Castling-ViT: Compressing Self-Attention via Switching Towards Linear-Angular Attention During Vision Transformer Inference

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Abstract

Vision Transformers (ViTs) have shown impressive performance but still require a high computation cost as compared to convolutional neural networks (CNNs), due to the global similarity measurements and thus a quadratic complexity with the input tokens. Existing efficient ViTs adopt local attention (e.g., Swin) or linear attention (e.g., Performer), which sacrifice ViTs' capabilities of capturing either global or local context. In this work, we ask an important research question: Can ViTs learn both global and local context while being more efficient during inference? To this end, we propose a framework called Castling-**ViT**, which trains ViTs using both linear-angular attention and masked softmax-based quadratic attention, but then switches to having only linear angular attention during ViT inference. Our Castling-ViT leverages angular kernels to measure the similarities between queries and keys via spectral angles. And we further simplify it with two techniques: (1) a novel linear-angular attention mechanism: we decompose the angular kernels into linear terms and highorder residuals, and only keep the linear terms; and (2) we adopt two parameterized modules to approximate highorder residuals: a depthwise convolution and an auxiliary masked softmax attention to help learn both global and local information, where the masks for softmax attention are regularized to gradually become zeros and thus incur no overhead during ViT inference. Extensive experiments and ablation studies on three tasks consistently validate the effectiveness of the proposed Castling-ViT, e.g., achieving up to a 1.8% higher accuracy or 40% MACs reduction on ImageNet classification and 1.2 higher mAP on COCO detection under comparable FLOPs, as compared to ViTs with vanilla softmax-based attentions.

1. Introduction

Vision Transformers (ViTs) have made significant progress in image classification, object detection, and many

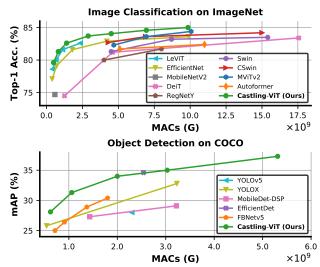


Figure 1. Castling-ViT over SOTA baselines on (1) ImageNet [16] image classification and (2) COCO [33] object detection.

other applications. It is well recognized that the superior performance achieved by ViTs is largely attributed to their self-attention modules that can better capture global context [18,53,60]. Nevertheless, ViTs' powerful self-attention module comes at the cost of quadratic complexity with the number of input tokens, causing a major efficiency bottleneck to ViTs' achievable runtime (i.e., inference latency). For example, although the self-attention module is not as dominant as MLPs in terms of the number of FLOPs, it consistently accounts for over 50% (as high as 69% in LeViT-128 [22]) of the total inference latency when executing the DeiT [51] and LeViT [22] models on a commonly used mobile device, edge GPU [39, 65]. To mitigate this issue, linear attention designs have been developed to alleviate the vanilla ViT attention's quadratic complexity. In particular, existing efforts can be categorized into two clusters: (1) ViTs with local attention by restricting the attention window size [35, 50], sharing the attention queries [1], or representing the attention queries/keys with low rank matrices [54]; and (2) ViTs with kernel-based linear attention, which approximate the non-linearity softmax function by

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decomposing it into separate kernel embeddings. This enables a change in the matrix computation order for a reduced computational complexity [3,4,12,27,34,36,41,62].

Despite their promise in alleviating ViTs' complexity and thus inference runtime, both the local and linear attention compromise ViTs' performance due to the lack of capabilities to capture global or local context. To marry the best of both worlds, we advocate training ViTs with both (1) efficient but less powerful linear attention, i.e., without the high-order residuals in angular kernel expansion, and (2) powerful yet costly softmax-based masked attention. The latter helps approximate high-order residuals at the early training stage while being dropped during inference, based on an assumption that the remaining networks can gradually learn the high-order components at the later training stage [63]. This concept resembles the "castling" move in chess when two pieces are moved at once. While it sounds promising, there are still two challenges to achieve this. First, existing linear attention modules still underperform their vanilla softmax-based counterparts. Therefore, a better linear attention is crucial for the final performance. We find that angular kernels perform equally as softmax-based attentions in terms of similarity measurements. While they still suffer from a quadratic complexity, they can be divided into linear terms and high-order residuals. The challenge is how to construct ViTs with only the linear terms. Second, doing so would require that the trained ViTs merely rely on the linear terms towards the end of training, which would call for an approximation of the above high-order residuals. The challenge is that how we can resort to costly but powerful modules to approximate high-order residuals during training but does not incur extra inference cost.

In this work, we develop techniques to tackle those challenges, and make the following contributions:

- We propose a framework called Castling-ViT, which trains ViTs using both linear-angular attention and masked softmax-based quadratic attention, but then switches to having only linear-angular attentions during ViT inference to save computational costs.
- We develop a new linear-angular attention leveraging angular kernels to close the accuracy gap between linear attention and softmax-based attention. It expands angular kernels where linear terms are kept while complex high-order residuals are approximated.
- We use two parameterized modules to approximate the high-order residuals above: a depthwise convolution and an auxiliary masked softmax-based attention, where the latter's attention masks are regularized to gradually become zeros to avoid inference overhead.
- We conduct extensive experiments to validate the effectiveness of the proposed Castling-ViT. Results on classification, detection, and segmentation tasks con-

sistently demonstrate its superior performance (†1.8% top-1 accuracy or †1.2 mAP) or efficiency (40% MACs savings) over state-of-the-art (SOTA) CNNs and ViTs.

