

# Computer Networks I

## Network Security

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# What is network security?

*confidentiality*: only sender, intended receiver should “understand” message contents

- sender encrypts message
- receiver decrypts message

*authentication*: sender, receiver want to confirm identity of each other

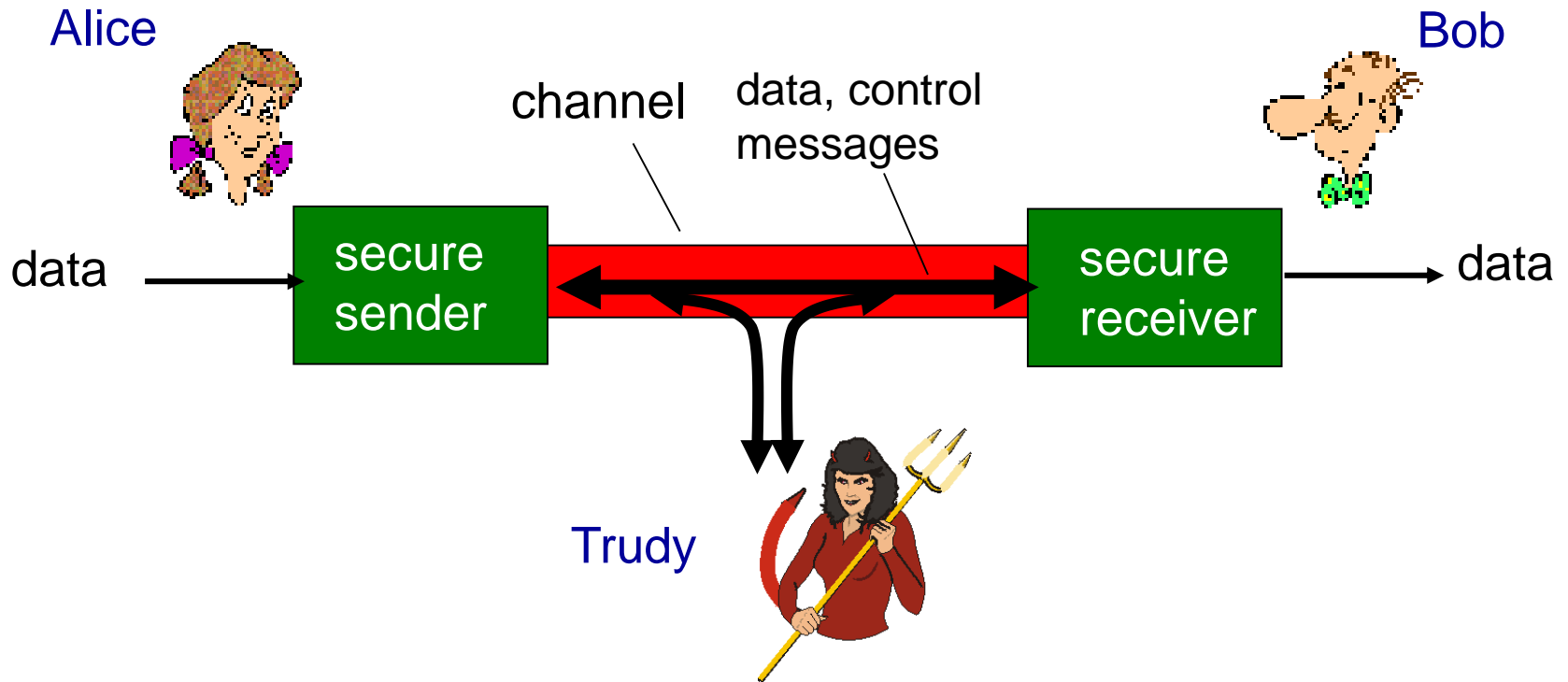
*message integrity*: sender, receiver want to ensure message not altered (in transit, or afterwards) without detection

*access and availability*: services must be accessible and available to users

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# Friends and enemies: Alice, Bob, Trudy

