WA0040

- 19. A wave is represented by the equation $y = 10 \sin 2\pi (100t - 0.02x) + 10 \sin 2\pi (100t + 0.02x)$. The maximum amplitude and loop length are respectively
 - (A) 20 units and 30 units

(B) 20 units and 25 units

(C) 30 units and 20 units

(D) 25 units and 20 units

WA0041

- 20. A wave represented by the equation $y = A \cos(kx - \omega t)$ is superimposed with another wave to form a statioary wave such that the point x = 0 is a node. The equation of the other wave is:
 - $(A) A \sin(kx + \omega t)$
- $(B) A \cos(kx + \omega t)$ (C) $A \sin(kx + \omega t)$
- (D) A cos $(kx + \omega t)$

WA0042

21. Five waveforms moving with equal speeds on the x-axis

$$y_1 = 8 \sin(\omega t + kx)$$
; $y_2 = 6 \sin(\omega t + \frac{\pi}{2} + kx)$; $y_3 = 4 \sin(\omega t + \pi + kx)$; $y_4 = 2 \sin(\omega t + \frac{3\pi}{2} + kx)$;

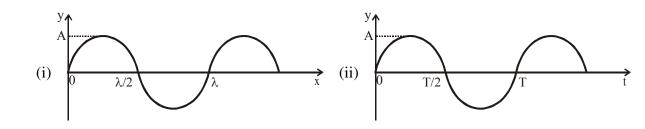
 $y_5 = 4\sqrt{2} \sin(\omega t - kx + \frac{\pi}{4})$ are superimposed on each other. The resulting wave is :

- (A) $8\sqrt{2} \cos kx \sin (\omega t + \frac{\pi}{4})$
- (B) $8\sqrt{2} \sin(\omega t kx + \frac{\pi}{4})$
- (C) $8\sqrt{2} \sin kx \cos (\omega t + \frac{\pi}{4})$
- (D) $8 \sin(\omega t + kx)$

nodeJ&\BCBA-BB\Kota\LEE[Advanose]\EMTHJSE\Phy\Woodule\Wove Optis, Wove on String & SoundWove\Eng\2-Woveon Shing\O1_Theory+Exp65

22. Here given figure (i) shows snap shot at t = T/4 and figure (ii) shows motion of particle at $x = \lambda/4$.

Then the possible equations of the wave will be $\left(\text{Here, T} = \frac{2\pi}{\Omega}\right)$:



(A)
$$y = A \sin \left(\omega t + kx - \frac{\pi}{2}\right)$$

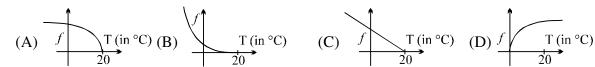
(B)
$$y = A \sin \left(\omega t - kx + \frac{\pi}{2}\right)$$

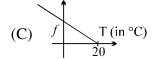
(C) Both
$$y = A \cos \left(\omega t + kx - \frac{\pi}{2}\right)$$
 and $y = A \cos \left(\omega t - kx + \frac{\pi}{2}\right)$

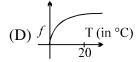
(D) Both
$$y = A \sin \left(\omega t + kx - \frac{\pi}{2}\right)$$
 and $y = A \sin \left(\omega t - kx + \frac{\pi}{2}\right)$

WA0044

23. A metal wire is clamped between two vertical walls. At 20 °C the unstrained length of the wire is exactly equal to the separation between walls. If the temperature of the wire is decreased the graph between fundamental frequency (f) and temperature (T) of the wire is







WA0045

- What is the fractional change in the tension necessary in a sonometer of fixed length to produce a note 24. one octave lower (half of original frequency) than before
 - (A) 1/4
- (B) 1/2
- (C) 2/3
- (D) 3/4(E) 2/1
 - WA0046
- 25. A string clamped at both ends is vibrating. At the moment the string looks flat, the instantaneous transverse velocity of points along the string, excluding its end-points, must be
 - (A) zero everywhere

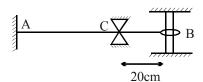
(B) dependent on the location along the string

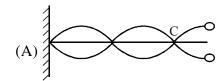
(C) non zero everywhere

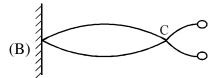
(D) non-zero and in the same direction everywhere

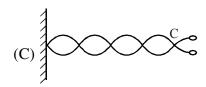
WA0047

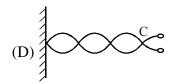
26. A 1m long wire having tension T is fixed at A and free at B. The point C, 20 cm from B is constrained to be stationary. What is shape of string for fundamental mode?











WA0048

- 27. The ends of a stretched wire of length L are fixed at x = 0 and x = L. In one experiment, the displacement of the wire is $y_1 = A \sin(\pi x/L) \sin \omega t$ and energy is E_1 and in another experiment its displacement is $y_2 = A\sin(2\pi x/L) \sin 2\omega t$ and energy is E_2 . Then [JEE 2001 (Scr)]
 - (A) $E_2 = E_1$
- (B) $E_2 = 2E_1$
- (C) $E_2 = 4E_1$
- (D) $E_2 = 16E_1$

1. Consider a hypothetical wave pulse (at time t = 0) given by the following (y, x in meter)

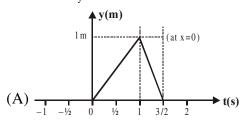
$$y = 0, x < 0$$

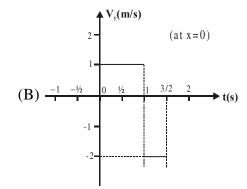
$$y = x/2, 2 > x \ge 0$$

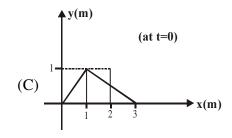
$$y = 3 - x, 3 \ge x \ge 2$$

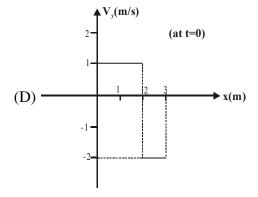
$$y = 0, x > 3$$

The pulse travels leftwards (negative x direction) at speed v = 2 m/s. Which of the following plots are correct? [V_v is the velocity of particle]



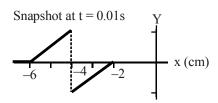


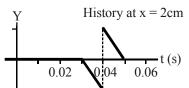




WA0050

2. Figure shows a snapshot graph and a history graph for a wave pulse on a stretched string. They describe the same wave from two perspectives.



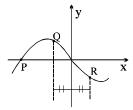


- (A) the wave is travelling in positive x-direction (B) the wave is travelling in negative x-direction
- (C) the speed of the wave is 2 m/s.
- (D) the peak is located at x = -6 cm at t = 0.

WA0051

Ε

3. At a certain moment, the photograph of a string on which a harmonic wave is travelling to the right is shown. Then, which of the following is true regarding the velocities of the points P, Q and R on the string.



- (A) v_p is upwards
- $(B) v_O = -v_R$
- $(C) | v_P | > | v_O | = | v_R | (D) v_O = v_R$

WA0052

- 4. An string has resonant frequencies given by 1001 Hz and 2639 Hz.
 - (A) If the string is fixed at one end only, 910 Hz can be a resonance frequency.
 - (B) If the string is fixed at one end only, 1911 Hz can be a resonance frequency.
 - (C) If the string is fixed at both the ends, 364 Hz can be one of the resonant frequency.
 - (D) 1001 Hz is definitely not the fundamental frequency of the string.

WA0053

- 5. In a travelling one dimensional mechanical sinusoidal, wave
 - (A) potential energy and kinetic energy of an element become maximum simultaneously.
 - (B) all particles oscillate with the same frequency and the same amplitude
 - (C) all particles may come to rest simultaneously
 - (D) we can find two particles, in a length equal to half of a wavelength, which have the same non zero acceleration simultaneously.

WA0054

Paragraph for Question Nos. 6 to 8

A wave represented by equation $y = 2(mm) \sin [4\pi (sec^{-1})t - 2\pi (m^{-1})x]$ is superimposed with another wave $y = 2 (mm) \sin [4\pi (sec^{-1})t + 2\pi (m^{-1})x + \pi/3]$ on a tight string.

- 6. Phase difference between two particles which are located at $x_1 = 1/7$ and $x_2 = 5/12$ is :-
 - (A) 0
- (B) $\frac{5\pi}{6}$
- (C) π
- (D) $\frac{5\pi}{3}$

WA0055

- **7.** Which of the following is not a location of antinode?
 - (A) $\frac{2}{3}$
- (B) $\frac{11}{12}$
- (C) $\frac{5}{12}$
- (D) $\frac{17}{12}$

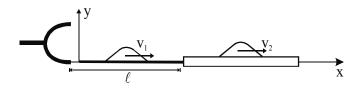
WA0055

- **8.** The location having maximum potential energy is
 - (A) 1/7
- (B) 1/6
- (C) 5/12
- (D) 23/12

Paragraph for Question Nos. 9 to 11

A harmonic oscillator at x = 0, oscillates with a frequency $\frac{\omega}{2\pi}$ and amplitude a. It is generating waves

at end of a thin string in which velocity of wave is v_1 and which is connected to another heavier string in which velocity of wave is v_2 as shown, length of first string is ℓ .



9. If harmonic oscillator oscillates by an equation $y = a \sin \omega t$. The equation of incident wave in first string is

(A)
$$y = a \sin \omega \left(t - \frac{x}{v_1} \right)$$

(B)
$$y = a \sin \omega \left(t + \frac{x}{v_1} \right)$$

(C)
$$y = a \sin \left[\omega \left(t - \frac{x}{v_1} \right) + \pi \right]$$

(D)
$$y = a \sin \left[\omega \left(t + \frac{x}{v_1} \right) + \pi \right]$$

WA0056

10. Equation of transmitted wave in second string if its amplitude is a is

(A)
$$y = a_t \sin \omega \left(t - \frac{x}{v_2} \right)$$

(B)
$$y = a_t \sin \omega \left(t - \frac{\ell}{v_1} \right)$$

(C)
$$y = a_t \sin \omega \left(t - \frac{\ell}{v_1} - \frac{x - \ell}{v_2} \right)$$

(D)
$$y = a_t \sin \omega \left(t - \frac{x}{v_2} \right)$$

WA0056

11. Equation of reflected wave, if it is reflecting at the joint and amplitude of reflected wave is a_R

(A)
$$y = a_R \sin \omega \left(t - \frac{x}{v_2} \right)$$

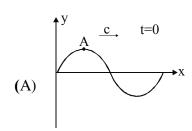
(B)
$$y = a_R \sin \left[\omega \left(t - \frac{\ell}{v_1} - \frac{\ell - x}{v_1} \right) + \pi \right]$$

(C)
$$y = a_R \sin \left[\omega \left(t + \frac{x}{v_1} \right) + \pi \right]$$

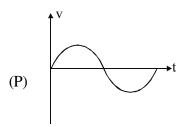
(D)
$$y = a_R \sin \left[\omega \left(t + \frac{2\ell + x}{v_1} \right) + \pi \right]$$

12. In column-I transverse waves travelling on a string at t = 0 is shown. Wave velocity is indicated by 'c'. Column-II describes variation of different parameters for particle A or for all the particles.

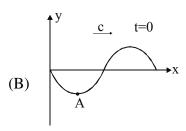
Column-I

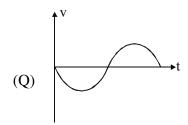


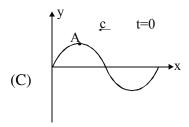
Column-II

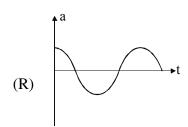


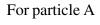
For particle A

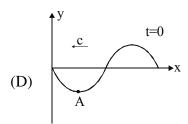


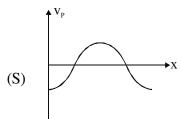




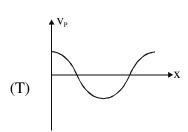








At t = 0 for all the particles



At t = 0 for all the particles

In a string a standing wave is set up whose equation is given as $y = 2A \sin kx \cos \omega t$. The mass per 13. unit length of the string is μ .

Column-I

Column-II

A) at
$$t = 0$$

Column-II

(P) Total energy per unit length at $x = 0$ is $2\mu A^2 \omega^2$.

(A) at
$$t = 0$$

(B) at $t = \frac{T}{8}$

Total energy per unit length at $x = \lambda/4$ is $2\mu A^2\omega^2$. (Q)

(C) at
$$t = \frac{T}{4}$$

Total energy per unit length at $x = \lambda$ is $2\mu A^2\omega^2$. (R)

(D) at
$$t = \frac{T}{2}$$

- power transmitted through a point at $x = \lambda$ is 0. **(S)**
- power transmitted through a point at $x = \lambda/4$ is 0. (T)

EXERCISE-JM

4	TD1 . •	of a wave on a	. •	C 1 *	1 .	$\Omega \Omega \Lambda \Lambda$	1	1
	The equation	of a wave on a	o etrina at	f linear macc	dencity	11 11/1 kg m-	1 10 O1V/	an hu
1.	THE CHUALION	OI a wave on a	a sume o	i iiiicai iiiass	uchsity	0.07 Kg III	15 21 11	JII 17 V

 $y = 0.02(m) \sin \left[2\pi \left(\frac{t}{0.04(s)} - \frac{x}{0.50(m)} \right) \right].$ The tension in the string is: [AIEEE - 2010]

- (1) 6.25 N
- (2) 4.0 N
- (3) 12.5 N
- (4) 0.5 N

WA0059

- 2. The transverse displacement y(x, t) of a wave on a string is given by $y(x, t) = e^{-(ax^2 + bt^2 + 2\sqrt{abx}t)}$. This represents a:-
 - (1) standing wave of frequency \sqrt{b}
- (2) standing wave of frequency $\frac{1}{\sqrt{b}}$
- (3) wave moving in +x direction with speed $\sqrt{\frac{a}{b}}$ (4) wave moving in -x direction with speed $\sqrt{\frac{b}{a}}$

WA0060

- 3. A travelling wave represented by $y = A \sin(\omega t kx)$ is superimposed on another wave represented by $y = A \sin(\omega t + kx)$. The resultant is:- [AIEEE-2011]
 - (1) A standing wave having nodes at $x = \left(n + \frac{1}{2}\right)\frac{\lambda}{2}$, n = 0, 1, 2
 - (2) A wave travelling along + x direction
 - (3) A wave travelling along –x direction
 - (4) A standing wave having nodes at $x = \frac{n\lambda}{2}$; n = 0, 1, 2

WA0061

- 4. A sonometer wire of length 1.5m is made of steel. The tension in it produces an elastic strain of 1%. What is the fundamental frequency of steel if density and elasticity of steel are 7.7×10^3 kg/m³ and 2.2 $\times 10^{11}$ N/m² respectively? [JEE-Main-2013]
 - (1) 188.5 Hz
- (2) 178.2 Hz
- (3) 200.5 Hz
- (4) 770 Hz

WA0062

- A uniform string of length 20m is suspended from a rigid support. A short wave pulse is introduced at its lowest end. It starts moving up the string. The time taken to reach the support is:

 (take $g = 10 \text{ ms}^{-2}$)

 [JEE-Main-2016]
 - (1) $\sqrt{2}$ s
- (2) $2\pi\sqrt{2}$ s
- (3) 2s
- (4) $2\sqrt{2}$ s

SELECTED PROBLEMS FROM JEE-MAINS ONLINE PAPERS

6. A heavy ball of mass M is suspended from the ceiling of a car by a light string of mass m (m<<M). When the car is at rest, the speed of transverse waves in the string is 60 ms⁻¹. When the car has acceleration a, the wave-speed increases to 60.5 ms⁻¹. The value of a, in terms of gravitational acceleration g, is closest to:

[JEE-Main-2019 Jan]

$$(1) \frac{g}{5}$$

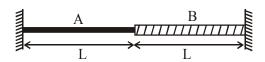
(2)
$$\frac{g}{20}$$

$$(3) \frac{g}{10}$$

$$(4) \frac{g}{30}$$

7. A wire of length 2L, is made by joining two wires A and B of same length but different radii r and 2r and made of the same material. It is vibrating at a frequency such that the joint of the two wires forms a node. If the number of antinodes in wire A is p and that in B is q then the ratio p : q is :

[JEE-Main-2019 April]



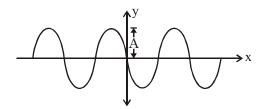
8. A string is clamped at both the ends and it is vibrating in its 4th harmonic. The equation of the stationary wave is $Y = 0.3 \sin(0.157x) \cos(200\pi t)$. The length of the string is: (All quantities are in SI units.)