2. Related Works

Vision Transformers (ViTs). ViT [18] beats CNNs with a simple encoder-only transformer architecture taking the splitted non-overlapped image patches as sequential inputs, but relies on costly pretraining on a huge JFT-300M dataset [47]. Later, DeiT [51] and T2T-ViT [68] leverage an improved ViT training recipe or enhanced tokenization mechanism to achieve a comparable accuracy without the necessity of costly pretraining. To further improve ViTs' achievable accuracy-efficiency tradeoffs, CrossViT [7], PiT [24], PVT [55], MViT [19] and Swin-Transformer [35] propose a pyramid-like architecture, which is commonly used in CNNs [14, 26, 61]; DynamicViT [44], A-ViT [64], ToME [2], and MIA-Former [67] propose to adaptively identify and remove unnecessary input tokens for saving computational costs. With the goal of deploying ViTs in resource-constrained devices, various efficient ViT architectures have been proposed [4, 22, 32, 37]. For example, LeViT [22], CvT [59], and MobileViT [37] adopt more efficient self-attention implementation or incorporate convolutional feature extraction blocks into their early layers; EfficientFormer [32] further enables pure ViTs to run as fast as MobileNets. In contrast, our Castling-ViT explores whether ViTs can learn both global and local features while still being efficient at runtime. Also, we target a generic linear-angular attention that can serve as a drop-in replacement for all kinds of ViT architectures and thus is orthogonal to new ViT architecture designs.

Efficient ViT Variants. As commonly recognized, ViTs rely heavily on their self-attention module which is however costly due to its quadratic computational complexity with the total number of input tokens [27,72]. To make the selfattention module more efficient, a surge of linear attention works have been proposed and can be roughly categorized into two groups: local attention [1, 35, 54] or kernel-based linear attention [3, 4, 12, 27, 34, 36, 41, 62]. For local attention, Swin [35] restricts the window size of self-attention; QnA [1] shares the attention queries among all tokens; Linformer [54] approximates the queries and keys with lowrank factorization to reduce their vector length. For kernelbased linear attention, common designs approximate the softmax function [3, 12, 27] or the full self-attention matrix [36,62] with orthogonal features or kernel embeddings, in which way the computation order can be changed from $(\mathbf{Q}\mathbf{K})\mathbf{V}$ to $\mathbf{Q}(\mathbf{K}\mathbf{V})$. Despite their decent performance, currently kernel-based linear attention in general underperform the softmax-based attention. Recent works [6, 15] unify both low rank approximated and sparse attention (can also be dropped at inference) to improve ViTs' accuracyefficiency tradeoffs. Different from the above works, we explore from a new perspective by taking spectral angles into consideration when measuring the similarities among tokens, resulting in linear-angular attention that can achieve even better performance than softmax-based attention.

ViTs have also been used as the backbones for down-stream tasks, e.g., detection [31, 56, 73] and segmentation [9,40]. We supply more literature review to Appendix.

3. The Proposed Methods

3.1. Preliminary of Self-Attention

Self-Attention. Self-attention module is a core component of transformers [18,53], and usually consists of multiple heads (Let M denote the number of heads). Each head captures global-context information by measuring pairwise correlations among all N tokens as defined below:

$$\mathbf{H}_{t} = \sum_{i=1}^{N} \frac{\exp(\mathbf{Q}_{t} \cdot \mathbf{K}_{i}^{T} / \sqrt{d})}{\sum_{j=1}^{N} \exp(\mathbf{Q}_{t} \cdot \mathbf{K}_{j}^{T} / \sqrt{d})} \cdot \mathbf{V}_{i}, \tag{1}$$

where $t \in \{1, \cdots, N\}$, \mathbf{H}_t refers to t-th row of the head's attention matrix \mathbf{H} , $\mathbf{Q}_t, \mathbf{K}_t, \mathbf{V}_t \in \mathbf{R}^d$, are the query, key, and value vectors obtained by linearly projecting the input $\mathbf{X}_t \in \mathbb{R}^D$ with three learnable weight matrices $W^Q, W^K, W^V \in \mathbb{R}^{D \times d}$. The attention head first computes the inner product between the query-key pairs, then scales the product results to stabilize the training and uses Softmax to normalize the resulting attention scores, and finally computes a weighted sum over all value vectors. Outputs from all attention heads are then concatenated together before a final linear projection with learnable weights. Note that $\exp(\cdot)$ denotes an exponential function. Computing Eq. (1) has a quadratic complexity of $\mathcal{O}(N^2)$.

Kernel-based Linear Attention. The core idea of linear attention [27, 46, 54] is to decompose the similarity measurement function into separate kernel embeddings, i.e., $\operatorname{Sim}(\mathbf{Q}, \mathbf{K}) \approx \phi(\mathbf{Q})\phi(\mathbf{K})^T$, so that we can change the computation order to $\phi(\mathbf{Q})(\phi(\mathbf{K})^T\mathbf{V})$ based on the associative property of matrix multiplication. In this way, the attention complexity is quadratic to the feature dimension d instead of the token length N. One straightforward implementation of linear attention is to use Gaussian RBF kernels to measure the similarity, which can serve as an unbiased estimation of $\exp(\langle \cdot, \cdot \rangle)$ in Eq. (1):

$$\exp(\frac{\langle \mathbf{x}, \mathbf{y} \rangle}{\sigma^2}) = \underbrace{\exp(\frac{-\|\mathbf{x} - \mathbf{y}\|^2}{2\sigma^2})}_{\text{Gaussian RBE Kernel}} \exp(\frac{\|\mathbf{x}\|^2 + \|\mathbf{y}\|^2}{2\sigma^2}) \quad (2)$$

where $\langle \cdot, \cdot \rangle$ denotes the inner product operator. According to [43], we can induce a function $\phi(\cdot)$ to approximate the Gaussian RBF kernel, mapping the input space to the feature space. Assuming that both **Q** and **K** are normalized

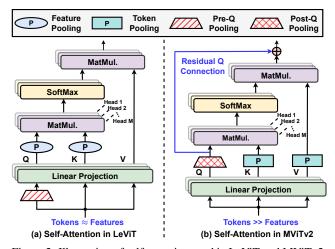


Figure 2. Illustration of self-attention used in LeViT and MViTv2. as unit row vectors along the feature dimension, then the attention formula can be approximated by:

$$\mathbf{H}_{t} = \frac{\phi(\mathbf{Q}_{t}) \cdot \sum_{i=1}^{N} (\phi(\mathbf{K}_{i})^{T} \cdot \mathbf{V}_{i})}{\phi(\mathbf{Q}_{t}) \cdot \sum_{j=1}^{N} \phi(\mathbf{K}_{j}^{T})}$$
(3)

While doing so can alleviate the attention complexity to become linear w.r.t. the token length N, it often causes a nontrivial accuracy drop as compared to the corresponding ViTs with vanilla softmax-based attention [4, 11, 68].

