

Q. ~~9~~

Eg.  $A_n = \emptyset$  given  $(\forall n)$

Prove that  $A_n = \emptyset$  <sup>given  $(\forall n)$</sup>  satisfies the stated properties.

Proof: If  $(\forall n)(A_n = \emptyset)$ , then  $A_{n+1} = \emptyset$ . Thus,  $A_{n+1} \subseteq A_n$ . ( $\emptyset \subseteq \emptyset$ )

Since  $(\forall n)(A_n = \emptyset)$ , then  $\bigcap_{n=1}^{\infty} A_n = \bigcap_{n=1}^{\infty} \emptyset = \emptyset$ .

Thus, the ~~statement~~ example is proven.

QED 