

Table 10-5 Summary of Confidence Interval Procedures

Problem Type	Point Estimator	Two-Sided $100(1 - \alpha)\%$ Confidence Interval
Mean μ of a normal distribution, variance σ^2 known	\bar{X}	$\bar{X} - Z_{\alpha/2} \sigma / \sqrt{n} \leq \mu \leq \bar{X} + Z_{\alpha/2} \sigma / \sqrt{n}$
Difference in means of two normal distributions μ_1 and μ_2 , variances σ_1^2 and σ_2^2 known	$\bar{X}_1 - \bar{X}_2$	$\bar{X}_1 - \bar{X}_2 - Z_{\alpha/2} \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}} \leq \mu_1 - \mu_2 \leq \bar{X}_1 - \bar{X}_2 + Z_{\alpha/2} \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}$
Mean μ of a normal distribution, variance σ^2 unknown	\bar{X}	$\bar{X} - t_{\alpha/2, n-1} S / \sqrt{n} \leq \mu \leq \bar{X} + t_{\alpha/2, n-1} S / \sqrt{n}$
Difference in means of two normal distributions $\mu_1 - \mu_2$, variance $\sigma_1^2 = \sigma_2^2$ unknown	$\bar{X}_1 - \bar{X}_2$	$\bar{X}_1 - \bar{X}_2 - t_{\alpha/2, n_1+n_2-2} S_p \sqrt{\frac{1}{n_1} + \frac{1}{n_2}} \leq \mu_1 - \mu_2 \leq \bar{X}_1 - \bar{X}_2 + t_{\alpha/2, n_1+n_2-2} S_p \sqrt{\frac{1}{n_1} + \frac{1}{n_2}},$ <p style="text-align: center;">where $S_p = \sqrt{\frac{(n_1-1)S_1^2 + (n_2-1)S_2^2}{n_1 + n_2 - 2}}$</p>
Difference in means of two normal distributions for paired samples $\mu_D = \mu_1 - \mu_2$	\bar{D}	$\bar{D} - t_{\alpha/2, n-1} S_D / \sqrt{n} \leq \mu_D \leq \bar{D} + t_{\alpha/2, n-1} S_D / \sqrt{n}$
Variance σ^2 of a normal distribution	S^2	$\frac{(n-1)S^2}{\chi_{\alpha/2, n-1}^2} \leq \sigma^2 \leq \frac{(n-1)S^2}{\chi_{1-\alpha/2, n-1}^2}$
Ratio of the variances σ_1^2 / σ_2^2 of two normal distributions	$\frac{S_1^2}{S_2^2}$	$\frac{S_1^2}{S_2^2} F_{1-\alpha/2, n_1-1, n_2-1} \leq \frac{\sigma_1^2}{\sigma_2^2} \leq \frac{S_1^2}{S_2^2} F_{\alpha/2, n_1-1, n_2-1}$
Proportion or parameter of a binomial distribution p	\hat{p}	$\hat{p} - Z_{\alpha/2} \sqrt{\frac{\hat{p}(1-\hat{p})}{n}} \leq p \leq \hat{p} + Z_{\alpha/2} \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$
Difference in two proportions or two binomial parameters $p_1 - p_2$	$\hat{p}_1 - \hat{p}_2$	$\hat{p}_1 - \hat{p}_2 - Z_{\alpha/2} \sqrt{\frac{\hat{p}_1(1-\hat{p}_1)}{n_1} + \frac{\hat{p}_2(1-\hat{p}_2)}{n_2}} \leq p_1 - p_2 \leq \hat{p}_1 - \hat{p}_2 + Z_{\alpha/2} \sqrt{\frac{\hat{p}_1(1-\hat{p}_1)}{n_1} + \frac{\hat{p}_2(1-\hat{p}_2)}{n_2}}$