Revisit Attention Designs. Recent ViTs have achieved a low complexity for classification tasks (e.g., LeViT [22]) but still be costly for downstream tasks due to high input resolutions, i.e., the number of tokens (e.g., MViTv2 [31]). Therefore, one dilemma is the tradeoff between the model efficiency and generalizability. As illustrated in Fig. 2, LeViT shrinks the feature dimension to be more efficient on low-resolution tasks but cannot be well generalized to downstream tasks, due to the resulting (1) feature bottlenecks, i.e., insufficient feature dimensions, and (2) fixed attention biases. On the other hand, MViTv2 performs token pooling for better fitting high-resolution tasks but is less effective for low-resolution due to the caused token bottlenecks, i.e., insufficient number of tokens. Our ablation studies in Table 1 show that (1) for ImageNet classification, both token and feature pooling can lead to accuracy drops in ViTs; and (2) for downsampling layers, post-Q pooling (i.e., pooling after linear projection) together with residual connections in MViTv2 performs better than pre-Q pooling (i.e., pooling during linear projection) in LeViT. Therefore, we develop Castling-LeViTs on top of attention with merely post-Q pooling and residual connections.

3.2. The Proposed Castling-ViT Framework

Castling-ViT Overview. Fig. 4 illustrates an overview of the proposed Castling-ViT, which makes linear attention more powerful than previous designs while still being efficient during inference. In particular, we propose (1) a novel

Table 1. Analyze the attention design on ImageNet classification.

Pooling				D 1 O	FLOD- AO	Top-1
Token	Feat.	Pre-Q	Post-Q	Residual Q	FLOPs (M)	Accuracy (%)
$\overline{}$		√			685	78.00
	\checkmark	✓			661	78.19
		✓			736	79.11
√			\checkmark	✓	771	78.73
	✓		\checkmark	✓	763	77.23
			\checkmark	✓	838	80.05

kernel-based linear-angular attention from the spectral angle perspective to close the accuracy gap between linear attention and softmax-based attention; and (2) a training augmentation method that leverages softmax-based attention as an auxiliary branch to assist the linear-angular attention only during ViT training. Note that a mask is applied to the auxiliary branch to manifest linear-angular attention and drop the auxiliary branch.

3.2.1 Linear-Angular Attention

Angular Kernel. In addition to the previously adopted polynomial, exponential, or RBF kernel that focuses on spatial similarity measurements [27, 34], we propose to consider measuring spectral similarity via angular kernel as an alternative to existing softmax-based attentions, leading to similar or better performance since it additionally takes into consideration the nature of spectral characteristics, e.g., the spectral angle as a distance measurement function [25, 28]. Such a spectral angle between two vectors is defined as:

$$\theta(\mathbf{x}_i, \mathbf{x}_j) = \arccos\left(\frac{\langle \mathbf{x}_i, \mathbf{x}_j \rangle}{\|\mathbf{x}_i\| \cdot \|\mathbf{x}_j\|}\right),$$
 (4)

where $\|\cdot\|$ is the Euclidean distance and $\langle\cdot,\cdot\rangle$ is the inner product. The output range of θ is $[0,\pi]$. Such an angle can be used as a distance. In our design, we define the angular kernel as a similarity measurement function between the queries ${\bf Q}$ and keys ${\bf K}$ as:

$$Sim(\mathbf{Q}_i, \mathbf{K}_j) = 1 - \frac{1}{\pi} \cdot \theta(\mathbf{Q}_i, \mathbf{K}_j), \tag{5}$$

and the output range is thus [0,1]. With more aligned \mathbf{Q}_i and \mathbf{K}_j , θ is closer to 0 and thus the similarity is closer to 1; In contrast, if \mathbf{Q}_i and \mathbf{K}_j have opposite features, θ is closer to π and thus the similarity is closer to 0.

Properties of Angular Kernel and Its Feature Space. One property of our angular kernel is that replacing the similarity measurement in self-attention with such a kernel provides an efficient way to implicitly map the input data to a high (even infinite after expansion) dimensional feature space [25], where the distances/angles are calculated based on a rich feature structure. Let $\phi(\cdot)$ denotes the implicit map induced by this kernel, the norm of mapped input data is:

$$\|\phi(\mathbf{x}_i)\|^2 = \text{Sim}(\mathbf{x}_i, \mathbf{x}_i) = 1 - \frac{1}{\pi} \cdot 0 = 1,$$
 (6)



(a) Input space

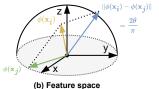


Figure 3. (a) A simple 2D input space and (b) the corresponding 3D feature space after applying the angular kernel to the 2D input data. Note that real input data/features are of higher dimensions.

which means that all data in the input space are mapped onto the sphere of radius 1 in the feature space. Also, the distance between two input features is given by:

$$\|\phi(\mathbf{x}_i) - \phi(\mathbf{x}_j)\|^2 = 1 + 1 - 2 \cdot \phi(\mathbf{x}_i)\phi(\mathbf{x}_j)^T$$

= $2 \cdot (1 - \operatorname{Sim}(\mathbf{x}_i, \mathbf{x}_j)) = \frac{2}{\pi} \cdot \theta(\mathbf{x}_i, \mathbf{x}_j).$ (7)

That is, the square (Euclid) distance and the spectral angle is positively correlated and the distance range is [0, 2]. As shown in Fig. 3, the angles in the input space is correlated to the feature distance after applying our angular kernel.