[JEE-Main-2019_April]

$$(1) 20 \, \text{m}$$

$$(3) 60 \, \text{m}$$

9. A progressive wave travelling along the positive x-direction is represented by $y(x, t) = A \sin(kx - \omega t + \phi)$. Its snapshot at t = 0 is given in the figure:



For this wave, the phase ϕ is:

[JEE-Main-2019 April]

$$(2) - \frac{\pi}{2}$$

$$(3) \pi$$

$$(4) \frac{\pi}{2}$$

10. A transverse wave travels on a taut steel wire with a velocity of v when tension in it is 2.06×10^4 N. When the tension is changed to T, the velocity changed to v/2. The value of T is close to:

[JEE-Main-2020 Jan]

(1)
$$10.2 \times 10^2 \text{ N}$$

$$(2) 5.15 \times 10^3 \text{ N}$$

$$(3) 2.50 \times 10^4 \text{ N}$$

$$(4)\ 30.5 \times 10^4\ N$$

EXERCISE (JA)

- 1. A horizontal stretched string, fixed at two ends, is vibrating in its fifth harmonic according to the equation, $y(x, t) = (0.01\text{m}) \sin [(62.8 \text{ m}^{-1})x] \cos [(628 \text{ s}^{-1})t]$. Assuming $\pi = 3.14$, the correct statement(s) is (are)

 [JEE-Advance-2013]
 - (A) The number of nodes is 5.
 - (B) The length of the string is 0.25 m.
 - (C) The maximum displacement of the midpoint of the string, from its equilibrium position is 0.01m.
 - (D) The fundamental frequency is 100 Hz.

WA0065

2. One end of a taut string of length 3m along the x-axis is fixed at x = 0. The speed of the waves in the string is 100 ms^{-1} . The other end of the string is vibrating in the y direction so that stationary waves are set up in the string. The possible waveform (s) of these stationary waves is(are):-

[JEE-Advance-2014]

(A)
$$y(t) = A \sin \frac{\pi x}{6} \cos \frac{50\pi t}{3}$$

(B)
$$y(t) = A \sin \frac{\pi x}{3} \cos \frac{100\pi t}{3}$$

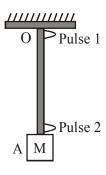
(C)
$$y(t) = A \sin \frac{5\pi x}{6} \cos \frac{250\pi t}{3}$$

(D)
$$y(t) = A \sin \frac{5\pi x}{2} \cos 250\pi t$$

WA0066

3. A block M hangs vertically at the bottom end of a uniform rope of constant mass per unit length. The top end of the rope is attached to a fixed rigid support at O. A transverse wave pulse (Pulse 1) of wavelength λ_0 is produced at point O on the rope. The pulse takes time T_{OA} to reach point A. If the wave pulse of wavelength λ_0 is produced at point A (Pulse 2) without disturbing the position of M it takes time T_{AO} to reach point O. Which of the following options is/are **correct**?

[JEE-Advance-2017]



- (A) The time $T_{AO} = T_{OA}$
- (B) The velocities of the two pulses (Pulse 1 and Pulse 2) are the same at the midpoint of rope
- (C) The wavelength of Pulse 1 becomes longer when it reaches point A
- (D) The velocity of any pulse along the rope is independent of its frequency and wavelength.

WA0067

94

4. Answer the following by appropriately matching the lists based on the information given in the paragraph.

A musical instrument is made using four different metal strings, 1,2,3 and 4 with mass per unit length μ , 2μ , 3μ and 4μ respectively. The instrument is played by vibrating the strings by varying the free length in between the range L_0 and $2L_0$. It is found that in string-1 (μ) at free length L_0 and tension T_0 the fundamental mode frequency is f_0 .

List-I gives the above four strings while list-II lists the magnitude of some quantity.

If the tension in each string is T_0 , the correct match for the highest fundamental frequency in f_0 units will be,

[JEE-Advance-2019]

List-I	List-II
(I) String- $1(\mu)$	(P) 1
(II) String-2 (2μ)	(Q) 1/2
(III) String-3 (3µ)	(R) $1/\sqrt{2}$
(IV) String-4 (4µ)	(S) $1/\sqrt{3}$
	(T) 3/16
	(U) 1/16
$(A) I \rightarrow P, II \rightarrow R, III \rightarrow S, IV \rightarrow Q$	(B) $I \rightarrow P$, $II \rightarrow Q$, $III \rightarrow T$, $IV \rightarrow S$
$(C) I \rightarrow Q, II \rightarrow S, III \rightarrow R, IV \rightarrow P$	(D) $I \rightarrow Q$, $II \rightarrow P$, $III \rightarrow R$, $IV \rightarrow T$ WA0068

5. Answer the following by appropriately matching the lists based on the information given in the paragraph.

A musical instrument is made using four different metal strings, 1,2,3 and 4 with mass per unit length μ , 2μ , 3μ and 4μ respectively. The instrument is played by vibrating the strings by varying the free length in between the range L_0 and $2L_0$. It is found that in string-1 (μ) at free length L_0 and tension T_0 the fundamental mode frequency is f_0 .

List-I gives the above four strings while list-II lists the magnitude of some quantity.

[JEE-Advance-2019]

List-I	List-II
(I) String-1(µ)	(P) 1
(II) String-2 (2µ)	(Q) 1/2
(III) String-3 (3µ)	(R) $1/\sqrt{2}$
(IV) String-4 (4 μ)	(S) $1/\sqrt{3}$
	(T) 3/16
	(U) 1/16
$(A)\:I{\rightarrow}P,\:II{\rightarrow}Q,\:III{\rightarrow}T,\:IV{\rightarrow}U$	$\text{(B) I} \rightarrow \text{T, II} \rightarrow \text{Q, III} \rightarrow \text{R, IV} \rightarrow \text{U}$
$(C) I \rightarrow P, II \rightarrow Q, III \rightarrow R, IV \rightarrow T$	(D) $I \rightarrow P$, $II \rightarrow R$, $III \rightarrow T$, $IV \rightarrow U$ WA0069

ANSWER KEY

EXERCISE (S-1)

- **1. Ans.** (a) DEF, (b) ABH, (c) CG, (D) AE
- **2.** Ans. (a) $\lambda = 4\text{m}$, $f = \frac{1}{4}$ Hz, 1 m/s, (b) $\frac{3\pi}{2}$ mm/s, $\frac{3\pi^2}{4}$ mm/s², (c) $\frac{3\pi}{2} \times 10^{-3}$ **3.** Ans. $40\sqrt{2}$
- **4.** Ans. (a) 20 m/s; (b) 2 m; (c) $y(x,t) = 0.02\sin(\pi x 20\pi t + \pi/6)$]
- **5. Ans.** (a) negative x; (b) $y = 4 \times 10^{-3} \sin 100\pi \left(3t + 0.5x + \frac{1}{400}\right) (x, y \text{ in meter})$; (c) $144\pi^2 \times 10^{-5} \text{ J}$
- 6. Ans. 1.22 v
- 7. Ans. $\frac{\pi}{\sqrt{2}\omega}$
- 8. Ans. 70 m/s
- 9. Ans. $10.8 \times 10^4 \text{W}$

- **10. Ans.** (a) , (b) 2 cm/s
- 11. Ans. $1 \times 10^9 \text{ Nm}^2$
- **12.** Ans. $A_t = \frac{4}{3}A_i$, $A_r = \frac{1}{3}A_i$, $y_r = -\frac{0.04}{3}\sin(0.5 \pi x + 100 \pi t)$; $y_t = +\frac{0.16}{3}\sin(0.25\pi x 100 \pi t)$
- **13.** Ans. $E = \frac{A^2 \pi^2 T}{A^T}$

EXERCISE (S-2)

- 1. Ans. (i) $\sqrt[9]{\frac{1}{0}}$ x (ii) 25 × 10⁻⁶ W (iii) $\sqrt[4]{\frac{\pi}{2}}$ 0.01 0.02 0.03 0.04 t, solved
- 2. Ans. 300 Hz
- 3. Ans. L/9
- 4. Ans. 0.2 $\cos[2\pi/5(x-10t)]$, (ii) 5n-(15/4)]

- 5. Ans. π , 0
- 6. Ans. 10800 Hz
- 7. Ans. 17.5°

EXERCISE (0-1)

- 1. Ans. (C)
- 2. Ans. (B)
- 3. Ans. (A)
- 4. Ans. (B)
- 5. Ans. (C)
- 6. Ans. (B)

- 7. Ans. (D)

- 8. Ans. (A)
- 9. Ans. (A)
- 10. Ans.(C)
- 11. Ans. (B)
- 12. Ans. (B)

- 13. Ans.(D)
- 14. Ans. (D)
- 15. Ans.(B)
- 16. Ans.(B)
- 17. Ans. (C)
- 18. Ans. (C)

- 19. Ans.(B)
- 20. Ans.(B)
- 21. Ans. (A)
- 22. Ans.(D)
- 23. Ans. (A)
- 24. Ans.(D)

- 25. Ans.(B)
- 26. Ans. (A)
- 27. Ans. (C)

EXERCISE (0-2)

1. Ans. (A,B,D)

2. Ans. (A,C,D)

3. Ans. (C,D)

4. Ans. (B,C,D)

5. Ans. (A,B,D)

6. Ans. (C)

7. Ans. (A)

8. Ans. (B)

9. Ans. (A)

10. Ans. (C)

11. Ans. (B)

12. Ans. (A)–(Q,S); (B)–(P,R,T); (C)–(Q,T); (D)–(P,R,S)

13. Ans. (A)–(P,R,S,T) ; (B)–(S,T) ; (C)–(Q,S,T) ; (D)–(P,R,S,T)

13. Ans. (A) -(P,R,S,T); (B) -(S,T); (C) -(Q,S,T); (D) -(P,R,S,T)

EXERCISE-JM

1. Ans. (1)

2. Ans. (4)

3. Ans. (1)

4. Ans. (2)

5. Ans. (4)

6. Ans. (1)

7. Ans. (4)

8. Ans. (2)

9. Ans. (3)

10. Ans. (2)

EXERCISE (JA)

1. Ans. (B,C)

2. Ans. (A,C,D)

3. Ans. (A,D)

4. Ans. (A)

5. Ans. (A)



hapter	03	3)(
Cont	tent	S_

SOUND WAVES

01.	THEORY	99
02.	EXERCISE (S-1)	117
03.	EXERCISE (S-2)	119
04.	EXERCISE (O-1)	122
05.	EXERCISE (O-2)	129
06.	EXERCISE (JM)	135
07.	EXERCISE (JA)	138
08.	ANSWER KEY	142

Important Notes

Sound is a mechanical three dimensional and longitudinal wave that is created by a vibrating source such as a guitar string, the human vocal cords, the prongs of a tuning fork or the diaphragm of a loudspeaker.

Sound waves are the most common example of longitudinal waves. They travel through any material waves. They travel through any material medium with a speed that depends on the properties of the medium. As the waves travel through air, the elements of air vibrate to produce changes in density and pressure along the direction of motion of the wave. If the source of the sound waves vibrates sinusoidally, the pressure variations are also sinusoidal. The mathematical description of sinusoidally, the pressure variations are also sinusoidal sound waves is very similar to that of sinusoidal string waves.

EQUATION OF SOUND WAVES

As the piston oscillates sinusoidally, regions of compression and rarefaction are continuously set up. The distance between two successive compressions (or two successive rarefactions) equals the wavelength λ . As these regions travel through the tube, any small element of the medium moves with simple harmonic motion parallel to the direction of the wave. If s(x, t) is the position of a small element relative to its equilibrium position, We can express this harmonic position function as

$$s(x, t) = s_{max} \cos(kx - \omega t)$$

Where s_{max} is the maximum position of the element relative to equilibrium. This is often called the displacement amplitude of the wave. The parameter k is the wave number and ω is the angular frequency of the piston . Note that the displacement of the element is along s, in the direction of propagation of the sound wave, which means we are describing a longitudinal wave.

Consider a thin disk-shaped element of gas whose circular cross section is parallel to the piston in figure. This element will undergo changes in position, pressure, and density as a sound wave propagates through the gas. From the definition of bulk modulus, the pressure variation in the gas is

$$\Delta P = -B \frac{\Delta V}{V_i}$$

The element has a thickness Δx in the horizontal direction and a cross-sectional area A, so its volume is $V_i = A\Delta x$. The change in volume ΔV accompanying the pressure change is equal to $A\Delta s$, where Δs is the difference between the value of s at $x + \Delta x$ and the value of s at x. Hence, we can express ΔP as

$$\Delta P = -B \frac{\Delta V}{V_i} = -B \frac{A\Delta s}{A\Delta x} = -B \frac{\Delta s}{\Delta x}$$

As Δx approaches zero, the ratio $\Delta s/\Delta x$ becomes ∂_S/∂_X (The partial derivative indicates that we are interested in the variation of s with position at a fixed time.) Therefore,

$$\Delta P = -B \frac{\partial s}{\partial x}$$

nodeO6\BOBA:BB\Kota\EEJAdvanced\\ENTHJSE\Ahy\Woodule\WoveOptics, Wavean Shing & Sound Wave\Līng\3:Sound Wave\0]_Theory+Ex.p65

If the position function is the simple sinusoidal function given by Equation, we find that

$$\Delta P = -B \frac{\partial}{\partial x} [s_{max} \cos(kx - \omega t)] = Bs_{max} k \sin(kx - \omega t)$$

$$\Delta P = \Delta P_{\text{max}} \sin (kx - \omega t)$$

Thus we can describe sound waves either in terms of excess pressure (equation 1.1) or in terms of the longitudinal displacement suffered by the particles of the medium.

If $s = s_0 \sin \omega (t - x/v)$ represents a sound wave where

s = displacement of medium particle from its mean position at x, then it can be proved that

$$P = P_0 \sin \{w(t - x/v) + \pi/2\} \qquad ... (3.2)$$

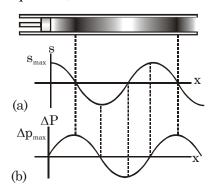


Figure: (a) Displacement amplitude and (b) pressure amplitude versus position for a sinusoidal longitudinal wave

represents that same sound wave where, P is excess pressure at position x, over and above the average atmospheric pressure and the pressure amplitude P_0 is given by

$$P_0 = \frac{B\omega s_0}{V} = BKs_0$$
 ... (3.3)

(B = Bulk modulus of the medium, K = angular wave number)

Note from equation (3.1) and (3.2) that the displacement of a medium particle and excess pressure at

any position are out of phase by $\frac{\pi}{2}$. Hence a displacement maxima corresponds to a pressure minima and vice-versa.

- Ex. The equation of a sound wave in air is given by $P = 0.2 \sin [3000 t 9x]$, where all variables are in S.I. units.
 - (a) Find the frequency, wavelength and the speed of sound wave in air.
 - (b) If the equilibrium pressure of air is 1.0×10^5 N/m², what are the maximum and minimum pressures at a point as the wave passes through that point?
- **Sol.** (a) Comparing with the standard form of a travelling wave

$$P = P_0 \sin \left[\omega \left(t - x/v\right)\right]$$

we see that $\omega 3000 \text{ s}^{-1}$. The frequency is

$$t = \frac{\omega}{2\pi} = \frac{3000}{2\pi} \text{ Hz}$$

Also from the same comparison, $\omega/v = 9.0 \text{ m}^{-1}$.

or,
$$v = \frac{\omega}{9.0 \, \text{m}^{-1}} = \frac{3000 \, \text{s}^{-1}}{9.0 \, \text{m}^{-1}}$$
 $\frac{1000}{3} \, \text{m/s}^{-1}$

The wavelength is
$$\lambda=\frac{v}{f}=\frac{1000/3m/s}{3000/2\pi\,Hz}=\frac{2\pi}{9}~m$$

(b) The pressure amplitude is $P_0 = 0.02 \text{ N/m}^2$. Hence, the maximum and minimum pressures at a point in the wave motion will be $(1.01 \times 10^5 \pm 0.02) \text{ N/m}^2$.

