

Ch 4 (Important Topics)

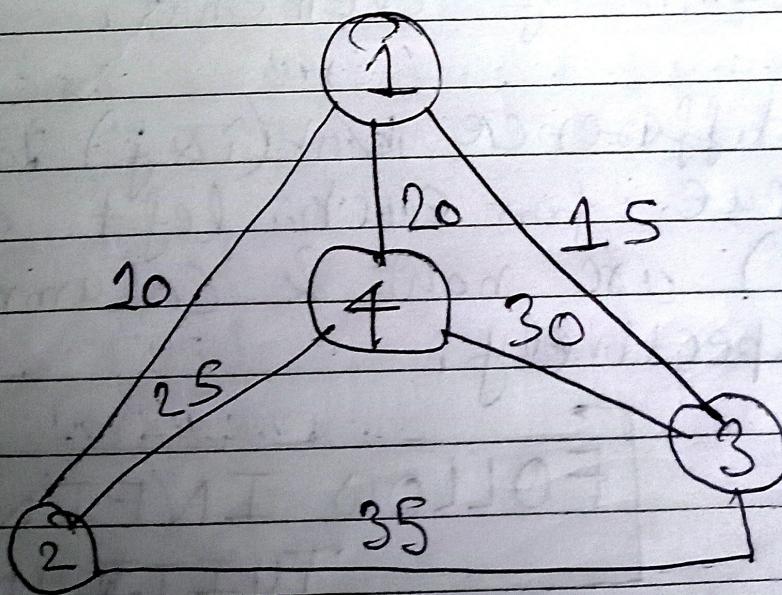
Dynamic Programming

\Rightarrow 1st Priority: \rightarrow TSP \rightarrow Hamilton Cycle

\Rightarrow 2nd Priority: \rightarrow State Space Problem

★(1): TSP (Travelling Salesman Problem):

\rightarrow Let say a set of cities and the distance between every pair of cities, the problem is to find the shortest possible route that visits every city exactly once & returns to the starting point.



→ Let Consider, this graph previous. A (TSP) tour in the graph is 1-2-4-3-1. The cost of the tour is $10 + 25 + 30 + 15$ which is 80. The problem is a famous NP-hard problem. There is no polynomial-time known solution of this problem.

→ Native Solution:

- 1) Consider city (1) as the starting & ending point.
- 2) Generate all $(n-1)!$ (Permutations) of cities.
- 3) Calculate the ~~Cost~~ Cost of every permutation & keep track of the minimum ~~Cost~~ Cost n permutation.
- 4) Return the permutation with minimum cost.

→ Time Complexity: $\Theta(n^2 * 2^n)$, where $\Theta(n^2 * 2^n)$ are maximum no. of unique subproblems/states and $\Theta(n)$ for transition (through for loop as in code) in every state.

→ Auxillary space: $\Theta(n * 2^n)$, where (n) is a number of nodes/cities.

*(2) : 2nd Priority Topic:

* State Space Problem:

- It is a mathematical representation of a problem that defines all possible states that a problem can be.
- It's common techniques used in (AI) Artificial Intelligence.
- A state space problem consists of:
 - 1) A set of states S .
 - 2) An initial state $s \in S$
 - 3) A set of goal states $T \subseteq S$
 - 4) A finite set of actions $A = \{a_1, \dots, a_m\}$
- Each action (a) : $S \rightarrow S$, transforms a state into another state.
- The goal of state space problem is to find the path that leads from the initial to final path/state.