Expansion of Angular Kernel. A natural following question is how to incorporate the above angular kernel for designing linear attention given its quadratic complexity w.r.t. the input token length. Recalling from trigonometric identities and the expansion of the arccos function into an infinite series, we reformulate the similarity function as:

$$\operatorname{Sim}(\mathbf{Q}_{i}, \mathbf{K}_{j}) = 1 - \frac{1}{\pi} \cdot \left(\frac{\pi}{2} - \arcsin\left(\mathbf{Q}_{i} \cdot \mathbf{K}_{j}^{T}\right)\right)$$

$$= \underbrace{\frac{1}{2} + \frac{1}{\pi} \cdot \left(\mathbf{Q}_{i} \cdot \mathbf{K}_{j}^{T}\right)}_{\text{Linear-angular terms}}$$

$$+ \underbrace{\frac{1}{\pi} \cdot \sum_{k=1}^{\infty} \frac{(2k)!}{2^{2k}(k!)^{2}(2k+1)} \left(\mathbf{Q}_{i} \cdot \mathbf{K}_{j}^{T}\right)^{2k+1}}_{(2k+1)},$$
(8)

where $\mathbf{Q}_i \cdot \mathbf{K}_j^T$ denotes the normalized linear kernel function $\langle \mathbf{Q}_i, \mathbf{K}_j \rangle / \|\mathbf{Q}_i\| \cdot \|\mathbf{K}_j\|$, which is equivalent to the inner product if \mathbf{Q}_i and \mathbf{K}_j are unit vectors. We see that the first linear-angular terms can be directly used as the similarity measurement in linear attention, while the remaining higher-order terms of an infinite series introduce a much higher complexity. As such, we propose to adopt a relaxation to approximate it.

Linear-Angular Attention. To construction our linear-angular attention, we leverage parametrized DNN modules to approximate the expectation of the high-order residuals, i.e., $\mathbf{M}_{ij} = \mathbb{E}_{\mathbf{Q}_i \sim p_{Q_i}, \mathbf{K}_j \sim p_{K_j}} \left(\sum_{k=1}^{\infty} \alpha_k (\mathbf{Q}_i \cdot \mathbf{K}_j^T)^{2k+1} \right)$, where α_k is the coefficient for the k-th order term in Eq. (8). The key question is *how to design such DNN modules*. Kim et al. [29] conducted an analysis on average attention weights of ViT models, which show a strong inductive bias to attend to neighboring tokens. To capture this,

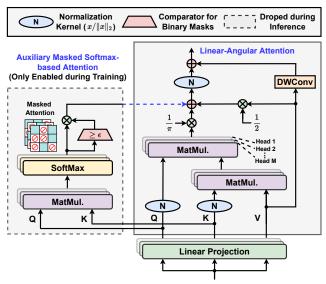


Figure 4. The visualization of the proposed Castling-ViT with both linear angular attention and auxiliary softmax-based self-attention.

we introduce a learnable depthwise convolution (DWConv) module which is applied on all the value tokens, so \mathbf{M}_{ij} by-design attends to nearby tokens, as illustrated in Fig. 4. Second, DWConv is limited by its receptive field [38] while the averaged attention map also has a small number of off-diagonal scores to connect to nonadjacent tokens [29]. To capture that, we adopt a sparse softmax-based attention as described in Section 3.2.2. In practice, we found that such a sparse softmax attention tends to converge to all zeros after adding a simple threshold regularization. We provide more explanation and visualization in Sec. 3.2.2 and Sec. 4.5.

In this way, our attention module can be formulated as:

$$H = Sim(\mathbf{Q}, \mathbf{K}) \cdot \mathbf{V} \approx \frac{1}{2} \cdot \mathbf{V} + \frac{1}{\pi} \cdot \mathbf{Q} \cdot (\mathbf{K}^T \cdot \mathbf{V}) + \mathbf{M}_{DW} \cdot \mathbf{V} + \mathbf{M}_{SparseAttn} \cdot \mathbf{V},$$
(9)

where $1/\pi \cdot Q \cdot (K^T \cdot V)$ is the linear term with $\mathcal{O}(N)$ complexity, $\mathbf{M}_{DW} \cdot V$ is the matrix form of DWConv, and $\mathbf{M}_{SparseAttn} \cdot V$ is the sparse softmax attention. The overall complexity to compute Eq. (9) is linear with respect to the input token length, where the MACs of DWConv is also negligible (e.g., < 1% of the total MACs). Also, normalizations ($\mathbf{x}/\|\mathbf{x}\|_2$) are inserted to the \mathbf{Q}/\mathbf{K} branches to help the similarity measurement following [3].

3.2.2 Switch Towards Linear-Angular Attention

Recall that we add a sparse softmax-based attention as an auxiliary branch in the linear-angular attention to help approximate the high-order residuals. Such a costly attention can be potentially dropped without hurting the inference accuracy, drawing inspiration from [63] that the remaining network can gradually learn the high-order/frequency components at the later training stage. Next, we explain how it is constructed and dropped.

Sparse Training Augmentation. As illustrated in Fig. 4, we adopt a masked softmax-based attention as an auxiliary branch to augment ViT training. In particular, we first use a comparator with a predefined threshold ϵ to generate a binary mask, where attentions greater than ϵ are set to 1 and 0 otherwise. These masks are then applied to the attention maps to generate masked attention maps that will be summed up with our linear-angular attention together as the final attention. The resulting sparse attention is given by:

$$\mathbf{M}_{SparseAttn}(\mathbf{Q}, \mathbf{K}) = \mathtt{Mask}_{\epsilon}(\mathtt{Softmax}(\mathbf{Q} \cdot \mathbf{K}^{\mathtt{T}})).$$
 (10)

where $\mathrm{Mask}_{\epsilon}(\mathbf{x}) = \mathbf{x}$ if $\mathbf{x} > \epsilon$ else 0, acting as an element-wise threshold function. As such, the sparse attention captures the higher attention scores (i.e., strong local features), and can potentially complement our linear-angular attention by supplementing the missing higher-order terms. Such an assumption aligns well with recent findings that (1) low-rank and sparse approximations complement each other [6, 15, 29]; and (2) linear attention lacks local feature extraction capabilities over its softmax-based counterpart [4].