Sol. The pressure amplitude is

$$p_0 = \frac{4.0 \times 10^{-3} \text{ N/m}^2}{2} = 2 \times 10^{-3} \text{ N/m}^2$$

The displacement amplitude s_0 is given by

$$p_0 = Bks_0$$

or

$$s_0 = \frac{p_0}{Bk} = \frac{p_0 \lambda}{2\pi B}$$

$$= \frac{2 \times 10^{-3} \text{ N/m}^2 \times (40 \times 10^{-2} \text{ m})}{2 \times \pi \times 14 \times 10^4 \text{ N/m}^2} = \frac{200}{7\pi} \text{ A}$$
$$= 13.2 \text{ A}$$

SPEED OF SOUND WAVES:

Velocity of sound waves in a linear solid medium is given by

$$v = \sqrt{\frac{Y}{\rho}} \tag{4.1}$$

where Y = young's modulus of elasticity and ρ = density

Velocity of sound wave in a fluid medium (liquid or gas) is given by

$$v = \sqrt{\frac{B}{\rho}} \tag{4.2}$$

where, ρ = density of the medium and B = Bulk modulus of the medium given by,

$$B = -V \frac{dP}{dV}$$
 (4.3)

Newton's formula: Newton assumed propagation of sound through a gaseous medium to be an isothermal process.

$$PV = constant$$

$$\Rightarrow$$

$$\frac{\mathrm{dP}}{\mathrm{dV}} = \frac{-P}{V}$$

and

hence
$$B = P$$

and thus he obtained for velocity of sound in a gas.

$$v = \sqrt{\frac{P}{\rho}} = \sqrt{\frac{RT}{M}}$$
 where $M = molar$ mass

Laplace's correction: Later Laplace established that propagation of sound in a gas is not an isothermal but an adiabatic process and hence PV' = constant

$$\Rightarrow \frac{dP}{dV} = -\gamma \frac{P}{V}$$

where,
$$B = -V \frac{dP}{dV} = \gamma P$$

and hence speed of sound in a gas,

$$v = \sqrt{\frac{\gamma P}{\rho}} = \sqrt{\frac{\gamma RT}{M}} \tag{4.4}$$

FACTORS AFFECTING SPEED OF SOUND IN ATMOSPHERE

- (a) Effect of temperature: as temperature (T) increases velocity (v) increases. For small change in temperature above room temperature v increases linearly by 0.6 m/s for every 1°C rise in temp.
- **(b) Effect of humidity:** With increase in humidity density decreases. This is because the molar mass of water vapour is less than the molar mass of air.
- (c) Effect of pressure:

The speed of sound in a gas is given by $v = \sqrt{\frac{\gamma P}{P}} = \sqrt{\frac{\gamma RT}{M}}$

So at constant temperature, if P changes then ρ also changes in such a way that P/ ρ remains constant. Hence pressure does not have any effect on velocity of sound as long as temperature is constant.

Ex. The constant γ for oxygen as well as for hydrogen is 1.40. If the speed of sound in oxygen is 450 m/s, what will be the speed of hydrogen at the same temperature and pressure?

Sol.
$$v = \sqrt{\frac{\gamma RT}{M}}$$

since temperature, T is constant

$$\therefore \quad \frac{v_{(H_2)}}{v_{(O_2)}} = \sqrt{\frac{M_{O_2}}{M_{H_2}}} = \sqrt{\frac{32}{2}} = 4$$

$$\Rightarrow$$
 v(H₂) = 4 × 450 = 1800 m/s

Aliter : The speed of sound in a gas is given by $u = \sqrt{\frac{\gamma P}{\rho}}$. At STP, 22.4 litres of oxygen has a mass

of 32g whereas the same volume of hydrogen has a mass of 2g. Thus, the density of oxygen is 16times the density of hydrogen at the same temperature and pressure. As γ is same for both the gases.

$$\frac{f_{(\text{hydrogen})}}{f_{(\text{oxygen})}} = \sqrt{\frac{\rho_{(\text{oxygen})}}{\rho_{(\text{hydrogen})}}}$$

$$f_{\text{(hydrogen)}} = 4f_{\text{(oxygen)}} = 4 \times 450 \text{ m/s} = 1800 \text{ m/s}$$

INTENSITY OF PERIODIC SOUND WAVES

Like any other progressive wave, sound waves also carry energy from one point of space to the other. This energy can be used to work, for example, forcing the eardrums to vibrate or in the extreme case of a sonic boom created by supersonic jet, can even cause glass panes of windows to crack.

The amount of energy carried per unit by a wave is called its power and power per unit area held perpendicular a sound wave travelling along positive x-axis described by the equation.

We define the intensity I of a wave, or the power per unit area, to be the rate at which the energy being transported by the wave transfers through a unit area A perpendicular to the direction of travel of the wave:

$$I = \frac{P}{A}$$

In the present case, therefore, the intensity is

$$I = \frac{P}{A} = \frac{1}{2} \rho A v (\omega s_{max})^2$$

Thus, we see that the intensity of a periodic sound wave is proportional to the square of the displacement amplitude and to the square of the angular frequency (as in the case of a periodic string wave). this can also be written in terms of the pressure amplitude ΔP_{max} ; in this case, we use Equation to obtain

$$I = \frac{\Delta P_{\text{max}}^2}{2ov}$$

- Ex. The pressure amplitude in a sound wave from a radio receiver is 4.0×10^{-3} N/m² and the intensity at a point is 10^{-6} W/m². If by fuming the "Volume" knob the pressure amplitude is increased to 6×10^{-3} N/m², evaluate the intensity.
- **Sol.** The intensity is proportional to the square of the pressure amplitude.

Thus,
$$\frac{I'}{I} = \left(\frac{p_0'}{p_0}\right)^2$$

or
$$I' = \left(\frac{p_0'}{p_0}\right)^2 I = \left(\frac{p_0'}{p_0}\right)^2 \times 10^{-6} \text{ W/m}^2 = 2.25 \times 10^{-16} \text{ W/m}^2.$$

APPEARANCE OF SOUND TO HUMAN EAR

Pitch and Frequency

Frequency as we have discussed till now is an objective property measured its units of Hz and which can be assigned a unique value. However a person's perception of frequency is subjective. The brain interprets frequency primarily in terms of a subjective quality called Pitch. A pure note of high frequency is interpreted as high-pitched sound and a pure note of low frequency as low-pitched sound.

Pitch of a sound is that sensation by which we differentiate a buffalo voice, a male voice is of low pitch, a male voice has higher pitch and a female voice has (generally) still higher pitch. This sensation primarily depends on the dominant frequency present in the sound. Higher the frequency, higher will be the pitch and vice versa. The dominant frequency of a buffalo voice is smaller than that of a male voice which in turn is smaller than that of a female voice.

Loudness and Intensity

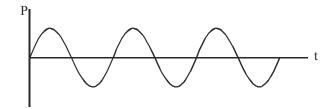
The loudness that we sense is related to the intensity of sound through it is not directly proportional to it. Our perception of loudness is better correlated with the sound level measured in decibels (abbreviated and dB) and defined as follows.

$$\beta = 10 \log_{10} \left(\frac{I}{I_0} \right),\,$$

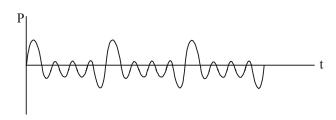
where I is the intensity of the sound and I_0 is a constant reference intensity 10^{-12} W/m². The reference intensity represents roughly the minimum intensity that is just audible at intermediate frequencies. For $I = I_0$, the sound level $\beta = 0$. Table shows the approximate sound levels of some of the sounds commonly encountered.

Quality and Waveform

A sound generated by a source may contain a number of frequency components in it. Different frequency components have different amplitudes and superposition of them results in the actual waveform. The appearance of sound depends on this waveform apart from the dominant frequency and intensity. Figure shows waveforms for a tuning fork, a clarinet and a cornet playing the same note (fundamental frequency = 440 Hz) with equal loudness.







We differentiate between the sound from a table and that from a mridang by saying that they have different quality. A musical sound has certain well-defined frequencies which have considerable amplitude. These frequencies are generally harmonics of a fundamental frequency. Such a sound is particularly pleasant to the ear. On the other hand, a noise has frequencies that do not bear well-defined relationship among themselves.

Sol.
$$\beta_1 = 10 \log \frac{I_1}{I_0}$$

$$\beta_2 = 10 \log \frac{I_2}{I_0} \implies \beta_2 - \beta_1 = 10 \log \frac{I_2}{I_1}$$
 or $10 = 10 \log_{10} \left(\frac{I_2}{I_1}\right)$

$$\Rightarrow \frac{I_2}{I_1} = 10^1 = 10$$

for point source
$$I \propto \frac{1}{r^2} \Rightarrow \frac{r_1}{r_2} = \sqrt{\frac{I_2}{I_1}} = \sqrt{10}$$

INTERFERENCE OF SOUND WAVES:

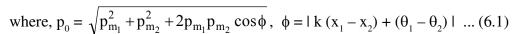
If
$$p_1 = p_{m1} \sin (\omega t - kx_1 + \theta_1)$$

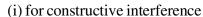
and $p_2 = p_{m2} \sin (\omega t - kx_2 + \theta_1)$

resultant excess pressure at point O is

$$p = p_1 + p_2$$

$$\Rightarrow p = p_0 \sin(\omega t - kx + \theta)$$





$$\phi = 2n\pi \qquad \Rightarrow p_0 = p_{m1} + p_{m2}$$

(ii) for destructive interference

$$\phi = (2n + 1) \pi \qquad \Rightarrow p_0 = |p_{m1} - p_{m2}|$$

If ϕ is only due to path difference, then $\varphi=\frac{2\pi}{\lambda}~\Delta x,$ and

Condition for constructive interference : $\Delta x = n\lambda$, $n = 0, \pm 1, \pm 2$

Condition for destructive interference :
$$\Delta x = (2n + 1) \frac{\lambda}{2}$$
, $n = 0 \pm 1, \pm 2$

from equation (6.1)

$$P_0^2 = P_{m_1}^2 + P_{m_2} + 2P_{m_1} P_{m_2} \cos \phi$$

Since intensity, $I \propto (Pressure amplitude)^2$,

we have, for resultant intensity, $I = I_1 + I_2 + 2\sqrt{I_2I_2}\cos\phi$... (6.2)

If
$$I_1 = I_2 = I_0$$

 $I = 2I_0 (1 + \cos \phi)$

$$\Rightarrow I = 4I_0 \cos^2 \frac{\phi}{2} \qquad \dots (6.3)$$

Hence in this case,

for constructive interference : $\phi = 0.2\pi$, 4π and $I_{max} = 4I_0$ and for destructive interference : $\phi = \pi$, 3π and $I_{min} = 0$

Coherence: Two sources are said to be coherent if the phase difference between them does not change with time. In this case their resultant intensity at any point in space remains constant with time. Two independent sources of sound are generally incoherent in nature, i.e. phase difference between them changes with time and hence the resultant intensity due to them at any point in space changes with time.

Ex. Figure shows a tube structure in which a sound signal is sent from one end and is received at the other end. The semicircular part has a radius of 10.0 cm. The frequency of the sound source can be varied from 1 to 10 kHz. Find the frequencies at which the ear perceives maximum intensity. The speed of sound in air = 342 m/s.



Sol. The sound wave bifurcates at the junction of the straight and the semicircular parts. The wave through the straight part travels a distance $s_1 = 2 \times 10$ cm and the wave through the curved part travels a distance $s_2 = \pi 10$ cm = 31.4 cm before they meet again and travel to the receiver. The path difference between the two waves received is, therefore.

$$\Delta s = s_2 - s_1 = 31.4 \text{ cm} - 20 \text{ cm} = 11.4 \text{ cm}$$

The wavelength of either wave is $\frac{v}{v} = \frac{330 \text{ m/s}}{v}$. For constructive interference, $\Delta p = n\lambda$, where n is an integer.

or,
$$\Delta p = n \cdot \frac{v}{v}$$
 $\Rightarrow v = \frac{n \cdot v}{\Delta p} \Rightarrow \frac{n \cdot 342}{(0.114)} = 3000 \text{ n}$

Thus, the frequencies within the specified range which cause maximum of intensity are 3000×1 3000×2 and 3000×3 Hz

LONGITUDINAL STANDING WAVES:

Two longitudinal waves of same frequency and amplitude travelling in opposite directions interfere to produce a standing wave.

If the two interfering wave are given by

$$p_1 = p_0 \sin(\omega t - kx)$$

and $p_2 = p_0 \sin(\omega t + kx + \phi)$

then the equation of the resultant standing wave would be given by

$$p + p_1 + p_2 = 2p_0 \cos(kx + \frac{\phi}{2}) \sin(\omega t + \frac{\phi}{2})$$

$$\Rightarrow p = p_0' \sin(\omega t + \frac{\phi}{2}) \qquad \dots (8.1)$$

VIBRATION OF AIR COLUMNS

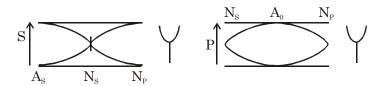
Standing waves can be set up in air-columns trapped inside cylindrical tubes if frequency of the tuning fork sounding the air column matches one of the natural frequency of air columns. In such a case the sound of the tuning fork becomes markedly louder, and we say there is resonance between the tuning fork and air column. To determine the natural frequency of the air column, notice that there is a displacement node (pressure antinode) at each closed end of the tube as air molecules there are not free to move, and a displacement antinode (pressure-node) at each open end of the air-column. In reality antinodes do not occurs exactly at the open end but a little distance outside. However if diameter of tube is small compared to its length, this end correction can be neglected.

Closed organ pipe

(In the diagram, A_p = Pressure antinode, A_S = displacement antinode, N_p = pressure node, N_s = displacement node.)

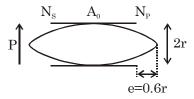


Open organ pipe:



End correction: As mentioned earlier the displacement antinode at an open end of an organ pipe lies slightly outside the open lend. The distance of the antinode from the open end is called end correction and its value is given by

$$e = 0.6 r$$



where r = radius of the organ pipe.

with end correction, the fundamental frequency of a closed pipe (f_c) and an open argon pipe (f_0) will be given by

$$f_c = \frac{v}{4(\ell + 0.6r)} \text{ and}$$

$$f_0 = {v \over 2(\ell + 1.2r)}$$
(9.5)

Ex. A tuning fork is vibrating at frequency 200 Hz. When another tuning fork is sounded simultaneously, 6 beats per second are heard. When some mass is added to the tuning fork of 200 Hz, beat frequency decreases. Find the frequency of the other tuning fork.

Sol.
$$|f - 200| = 6$$

$$\Rightarrow$$
 f = 194 or 206

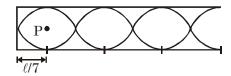
when 1st tuning fork is loaded its frequency decreases and so does beat frequency

$$\Rightarrow 200 > f$$

$$\Rightarrow$$
 f = 194 Hz

- **Ex.** A closed organ pipe has length ' ℓ '. The air in it is vibrating in 3^{rd} overtone with maximum amplitude 'a'. Find the amplitude at a distance of $\ell/7$ from closed end of the pipe.
- **Sol.** The figure shows variation of displacement of particles in a closed organ pipe for 3rd overtone.

For third overtone
$$\ell = \frac{7\lambda}{4}$$
 or $\lambda = \frac{4\ell}{7}$ or $\frac{\lambda}{4} = \frac{\ell}{7}$



Hence the amplitude at P at a distance $\frac{\ell}{7}$ from closed end is 'a' because there is an antinode at that point.

BEATS

When two sound waves of same amplitude and different frequency superimpose, then intensity at any point in space varies periodically with time. This effect is called beats.

If the equation of the two interfering sound waves emitted by s_1 and s_2 at point O are,

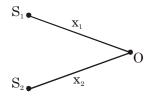
$$p_1 = p_0 \sin (2\pi f_1 t - kx_1 + \theta_1)$$

$$p_2 = p_0 \sin (2\pi f_2 t - kx_2 + \theta_2)$$

By principle of superposition

$$p = p_1 + p_2$$

$$= 2\pi_0 \cos \left\{ \pi (f_1 - f_2)t + \frac{\theta_1 + \theta_2}{2} \right\} \sin \left\{ \pi (f_1 + f_2)t + \frac{\theta_1 + \theta_2}{2} \right\}$$



i.e., the resultant sound at point O has frequency $\left(\frac{f_1+f_2}{2}\right)$ while pressure amplitude p_0' (t) variex

with time as

$$p_0(t) = 2p_0 \cos \left\{ \pi (f_1 - f_2)t + \frac{\phi_1 + \phi_2}{2} \right\}$$

Hence pressure amplitude at point O varies with time with a frequency of $\left(\frac{f_1-f_2}{2}\right)$.

Hence sound intensity will vary with a frequency $f_1 - f_2$.