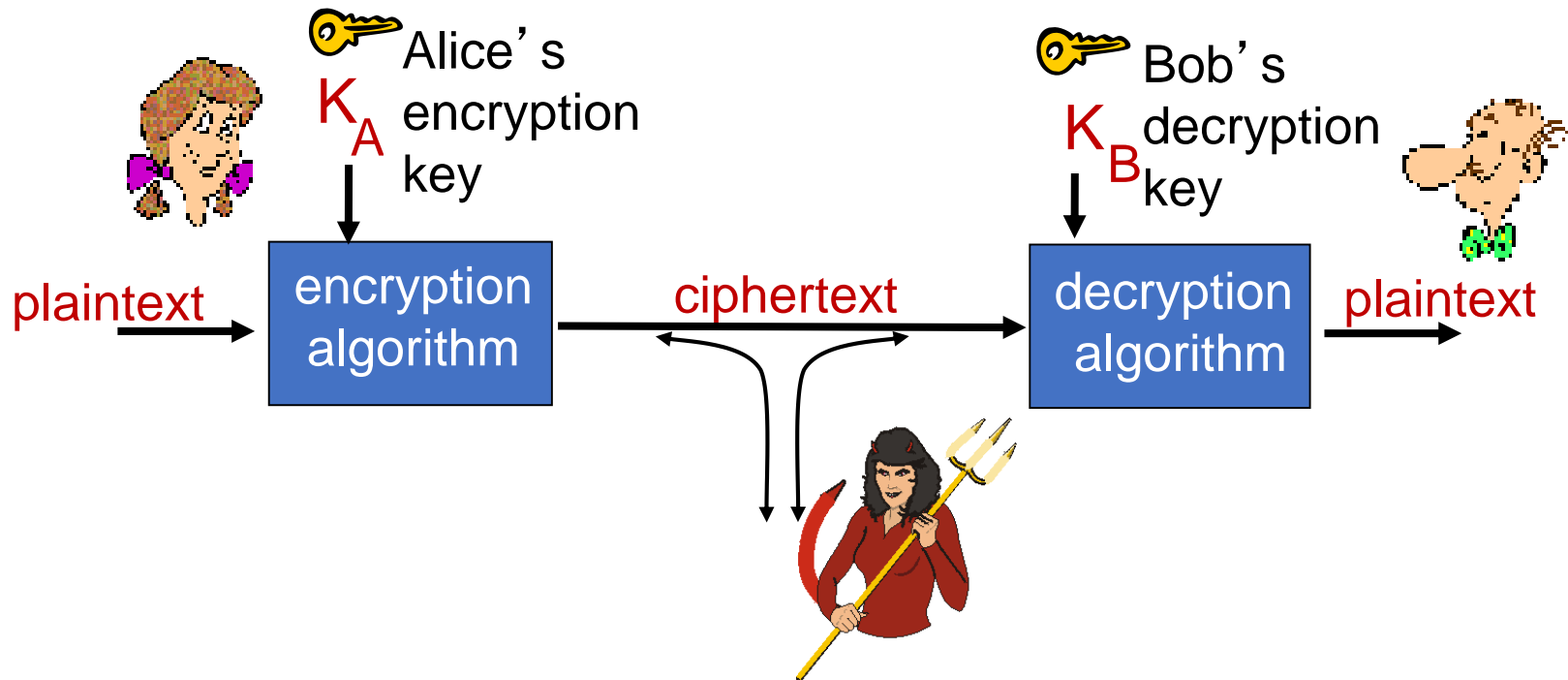
- Bob, Alice want to communicate “securely”
- Trudy (intruder) may intercept, delete, add messages



# Principles of Cryptography

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# The language of cryptography



