

Warming up to looking at “Energy inwards”!

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Let us get to Work with Ideal Gas!

- $P_{\text{external}} * V = \frac{F_{\text{external}}}{L^2} * L^3 = \frac{N_A m v^2}{3 L^3} * L^3 = \frac{N_A m v^2}{3} = N_A * K_B * T$
- $PV = N_{\text{Ava}} * K_{\text{Boltzmann constant}} * T = R_{\text{gas constant}} * T$
- $\frac{mv^2}{2} = 3 * \left(\frac{K_B * T}{2} \right)$!!!-Equipartition theorem-3 DOF
- v =Average velocity of an ideal gas atom; It is NOT C.O.M velocity!
- What has been accomplished: Meaning of measured macroscopic TD T in terms of microscopic mechanical variable v

Energy of a “continuum” in classical mechanics

- Continuum: “a **continuous** sequence in which adjacent **segments** are not **perceptibly** different from each other...”
- We are not resolving material segments into atoms/electrons...
- Energy due to the motion of the Center Of Mass: Kinetic energy
- Energy due to position of the C.O.M in a force-field: Potential Energy
- From mechanics to thermodynamics...?
- Is the “energy content” of Bumbrah’s ball at 150 km/h same when he is bowling in Australian winter and Kanpur summer?
- Is the “energy content” of Cu metal block elevated to 1000 m different when it is at 50°C and 500 °C?
- **In addition to K. E & P.E, how does T affect the energy content?**

Work-Energy theorem of classical mechanics

- The net work done on a particle equals the change in the particle's kinetic energy: $W_{\text{net}} = K_B - K_A$
- $dW_{\text{net}} = \vec{F} \cdot d\vec{r}$
- $\vec{F} = \frac{d\vec{v}}{dt}$
- How do we extend work-energy theorem to thermodynamics?

Joule's Experiments (1843 to 1848)

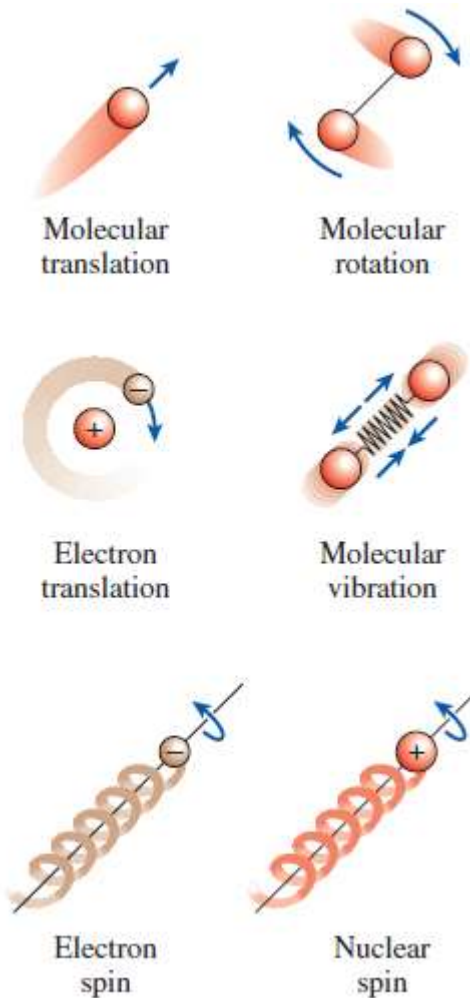
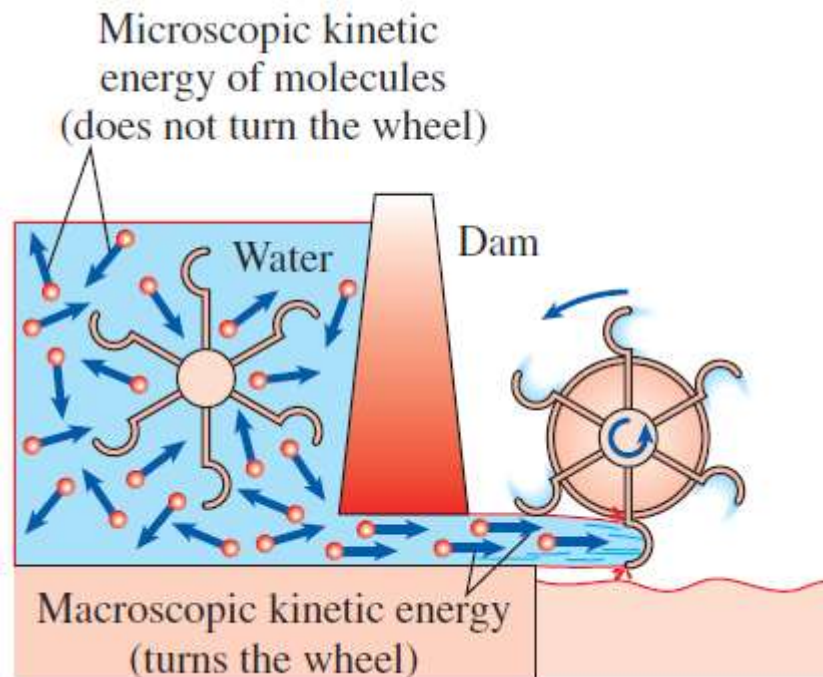
- <https://demonstrations.wolfram.com/JoulesExperiment/>
- What happens to the work done on the system contained within a adiabatically walled container whose C.O.M Kinetic & Potential Energy does not change?
- Temperature increased!
- By equipartition theorem, temperature is correlated to average velocity of atoms of the liquid in the adiabatically walled contained
- Note: Not C.O.M velocity; Atomic velocities are random and are correlated to temperature