Castling During ViT Inference. As we are targeting efficient ViT inference, it is desired to reduce or completely remove the costly softmax-based attentions while only keeping our linear-angular attention at runtime, i.e., performing castling. In our experiments, we found that under the sparsity regularization above, the softmax attention naturally converges to all zeros as the training progresses. We consider both fixed and dynamic schedules for ϵ and find that our Castling-ViT is not sensitive to neither the threshold value nor the threshold schedule for a given task. Given a fixed mask threshold (e.g., $\epsilon = 0.02$ in image classification experiments), the masks become all zeros at latter training stages and thus the auxiliary branch can be removed without hurting the model accuracy. We supply the visualization of the mask-evolving trajectory and our conjecture for understanding such a phenomenon in Sec. 4.5.

4. Experiments

4.1. Experiment Settings

Tasks, Datasets, and Models. <u>Tasks and Datasets</u>. We consider three benchmark datasets and three representative vision tasks to demonstrate the superiority of the proposed Castling-ViT, including image classification on ImageNet dataset [16] with 1.2 million training and 50K validation images; Object detection on COCO dataset [33] with 118K training and 5K validation images; Semantic segmentation on ADE20K dataset [71] with 20K/2K/3K images for training, validation, and testing, respectively. <u>Models</u>. We apply our proposed Castling-ViT idea on top of various models. For the classification task, we consider LeViT [22], MViTv2 [31], and DeiT [51]; For the detection task, we consider models with efficient ViT backbones (e.g., PicoDet [66] with modified ESNet and LCNet backbones [13] with

Table 2.	Castling-ViT	over SOTA	baselines of	on ImageNet.

MACs	2. Castillig- VII OVE	Params	MACs	Top-1	Top-5
Ranges	Models	(M)	(G)	Acc.(%)	Acc.(%)
	MobileNetV2-1.4 [45]	6.9	0.58	74.7	-
	EfficientNet-B0 [48]	5.3	0.39	77.1	93.3
	EfficientNet-B1 [48]	7.8	0.70	79.1	94.4
	MobileViT-XS [37]	2.3	0.70	74.8	92.3
<1G	LeViT-128 [22]	9.2	0.41	78.6	_
	LeViT-192 [22]	10.9	0.66	80.0	_
	Castling-LeViT-128	10.5	0.49	79.6	94.6
	Castling-LeViT-192	12.7	0.82	81.3	95.5
	EfficientNet-B3 [48]	12.0	1.80	81.6	95.7
	HRFormer-T [69]	8.0	1.80	78.5	-
	DeiT-T [51]	5.6	1.25	74.5	91.9
	LeViT-256 [22]	18.9	1.12	81.6	-
$1\sim3G$	LeViT-384 [22]	39.1	2.35	82.6	-
	Caslting-DeiT-T	5.64	1.18	76.0	92.5
	Castling-LeViT-256	22.0	1.40	82.6	96.1
	Castling-LeViT-384	45.8	2.90	83.7	96.7
	RegNetY-4G [42]	21.0	4.00	80.0	-
	RegNetY-8G [42]	39.0	8.00	81.7	-
	EfficientNet-B4 [48]	19.0	4.20	82.9	96.4
	EfficientNet-B5 [48]	30.0	9.90	83.6	96.7
	Swin-T [35]	29.0	4.50	81.3	95.5
	Swin-S [35]	50.0	8.70	83.2	96.2
	CSWin-T [17]	23.0	4.30	82.7	-
2 100	CSWin-S [17]	35.0	6.90	83.6	-
3~10G	DeiT-S [51]	21.9	4.60	81.2	95.4
	AutoFormer-S [8]	22.9	5.10	81.7	95.7
	PVTv2-V2 [57]	25.0	4.00	82.0	-
	MViTv2-T [31]	24.0	4.68	82.3	-
	MViTv2-S [31]	34.7	6.95	83.6	-
	Castling-MViTv2-T	24.1	4.50	84.1	96.8
	Castling-MViTv2-S	34.7	6.95	84.6	97.0
	CaiT-S36 [52]	68.0	13.90	83.3	- 06.5
	Swin-B [35]	88.0	15.40	83.5	96.5
	CSWin-B [17]	78.0	15.00	84.2	- 05.7
>10G	AutoFormer-B [8]	54.0	11.00	82.4	95.7
/100	MViTv2-B [31]	51.2	10.07	84.4	- 06.5
	DeiT-B [51]	86.3	17.56	83.4	96.5
	Castling-MViTv2-B	51.9	9.82	85.0	97.2

transformer blocks); For the segmentation task, we consider Mask2former [9] with ViT-Base backbone.

Training Settings. For the classification task, we use a SGD optimizer with 0.9 momentum and 2×10^{-5} weight decay to train ViTs for 1000 epochs using 64 V100 GPUs, with each card having 64 (LeViT) or 32 (MViTv2/DeiT) batch sizes. The learning rate is 2.0 with first 11 epochs warm-up starting from 0.01 and decays by a factor of 0.9875 per epoch [58]. Also, we use the distillation [51] based on a teacher model with a 85.5% accuracy. For the detection task, we adopt SGD optimizer with momentum 0.9 and weight decay 4e-5 to train models on COCO. All models are trained on 8 V100 GPUs with each card having 80 batch sizes following PicoDet's training recipe [66]. Also, we follow LeViT's training recipe [22] to pretrain backbones on ImageNet; For the segmentation task, we follow Mask2former's training recipe [9] to train models on ADE20K, where ViT backbones are pretrained following MAE [23] if specified.