$m$  plaintext message

$K_A(m)$  ciphertext, encrypted with key  $K_A$

$m = K_B(K_A(m))$

# Simple encryption scheme

*substitution cipher*: substituting one thing for another

- monoalphabetic cipher: substitute one letter for another

**plaintext:**    abcdefghijklmnopqrstuvwxyz

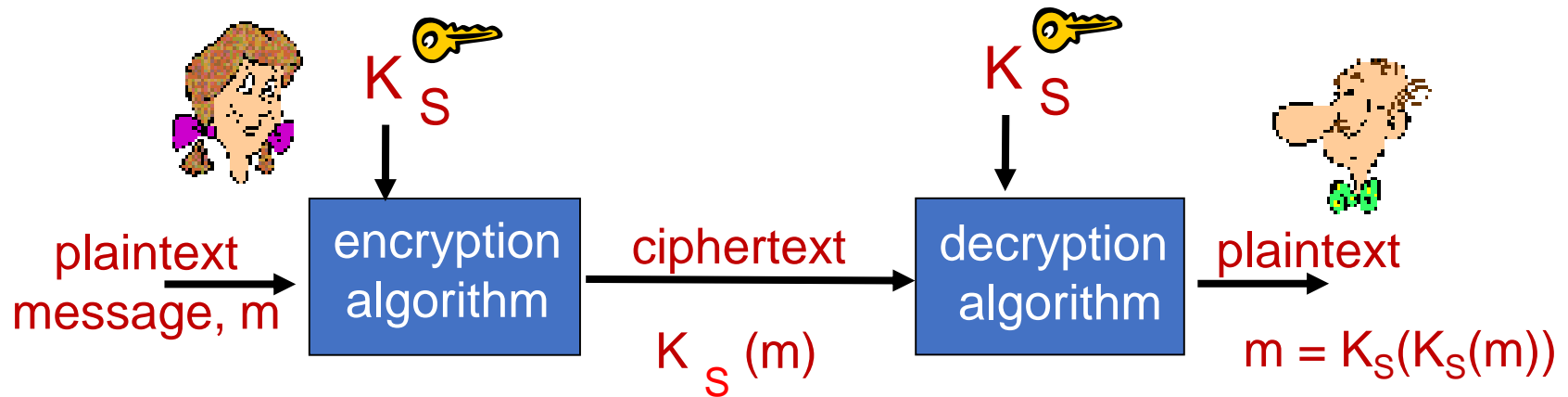
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**ciphertext:**   mnbvcxzasdfghjklpoiuytrewq

e.g.: Plaintext:     i                   Alice  
          ciphertext:   s gktc wky    mgsbc

🔑 **Encryption key:** mapping from set of 26 letters to set of 26 letters

# Symmetric key cryptography



**symmetric key crypto:** Bob and Alice share same (symmetric) key:  $K_S$

**Examples:** DES (Data Encryption Standard), AES (Advanced Encryption Standard)

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# Public Key Cryptography

## *symmetric key crypto*

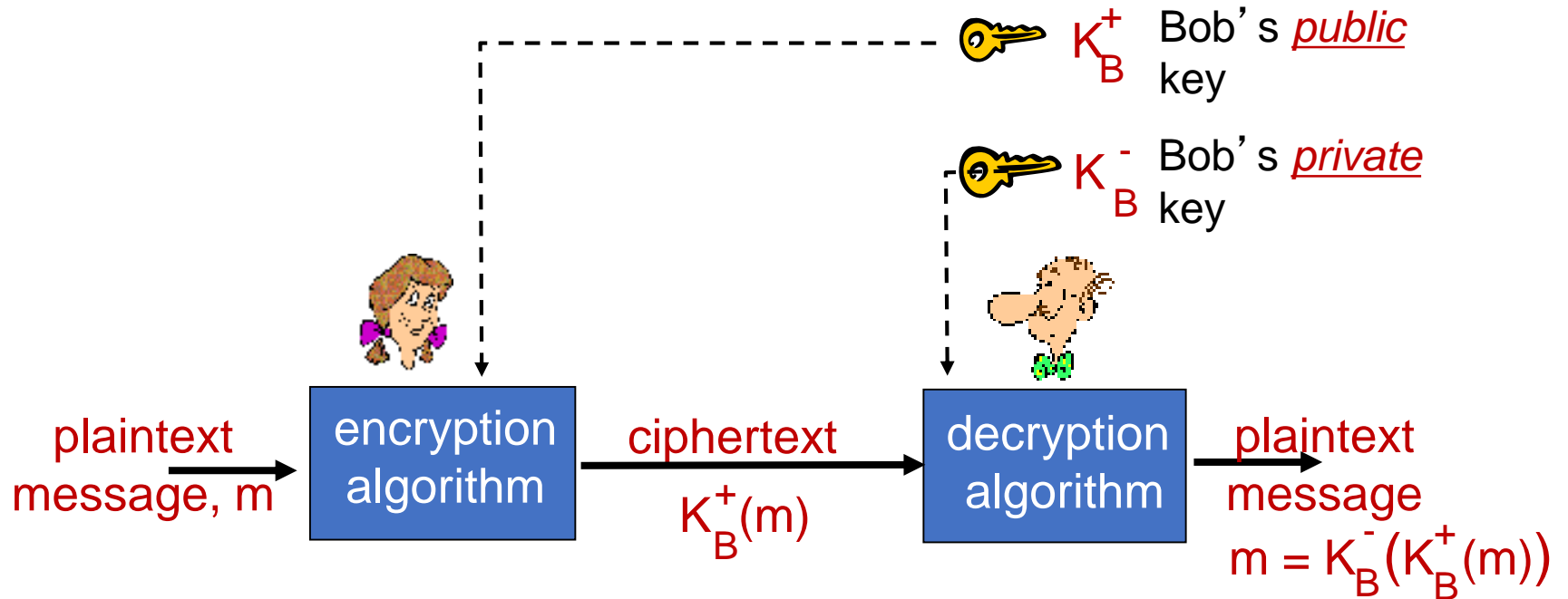
- requires sender, receiver know shared secret key
- Q: how to agree on key in first place (particularly if never “met”)?