Microscopic DOF provides additional ways of storing energy

- Beyond C.O.M “directional positional change” (potential E) & “directional motion” (kinetic E), there is “internal energy” due to “random” motion atoms
- In Joule's experiment, the work done on the system within the adiabatically walled container increased the capacity of the system to store heat, with the increase corresponding to an increase in temperature
- Joule also found that similar amount of other forms of work (like electrical) also gave rise to similar increase in temperature
- All work can be converted to heat resulting in increase of temperature!

Relevant microscopic DOF depends on T

- Excitable DOF
- Typically, engineering systems are “cold” in terms of electronic and nuclear DOF



Figs: Cengel & Boles 7

Multi Scale Nature of Energy

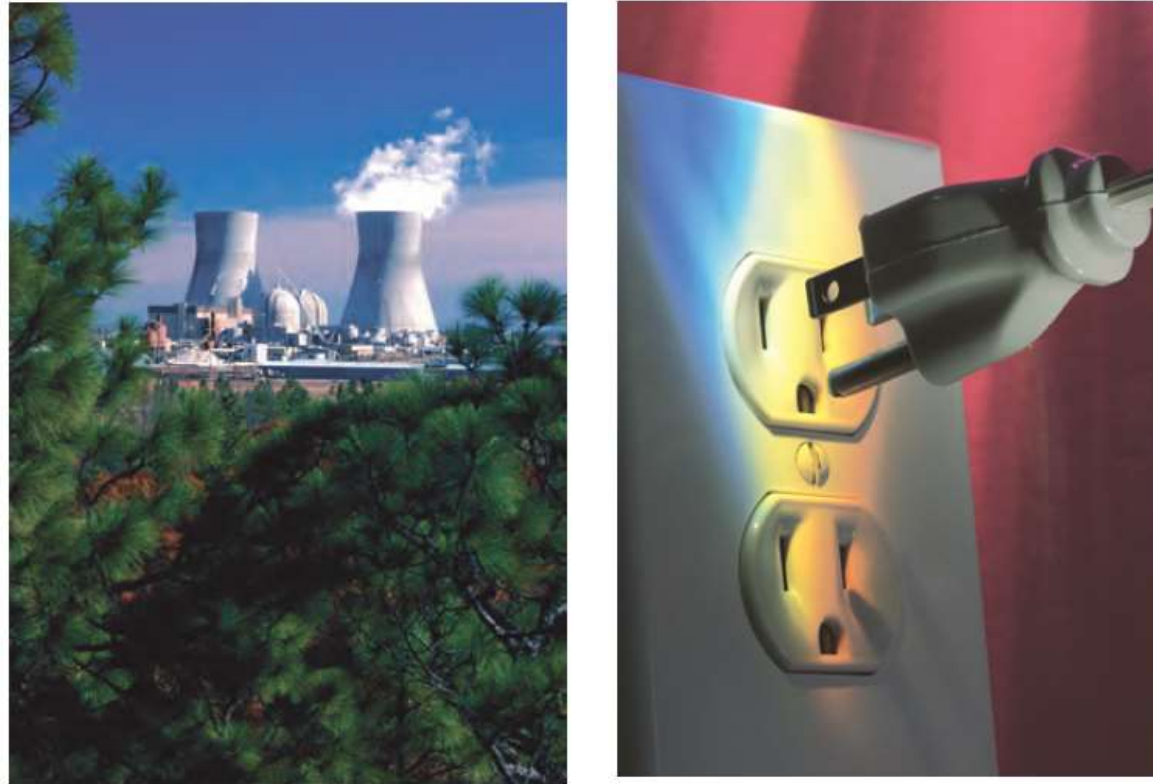


FIGURE 2-3

At least six different forms of energy are encountered in bringing power from a nuclear plant to your home: nuclear, thermal, mechanical, kinetic, magnetic, and electrical.

Advertising First Law of Thermodynamics: Extending Work-Energy beyond mechanics

$$\Delta U = \text{Change in Internal Energy } U = \text{"Heat \& work exchange"} = "q - W"$$