Binary Search Advanced Problems

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Class	
• Туре	
Materials	

Minimax Searching Problems

In minimax Searching problem, we are generally expected to minimise the maximum of a value or maximise the minimum of a value.

SPOJ.com - Problem AGGRCOW Farmer John has built a new long barn, with N (2 <= N <= 100,000) stalls. The stalls are located along a straight line at positions x1,...,xN (0 <= xi <= 1,000,000,000). His C (2 <= C <= N) cows don't S https://www.spoj.com/problems/AGGRCOW/

In the above given problem, we are expected to maximise the minimum distance between two cows. Hence a Minimax Searching problem it is.

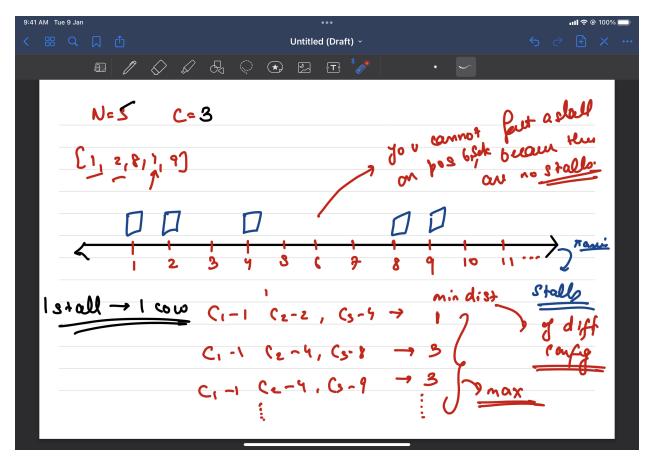
Note: These minimax problems are different than the one mentioned in AI and related subjects.

And if at any point of time we see that we are trying to solve a minimax problem then Binary Search is very helpful in those cases.

A lot of times these minimax problems are asked clubbed with binary search on answer.

Problem 1:





In this problem, we have to maximise the minimum distance. By maximising the minimum distance we say that we have placed all the cows as far apart as possible.

There can be different configurations to place the cows in the stalls. In each configuration we can calculate min distance between any two adjacent cows in the configuration. Now among all of these minimum distance we have to return the distance which is maximum of all. We don't need the config, but only to return the value of maximised minimum distance between any two cows.

Solutions:

Brute Force?

In the given problem, we have N stalls and C cows, so we can try all possible combinations? Try to put the next available cow to all the next available stalls.

How to optimise?

Because it is a minimax problem, we can try first of all to reduce it to a binary search based problem. Binary search is a searching algorithm, and what is the quantity of ans we want to search for? Distance is the quantity. If somehow we can define the range of minimum distances possible between any two cows then we can try to think this range as a search space and apply binary search.

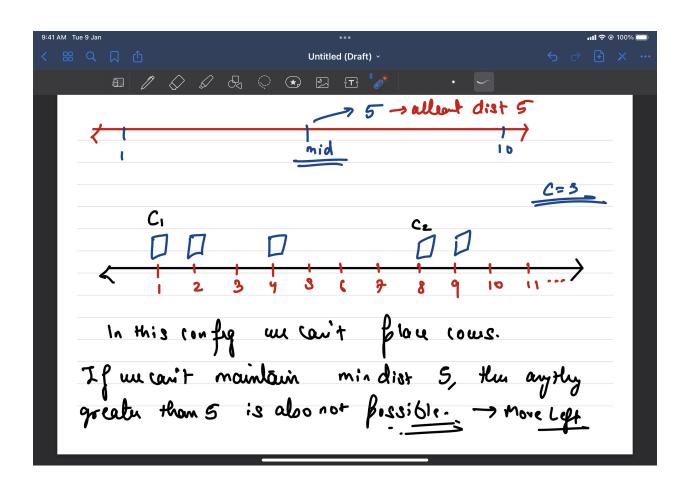
For N = 5, $[1,2,8,4,9] \rightarrow$ In the worst case what can be the minimum distance between any two cows for this given array? Ans : 1