Baselines and Evaluation Metrics. *Baselines.* For the classification task, we compare the proposed Castling-ViT with LeViT [22], MviTv2 [31], DeiT [51], Swin [35],

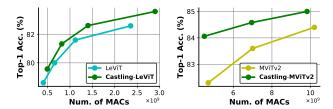


Figure 5. Castling vs. baseline ViT on ImageNet.

CSWin [17], PVT [55], etc. For the detection task, we compare with FBNetV5 [58], YOLOX [21], YOLOv5, MobileDet [61], and EfficientDet [49]. For the segmentation task, we compare with Mask2former [9] with ViT backbones. *Evaluation Metrics*. We evaluate the Castling-ViT and all baselines in terms of accuracy-efficiency tradeoffs. Specifically, the accuracy metrics refer to top-1/5 accuracy for the classification task; AP, AP⁵⁰, AP⁷⁵ for the detection task (AP: average precision); mIoU, mAcc, and pAcc for the segmentation task (mIoU: mean intersection over union). For efficiency metrics, we compare the number of model parameters or inference FLOPs (or MACs).

4.2. Castling-ViT over SOTA Baslines

Image Classification. To evaluate the effectiveness of our proposed techniques on the image classification task, we apply the proposed Castling-ViT idea to three typical or SOTA ViT architectures: DeiT [51] as typical ViTs, LeViT [22] as representative efficient ViTs, and MViTv2 [31] as representative hierarchical ViTs for downstream applications of high input resolutions, and compare their performance over baselines on ImageNet. As shown in Tab. 2, the comparison across a large MACs (or FLOPs) range starting from 0.4G to 17G. We categorize ViT models into four regimes: <1G, $1\sim3G$, $3\sim10G$, and >10G, and select baselines in each regime to benchmark separately for the clarity purpose. Castling-ViTs consistently perform better than all baselines across various MACs ranges in terms of the accuracy-efficiency tradeoff. For example, Castling-LeViT achieves 82.6% top-1 accuracy with only 1.40G MACs while LeViT requires 2.35G FLOPs instead, i.e., \$\pm40\% MACs; On the other hand, under comparable MACs, Castling-MViTv2 achieves 84.1% accuracy vs. MViTv2 with 82.3% accuracy instead, i.e., \\$\dagger\$1.8% top-1 accuracy. Overall, Castling-ViT achieves an improved accuracy of $\uparrow 0.5\% \sim \uparrow 6.6\%$, $\uparrow 1.0\% \sim \uparrow 8.1\%$, $\uparrow 1.0\%$ $\sim 14.1\%$, and $10.6\% \sim 12.6\%$ over baselines under<1G MACs, $1\sim3G$ MACs, $3\sim10G$ MACs, and >10G MACs, respectively. Note that we calculate improvements under comparable MACs. In addition to the overall comparison, we also visualize the apple-to-apple benchmark, e.g., Castling-LeViT vs. LeViT, to validate the effectiveness of proposed techniques. As shown in Fig. 5, Castling-LeViT/MViTv2 achieves \downarrow **25.7**% $\sim \downarrow$ **55.3**% MACs reductions under comparable accuracies or offers a comparable or

Table 3. Castling-ViT over SOTA baselines on COCO detection, where Castling-ViT[†] means that the detection model adopts modified ESNet (use transformer blocks in the last stage; referred to ESNet-ViT) as backbone while Castling-ViT^{*} uses modified LCNet (use transformer blocks in the last two stage; referred to LCNet-ViT) as backbone. Also, "-S/M/L" and "-320/416" represent small/medium/large model variants and 320x320/416x416 input resolutions, respectively.

Models	Params (M)	MACs (G)	mAP	AP50	AP75
MobileDet-DSP [61]	4.85	1.43	27.3	-	-
MobileDet-DSP-Fused [61]	9.15	3.22	29.1	-	-
EfficientDet-D0 [49]	3.90	2.54	34.6	53.0	37.1
YOLOv5-N	1.90	2.30	28.0	45.7	-
YOLOX-Nano [21]	0.91	0.54	25.8	-	-
YOLOX-Tiny [21]	5.06	3.23	32.8	-	-
FBNetV5-AC-224x320 [58]	-	0.71	25.0	-	-
FBNetV5-AR-224x320 [58]	-	0.91	26.4	-	-
FBNetV5-A-224x320 [58]	-	1.35	27.2	-	-
FBNetV5-AC-320x640 [58]	-	1.37	28.9	-	-
FBNetV5-AR-320x640 [58]	-	1.80	30.4	-	-
Castling-ViT-S-320 [†]	3.25	0.62	28.1	42.3	29.2
Castling-ViT-S-416 [†]	3.25	1.06	31.3	46.7	32.5
Castling-ViT-M-416 [†]	6.01	2.00	34.0	49.5	35.9
Castling-ViT-L-416 [†]	9.32	3.03	35.0	50.7	37.2
Castling-ViT-L-416*	13.10	5.31	37.3	53.4	39.6

better accuracy (\uparrow **0.6%** ~ \uparrow **1.8%**) under comparable MACs over corresponding LeViT/MViTv2 baselines.

Object Detection. We also extend the Castling-ViT to the downstream object detection task and compare it with previous efficient detectors on COCO dataset to evaluate its efficacy. Specifically, we construct the detector with modified ESNet [66] or LCNet [13] (replace the last one or two stages with transformer blocks) as backbones and follow PicoDet [66]'s detection head design as well as their training recipe. Fig. 1 and Tab. 3 show the overall comparison between the proposed Castling-ViT and other baselines. We can see that our Castling-ViT consistently achieves better accuracy-efficiency tradeoffs, leading to \uparrow **6.0**, \uparrow **2.2** \sim \uparrow 2.3, \uparrow 4.0 $\sim \uparrow$ 5.9, \uparrow 3.1 $\sim \uparrow$ 4.0 mAP improvements as compared to YOLOv5, YOLOX [21], MobileDet [61], and FBNetv5 [58], respectively, under comparable or even less MACs. As for EfficientDet [49], our method achieves comparable accuracy-efficiency trade-offs. Apart from the overall comparison with baselines, we also provide the apple-toapple comparison with detectors with softmax-based attention, we supply the comparison results and Castling-ViT's breakdown analysis to Sec. 4.4. This set of experiments validate the effectiveness of the proposed Castling-ViT for servering as efficient detector backbones (e.g., ≤3G MACs) in the object detection task.