This frequency is called beat frequency (f_B) and the time interval between two successive intensity maxima (or minima) is called beat time period (T_B)

$$f_B = f_1 - f_2$$

$$T_{B} = \frac{1}{f_1 - f_2}$$

IMPORTANT POINTS:

- (i) The frequency $|f_1 f_2|$ should be less than 16 Hz, for it to be audible.
- (ii) Beat phenomenon can be used for determining an unknown frequency by sounding it together with a sound of known frequency.
- **Ex.** Two strings X and Y of a sitar produces a beat of frequency 4Hz. When the tension of string Y is slightly increased, the beat frequency is found to be 2Hz. If the frequency of X is 300 Hz, then the original frequency of Y was.

Ans. 296 Hz

DOPPLER EFFECT

We can express the general relationship for the observed frequency when a source is moving and an observer is at rest as equation, with the same sign convention applied to vs as was applied to v0: a positive value is substituted for vs when the source moves toward the observer and a negative value is substituted when the source moves away from the observer.

Finally, we find the following general relationship for the observed frequency:

$$f' = \left(\frac{v + v0}{v - vs}\right) f$$

In this expression, the signs for the values substituted for v0 and vs depend on the direction of the velocity. A positive value is used for motion of the observer or the source toward the other, and a negative sign for motion of one away from the other.

A convenient rule concerning signs for you to remember when working with all Doppler effect problems is as follows:

The word toward is associated with an increase in observed frequency. The words away from are associated with a decrease in observed frequency.

- **Ex.** A submarine (sub A) travels through water at a speed of 8.00 m/s, emitting a sonar wave at a frequency of 1400 Hz. The speed of sound in the water is 1533 m/s. A second submarine (sub B) is located such that both submarines are traveling directly toward one another. The second submarine is moving at 9.00 m/s.
 - (A) What frequency is detected by an observer riding on sub B as the subs approach each other?
 - (B) The subs barely miss each other and pass. What frequency is detected by an observer riding on sub B as the subs recede from each other?
- **Sol.** (A) We use equation to find the Doppler shifted frequency. As the two submarines approach each other, the observer in sub B hears the frequency

$$f' = \left(\frac{v + v0}{v - vs}\right) f = \left(\frac{1533m/s + (+9.00m/s)}{1533m/s - (+8.00m/s)}\right) (1400 \text{ Hz}) = 1416 \text{ Hz}$$

oddoó 1808A: 86 Koro J.EEFAdvanced|\FNTHJSE\ffy\Woodule\WaveOptics, Wovean Shing & Saund Wove\Eng\3-Saund Wove\01_Theory+Exp65

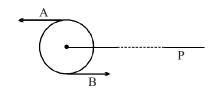
(B) As the two submarines recede from each other, the observer in sub B hears the frequency

$$f' = \left(\frac{v + v0}{v - vs}\right) f$$

$$= \left(\frac{1533 \text{m/s} + (-9.00 \text{m/s})}{1533 \text{m/s} - (-8.00 \text{m/s})}\right) (1400 \text{ Hz}) = 1385 \text{ Hz}$$

- Ex. A whistle of frequency 540 Hz is moving in a circle of radius 2m at a constant angular speed of 15rad/s. What are the lowest and height frequencies heard by a listener standing at rest, a long distance away from the centre of the circle? (velocity of sound in air is 330 m/s ft/sec.)
- **Sol.** The whistle is moving along a circular path with constant angular velocity ω . The linear velocity of the whistle is given by

$$v_s = \omega R$$



where, R is radius of the circle

At points A and B, the velocity v_s of whistle is parallel to line OP, i.e. with respect to observer at P, whistle has maximum velocity v_s away from P at point A, and towards P at point B. (Since distance OP is large compared to radius R, whistle may be assumed to be moving along line OP)

Observer, therefore, listens maximum frequency when source is at B moving towards observer.

$$f_{\text{max}} = f \frac{v}{v - v_s} = 540 \times \frac{330}{330 - 30} = 540 \times \frac{330}{300} = 594 \text{ Hz}$$

where, v is speed of sound in air. Similarly, observer listens minimum frequency when source is at A, moving away from observer.

$$f_{min} = \frac{f v}{v + v_s} = 540 \times \frac{330}{360} = 495 \text{ Hz}$$

1. Vibrating air columns:

- (i) In a pipe of length L closed at one end, the fundamental note has a frequency $f_1 = \frac{v}{4L}$, where v is the velocity of sound in air.
- (ii) The first overtone $f_2 = \frac{v}{L} = 2f_1$

2. Propagation of sound in solids:

- (i) The velocity of propagation of a longitudinal wave in a rod of Young's modulus Y and density ρ is given by $v = \sqrt{\frac{Y}{\rho}}$
- (ii) In a sonometer wire of length L and mass per unit length m under tension T vibrating in n loops

$$f_n = \frac{n}{2L} \sqrt{\frac{T}{m}}$$

ALLEN

(iii) Propagation of sound in gases

Laplace formula $v = \sqrt{\frac{\gamma P}{\rho}}$ where γ is the ratio of specific heats, P is the pressure and ρ is the density.

$$\frac{v_t}{v_0} = \sqrt{\frac{T}{T_0}} = \sqrt{\frac{273 + t}{273}}$$

3. Doppler Effect:

(i) When a source of sound moves with a velocity v_s in a certain direction, the wavelength decreases in front of the source and increases behind the source.

$$\lambda'$$
 (in front) = $\frac{v - v_s}{f_s}$; $f' = \frac{v}{\lambda'} = \frac{v}{v - v_s} f_s$

$$\lambda'''$$
(behind) = $\frac{v + v_s}{f_s}$; $f'' = \frac{v}{\lambda''} = \frac{v}{v + v_s} f_s$

Here v is the velocity of sound in air.

- (ii) The apparent frequency = $\frac{v v_0}{v} f_s$
- (a) When the source is moving towards the observer and the observer is moving away from the source, the apparent frequency

$$f_a = \frac{v - v_0}{v - v_0} f_s$$

$$v_0$$
 o v_s s

(b) When the source and the observer are moving towards each other.

$$f_{a} = \frac{v + v_{0}}{v - v_{s}} f_{s}$$

(c) When the source and observer are moving away from each other,

$$f_{a} = \frac{v - v_{0}}{v + v_{s}} f_{s}$$

$$v_0$$
 o \overline{s} v_s

(d) When the source is moving away from the observer and the observer is moving towards the source

$$f_a = \frac{v + v_0}{v + v_s} f_s$$

$$\overline{o}$$
 $\overline{v_0}$ \overline{s} $\overline{v_s}$

Here all velocities are relation to the medium.

4. Loudness of sound:

The loudness level B of sound is expressed in decibels, $B = 10 \log \frac{I}{I_0}$ where I is the intensity, I_0 is a reference intensity.

5. Beats:

When two tuning forks of close but different frequencies f_1 and f_2 are vibrating simultaneously at nearby places, a listener observes a fluctuation in the intensity of sound, called beats. The number of beats heard per second is $f_1 - f_2$.

WORKED OUT EXAMPLES

- Ex.1 It is found that an increase in pressure of 100 kPa causes a certain volume of water to decrease by 5×10^{-3} percent of its original volume. Then the speed of sound in the water is about (density of water 10^3 kg/m³)
 - (A) 330 m/s
- (B) 1414 m/s
- (C) 1732 m/s
- (D) 2500 m/s

- Ans. (B)
- **Sol.** Bulk modulus $\beta = -\frac{\Delta P}{\frac{\Delta v}{v}} = \frac{100 \times 10^3}{\frac{5 \times 10^{-3}}{100}} = 2 \times 10^9$

speed v =
$$\sqrt{\frac{\beta}{\rho}} = \sqrt{\frac{2 \times 10^9}{10^3}} \approx 1414 \text{ m/s}$$

- Ex.2 A sound wave is travelling in a uniform pipe with gas of adiabatic exponent γ . If u is the particle velocity at any point in medium and c is the wave velocity, then relative change in pressure $\frac{dP}{P}$ while wave passes through this point is :-
 - (A) $\frac{u}{vc}$
- (B) $\gamma \sqrt{\frac{u}{c}}$
- (C) $\gamma \frac{u}{c}$
- (D) $\frac{u^2}{vc^2}$

- Ans. (C)
- **Sol.** $\Delta P = -B \left(\frac{dv}{v} \right)$
 - $\Delta P = -B \left(\frac{\delta y}{\delta x} \right)$
 - $\Delta P = -\gamma P \frac{\delta y}{\delta x}$
 - $\frac{\Delta P}{P} = \gamma \left(\frac{u}{c}\right)$

Ex.3

- (A) 5:3
- (B) 3:5
- (C) 25:9

A point source emits sound equally in all directions in a non-absorbing medium. Two points P and Q are at a distance of 9 meters and 25 meters respectively from the source. The ratio of the amplitudes

(D) 625:81

Ans. (C)

Sol.
$$I \propto A^2$$
, $I \propto \frac{1}{r^2}$, $\frac{A_1}{A_2} = \frac{r_2}{r_1}$

Ex.4 In a resonance tube experiment, an 80 cm air column is in resonance with a turning fork in first overtone. Which equation can represent correct pressure variation in the air column (x = 0 is the top point of the tube, neglect end correction, speed of sound = 320 m/sec):-

(A) A sin
$$\frac{15\pi}{8}x\cos 600\pi t$$

(B) A cos
$$\frac{15\pi}{8}x \sin 600 \pi t$$

(C) A cos
$$\frac{15\pi}{8}x \sin 300 \pi t$$

(D) A sin
$$\frac{15\pi}{8}x \sin 300 \pi t$$

Ans. (A)

Sol.
$$\frac{\omega}{k} = 320$$

Ex.5 The displacement of the medium in a sound wave is given by the equation; $y_1 = A\cos(ax + bt)$ where A, a & b are positive constants. The wave is reflected by an obstacle situated at x = 0. The intensity of the reflected wave is 0.64 times that of the incident wave.

- (a) what are the wavelength & frequency of the incident wave.
- (b) write the equation for the reflected wave.

(c) in the resultant wave formed after reflection, find the maximum & minimum values of the particle speeds in the medium.

Ans. (a) $2 \pi/a$, $b/2\pi$, (b) $y_2 = \pm 0.8 \text{ A} \cos (ax - bt)$, (c) max.=1.8 b A, min. = 0,

Sol. (a) $\omega = b \& k = a$

$$f = \frac{2\pi}{\omega} \& \lambda = \frac{2\pi}{k}$$

(b) I \propto A²

So
$$A_{r} = 0.8 \text{ A}$$

(c)
$$(A_{\text{net}})_{\text{max}} = A + 0.8 A = 1.8 A$$

Ex.6 An observer moves towards a stationary source of sound, with a velocity one-fifth of the velocity of sound. what is the percentage increase in the apparent frequency? [AIEEE - 2005]

- (1) zero
- (2) 0.5%
- (3)5%
- (4) 20%

Ans.

(4)

Sol.
$$\frac{f_{app}}{f} = \left(\frac{v + \frac{v}{5}}{v}\right) = \frac{6}{5}$$

node06\B08A-B8\Koto\EE|Advanced\BVITHJSE\Ry\Woodu|e\WoveOptics, Wovean Shing&Sound Wove\bng\3-Sound Wove\0) _Theory+Ex.p65

- Ex.7 The equation of a longitudinal standing wave due to superposition of the progressive waves produced by two sources of sound is $s = -20 \sin 10 \pi x \sin 100 \pi t$ where s is the displacement from mean position measured in mm; x is in meters and t in seconds. The specific gravity of the medium is 10^{-3} . Find
 - (a) wavelength, frequency and velocity of the progressive waves.
 - (b) Bulk modulus of the medium and the pressure amplitude of the progressive waves.
 - (c) minimum distance between pressure antinode and the displacement antinode.

Ans. (a) 1/5 m, 50 Hz, 10 m/s; (b) 100 Pa, 10π Pa, (c) 1/20 m

Sol. $k = 10\pi$

 $\omega = 100 \ \pi$

 $\therefore \lambda = \frac{1}{5} \& f = 50 \text{ Hz}$

 $v = \lambda f = 10 \text{ m/s}$

 $B = \rho v^2$

 $P_0 = BKs$

Minimum distance between pressure antinode and displacment antinode = $\frac{\lambda}{4}$

Ex.8 The air column in a pipe closed at one end and open to atmosphere at the other end is made to vibrate in its fifth harmonic by a tuning fork of frequency 470 Hz. The length of air column is $\frac{15}{16}$ m.

Neglect end correction. Let p_0 denote the maximum gauge pressure at the closed end

- (a) Find the speed of sound in air.
- (b) Draw the graph of pressure amplitude vs distance from the open end of the tube.
- (c) Find the points where the maximum gauge pressure is $\frac{p_0}{2}$.
- **Ans.** (a) 352.5 m/s, (b) $P_0/2$ x, (c) $\frac{l}{15}$, $\frac{5l}{15}$, $\frac{7l}{15}$, $\frac{11l}{15}$, $\frac{13l}{15}$

Sol. $\frac{5\lambda}{4} = \frac{15}{16}$

 $\lambda = 0.75 \text{ m}$

f = 470

 $v = \lambda f = 352.5 \text{ m/s}$

$$P = P_0 \sin\left(\frac{2\pi}{\lambda}x\right)$$

where $\lambda = \frac{4\ell}{5}$

$$P = P_0 \sin\left(\frac{5\pi}{2\ell}x\right)$$

Ex.9 A metal rod of length l = 100 cm is clamped at two points. Distance of each clamp from nearer end is a = 30cm. If density and Young's modulus of elasticity of rod material are $\rho = 9000$ kg m⁻³ and Y = 144 GPa respectively, calculate minimum and next higher frequency of natural longitudinal oscillations of the rod.

Ans. 10kHz, 30kHz

Sol.
$$v = \sqrt{\frac{Y}{\rho}} = 4 \times 10^3 \text{ m/s}$$

$$\lambda = 0.4 \text{ m}$$

$$f_0 = \frac{v}{\lambda} = 10 \text{kHz}$$

Ex.10 When two tuning forks (fork 1 and fork 2) are sounded simultaneously, 4 beats per second are heard. Now, some tape is attached on the prong of the fork 2. When the tuning forks are sounded again, 6beats per second are heard. If the frequency of fork 1 is 200 Hz, then what was the original frequency of fork 2?

[AIEEE - 2005]

(1) 200 Hz

- (2) 202 Hz
- (3) 196 Hz
- (4) 204 Hz

Ans. (3)

Sol.
$$f_1 - f_2 = 4$$
 or $f_2 - f_1 = 4$

But according to question

$$f_1 - f_2 = 4$$

So
$$f_2 = 196$$

Ex.11 A whistling train approaches a junction. An observer standing at junction observers the frequency to be 2.2 KHz and 1.8 KHz of the approaching and the receding train. Find the speed of the train (speed of sound = 300 m/s). [JEE 2005]

Ans. $V_{s} = 30 \text{ m/s}$

$$\textbf{Sol.} \qquad \left(\frac{v}{v - v_{\rm S}}\right) f_0 = 2.2 \times 10^3$$

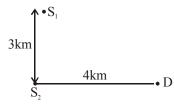
$$\left(\frac{v}{v + v_S}\right) f_0 = 1.8 \times 10^3$$

Dividing both we get

$$\frac{\mathbf{v} + \mathbf{v}_{\mathrm{S}}}{\mathbf{v} - \mathbf{v}_{\mathrm{S}}} = \frac{11}{9}$$

$$v_{s} = 30$$

Ex.12 Two point sound source S_1 and S_2 are both have the same power and send out sound waves in the same phase. The wavelength of both the waves is $\frac{48}{5}$ m. The intensity due to S_2 alone at D is 25 W/m². The resultant intensity at D is:



- $(A) 59 \text{ W/m}^2$
- (B) 61 W/m^2
- (C) 65 W/m^2
- (D) None of these

- Ans.
- $I \propto \frac{1}{r^2}$ Sol.

Intensity due to S_1 alone at $D = 16 \text{ W/m}^2$

Phase difference = $\frac{2\pi}{\left(\frac{48}{5}\right)} \times 1000 = \frac{625}{3}\pi$

$$I_{res} = I_1 + I_2 + 2\sqrt{I_1}\sqrt{I_2} \cos\phi$$

$$= 25 + 16 + 2(5)(4)\left(\frac{1}{2}\right)$$

Ex.13 Spherical sound waves are emitted uniformly in all directions from a point source. The variation in sound level SL as a function of distance r(>0) from the source can be written as :- (where a and b are positive constant)

(A)
$$SL = -b \log r^4$$

(B)
$$SL = a - b \log a$$

(A)
$$SL = -b \log r^a$$
 (B) $SL = a - b \log r$ (C) $SL = a - b (\log r)^2$ (D) $SL = a - \frac{b}{r^2}$

(D)
$$SL = a - \frac{b}{r^2}$$

(B) Ans.