## *public key crypto*

- radically different approach [Diffie-Hellman76, RSA78]
- sender, receiver do *not* share secret key
- *public* encryption key known to *all*
- *private* decryption key known only to receiver



# Public key cryptography



# Public key encryption algorithms

① need  $K_B^+(\cdot)$  and  $K_B^-(\cdot)$  such that

$$K_B^-(K_B^+(m)) = m$$

② given public key  $K_B^+$ , it should be impossible to compute private key  $K_B^-$

**RSA:** Rivest, Shamir, Adelson algorithm

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# RSA: Creating public/private key pair

1. choose two large prime numbers  $p, q$ .  
(e.g., 1024 bits each)
  2. compute  $n = pq$ ,  $z = (p-1)(q-1)$
  3. choose  $e$  (with  $e < n$ ) that has no common factors with  $z$  ( $e, z$  are “relatively prime”).
  4. choose  $d$  such that  $ed-1$  is exactly divisible by  $z$ .  
(in other words:  $ed \bmod z = 1$ ).
- 
5. public key is  $\underbrace{(n, e)}_{K_B^+}$ . private key is  $\underbrace{(n, d)}_{K_B^-}$ .

# RSA: encryption, decryption

0. given  $(n,e)$  and  $(n,d)$  as computed above

1. to encrypt message  $m$  ( $<n$ ), compute

$$c = m^e \bmod n$$

2. to decrypt received bit pattern,  $c$ , compute

$$m = c^d \bmod n$$

*magic happens!*

$$m = \underbrace{(m^e \bmod n)}_c^d \bmod n$$

$$\text{Why? } m = \underbrace{(m^e \bmod n)}_c^d \bmod n$$

- Useful number theory result: If  $p, q$  are prime and  $n = pq$ , then  $x^y \bmod n = x^{y \bmod (p-1)(q-1)} \bmod n$
  - $(m^e \bmod n)^d \bmod n$ 
    - $= m^{ed} \bmod n$
    - $= m^{ed \bmod (p-1)(q-1)} \bmod n$  [using the theorem]
    - $= m^1 \bmod n$  [as  $ed-1$  is divisible by  $(p-1)(q-1)$ ]
    - $= m$
-

# RSA: another important property

The following property will be *very* useful later:

$$\underbrace{K_B^-(K_B^+(m))}_{\text{use public key first, followed by private key}} = m = \underbrace{K_B^+(K_B^-(m))}_{\text{use private key first, followed by public key}}$$

use public key first,  
followed by  
private key

use private key  
first, followed by  
public key

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Why  $K_B^-(K_B^+(m)) = m = K_B^+(K_B^-(m))$  ?

follows directly from modular arithmetic:

$$\begin{aligned}(m^e \bmod n)^d \bmod n &= m^{ed} \bmod n \\ &= m^{de} \bmod n \\ &= (m^d \bmod n)^e \bmod n\end{aligned}$$