Semantic Segmentation. We further extend the proposed Castling-ViT to the semantic segmentation task to evaluate its effectiveness. Specifically, we use ViT-Base as the backbone in Mask2former [9] framework to serve as our baseline and testbed. Then we build the Castling-ViT-Base as the backbone to benchmark on the ADE20K dataset. As

Table 4. Castling-ViT over baselines on the ADE20K segmentation dataset, serving as backbones in the Mask2former framework. Note that we report both total MACs and backbone MACs, i.e., (\cdot) .

Mask2former w/	MAE Pretrain	Params (M)	MACs (G)	mIoU	mAcc	pAcc
ViT-Base	N	118	229 (182)	34.54	46.36	75.84
Castling-ViT-Base	N	118	195 (147)	34.67	46.47	76.20
ViT-Base	Y	118	229 (182)	47.92	61.00	83.02
Castling-ViT-Base	Y	118	195 (147)	48.44	61.82	83.29

Table 5. Ablation studies of Castling-ViT with various kernel-based linear attentions, where MC refers to mean-centering kernel function applied to \mathbf{Q}/\mathbf{K} ; Softmax also means the kernel function; ReLU-S and ReLU-E denote applying ReLU as kernels for decomposing softmax or exponential terms, respectively. All models are trained on COCO from scratch without pretraining.

Backbone	Linear Attn	S-320		S-416		M-416	
Dackbone	Linear Attn	mAP	AP50	mAP	AP50	mAP	AP50
LCNet	N/A	25.5	39.0	29.7	44.2	34.3	49.9
LCNet-ViT	N/A	25.9	39.6	29.8	44.4	34.9	50.4
	MC [15]	22.8	34.9	26.3	39.6	31.5	46.1
	Softmax [46]	26.0	39.6	29.2	43.4	34.4	49.8
	Cosine [3]	24.4	37.4	27.2	41.0	32.9	48.0
LCNet-ViT	ReLU-S	23.9	36.7	-	-	30.9	45.3
	ReLU-E [4]	26.5	40.2	30.2	44.7	34.3	49.7
	LinAngular	27.0	40.6	30.4	45.5	35.5	51.1

shown in Tab. 4, Mask2former with Castling-ViT backbone achieves 15% total MACs reductions and 19% backbone MACs reduction under comparable or slightly better mIoU, i.e., †0.13% and †0.52% without or with MAE pretraining on ImageNet [23]. This set of experiments validate that our proposed techniques could be well generalized to various downstream tasks that require large input resolutions.

4.3. Linear-Angular Attention over SOTA Baselines

We also conduct ablation studies among various kinds of kernels used in linear attention to evaluate the superiority of our proposed linear-angular kernel. Also shown in Tab. 5, we compare the angular kernel with five other commonly adopted kernels, results on three model and resolution settings consistently demonstrate that our proposed angular kernel helps achieve better mAP, e.g., $\uparrow 4.0\% \sim \uparrow 4.2\%$ over MC [15], $\uparrow 1.0\% \sim \uparrow 1.2\%$ over Softmax [46], $\uparrow 2.6\% \sim \uparrow 3.2\%$ over Cosine [3], $\uparrow 3.1\% \sim \uparrow 4.6\%$ and $\uparrow 0.2\% \sim \uparrow 1.2\%$ over ReLU-S and ReLU-E [4], respectively. This set of experiments validate the superiority of the proposed linear-angular kernels.

4.4. Ablation Studies of Castling-ViT

We conduct ablation studies on Castling-ViT's linear angular attention, added DWConv, as well as auxiliary masked softmax-based attention, as shown in Tab. 6 and Tab. 7, where the experiments are performed on Castling-ViT-S-320*/M-416*, respectively, without pretraining on ImageNet. Note that here * means that we use LCNet-ViT, i.e., replacing all layers in last two stages with transformer blocks, as backbones. Results in three tables show detailed performance breakdown and consistently demonstrate that

Table 6. Ablation studies of Castling-ViT-S-320 w/ LCNet backbone, or LCNet-ViT backbone + linear-angular attention (denoted as Lin.) + DWConv (denoted as DW.) + auxiliary softmax-based attention (denoted as SparseAttn.).

Castling-ViT-S-320 w/	Params (M)	MACs (G)	mAP	AP50	AP75
LCNet	1.10	0.48	25.5	39.0	26.5
LCNet-ViT	2.14	0.69	25.9	39.6	26.9
+ Lin.	2.14	0.62	26.2	39.7	27.3
+ Lin.+DW.	2.14	0.62	26.8	40.7	28.0
+ Lin.+DW.+SparseAttn.	2.14	0.62	27.0	40.6	28.0

Table 7. Ablation studies of Castling-ViT-M-416 w/ LCNet backbone, or LCNet-ViT backbone + Lin. + DW. + SparseAttn.