Sol.
$$I \propto \frac{1}{r^2}$$

$$SL = 20\log_{10} = \frac{I}{I_0}$$

EXERCISE (S-1)

Sound basics

1. Find the intensity of sound wave whose frequency is 250 Hz. The displacement amplitude of particles of the medium at this position is 1×10^{-8} m. The density of the medium is 1 kg/m^3 , bulk modulus of elasticity of the medium is 400 N/m^2 .

SW0001

2. In a mixture of gases, the average number of degrees of freedom per molecule is 6. The rms speed of the molecules of the gas is c. Find the velocity of sound in the gas.

SW0002

3. The loudness level at a distance R from a long linear source of sound is found to be 40dB. At this point, the amplitude of oscillations of air molecules is 0.01 cm. Then find the loudness level & amplitude at a point located at a distance '10R' from the source.

SW0003

Superposition of sound

4. The first overtone of a pipe closed at one end resonates with the third harmonic of a string fixed at its ends. The ratio of the speed of sound to the speed of transverse wave travelling on the string is 2:1. Find the ratio of the length of pipe to the length of string.

SW0004

5. In a resonance-column experiment, a long tube, open at the top, is clamped vertically. By a separate device, water level inside the tube can be moved up or down. The section of the tube from the open end to the water level act as a closed organ pipe. A vibrating tuning fork is held above the open end, first and the second resonances occur when the water level is 24.1 cm and 74.1 cm respectively below the open end. Find the diameter of the tube.

SW0005

6. A tuning fork of frequency 480 Hz resonates with a tube closed at one end of length, 16 cm and diameter 5 cm in fundamental mode. Calculate velocity of sound in air. [JEE 2003]

SW0006

7. An open organ pipe filled with air has a fundamental frequency 500Hz. The first harmonic of another organ pipe closed at one end and filled with carbon dioxide has the same frequency as that of the first harmonic of the open organ pipe. Calculate the length of each pipe. Assume that the velocity of sound in air and in carbondioxide to be 330 and 264 m/s respectively.

- 8. A steel rod having a length of 1 m is fastened at its middle. Assuming young's modulus to be 2×10^{11} Pa, and density to be 8 gm/cm³ find the fundamental frequency of the longitudinal vibration and frequency of first overtone.
- 9. Two narrow cylindrical pipes A and B have the same length. Pipe A is open at both ends and is filled with a monoatomic gas of molar mass M_A. Pipe B is open at one end and closed at the other end, and is filled with a diatomic gas of molar mass M_B. Both gases are at the same temperature. [JEE 2002]

 (a) If the frequency of the second harmonic of the fundamental mode in pipe A is equal to the frequency
 - of the third harmonic of the fundamental mode in pipe B, determine the value of M_A/M_B .
 - (b) Now the open end of pipe B is also closed (so that the pipe is closed at both ends). Find the ratio of the fundamental frequency in pipe A to that in pipe B.

 SW0009

118 JEE-Physics ALLEN

10. A tube of a certain diameter and of length 48 cm is open at both ends. Its fundamental frequency of resonance is found to be 320 Hz. The velocity of sound in air is 320m/sec. Estimate the diameter of the tube.
[IIT-1980]

SW0010

Beats

11. A stretched uniform wire of a sonometer between two fixed knife edges, when vibrates in its second harmonic gives 1 beat per second with a vibrating tuning fork of frequency 200 Hz. Find the percentage change in the tension of the wire to be in unison with the tuning fork.

SW0011

12. A, B and C are three tuning forks. Frequency of A is 350Hz. Beats produced by A and B are 5 per second and by B and C are 4 per second. When a wax is put on A beat frequency between A and B is 2Hz and between A and C is 6Hz. Then, find the frequency of B and C respectively.

SW0012

- 13. A source of sound of frequency 256 Hz is moving rapidly towards wall with a velocity of 5 m/sec. How many beats per second will be heard if sound travels at a speed of 330 m/sec? [IIT-1981] SW0013
- 14. Two tuning forks with natural frequencies of 340 Hz each move relative to a stationary observer. One fork moves away from the observer, while the other moves towards him at the same speed. The observer hears beats of frequency 3 Hz. Find the speed of the tuning fork (assume $v_{sound} = 340 \text{ m/s}$)

[IIT-1986]

SW0014

Doppler effect

15. Two tuning forks A and B lying on opposite sides of observer 'O' and of natural frequency 85 Hz move with velocity 10 m/s relative to stationary observer O. Fork A moves away from the observer while the fork B moves towards him. A wind with a speed 10 m/s is blowing in the direction of motion of fork A. Find the beat frequency measured by the observer in Hz. [Take speed of sound in air as 340 m/s]

SW0015

- 16. A car is moving towards a huge wall with a speed = c/10, where c = speed of sound in still air. A wind is also blowing parallel to the velocity of the car in the same direction and with the same speed. If the car sounds a horn of frequency f, then what is the frequency of the reflected sound of the horn heard by driver of the car?

 SW0016
- 17. A plane sound wave of frequency f_0 and wavelength λ_0 travels horizontally toward the right. It strikes and is reflected from a large, rigid, vertical plane surface, perpendicular to the direction of propagation of the wave and moving towards the left with a speed v.
 - (a) How many positive wave crests strike the surface in a time interval t?
 - (b) At the end of this time interval, how far to the left of the surface is the wave that was reflected at the beginning of the time interval?
 - (c) What is the wavelength of the reflected waves, in terms of λ_0 ?
 - (d) What is the frequency, in terms of f_0 ?
 - (e) A listener is at rest at the left of the moving surface. Describe the sensation of sound that he hears as a result of the combined effect of the incident and reflected wave trains.

SW0017

18. A bus is moving towards a huge wall with a velocity of 5 ms^{-1} . The driver sounds a horn of frequency 200 Hz. The frequency of the beats heard by a passenger of the bus will be..... Hz (speed of sound in air = 342 ms^{-1})

SW0018

E

- 1. A boat is travelling in a river with a speed of 10 m/s along the stream flowing with a speed 2 m/s. From this boat, a sound transmitter is lowered into the river through a rigid support. The wavelength of the sound emitted from the transmitter inside the water is 14.45 mm. Assume that attenuation of sound in water and air is negligible.

 [JEE 2001]
 - (a) What will be the frequency detected by a receiver kept inside the river downstream?
 - (b) The transmitter and the receiver are now pulled up into air. The air is blowing with a speed 5 m/sec in the direction opposite the river stream. Determine the frequency of the sound detected by the receiver.

(Temperature of the air and water = 20° C; Density of river water = 10^{3} Kg/m³; Bulk modulus of the water = 2.088×10^{9} Pa; Gas constant R = 8.31 J/mol-K; Mean molecular mass of air = 28.8×10^{-3} kg/mol; C_p/C_v for air = 1.4)

Note: Boat velocity is with respect to ground & receiver is stationary w.r.t. ground

SW0019

- 2. The air column in a pipe closed at one end is made to vibrate in its second overtone by a tuning fork of frequency 440 Hz. The speed of sound in air is $330 \, \text{ms}^{-1}$. End corrections may be neglected. Let P_0 denote the mean pressure at any point in the pipe & ΔP_0 the maximum amplitude of pressure variation.
 - (i) Find the length L of the air column.
 - (ii) What is the amplitude of pressure variation at the middle of the column?
 - (iii) What are the maximum & minimum pressures at the open end of the pipe.
 - (iv) What are the maximum & minimum pressures at the closed end of the pipe? **SW0020**
- 3. A train of length *l* is moving with a constant speed v along a circular track of radius R, The engine of the train emits a whistle of frequency f. Find the frequency heard by a guard at the rear end of the train. Make suitable assumption.

SW0021

4. A string 25 cm long and having a mass of 2.5 gm is under tension. A pipe closed at one end is 40 cm long. When the string is set vibrating in its first overtone and the air in the pipe in its fundamental frequency, 8 beats per second are heard. It is observed that decreasing the tension in the string decreases beat frequency. If the speed of sound in air is 320 m/s, find the tension in the string. [IIT-1982]

SW0022

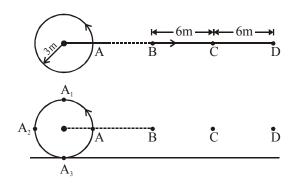
- 5. A train approaching a hill at speed of 40 km/hr sound a whistle of frequency 580 Hz when it is at a distance of 1 km from a hill. A wind a speed of 40 km/hr blowing the direction of motion of the train. Find
 - (i) the frequency of the whistle as heard by an observer on the hill.
 - (ii) the distance from the hill at which the echo from the hill is heard by the driver and its frequency. (Velocity of sound in air = 1,200 km/hr) [IIT-1988]

6. A source of sound is moving along a circular orbit of radius 3 meteres with an angular velocity of 10 rad/s. A sound detector located far away from the source is executing linear simple harmonic motion along the line BD with an amplitude BC = CD = 6 metres. The frequency of oscillation of the

detector is $\frac{5}{\pi}$ per second. The source is at the point A when the detector is at the point B. If the source

is at the point A when the detector is at the point B. If the source emits a continuous sound wave of frequency 340 Hz, find the maximum and the minimum frequencies recorded by the detector.

[IIT-1990]



SW0024

- 7. Two radio stations broadcast their programmes at the same amplitude A and at slight different frequencies ω_1 and ω_2 respectively, where $\omega_1 \omega_2 = 10^3$ Hz A detector receives the signals from the two stations simultaneously. It can only detect signals of intensity ≥ 2 A².
 - (i) Find the time interval between successive maxima of the intensity of the signal received by the detector.
 - (ii) Find the time for which the detector remains idle in each cycle of the intensity of the signal.

[IIT-1993]

SW0025

8. A sonometer wire under tension of 64 Newtons vibrating in its fundamental mode is in resonance with a vibrating tuning fork. The vibrating portion of the sonometer wire has a length of 10 cm and a mass of 1 gm. The vibrating tuning fork is now moved away of 1 gm. The vibrating wire with a constant speed and an observer standing near the sonometer hears oen beat per second. Calculate the speed with which the tuning fork is moved if the speed of sound in air is 300 m/s. [IIT-1983]

SW0026

- 9. The displacement of the medium in a sound wave is given by the equation $y_1 = A\cos(ax + bt)$ where A, a and b are positive constants. The wave is reflected by an obstacle situated at x = 0. The intensity of the reflected wave is 0.64 times that of the incident wave.
 - (a) What are the wavelength and frequency of incident wave?
 - (b) Write the equation for the reflected wave.

120

- (c) In the resultant wave formed after reflection, find the maximum and minimum values of the particle speeds in the medium.
- (d) Express the resultant wave as a superpositions of standing wave and a travelling wave. What are the positions of the antinodes of the standing wave? What is the directions of propagation of travelling wave?

- 1
- 10. The air colomn in a pipe closed at one end is made to vibrate in its second overtone by a tuning fork of frequency 440 Hz. The speed of sound in air is 330 ms⁻¹. End corrections may be neglected. Let P_0 denote the mean pressure at any point in the pipe, and ΔP_0 the maximum amplitude of pressure variation.
 - (a) Find the length L of the air column.
 - (b) What is the amplitude of pressure variation at the middle of the column?
 - (c) What are the maximum and minimum pressure at the open end of the pipe?
 - (d) What are the maximum and minimum pressure at the closed end of the pipe?

[IIT-1998]

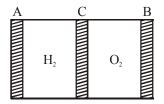
SW0028

11. A 3.6m long vertical pipe resonates with a source of frequency 212.5 Hz when water level is at certain height in the pipe. Find the height of water level (from the bottom of the pipe) at which resonance occurs. Neglect end correction. Now, the pipe is filled to a height H (\approx 3.6 m). A small hole is drilled very close to its bottom and water is allowed to leak. Obtain and expression for the rate of fall of water level in the pipe as a function of H. If the radii of the pipe and the hole are 2×10^{-2} m and 1×10^{-3} m respectively calculate the time interval between the occurance of first two resonances. Speed of sound in air is 340 m/s and g = 10 m/s². [IIT-2000]

SW0029

12. AB is a cylinder of length 1m fitted a thin flexible diaphragm C at the middle and other thin flexible diaphragms A and B at the ends. The portions AC and BC contain hydrogen and oxygen gases respectively. The diaphragms A and B are set into vibrations of same frequency. What is the minimum frequency of these vibration for which diaphragm C is a not? (Under the conditions of experiment

$$v_{H_2} = 1100 \text{ m/s}, v_{O_2} = 300 \text{ m/s}.$$
 [IIT-1978]



EXERCISE (O-1)

Sound basics

1. A sound wave has a wavelength of 3.0 m. The distance from a compression center to the adjacent rarefaction center is:-

(A) 0.75 m

(B) 1.5 m

(C) 3.0 m

(D) need to know wave speed

SW0030

2. You are listening to an "A" note played on a violin string. Let the subscript "s" refer to the violin string and "a" refer to the air. Then:-

(A) $f_s = f_a$ but $\lambda_s \neq \lambda_a$

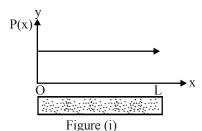
(B) $f_s = f_a$ and $\lambda_s = \lambda_a$

(C) $\lambda_s = \lambda_a$ but $f_s \neq f_a$

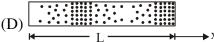
(D) $\lambda_s \neq \lambda_a$ and $f_s \neq f_a$

SW0031

3. The fig.(i) shows the graphical representation of the air molecules in a tube of air (length = L) at atmospheric pressure on the absolute pressure P(x) graph. Which one of the following pictures corresponds to the absolute pressure P(x) graph of fig. (ii).

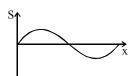


(B) L →

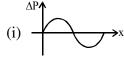


SW0032

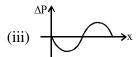
4. If a sound wave is travelling and snap shot at t = 0 is as shown in figure.



Choose snapshot of pressure variation.



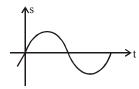
(ii) $\Delta P \longrightarrow x$



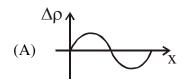


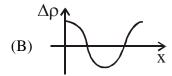
- (A) For wave travelling towards right or left (i) is correct.
- (B) For wave travelling towards right graph (iv) and for wave travelling towards left graph (iv) is correct.
- (C) For wave travelling towards right graph (i) and for wave travelling towards left graph (iii) is correct
- (D) For wave travelling towards right or left (ii) is correct.

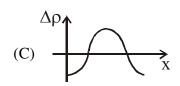
A sound waves is travelling towards right and its s-t graph is as shown for x = 0. 5.

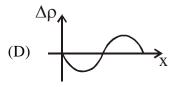


What will be the variation in density vs x graph at t = T/4:









SW0034

6. A point source of sound is located somewhere along the x-axis. Experiments show that the same wave front simultaneously reaches listeners at x = -8 m and x = +2.0 m.

A third listener is positioned along the positive y-axis. What is her y-coordinate (in m) if the same wave front reaches her at the same instant as it does the first two listeners?

SW0035

7. Two monatomic ideal gases 1 and 2 of molecular masses m, and m, respectively are enclosed in separate container kept at the same temperature. The ratio of the speed of sound in gas 1 to that in gas [JEE 2000 (Scr)] 2 is given by

(A)
$$\sqrt{\frac{m_1}{m_2}}$$

(B)
$$\sqrt{\frac{m_2}{m_1}}$$
 (C) $\frac{m_1}{m_2}$

$$(C) \frac{m_1}{m_2}$$

(D)
$$\frac{m_2}{m_1}$$

SW0036

8. A firecracker exploding on the surface of a lake is heard as two sounds a time interval t apart by a man on a boat close to water surface. Sound travels with a speed u in water and a speed v in air. The distance from the exploding firecracker to the boat is

(A)
$$\frac{uvt}{u+v}$$

$$(B) \frac{t(u+v)}{uv}$$

(B)
$$\frac{t(u+v)}{uv}$$
 (C) $\frac{t(u-v)}{uv}$ (D) $\frac{uvt}{u-v}$

(D)
$$\frac{uvt}{u-v}$$
 SW0037

9. The speed of longitudinal wave is 100 times the speed of transverse wave in a taut brass wire. If the Young's modulus of brass is 1.0×10^{11} N/m², the stress in wire is :-

(A)
$$1.0 \times 10^7 \text{ N/m}^2$$

(B)
$$1.0 \times 10^6 \text{ N/m}^2$$

(C)
$$1.0 \times 10^5 \text{ N/m}^2$$

(D)
$$1.0 \times 10^8 \text{ N/m}^2$$

SW0038

The equations of S.H.M. of medium particle due to sound waves propagating in a medium are given by $s_1 = 2 \sin{(200\pi t)}$ and $s_2 = 5 \sin{(150\pi t)}$. The ratio of average intensities of sound at these points is:

(A) 4:25

(B) 9:100

(C) 8:15

(D) 64:225

- A is singing a note and at the same time B is also singing a note with 1/8th the frequency of A. The 11. energies of the two sounds are equal. The displacement amplitude of the note of B is:
 - (A) same as that of A

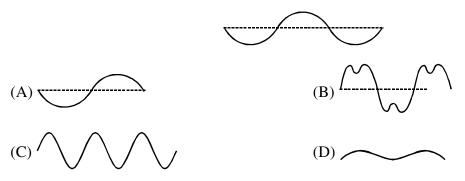
(B) twice that of A

(C) four times that of A

(D) eight times that of A

SW0040

12. A microphone is connected to an oscilloscope. The diagram shows the trace on the screen when the microphone receives a pure note. Which trace can be obtained when a musical instrument produces a note of the same pitch but of a different quality?