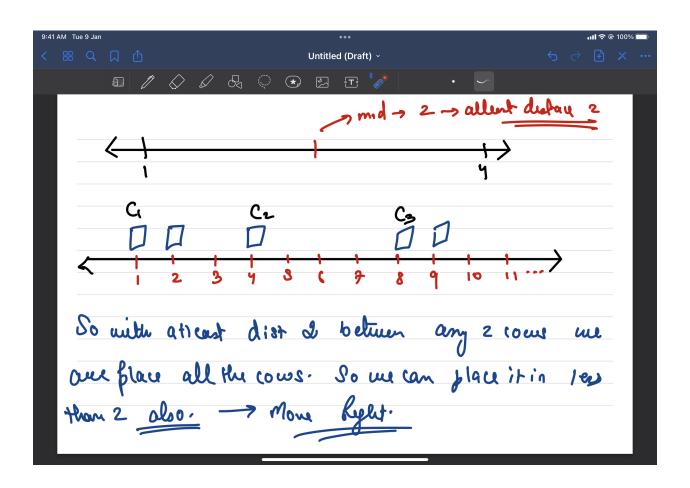
In the worst case what can be the maximum distance between two cows for this array ?

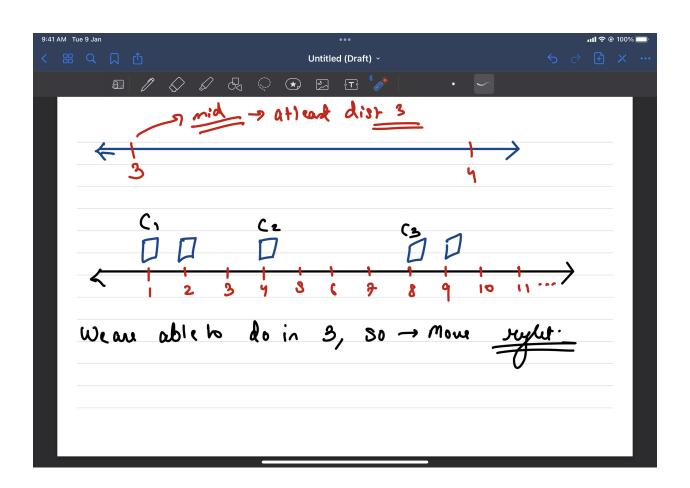
Calculating the range of the search space in few problems can be tedious. So what we can do is assume some very large and some very small valid values.

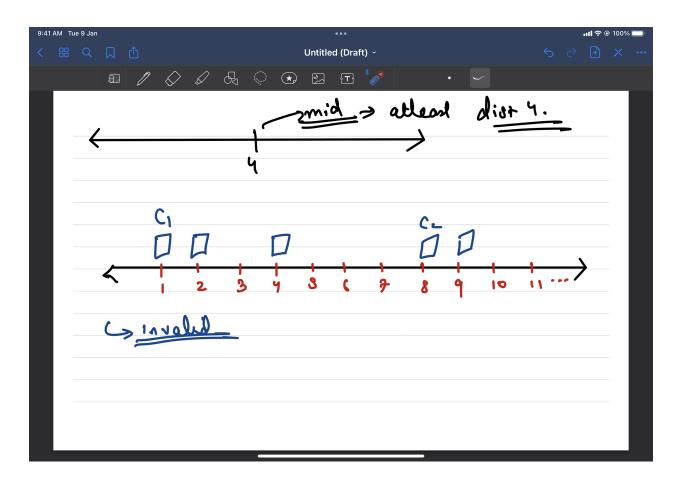
Range: $[1, 10] \rightarrow$ All those values that won't be possible in our ans will be eventually removed from the search space.

In this range, I will try to get a possible value say mid, and then check is it possible to place the cows such that minimum distance between any two cows is mid.









```
function canPlaceCows(c, mid, stalls) {
 // Time: O(n)
 let lastPlacedPosition = 0;
 c--; // as first cow is already placed;
 for(let i = 1; i < stalls.length; i++) {
   if(stalls[i] - stalls[lastPlacedPosition] >= mid) {
     c--; // place one more cow
      lastPlacedPosition = i;
   }
   if(c == 0) return true; // we placed all the cows
  // if we didn't place all the cows, then we will never retrun true from above
  return false;
function getMaximisedMinDist(stalls, c) {
// time: 0(nlogn) Space: 0(1)
  stalls.sort((a, b) \Rightarrow a-b); // sorting the stalls to iterate easily
 let lo = 1, hi = stalls[stalls.length - 1];
 let ans = 1;
 while(lo <= hi) {</pre>
   let mid = lo + Math.floor((hi - lo) / 2);
   if(canPlaceCows(c, mid, stalls) == true) {
      // if we are able to place the cows with atleast mid distance, then
      // mid is a possible ans, but we can find something greater than mid also
```

```
ans = mid;
lo = mid + 1;
} else {
    hi = mid - 1;
}
return ans;
}
```