Castling-ViT-M-416 w/	Params (M)	MACs (G)	mAP	AP50	AP75
LCNet	3.32	2.15	34.3	49.9	36.5
LCNet-ViT	7.53	3.51	34.9	50.4	37.0
+ Lin.	7.53	3.15	34.8	50.3	36.7
+ Lin.+DW.	7.53	3.15	35.1	50.9	36.9
+ Lin.+DW.+SparseAttn.	7.53	3.15	35.3	51.1	37.3

all components in our proposed Castling-ViT contribute to the final performance. Specifically, linear-angular attention itself already achieves $\downarrow 0.1\% \sim \uparrow 0.5\%$ mAP improvements while leading to $10.1\% \sim 15.3\%$ MACs reductions simultaneously. Adding DWConv in the middle of MLP layers further leads to $\downarrow 0.1\% \sim \uparrow 0.6\%$ mAP improvements while only incur negligible MACs overhead. Adding auxiliary masked softmax-based attention further increases the mAP by 0.2% without incurring any overhead since it only assists the training while being removed during inference. Note that although LCNet-ViT backbone leads to better mAP, it also introduces more MACs as compared to efficient convolutions. As such, LCNet-ViT still slightly underperforms LCNet backbones in terms of accuracy-efficiency trade-offs, since we directly replace the CNN backbones with transformer blocks, whose architecture could not be optimal for ViTs. It remains to an open problem to build ViT based models that achieves higher accuracy-efficiency trade-off than pure ConvNet models.

4.5. Discussion on the Auxiliary Branch

Trajectory of Nonzeros in Masks. To further understand the effect of the auxiliary branch, we visualize the trajectories of nonzeros in masks of auxiliary softmax-based attention. As shown in Fig. 6, we count the nonzeros in first the attention layer's masks throughout the training of both Castling-ViT-S-416

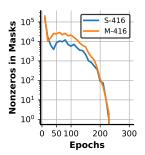


Figure 6. Visualizing the trajectories of nonzeros in auxiliary masks during training.

and Castling-ViT-M-416 with the LCNet-ViT backbone on

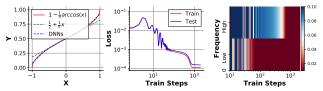


Figure 7. **Left:** Visualizing the taget similarity function, linear-angular terms, and DNNs' fitting curve; **Middle:** Visualizing the loss trajectory during DNN training; **Right:** Visualizing the learning trajectory of both low and high frequency components.

COCO. we observe that the introduced auxiliary attention will only assist the training in the early or middle training stages and will gradually vanish towards all zeros in the later training stage, which is well aligned with the assumption in our Castling-ViT. This set of experiments validate the idea of performing "castling" in ViTs, i.e., drop the auxiliary branch without sacrificing performance.

Conjecture of Castling. We conduct a synthetic experiment to give an analogy for explaining the castling phenomenon. In Fig. 7 (Left), we visualize the curve of (1) angular similarity function (denoted in Red), (2) linearangular terms (denoted in Green), and (3) two-layer DNN's approximation. We see that only keeping linear-angular terms leads to distortion, while DNN is capable of learning the missing high-frequency parts, whose loss trajectory is shown in Fig. 7 (Middle). Also, the learning trajectory of frequency components is visualized in Fig. 7 (Right), following F-Principle [63], where x-axis is training steps, yaxis categorizes both low and high frequency components, blue/red colors refer to large/small difference between the learned frequency components and target frequency components, respectively. We observe that DNNs fit target functions from low to high frequencies during training. It indicates that DWConv itself is not sufficient for approximating the high-order residual at early training stages. Costly attention that contains high-order residuals is then desired to help training while being dropped at inference since the remaining networks can gradually learn the high-frequency components at later training stages [63].

5. Conclusion

We present Castling-ViT that trains ViTs with both linear-angular and softmax-based quadratic attention but switches to only having the former during inference. Castling-ViT leverages angular kernels to measure the similarities between the queries and keys via spectral angles and highlights two enablers: (1) a new linear-angular attention mechanism: we decompose angular kernels to linear terms and high-order residuals, and keep only the former for inference; and (2) we approximate the high-order residuals using a depthwise convolution and an auxiliary masked softmax attention whose masks gradually become zeros during training without incurring inference overhead. Extensive experiments consistently validate Castling-ViT's advantages.

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A. Review of ViTs for Downstream Tasks

Apart from image classification tasks, ViTs have also been leveraged to serve as backbones for downstream tasks, such as object detection [5,31,56,70,73] and semantic segmentation [9, 10, 40]. For example, DETR [5] directly detects and predicts objects by combining a common CNN with a transformer architecture; Maskformer [10] proposes to use a simple mask classification model to predict a set of binary masks, each associated with a single global class label prediction. One big difference is that ViTs can beat CNNs on classification tasks that have a lower image resolution while are still less efficient than lightweight CNNs on downstream tasks that heavily rely on multi-scale resolution features. Therefore, there have been various debates on designing powerful ViT backbones: (1) plain ViTs (e.g., ViTDet [30]) or hierarchical ViTs (e.g., MViTv2 [31], or Swin [35])? Plain ViTs win in terms of simplicity but could be hard to scale down to lower resolution and computation regimes; Hierarchical ViTs seamlessly match with feature pyramid networks (FPNs) for extracting multi-scale feature maps but have more design factors to be considered or searched over. (2) pure ViTs or hybrid CNN-ViTs? Pure ViTs are compatible with self-supervised masked autoencoder (MAE) pretraining [23]; Hybrid CNN-ViTs can suffer from the information leakage problem [20] when adopting MAE pretraining, while being more efficient especially for feature extractions in early layers. Our proposed method does not fall into the aforementioned debates. Instead, it is compatible with all ViT variants relying on the softmaxbased attention.

B. Further Experimental Results

Recall that in Sec. 4, we conduct experiments on three classical computer vision tasks. For object detection and semantic segmentation, we follow the baseline's training recipe for a fair and direct comparison. For the image classification, our training recipe has a minor difference due to the increased batch size and training epochs with more GPU nodes. As such, we further provide the detailed improvement breakdown here. Specifically, our adopted training recipe leads to $\uparrow 0.2\% \sim \uparrow 1.6\%$ top-1 accuracy improvements and our Caslting-ViT further reduces up to $\downarrow 40\%$ MACs and increases $\uparrow 0.1\% \sim \uparrow 1.2\%$ top-1 accuracy simultaneously.