

**Q.1** Let  $X \sim \text{Binomial}(3, \frac{1}{4})$ . Define  $Y = \frac{X}{1+X}$ . Which of the following statement(s) is(are) true?

Max. score: 1; Neg. score: 0; Your score: 1

- ☐  $\mathbb{E}(Y) > 0.42$
- ☒  $\mathbb{E}(Y) \leq 0.42$
- ☒  $\text{Var}(Y) \leq 0.09$
- ☐  $\text{Var}(Y) > 0.09$

**Q.2** Let  $X$  be a random variable taking values in the interval  $[1, 5]$ . Then, which of the following statement(s) is(are) always correct?

Max. score: 1.5; Neg. score: 0; Your score: 0

- ☐  $\text{Var}(X) \leq 8/3$
- ☒  $\text{Var}(X) \leq 4$
- ☐  $\text{Var}(X) \leq 16/5$
- ☐  $\text{Var}(X) \leq 2$

**Q.3** Suppose we are given three events A, B and C such that:

- (i) A and B are independent,
- (ii) B and C are independent.

Then, choose the correct option(s) from below:

Max. score: 1; Neg. score: 0; Your score: 1

- ☒ ☐ A, B and C may not be independent
- ☐ A, B and C are always independent
- ☒ ☐ B and  $A \cap C$  may not be independent
- ☐ B and  $A \cap C$  are always independent

**Q.4** Let  $X \sim N(5, 18)$ . Define  $Y = \exp(X)$  and

$$h(y) = \int_0^y \frac{1}{u} \exp\left(-\frac{(\ln u - 5)^2}{36}\right) du.$$

Find  $30 \times P[h(Y) \leq \sqrt{\pi}]$ .

*Max. score: 1.5; Neg. score: 0; Your score: 0*

Your answer:

1

Correct answer:

5