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# Authentication

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# Authentication

*Goal:* Bob wants Alice to “prove” her identity to him

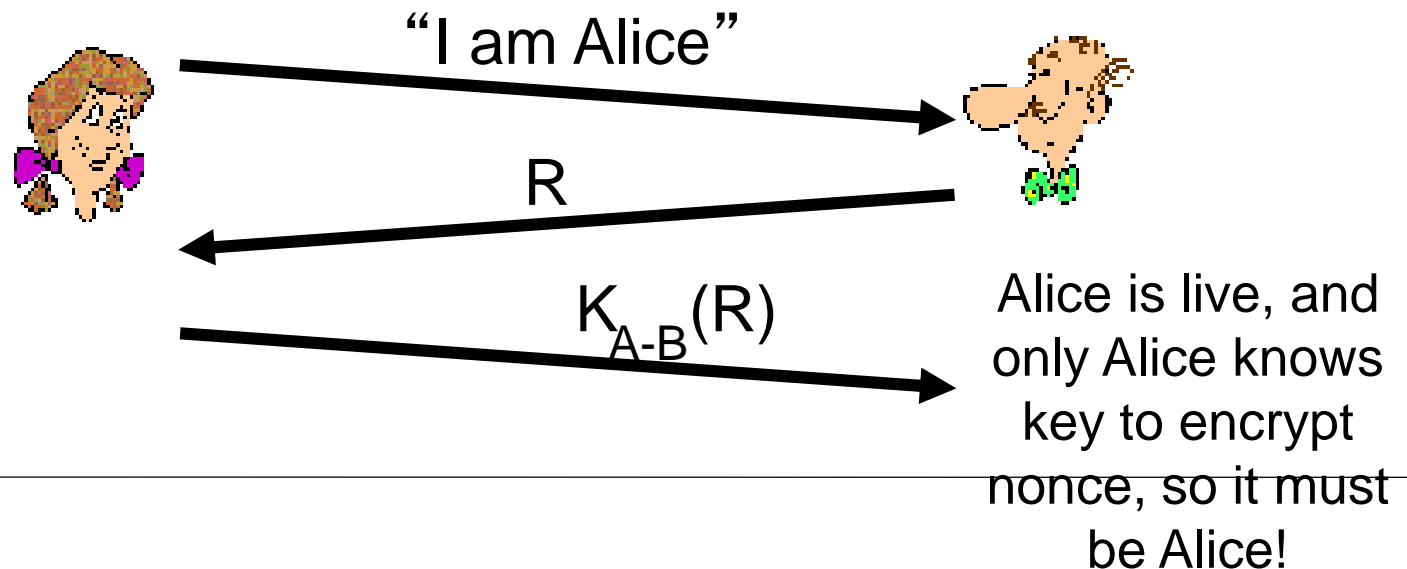
*Approach:* Alice says “I am Alice”



# Authentication

**nonce:** number (R) used only *once-in-a-lifetime*

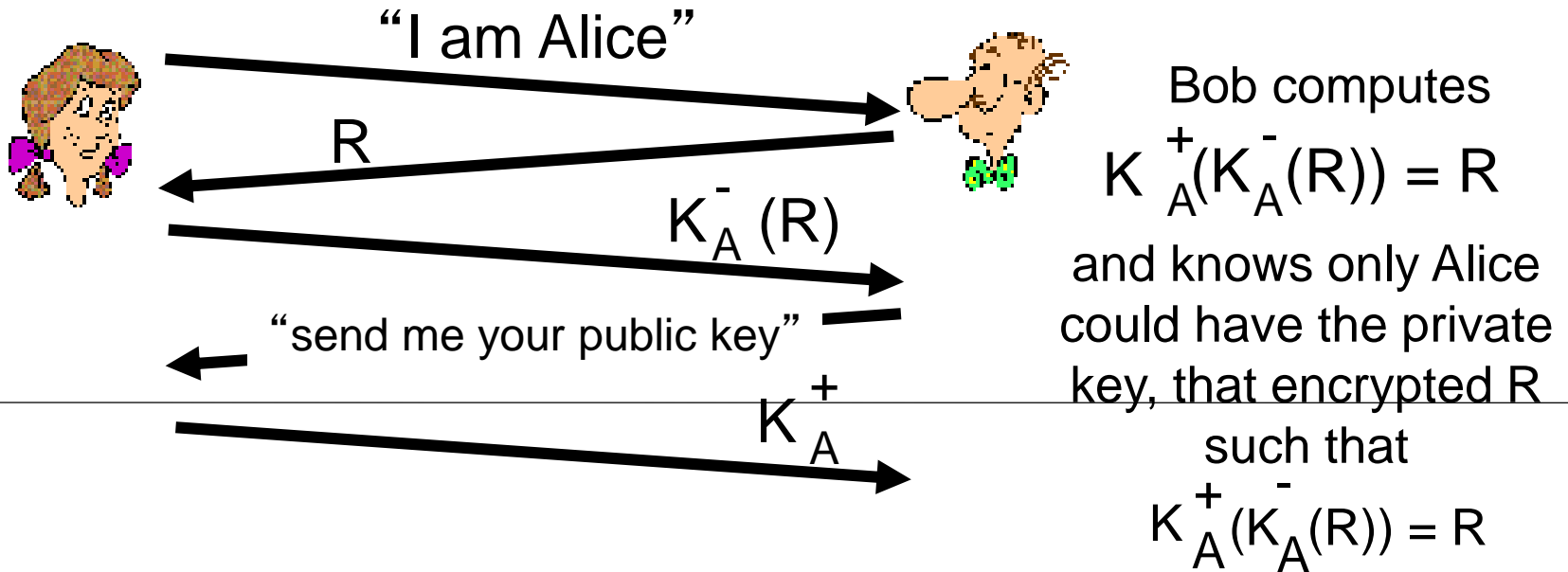
**Approach:** to prove Alice “live”, Bob sends Alice **nonce**, R.  
Alice must return R, encrypted with shared secret key



