School of Engineering and Applied Science (SEAS), Ahmedabad University

Probability and Stochastic Processes (MAT277)

Homework Assignment-1

Enrollment No: AU2140096 Name: Ansh Virani

- 1. While tossing a biased die, calculate the probability that face 3 has turned up, Given Alex tells either face 3 or face 6 has turned up.
 - (a) We are given that,

Face	1	2	3	4	5	6
Probability	0.2	0.22	0.11	0.25	0.15	0.07

Let A be the event that face 3 has turned up and B be the event that face 6 has turned up.

$$P(A) = 0.11$$
 & $P(B) = 0.07$

We know that these two are mutually exclusive events, hence:

$$∴ P(A \cup B) = P(A) + P(B)$$
= 0.11 + 0.32
= 0.43

Clearly, here we have to find the conditional probability, $P(A \mid A \cup B)$

$$P(A \mid A \cup B) = \frac{P(A \cap (A \cup B))}{P(A \cup B)}$$
$$= \frac{P(A)}{P(A \cup B)}$$
$$= \frac{0.11}{0.43}$$
$$= 0.2558139535.$$

Hence, the probability that face 3 has turned up, given either face 3 or face 6 has turned up is approx 25.59%

- 2. There exists two events E1 & E2 such that $P(E1 \mid E2) = 0.45, \ P(E2 \mid E1) = 0.5$ and $P(E1 \cup E2) = 0.4$
 - (a) Calculate $P(E1 \cap E2)$:

According to Conditional Probability theorem we can say,

$$P(E1 \mid E2)P(E2) = P(E2 \mid E1)P(E1)$$

 $0.45P(E2) = 0.5P(E1)$

Applying Basic Probaility theorem:

$$P(E1 \cup E2) = P(E1) + P(E2) + P(E1 \cap E2)$$
$$0.4 = 0.9P(E2) + P(E2) + P(E1 \cap E2)$$

$$P(E1 \cap E2) = 1.9P(E2) - 0.4$$

Now, Substituting these values in equation:

$$P(E1 \mid E2) = \frac{P(E1 \cap E2)}{P(E2)}$$
$$0.45 = \frac{1.9P(E2) - 0.4}{P(E2)}$$

$$P(E2) = 0.275$$

Substituting value of e2 in equation 1, we get

0.4 = 1.45P(E2)

$$P(E1) = 0.2475$$

(b) Comment on the dependency relation between event E1 and E2:

When event E2 occurs, there's a 45% chance that event E1 will occur. On the other hand if event E1 occurs, there's a 50% chance that event E2 will occur. This shows that the events are unsymmetrically related.

Also upon calculating it was found that, there's some shared occurance happening beteen two of the given events, as probability of them happening together was found to be 12.25%