SW0041

- 13. Choose **correct** statement?
 - (A) Two different acoustic musical instruments can not have same loudness
 - (B) Two different acoustic musical instruments can not have same pitch
 - (C) Two different acoustic musical instruments can not have same quality
 - (D) Two different acoustic musical instruments can have more than two characteristics same

SW0042

A plane transverse wave is propagating in a direction making an angle of 30° with positive x-axis in 14. the x-y plane. Find phase difference between points (0, 0, 0) and (1, 1, 1). Wavelength of the wave is 1m:-

(B)
$$\left(\sqrt{3}+1\right)\pi$$
 rad (C) $\left(\sqrt{2}+1\right)\pi$ rad

(C)
$$(\sqrt{2}+1)\pi$$
 rad

(D) None

SW0043

Which of the following is the equation of a spherical wave :-15.

(A)
$$S = S_0 \sin(Kx - \omega t)$$

(B)
$$S = S_0 \cos(Kx - \omega t)$$

(C)
$$S = (S_0/x) \sin(\omega t - Kx)$$

(D)
$$S = (S_0/x^2) \sin(\omega t - Kx)$$

SW0044

A note is produced when you blow air across the top of a test tube. Two students were asked about **16.** the effect of blowing harder.

Student-A: The pitch of sound would increase.

Student-B: The intensity of sound would increase

(A) A is correct, B is wrong

(B) B is correct, A is wrong

(C) both are correct

(D) both are wrong

SW0045

A sound absorber attenuates the sound level by 20 dB. The intensity decreases by a factor of-**17.**

[AIEEE - 2007]

(A) 1000

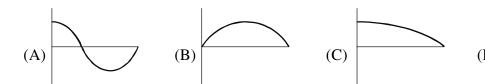
(B) 10000

(C) 10

(D) 100

Standing waves

Which of the figures, shows the pressure difference from regular atmospheric pressure for an organ pipe of length L closed at one end, corresponds to the 1st overtone for the pipe?



SW0047

In an organ pipe whose one end is at x = 0, the pressure is expressed by 19.

 $p = p_0 \cos \frac{3\pi x}{2} \sin 300\pi t$ where x is in meter and t in sec. The organ pipe can be

- (A) closed at one end, open at another with length = 0.5m
- (B) open at both ends, length = 1m
- (C) closed at both ends, length = 2m
- (D) closed at one end, open at another with length = $\frac{2}{3}$ m

SW0048

20. If 1, and 1, are the lengths of air column for the first and second resonance when a tuning fork of frequency n is sounded on a resonance tube, then the distance of the displacement antinode from the top end of the resonance tube is:

(A)
$$2(l_2 - l_1)$$

(B)
$$\frac{1}{2}(2l_1 - l_2)$$
 (C) $\frac{l_2 - 3l_1}{2}$ (D) $\frac{l_2 - l_1}{2}$

(C)
$$\frac{l_2 - 3l_1}{2}$$

(D)
$$\frac{l_2 - l_1}{2}$$

SW0049

- A student is experimenting with resonance tube apparatus in Physics lab to find the speed of sound at 21. room temperature. He got resonating lengths of air column as 17 cm and 51 cm, using tuning fork of frequency 512 Hz. Find speed of sound at room temperature and specify, whether the side water reservoir was moved upward or downward to obtain the second resonance (51 cm)?
 - (A) 348 m/s, downwards

(B) 348 m/s, upwards

(C) 332 m/s, downwards

(D) 332 m/s, upwards

SW0050

Interference

The ratio of maximum to minimum intensity due to superposition of two waves is $\frac{49}{9}$. Then the ratio 22. of the intensity of component waves is:-

(A)
$$\frac{25}{4}$$

(B)
$$\frac{16}{25}$$

(C)
$$\frac{4}{49}$$

(D)
$$\frac{9}{49}$$

SW0051

- Two waves of sound having intensities I and 4I interfere to produce interference pattern. The phase 23. difference between the waves is $\pi/2$ at point A and π at point B. Then the difference between the resultant intensities at A and B is
 - (A) 2I
- (B) 4I
- (C) 5I
- (D) 7I

24. Three coherent waves of equal frequencies having amplitude 10 μ m, 4 μ m and 7 μ m respectively, arrive at a given point with successive phase difference of $\pi/2$. The amplitude of the resulting wave in μ m is given by

(A)5

(B)6

(C)3

(D) 4

SW0053

25. The ratio of intensities between two coherent soud sources is 4 : 1. The different of loudness in dB between maximum and minimum intensities when they interfere in space is:

(A) 10 log 2

(B) 20 log 3

(C) 10 log 3

(D) 20 log 2

SW0054

26. In Quincke's tube a detector detects minimum intensity. Now one of the tube is displaced by 5 cm. During displacement detector detects maximum intensity 10 times, then finally a minimum intensity (when displacement is complete). The wavelength of sound is:

(A) 10/9 cm

(B) 1 cm

(C) 1/2 cm

(D) 5/9 cm

SW0055

27. S_1, S_2 are two coherent sources of sound located along x – axis separated by 4λ where λ is wavelength of sound emitted by them. Number of maxima located on the elliptical boundary around it will be:

S₁ S₂ 4λ

(A) 16

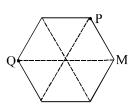
(B) 12

(C) 8

(D) 4

SW0056

28. Two sound source emitting sound of wavelength 1 m are located at points P and Q as shown in figure. All sides of the polygon are equal and of length 1m. The intensity of sound at M due to both the individual sources is I_0 . What will be the intensity of sound at point M when both the sources are on.



 $(A) 4I_0$

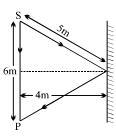
 $(B) 2I_0$

 $(C) I_0$

(D) $(1/2)I_0$

SW0057

29. A person standing at a distance of 6 m from a source of sound receives sound wave in two ways, one directly from the source and other after reflection from a rigid boundary as shown in the figure. The maximum wavelength for which, the person will receive maximum sound intensity, is



(A) 4 m

(B) $\frac{16}{3}$ m

(C) 2 m

(D) $\frac{8}{3}$ m

Beats

- **30.** Beats are heard when the A strings of two violins are played. The beat frequency decreases as the tension in the A string of violin 1 is slowly increased. Which of the following statement is correct?
 - (A) the fundamental frequency of the A string in violin 1 is less than that for violin 2
 - (B) the fundamental frequency of the A string in violin 1 is greater than that for violin 2
 - (C) the fundamental frequency of the A string in violin 1 may be greater or less than that for violin 2 depending on the linear mass densities of the two strings.

(D) None of these SW0059

31. Two waves with similar frequencies are added. The resulting waveform oscillates with the average frequency and with an oscillating amplitude that changes with a frequency equal to the difference between the original frequencies. These oscillations in the amplitude are known as beats. The traces show the resulting waveforms that occur when two different pairs of waves are added. Graph is for the same time interval in both cases, which of the following statements is TRUE?



- (A) On average, the waves on the left had higher frequencies, but the difference between frequencies less
- (B) On average, the waves on the right had higher frequencies, but the difference between frequencies
- (C) On average, the waves on the left had higher frequencies, but the difference between frequencies more
- (D) On average, the waves on the right had higher frequencies, but the difference between frequencies

SW0060

Doppler effect

A source when at rest in a medium produces waves with a velocity v and a wavelength of λ . If the source is set in motion with a velocity v_s what would be the wavelengths produced directly in front of the source?

(A)
$$\lambda \left(1 - \frac{v_s}{v}\right)$$
 (B) $\lambda \left(1 + \frac{v_s}{v}\right)$ (C) $\lambda \left(1 + \frac{v}{v_s}\right)$ (D) $\frac{\lambda v}{v + v_s}$

(B)
$$\lambda \left(1 + \frac{v_s}{v}\right)$$

(C)
$$\lambda \left(1 + \frac{v}{v_s}\right)$$

(D)
$$\frac{\lambda v}{v + v_s}$$

SW0061

33. A source of sound S having frequency f. Wind is blowing from source to observer O with velocity u. If speed of sound with respect to air is C, the wavelength of sound detected by O is:

(A)
$$\frac{C+u}{f}$$

(B)
$$\frac{C-u}{f}$$

(B)
$$\frac{C-u}{f}$$
 (C) $\frac{C(C+u)}{(C-u)f}$ (D) $\frac{C}{f}$

(D)
$$\frac{C}{f}$$

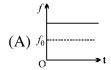
- 34. A train moving towards a hill at a speed of 72 km/hr sounds a whistle of frequency 500 Hz. A wind is blowing from the hill at a speed of 36 km/hr. If the speed of sound in air is 340 m/s, the frequency heard by a man on the hill is
 - (A) 532.25 Hz.
- (B) 565.0 Hz.
- (C) 516.1 Hz.
- (D) none of the above.

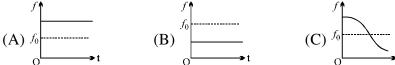
SW0063

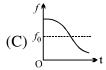
- A source is moving with constant speed $v_s = 20$ m/sec towards a stationary observer due east of 35. source. Wind is blowing at the speed of 20 m/sec due to 60° north of east. The source is generating of frequency 500 Hz. Then frequency registered by observer is: [Speed of sound in still air = 330 m/sec.
 - (A) 500 Hz
- (B) 532 Hz
- (C) 531 Hz
- (D) 530 Hz

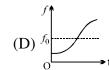
SW0064

36. Source and observer both start moving simultaneously from origin, one along x-axis and the other along y-axis with speed of source = twice the speed of observer. The graph between the apparent frequency observed by observer f and time t would approximately be:









SW0065

- A siren placed at a railway platform is emitting sound of frequency 5 kHz. A passenger sitting in a 37. moving train A records a frequency of 5.5 kHz while the train approaches the siren. During his return journey in a different train B he records a frequency of 6.0 kHz while approaching the same siren. The ratio of the velocity of train B to that of train A is :-
 - (A) 242/252
- (B) 2

- (C) 5/6
- (D) 11/6

SW0066

- A police van moving with velocity 22 m/s and emitting sound of frequency 176 Hz, follows a motor **38.** cycle in turn is moving towards a stationary car and away from the police van. The stationary car is emitting frequency 165 Hz. If motorcyclist does not hear any beats then his velocity is $(v_s = 330 \text{ m/s})$
 - (A) 22 m/s
- (B) 24 m/s
- (C) 20 m/s
- (D) 18 m/s

EXERCISE (O-2)

- 1. Two tuning forks of frequency 250 Hz and 256 Hz produce beats. If a maximum of intensity is observed just now, after how much time the minimum is observed at the same place?
 - (A) $\frac{1}{18}$ sec
- (B) $\frac{1}{4}$ sec.
- (C) $\frac{1}{3}$ sec.
- (D) $\frac{1}{12}$ sec.

SW0068

- 2. The particle displacement of a travelling longitudinal wave is represented by S = S(x, t). The midpoints of a compression zone and an adjacent rarefaction zone are represented by the letter 'C' and 'R'. Which of the following is true?
 - (A) $|\partial S / \partial x|_C = |\partial S / \partial x|_R$
 - (B) $|\partial S / \partial t|_{C} = |\partial S / \partial t|_{R} = 0$
 - (C) $(pressure)_{C} (pressure)_{R} = 2 |\partial S| / \partial x|_{C} \times Bulk modulus of air.$
 - (D) Particles of air are stationary mid-way between 'C' and 'R'.

SW0069

- 3. Which of the following statements are wrong about the velocity of sound in air:
 - (A) decreases with increases in temperature
- (B) increases with decrease in temperature
- (C) decreases as humidity increases
- (D) independent of density of air.

SW0070

- **4.** A car moves towards a hill with speed v_c . It blows a horn of frequency f which is heard by an observer following the car with speed v_c . The speed of sound in air is v.
 - (A) the wavelength of sound reaching the hill is $\frac{v}{f}$
 - (B) the wavelength of sound reaching the hill is $\frac{v v_c}{f}$
 - (C) the beat frequency observed by the observer is $\left(\frac{v+v_o}{v-v_c}\right)f$
 - (D) the beat frequency observed by the observer is $\frac{2v_c(v+v_o)f}{v^2-v_c^2}$

SW0071

- 5. Three coherent source kept along the same line produce intensity I_0 each at point P on this line. When $S_1 \& S_2$ are switched on simultaneously, intensity at point P is $2I_0$. When S_2 and S_3 are switched on simultaneously, intensity at point P is $2I_0$. Then
 - (A) When S_1 and S_3 are switched on simultaneously, intensity at point P can be $2I_0$
 - (B) When S_1 and S_3 are switched on simultaneously, intensity at point P can be 0
 - (C) When all 3 sources are switched on simultaneously, intensity at point P can be ${\rm I}_0$
 - (D) When all 3 sources are switched on simultaneously, intensity at point P can be $3I_0$

6. A sound consists of four frequencies \rightarrow 300 Hz, 900 Hz, 2400 Hz and 4500 Hz. A sound 'filter' is made by passing this sound through a bifurcated pipe as shown. The sound waves have to travel a distance of 50 cm more in the right branch-pipe than in the straight pipe. The speed of sound in air is 300 m/s. Then, which of the following frequencies will be almost completely muffled or "silenced" at the outlet?



(A) 300 Hz

(B) 900 Hz

(C) 2400 Hz

(D) 4500 Hz

SW0073

Paragraph for Question No. 7 to 9

A metallic rod of length 1m has one end free and other end rigidly clamped. Longitudinal stationary waves are set up in the rod in such a way that there are total six antinodes present along the rod. The amplitude of an antinode is 4×10^{-6} m. Young's modulus and density of the rod are 6.4×10^{10} N/m² and 4×10^3 Kg/m³ respectively. Consider the free end to be at origin and at t=0 particles at free end are at positive extreme.

7. The equation describing displacements of particles about their mean positions is

(A)
$$s = 4 \times 10^{-6} \cos\left(\frac{11\pi}{2}x\right) \cos\left(22\pi \times 10^{3}t\right)$$
 (B) $s = 4 \times 10^{-6} \cos\left(\frac{11\pi}{2}x\right) \sin\left(22\pi \times 10^{3}t\right)$

(B)
$$s = 4 \times 10^{-6} \cos\left(\frac{11\pi}{2}x\right) \sin\left(22\pi \times 10^{3}t\right)$$

(C)
$$s = 4 \times 10^{-6} \cos(5\pi x) \cos(20\pi \times 10^3 t)$$
 (D) $s = 4 \times 10^{-6} \cos(5\pi x) \sin(20\pi \times 10^3 t)$

(D)
$$s = 4 \times 10^{-6} \cos(5\pi x) \sin(20\pi \times 10^3 t)$$

SW0074

8. The equation describing stress developed in the rod is

(A)
$$140.8\pi \times 10^4 \cos\left(\frac{11}{2}\pi x + \pi\right) \cos\left(22\pi \times 10^3 t\right)$$

(B)
$$140.8\pi \times 10^4 \sin\left(\frac{11}{2}\pi x + \pi\right) \cos(22\pi \times 10^3 t)$$

(C)
$$128\pi \times 10^4 \cos(5\pi x + \pi)\cos(20\pi \times 10^3 t)$$

(D)
$$128\pi \times 10^4 \sin(5\pi x + \pi)\cos(20\pi \times 10^3 t)$$

SW0074

9. The magnitude of strain at midpoint of the rod at t= 1 sec is

(A)
$$11\sqrt{3}\pi \times 10^{-6}$$

(B)
$$11\sqrt{2}\pi \times 10^{-6}$$

(A)
$$11\sqrt{3}\pi \times 10^{-6}$$
 (B) $11\sqrt{2}\pi \times 10^{-6}$ (C) $10\sqrt{3}\pi \times 10^{-6}$ (D) $10\sqrt{2}\pi \times 10^{-6}$

(D)
$$10\sqrt{2}\pi \times 10^{-6}$$

Paragraph for Question No. 10 to 12

In an organ pipe (may be closed or open) of length 1m standing wave is setup, whose equation for longitudinal displacement is given by $\xi = (0.1 \text{ mm}) \cos \frac{2\pi}{0.8} (y) \cos (400) t$ where y is measured from the top of the tube in meters and t in second.