# Authentication

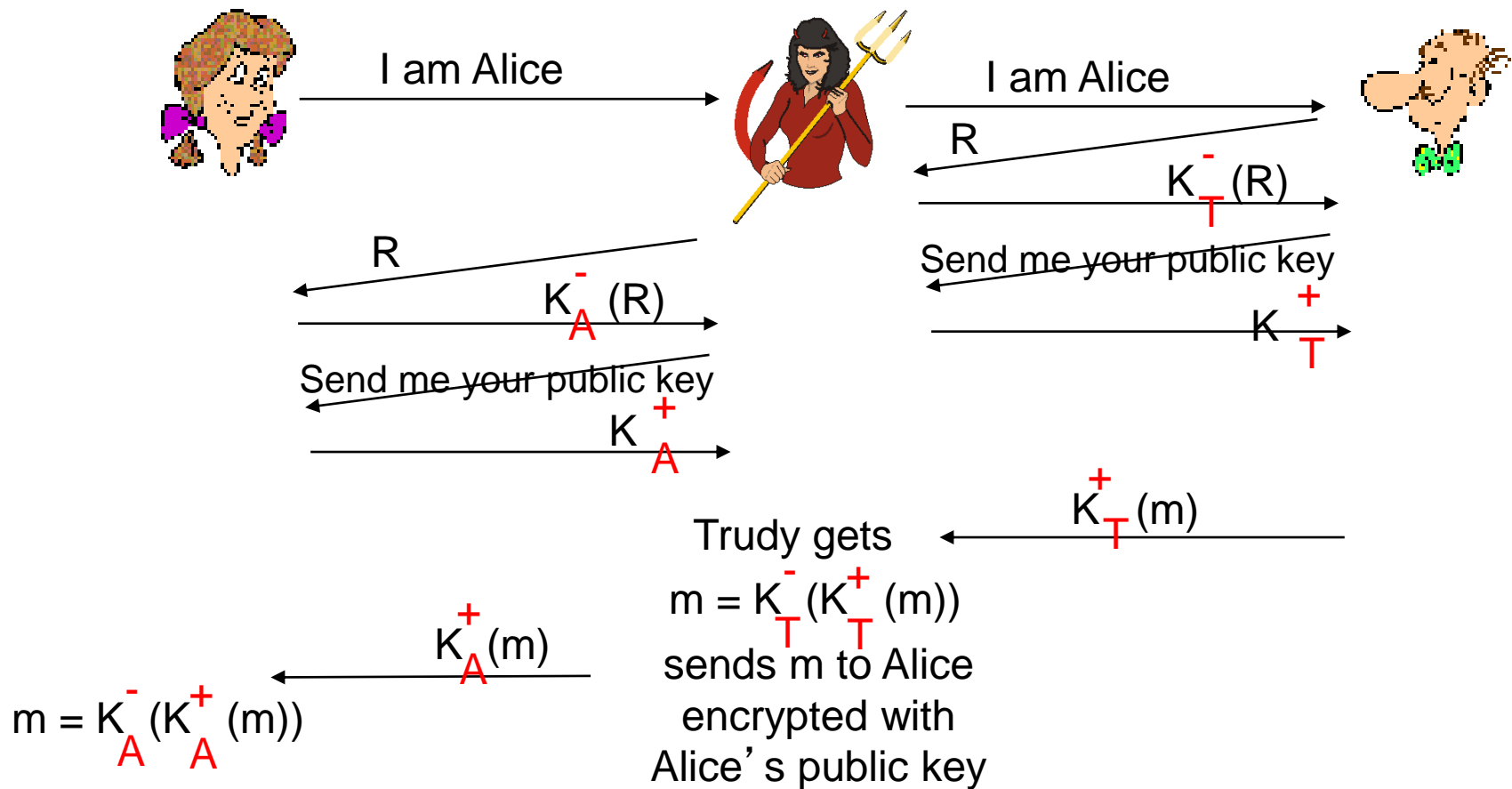
- Can we authenticate using public key techniques?

*Approach:* use nonce, public key cryptography



# Authentication

*man (or woman) in the middle attack:* Trudy poses as Alice (to Bob) and as Bob (to Alice)



# Message Integrity

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# Digital signatures

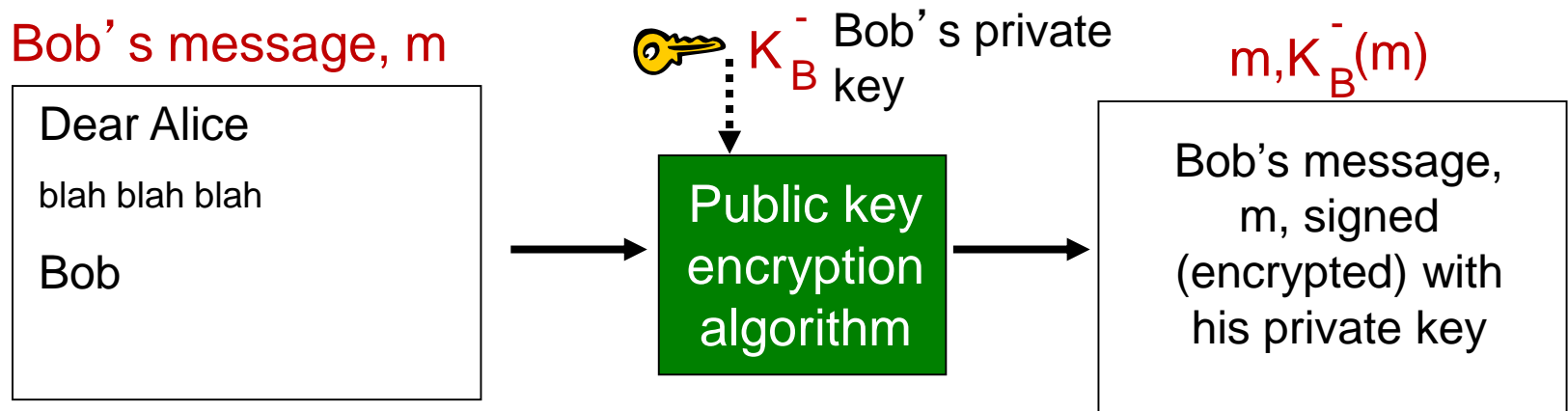
cryptographic technique analogous to hand-written signatures:

- sender (Bob) digitally signs document, establishing he is document owner/creator.
  - *verifiable, nonforgeable*: recipient (Alice) can prove to someone that Bob, and no one else (including Alice), must have signed document
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# Digital signatures

## simple digital signature for message $m$ :

- Bob signs  $m$  by encrypting with his private key  $K_B^-$ , creating “signed” message,  $K_B^-(m)$



# Digital signatures

- suppose Alice receives msg  $m$ , with signature:  $m, K_B^-(m)$
- Alice verifies  $m$  signed by Bob by applying Bob's public key  $K_B^+$  to  $K_B^-(m)$  then checks  $K_B^+(K_B^-(m)) = m$ .
- If  $K_B^+(K_B^-(m)) = m$ , whoever signed  $m$  must have used Bob's private key.

Alice thus verifies that:

- Bob signed  $m$
- no one else signed  $m$

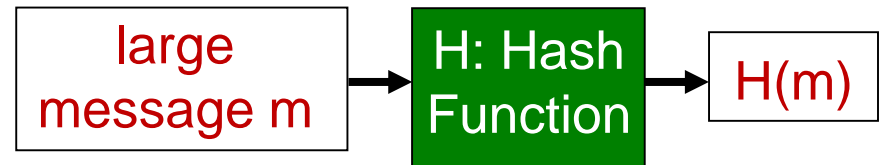


# Message digests

computationally expensive  
to public-key-encrypt long  
messages

**goal:** fixed-length, easy- to-  
compute digital  
“fingerprint”

- apply hash function  $H$  to  $m$ ,  
get fixed size message digest,  
 $H(m)$ .