- 10. The upper end and the lower ends of the tube are respectively:
 - (A) open closed
- (B) closed open
- (C) open open
- (D) closed closed

SW0075

- 11. The air column is vibrating in
 - (A) First overtone
- (B) Second overtone
- (C) Third harmonic
- (D) Fundamental mode

SW0075

Equation of the standing wave in terms of excess pressure is (Bulk modulus of air B = 5×10^5 N/m²) **12.**

(A)
$$P_{ex} = (125 \text{ mN/m}^2) \sin \frac{2\pi}{0.8}$$
 (y) $\cos (400 \text{ t})$

(A)
$$P_{ex} = (125 \pi \text{N/m}^2) \sin \frac{2\pi}{0.8}$$
 (y) $\cos (400 \text{t})$ (B) $P_{ex} = (125 \pi \text{N/m}^2) \cos \frac{2\pi}{0.8}$ (y) $\sin (400 \text{t})$

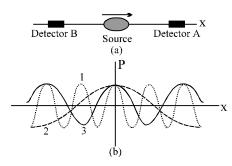
(C)
$$P_{ex} = (225 \pi \text{N/m}^2) \sin \frac{2\pi}{0.8}$$
 (y) $\cos (200 \text{ t})$

(C)
$$P_{ex} = (225 \pi \text{N/m}^2) \sin \frac{2\pi}{0.8}$$
 (y) $\cos (200 \text{ t})$ (D) $P_{ex} = (225 \pi \text{N/m}^2) \cos \frac{2\pi}{0.8}$ (y) $\sin (200 \text{ t})$

SW0075

Paragraph for Question No. 13 to 16

A source emitting a sound wave at a certain frequency moves with constant speed along an x-axis figure (a). The source moves directly towards a stationary detector A and directly away from another stationary detector B. The superimposed three plots of figure (b) indicate the pressure function P(x) of the sound wave as measured by detector A, by detector B, and by someone (c) in the rest frame of the source.



- 13. Which of the following plot corresponds to the measurement done by detector A?
 - (A) 1

(B)2

- (C) 3
- (D) These plots are not possible

SW0076

- 14. The plot corresponding to the measurement done by detector B is
 - (A) 1

(B)2

- (C)3
- (D) These plots are not possible

- 15. The plot corresponding to the measurement done by the detector C is
 - (A) 1

(B) 2

- (C)3
- (D) These plots are not possible

SW0076

- **16.** Now the source stops and begins to move along y-axis with same speed, the plot which corresponds to the measurement of B now is
 - (A) 1

(B) 2

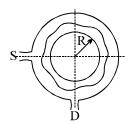
(C)3

(D) none of these

SW0076

Paragraph for Question No. 17 to 21

A narrow tube is bent in the form of a circle of radius R, as shown in the figure. Two small holes S and D are made in the tube at the positions right angle to each other. A source placed at S generated a wave of intensity I_0 which is equally divided into two parts: One part travels along the longer path, while the other travels along the shorter path. Both the part waves meet at the point D where a detector is placed



- 17. If a maxima is formed at the detector then, the magnitude of wavelength λ of the wave produced is given by :-
 - (A) πR
- (B) $\frac{\pi R}{2}$
- (C) $\frac{\pi R}{4}$
- (D) $\frac{2\pi R}{3}$

SW0077

- 18. If the minima is formed at the detector then, the magnitude of wavelength λ of the wave produced is given by :-
 - (A) 2πR
- (B) $\frac{3\pi R}{2}$
- (C) $\frac{2\pi R}{3}$
- (D) $\frac{2\pi R}{5}$

SW0077

- **19.** The maximum intensity produced at D is given by :-
 - $(A) 4I_0$
- (B) $2I_0$
- $(C) I_0$
- (D) $3I_0$

SW0077

- **20.** The maximum value of λ to produce a maxima at D is given by :-
 - (A) πR
- (B) 2πR
- (C) $\frac{\pi R}{2}$
- (D) $\frac{3\pi R}{2}$

SW0077

- **21.** The maximum value of λ to produce a minima at D is given by :-
 - (A) πR
- (B) 2πR
- (C) $\frac{\pi R}{2}$
- (D) $\frac{3\pi R}{2}$

Paragraph for Question Nos. 22 to 24

Two waves $y_1 = A \cos(0.5 \pi x - 100 \pi t)$ and $y_2 = A \cos(0.46 \pi x - 92 \pi t)$ are travelling in a pipe placed along x-axis. [JEE 2006]

- 22. Find the number of times intensity is maximum in time interval of 1 sec.
 - (A)4

(B)6

(C) 8

(D) 10

SW0078

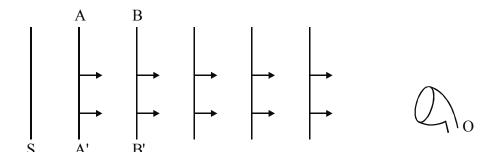
- 23. Find wave velocity of louder sound
 - (A) 100 m/s
- (B) 192 m/s
- (C) 200 m/s
- (D) $96 \, \text{m/s}$

SW0078

- **24.** At x = 0 how many times the value of $y_1 + y_2$ is zero in one second?
 - (A) 100
- (B) 46
- (C) 192
- (D) 96

SW0078

25. Consider a large plane diaphragm 'S' emitting sound and a detector 'O'. The diagram shows plane wavefronts for the sound wave travelling in air towards right when source, observer and medium are at rest. AA' and BB' are fixed imaginary planes. Column-I describes about the motion of source, observer or medium and column-II describes various effects. Match them correctly.



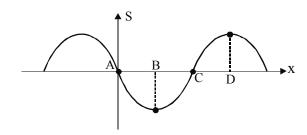
Column-I

- (A) Source starts moving towards right
- (B) Air starts moving towards right
- (C) Observer and source both move towards left with same speed.
- (D) Source and medium (air) both move towards right with same speed.

Column-II

- (P) Distance between any two wavefronts will increase.
- (Q) Distance between any two wavefronts will decrease.
- (R) The time needed by sound to move from plane AA' to BB' will increase.
- (S) The time needed by sound to move from plane AA' to BB' will decrease.
- (T) Frequency received by observer increases.

26. Figure shows a graph of particle displacement function of x at t = 0 for a longitudinal wave travelling in positive x-direction in a gas. A,B,C,D denote position of particles in space.



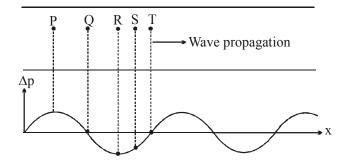
Column-I

Column II

- (A) point A
- (P) Particle velocity is in direction of wave propagation
- (B) point B
- (Q) Maximum magnitude of strain
- (C) point C
- (R) Excess pressure is zero
- (D) point D
- (S) Maximum density
- (T) Maximum magnitude of excess pressure

SW0080

- 27. Sound is travelling in a long tube towards right and the graph of excess pressure variation versus position (at some instant) is given below.
 - Match velocities in column-I with column-II. P,Q,R,S,T are medium particles inside the tube.



Column-I

Column-II

- (A) velocity is towards right
- (P) P

(B) velocity is towards left

(Q) Q

(C) velocity is zero

(R) R

(D) Speed is maximum

- (S) S
- (T) T

SW0081

E

amplitude only.

(1) 2.5 kHz

E

(2) 10 kHz

1.

[AIEEE - 2011]

(4) 5 kHz

EXERCISE - JM

 $y_2(x, t) = a \sin(2\omega t - 2kx)$ will have equal intensity.

(1) Statement-1 is false, statement-2 is true

Statement-1: Two longitudinal waves given by equations: $y_1(x, t) = 2a \sin(\omega t - kx)$ and

Statement-1: Intensity of waves of given frequency in same medium is proportional to square of

	(2) Statement-1 is ture, statement-2 is false						
	(3) Statement-1 is ture, statement-2 true; statement-2 is the correct explanation of statement-1						
	(4) Statement-1 is true, statement-2 is true; statement -2 is not correct explanation of statement-1.						
	(1) Statement 1 is			•	SW0082		
2.	A nine of langth 95	Samis alasad from ana a	nd Find the number of				
L.	A pipe of length 85 cm is closed from one end. Find the number of possible natural oscillations of air column in the pipe whose frequencies lie below 1250 Hz. The velocity of sound in air is 340 m/s.						
	column in the pipe	whose frequencies lie b	elow 1250 Hz. The velo	-			
				[JEE Main	· - 2014]		
	(1) 6	(2) 4	(3) 12	(4) 8			
					SW0083		
3.	A train is moving	on a straight track with sp	peed 20 ms ⁻¹ . It is blow	ng its whistle at the frequ	uency of		
	1000 Hz. The perc	centage change in the fre	quency heard by a pers	on standing near the trac	k as the		
	train passes him is	(speed of sound = 320 m	ns ⁻¹) close to :-				
				[JEE Main	- 2015]		
	(1) 18%	(2) 24%	(3) 6%	(4) 12%			
					SW0084		
4.	A pipe open at bot	h ends has a fundamenta	frequency f in air. The				
	A pipe open at both ends has a fundamental frequency f in air. The pipe is dipped vertically in water so that half of it is in water. The fundamental frequency of the air column is now:-						
				JEE-Mai	n-20161		
				[OLL IVI	2010]		
	(1) f	(2) $\frac{f}{2}$	(3) $\frac{3f}{4}$	(4) 2f			
	(1)1	2	4	(1)=1			
				S	SW0085		
5.	An observer is mo	An observer is moving with half the speed of light towards a stationary microwave source emitting					
	waves at frequency 10 GHz. What is the frequency of the microwave measured by the observer?						
	(speed of light $= 3$	$\times 10^8 \text{ms}^{-1}$					
				[JEE Main	- 2017]		
	(1) 17.3 GHz	(2) 15.3 GHz	(3) 10.1 GHz	(4) 12.1 GHz	_		
	` '	. ,	,	, ,	SW0086		
6.	A granite rod of 60 cm length is clamped at its middle point and is set into longitudinal vibrations. The						
	density of granite is 2.7×10^3 kg/m ³ and its Young's modulus is 9.27×10^{10} Pa. What will be the						
	fundamental frequency of the longitudinal vibrations?						
	runuamentai mequ	chey of the longitudinary	viorations:	iner Ma:	n 20101		
				[JEE-Mai	.II-ZV10]		

(3) 7.5 kHz

[JEE-Main-2019 Jan]

(4) 5:3

ratio: (1) 4 : 1

7.

8.

SELECTED PROBLEMS FROM JEE-MAINS ONLINE PAPERS

(2)25:9

Two coherent sources produce waves of different intensities which interfere. After interference, the ratio of the maximum intensity to the minimum intensity is 16. The intensity of the waves are in the

A resonance tube is old and has jagged end. It is still used in the laboratory to determine velocity of sound in air. A tuning fork of frequency 512 Hz produces first resonance when the tube is filled with water to a mark 11 cm below a reference mark, near the open end of the tube. The experiment is

(3) 16:9

	repeated with another fork of frequency 256 Hz which produces first resonance when water reaches a mark 27 cm below the reference mark. The velocity of sound in air, obtained in the experiment, is					
	close to:			[JEE-Main-2019 Jan]		
	$(1) 328 \text{ms}^{-1}$	$(2) 322 \text{ms}^{-1}$	$(3) 341 \text{ms}^{-1}$	$(4) 335 \text{ms}^{-1}$		
9.	A person standin	g on an open ground he	ars the sound of a jet aer	coplane, coming from north at an		
	angle 60° with gr	ound level. But he finds	the aeroplane right vertic	eally above his position. If v is the		
	speed of sound, s	peed of the plane is:		[JEE-Main-2019_Jan]		
	$(1) \frac{2v}{\sqrt{3}}$	(2) v	$(3)\frac{\upsilon}{2}$	$(4) \frac{\sqrt{3}}{2} v$		
	4 -		2	2		
10.				the sound produced by a vibrating		
	blade on a day when atmospheric temperature is 0°C. On some other day, when temperature is T, the					
	speed of sound p	produced by the same bl	lade and at the same free	quency is found to be 336 ms ⁻¹ .		
	Approximate val	ue of T is:		[JEE-Main-2019_April]		
	$(1) 15^{\circ} C$	$(2) 12^{\circ} C$	(3) 4°C	(4) 11°C		
11.	A tuning fork of	frequency 480 Hz is used	d in an experiment for me	easuring speed of sound (v) in air		
	by resonance tube	e method. Resonance is ol	oserved to occur at two su	ccessive lengths of the air column,		
	$l_1 = 30$ cm and l_2	= 70 cm . Then v is equal	ıl to :	[JEE-Main-2019_April]		
	$(1) 332 \text{ ms}^{-1}$	$(2) 379 \text{ ms}^{-1}$	$(3) 384 \text{ ms}^{-1}$	$(4) 338 \text{ ms}^{-1}$		
12.	A small speaker	delivers 2 W of audio of	output. At what distance	from the speaker will one detect		
	=		e intensity of sound as 10	-		
	,	L	J	[JEE-Main-2019 April]		
	(1) 10 cm	(2) 30 cm	(3) 40 cm	(4) 20 cm		
13.	` '	` '	` '	ne line of its velocity by another		
10.		-	-	· • • • • • • • • • • • • • • • • • • •		
	submarine (B) travelling at 27 km/hr. B sends a sonar signal of 500 Hz to detect A and receives a reflected sound of frequency v. The value of v is close to : (Speed of sound in water = 1500 ms^{-1})					
	(1) 499 Hz	(2) 502 Hz	(3) 507 Hz	(4) 504 Hz		
1.4	` '	` '	` /	` '		
14.	-			at has double the density of air at		
	STP. Assuming the speed of sound in air at STP is 300 m/s, the frequency difference between t					
	fundamental and	second harmonic of this	pipe is Hz.			
				[JEE-Main-2020_Jan]		
15.	Three harmonic	waves having equal freq	uency v and same intensi	ty I_0 , have phase angles 0 , $\frac{\pi}{4}$ and		
	$-\frac{\pi}{4}$ respectively. When they are superimposed the intensity of the resultant wave is close to:					
				[JEE-Main-2020_Jan]		
	$(1) 5.8 I_0$	$(2) 0.2 I_0$	(3) I_0	$(4)\ 3\ I_0$		
•		<u> </u>	-			
▼				•		

- 16. In a resonance tube experiment when the tube is filled with water up to height of 17.0 cm from bottom, it resonates with a given tuning fork. When the water level is raised the next resonance with the same tuning fork occurs at a height of 24.5 cm. If the velocity of sound in air is 330 m/s, the tuning fork frequency is:

 [JEE-Main-2020_Sep]

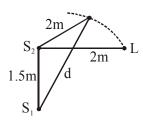
 (1) 1100 Hz

 (2) 3300 Hz

 (3) 2200 Hz

 (4) 550 Hz
- Assume that the displacement(s) of air is proportional to the pressure difference (Δp) created by a sound wave. Displacement(s) further depends on the speed of sound (v), density of air (ρ) and the frequency (f). If $\Delta p \sim 10$ Pa, v ~ 300 m/s, p ~ 1 kg/m³ and f ~ 1000 Hz, then s will be the order of (take multiplicative constant to be 1) [JEE-Main-2020_Sep]
 - (1) 10 mm (2) $\frac{3}{100}$ mm (3) 1 mm (4) $\frac{1}{10}$ mm
- 18. Two coherent sources of sound, S_1 and S_2 , produce sound waves of the same wavelength, $\lambda = 1$ m, in phase. S_1 and S_2 are placed 1.5 m apart (see fig.) A listener, located at L, directly in front of S_2 finds that the intensity is at a minimum when he is 2m away from S_2 . The listener moves away from S_1 , keeping his distance from S_2 fixed. The adjacent maximum of intensity is observed when the listener is at a distance d from S_1 . Then, d is:

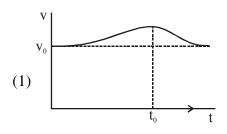
 [JEE-Main-2020_Sep]

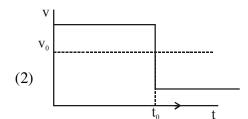


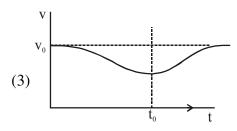
- (1) 12m (2) 3m (3) 5m (4) 2m
- 19. A sound source S is moving along a straight track with speed v, and is emitting sound of frequency v₀ (see figure). An observer is standing at a finite distance, at the point O, from the track. The time variation of frequency heard by the observer is best represented by:

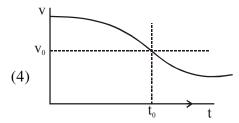
 (t₀ represents the instant when the distance between the source and observer is minimum)

[JEE-Main-2020_Sep]









20. A wire of density 9×10^{-3} kg cm⁻³ is stretched between two clamps 1 m apart. The resulting strain in the wire is 4.9×10^{-4} . The lowest frequency of the transverse vibrations in the wire is (Young's modulus of wire Y = 9×10^{10} Nm⁻²), (to the nearest integer),_____. [JEE-Main-2020_Sep]

EXERCISE (JA)

When two progressive waves $y_1 = 4 \sin(2x - 6t)$ and $y_2 = 3 \sin\left(2x - 6t - \frac{\pi}{2}\right)$ are superimposed, the 1. amplitude of the resultant wave is

[IIT-JEE 2010]

SW0087

2. **Column I** shows four systems, each of the same length L, for producing standing waves. The lowest possible natural frequency of a system is called its fundamental frequency, whose wavelength is denoted as λ_r . Match each system with statements given in Column II describing the nature and wavelength of the standing waves. [IIT-JEE 2011]

Column I

Column II

(A) Pipe closed at one end

Longitudinal waves (p)



(B) Pipe open at both ends

Transverse Waves (q)



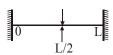
- Stretched wire clamped at both ends
- $\lambda_{f} = L$



- (D) Stretched wire clamped at both ends
- (s) $\lambda_f = 2L$

and at mid-point

 $\lambda_f = 4L$ (t)



SW0088

- 3. A police car with a siren of frequency 8 kHz is moving with uniform velocity 36 km/hr towards a tall building which reflects the sound waves. The speed of sound in air is 320 m/s. The frequency of the siren heard by the car driver is [JEE 2011]
 - (A) 8.50 kHz
- (B) 8.25 kHz
- (C) 7.75 kHz
- (D) 7.50 kHz

nodeJo\BOBA-BB\Kob\LEE[Advanced]\ENTHJSE\Ay\Wadule\WaveOptics, Wavean Shing & Sound Wave\Eng\3.5aund Wave\O]_Theory+Exp65

- A person blows into open-end of a long pipe. As a result, a high-pressure pulse of air travels down the 4. pipe. When this pulse reaches the other end of the pipe. [JEE 2012]
 - (A) a high-pressure pulse starts travelling up the pipe, if the other end of the pipe is open
 - (B) a low -pressure pulse starts travelling up the pipe, if the other end of the pipe is open
 - (C) a low pressure pulse starts travelling up the pipe, if the other end of the pipe is closed
 - (D) a high-pressure pulse starts travelling up the pipe, if the other end of the pipe is closed

SW0090

5. A student is performing the experiment of Resonance Column. The diameter of the column tube is 4cm. The frequency of the tuning fork is 512 Hz. The air temperature is 38°C in which the speed of sound is 336 m/s. The zero of the meter scale coincides with the top end of the Resonance column tube. When the first resonance occurs, the reading of the water level in the column is:- [JEE 2012]

SW0091

- (A) 14.0 cm
- (B) 15.2 cm
- (C) 16.4 cm
- (D) 17.6 cm
- **6.** A student is performing an experiment using a resonance column and a tuning fork of frequency 244 s⁻¹. He is told that the air in the tube has been replaced by another gas (assume that the column remains filled with the gas). If the minimum height at which resonance occurs is (0.350 ± 0.005) m, the gas in the tube is

(**Useful information**: $\sqrt{167RT} = 640 \text{ J}^{1/2} \text{ mole}^{-1/2}$; $\sqrt{140RT} = 590 \text{ J}^{1/2} \text{ mole}^{-1/2}$. The molar masses

M in grams are given in the options. Take the values of $\sqrt{\frac{10}{M}}$ for each gas as given there.)

[JEE Advanced-2014]

(A) Neon
$$\left(M = 20, \sqrt{\frac{10}{20}} = \frac{7}{10}\right)$$

(B) Nitrogen
$$\left(M = 28, \sqrt{\frac{10}{28}} = \frac{3}{5} \right)$$

(C) Oxygen
$$\left(M = 32, \sqrt{\frac{10}{32}} = \frac{9}{16} \right)$$

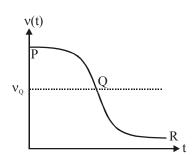
(D) Argon
$$\left(M = 36, \sqrt{\frac{10}{36}} = \frac{17}{32}\right)$$

Four harmonic waves of equal frequencies and equal intensities I_0 have phase angles 0, $\pi/3$, $2\pi/3$ and 7. π . When they are superposed, the intensity of the resulting wave is nI_0 . The value of n is.

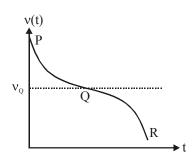
[JEE-Advance-2015]

SW0093

- 140
- 8. Two loudspeakers M and N are located 20m apart and emit sound at frequencies 118 Hz and 121 Hz, respectively. A car is initially at a point P, 1800 m away from the midpoint Q of the line MN and moves towards Q constantly at 60 km/hr along the perpendicular bisector of MN. It crosses Q and eventually reaches a point R, 1800 m away from Q. Let v(t) represent the beat frequency measured by a person sitting in the car at time t. Let v_p , v_0 and v_R be the beat frequencies measured at locations P, Q and R, respectively. The speed of sound in air is 330 ms⁻¹. Which of the following statement(s) is(are) true regarding the sound heard by the person? [JEE Advanced 2016] (A) The plot below represents schematically the variation of beat frequency with time



(B) The plot below represents schematically the variations of beat frequency with time



(C) The rate of change in beat frequency is maximum when the car passes through Q

(D)
$$v_P + v_R = 2v_Q$$

A stationary source emits sound of frequency $f_0 = 492$ Hz. The sound is reflected by a large car 9. approaching the source with a speed of 2 ms⁻¹. The reflected signal is received by the source and superposed with the original. What will be the beat frequency of the resulting signal in Hz? (Given that the speed of sound in air is 330 ms⁻¹ and the car reflects the sound at the frequency it has received).

[JEE Advanced 2017]

SW0095

Two men are walking along a horizontal straight line in the same direction. The man in front walks at 10. a speed 1.0 ms⁻¹ and the man behind walks at a speed 2.0 ms⁻¹. A third man is standing at a height 12m above the same horizontal line such that all three men are in a vertical plane. The two walking men are blowing identical whistles which emit a sound of frequency 1430 Hz. The speed of sound in air is 330 ms⁻¹. At the instant, when the moving men are 10 m apart, the stationary man is equidistant from them. The frequency of beats in Hz, heard by the stationary man at this instant, is

[JEE Advanced 2018]

- 11. In an experiment to measure the speed of sound by a resonating air column, a tuning fork of frequency 500 Hz is used. The length of the air column is varied by changing the level of water in the resonance tube. Two successive resonances are heard at air columns of length 50.7 cm and 83.9 cm. Which of the following statements is (are) true?

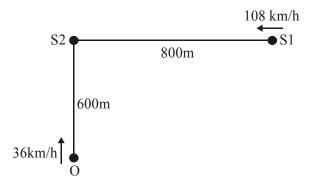
 [JEE Advanced 2018]
 - (A) The speed of sound determined from this experiment is 332 ms⁻¹
 - (B) The end correction in this experiment is 0.9 cm
 - (C) The wavelength of the sound wave is 66.4 cm
 - (D) The resonance at 50.7 cm corresponds to the fundamental harmonic

SW0097

12. A train S1, moving with a uniform velocity of 108 km/h, approaches another train S2 standing on a platform. An observer O moves with a uniform velocity of 36 km/h towards S2, as shown in figure. Both the trains are blowing whistles of same frequency 120 Hz. When O is 600 m away from S2 and distance between S1 and S2 is 800 m, the number of beats heard by O is _____.

[Speed of the sound = 330 m/s]

[JEE Advanced 2019]



SW0098

13. A stationary tuning fork is in resonance with an air column in a pipe. If the tuning fork is moved with a speed of 2 ms⁻¹ in front of the open end of the pipe and parallel to it, the length of the pipe should be changed for the resonance to occur with the moving tuning fork. If the speed of sound in air is 320 ms⁻¹, the smallest value of the percentage change required in the length of the pipe is ______.

[JEE Advanced 2020]

ANSWER KEY

EXERCISE (S-1)

1. Ans.
$$\frac{\pi^2 \times 10^{-9}}{4}$$
 W/m²

2. Ans. 2c/3

3. Ans. 30 dB, $10\sqrt{10}$ µm

4. Ans. 1 : 1

6. Ans. 336 m/s

7. Ans. 33 cm and 13.2 cm

9. Ans. (a) 2.116, (b)
$$\frac{3}{4}$$
 10. Ans. 3.33 cm, 163 Hz

12. Ans. 345, 341 or 349 Hz

13. Ans. 8

15. Ans. 5

16. Ans. 11f/9

$$\textbf{17. Ans. (a)} \left(\frac{v + \lambda_0 f_0}{\lambda_0} \right) t \text{ (b) } \left(\lambda_0 f_0 - v \right) t \text{ (c) } \lambda_0 \left(\frac{\lambda_0 f_0 - v}{\lambda_0 f_0 + v} \right) \text{ (d) } f_0 \left(\frac{\lambda_0 f_0 + v}{\lambda_0 f_0 - v} \right) \text{ (e) } \frac{2v f_0}{\lambda_0 f_0 - v} \text{ 18. Ans. 6 Hz}$$

EXERCISE (S-2)

1. Ans. (a) 100696 Hz (b) 103038 Hz

2. Ans. (i)
$$L = \frac{15}{16}$$
 m, (ii) $\frac{\Delta P_0}{\sqrt{2}}$, (iii) $P_{\text{max}} = P_{\text{min}} = P_0$ (iv) $P_{\text{max}} = P_0 + \Delta P_0$, $P_{\text{min}} = P_0 - \Delta P_0$

3. Ans. f

4. Ans. 27.04 N

5. Ans. (i) 599 Hz, (ii) 0.935 km, 620 Hz

6. Ans. 438.7 Hz, 257.3 Hz 7. Ans. (i)
$$10^{-3}$$
 sec, (ii) 2×10^{-3} sec

8. Ans. 0.75 m/s

9. Ans. (a)
$$\frac{2\pi}{a}$$
, $\frac{b}{2\pi}$, (b) $y = -0.8 \text{ Acos}(ax - bt)$ OR $y = 0.8 \text{ Acos}(ax - bt)$, (c) 1.8 Ab, 0

(d)
$$y = -1.6$$
 A sin ax sin bt + 0.2 A cos(ax + bt), $\left[n + \frac{(-1)^2}{2}\right] \frac{\pi}{a}$, -X direction **OR**

$$y = 0.2 \text{ A} \cos (ax + bt) + 1.6 \text{ A} \cos ax \cos bt, x = \frac{n\pi}{a}, -X \text{ direction}$$

10. Ans. (a)
$$\frac{15}{16}$$
m (b) $\frac{\Delta P_0}{\sqrt{2}}$ (c) equal to mean pressure (d) $P_0 + \Delta P_0$, $P_0 - \Delta P_0$

11. Ans.
$$\frac{-dH}{dt} = (1.11 \times 10^{-2})\sqrt{H}$$
, 43 sec.

12. Ans. 1650 Hz

EXERCISE (O-1)

- 1. Ans. (B) 2. Ans. (A)
- 3. Ans. (B)
- 4. Ans. (B)
- 5. Ans. (A)
- 6. Ans. (A)

- 7. Ans. (B)
- 8. Ans. (D)
- 9. Ans. (A)
- 10. Ans.(D)
- 11. Ans. (D)
- 12. Ans. (B)

- 13. Ans. (C)
- 14. Ans. (B)
- 15. Ans. (C)
- 16. Ans. (B)
- 17. Ans. (D)
- 18. Ans. (A)

- 19. Ans. (C)
- 20. Ans. (C)
- 21. Ans. (A)
- 22. Ans.(A)
- 23. Ans. (B)
- 24. Ans. (A)

- 25. Ans.(B)
- 26. Ans. (B)
- 27. Ans.(A)
- 28. Ans.(A)
- 29. Ans. (A)
- 30. Ans. (A)

- 31. Ans. (B)
- 32. Ans. (A)
- 33. Ans. (A)
- 34. Ans. (A)
- 35. Ans. (C)
- 36. Ans. (B)

37. Ans. (B) 38. Ans. (A)

EXERCISE (O-2)

- 1. Ans. (B,D)
- 2. Ans. (A,C,D)
- 3. Ans. (A,B,C,D)
- 4. Ans. (B,D)

- 5. Ans. (B, C)
- 6. Ans. (A, B, D)
- 7. Ans. (A)
- 8. Ans. (B)

- 9. Ans. (B)
- 10. Ans. (A)
- 11. Ans. (B)
- 12. Ans. (A)

- 13. Ans. (A)
- 14. Ans. (B)
- 15. Ans. (C)
- 16. Ans. (D)

- 17. Ans. (A,B,C) 21. Ans. (B)
- 22. Ans. (A)
- 19. Ans. (B) 23. Ans. (C)
- 20. Ans. (A) 24. Ans. (A)

- 25. Ans. (A) (Q,T); (B) (P,S); (C) (P) (D) (S,T)

18. Ans. (A,C,D)

- 26. Ans. (A) (P,Q,S,T); (B) (R); (C) (Q,T); (D) (R)
- 27. Ans. (A) (P); (B) (R,S); (C) (Q,T); (D) (P,R)

EXERCISE (JM)

1. Ans. (4)

- 2. Ans. (1)
- 3. Ans. (4)
- 4. Ans. (1)

5. Ans. (1)

6. Ans. (4)

SELECTED PROBLEMS FROM JEE-MAINS ONLINE PAPERS

7. Ans. (2)

- 8. Ans. (1)
- 9. Ans. (3)
- 10. Ans. (3)

- 11. Ans. (3)
- 12. Ans. (3)
- 13. Ans. (2)
- 14. Ans. (106.00 to 107.20)

- 15. Ans. (1)
- 16. Ans. (3)
- 17. Ans. (2)
- 18. Ans. (2)

- 19. Ans. (4)
- 20. Ans. 35.00

EXERCISE (JA)

1. Ans. 5

- 2. Ans. (A) p,t (B) p,s (C) q,s (D) q,r
- 3. Ans. (A)

- 4. Ans. (B,D)
- 5. Ans. (B)
- 6. Ans. (D)
- 7. Ans. 3

- 8. Ans. (A, C, D)
- 9. Ans. 6
- 10. Ans. 5 [4.99, 5.01] 11. Ans. (A,B,C)

- 12. Ans. (8.12 to 8.13)
- 13. Ans. (0.62 to 0.64)

Ε

144 JEE-Physics ALLEN

Important Notes	
	2
	e\01_Theory+Exp6
	/Eng\3-Sound Wav
	ring & Sound Wave
	Optics, Wavean St
	\Any\Wadule\Wave
	kanaed \ENTHUSE\
	nodoJO 1808A 1881 Koro LEEJAdvanood JENTHJSEN Fly Woodule Wove Optics, Wove on Shing & Sound Wove Ving 3'Sound Wove Vin Throny-EspoS
▲	
-	E

	Important Not	es
9		
-		
-		
Kore Vol_Throny		
Vbng)3 Sound V		
a & Sound Weav		
ptic, Wovers Sir		
Model le Wood		
NATURE (NATURE)		
ts).Eff.Advarsed		
nooledo GODek eBiVora) EE(Aderaned) ID/ITH/SEY/By/WoodsleWove-Optics, Wennern Sing & Sand Woon Engl S-Sand Woon Oi_Throsy-Englis		
E		