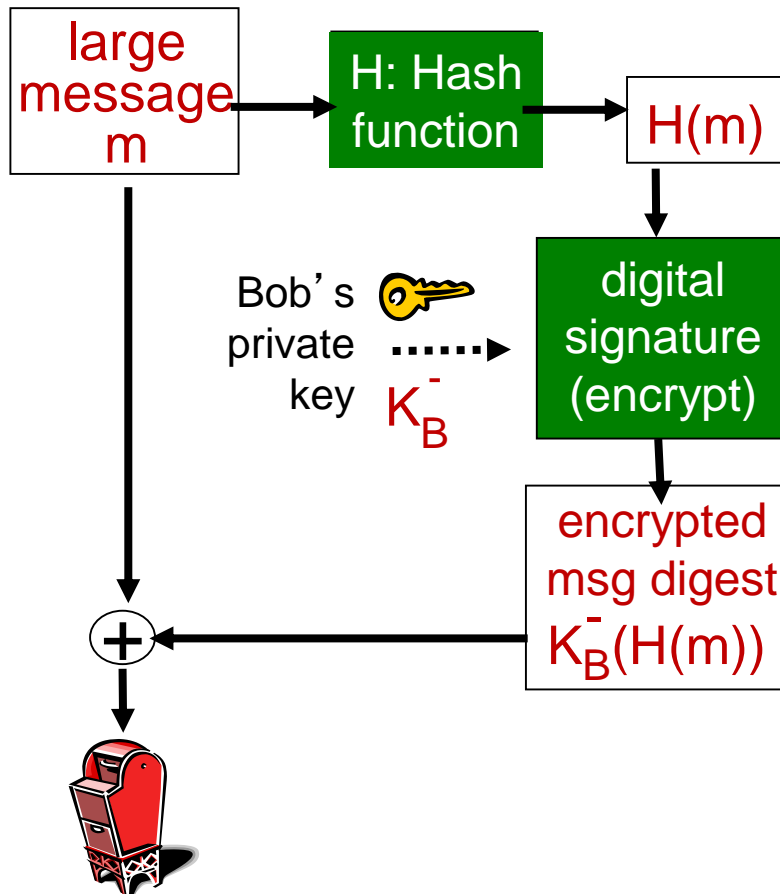


**Hash function properties:**

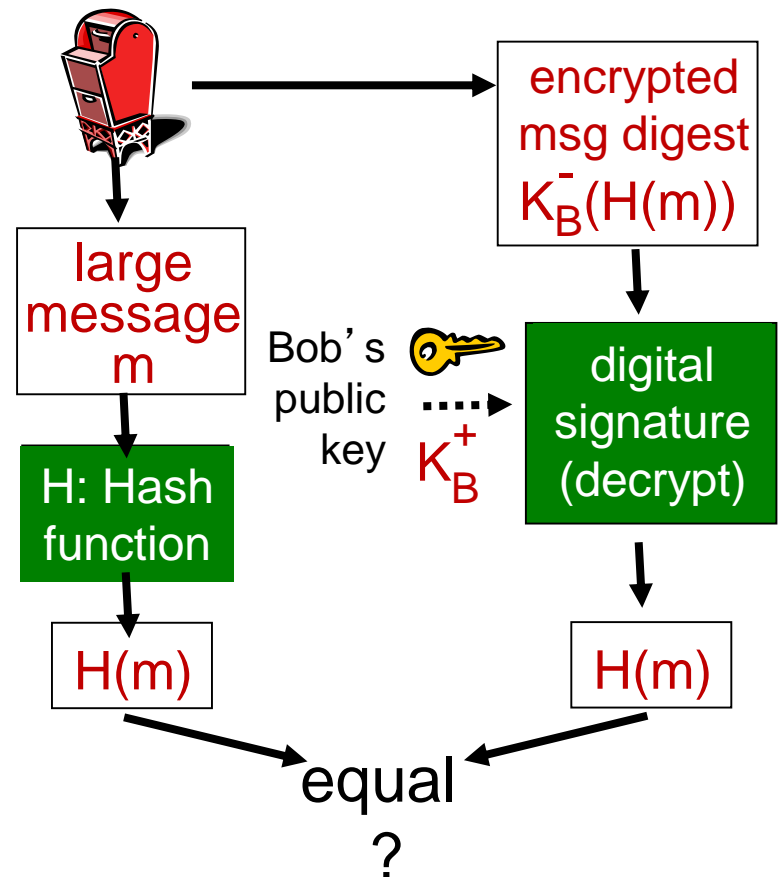
- many-to-1
- produces fixed-size msg  
digest (fingerprint)
- given message digest  $x$ ,  
computationally infeasible to  
find  $m$  such that  $x = H(m)$

# Digital signature = signed message digest

Bob sends digitally signed message:



Alice verifies signature, integrity of digitally signed message:



# Hash function algorithms

- MD5 hash function widely used (RFC 1321)
    - computes 128-bit message digest in 4-step process.
  - SHA-1 is also used
    - US standard [NIST, FIPS PUB 180-1]
    - 160-bit message digest
  - Other SHA standards:  
<https://en.wikipedia.org/wiki/SHA-1>
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# THANK YOU

QUESTIONS???

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