

Note: On the left side I have wrote the frequencies (only where it's required), in the middle I have pasted the code and on the right side I have wrote the units each instruction will take.

For sequential statements I have simply put ----- and wrote the unit it would take and for the loops I have used the bracket notation representing the units for each, for loop part respectively e.g. for(int I = 0; I < n; I++) \leftrightarrow (1; n + 1; n). I have highlighted my answers with yellow. I hope this will help you to understand my way of solving.

TASK – 01

1.

```
-      int a = 0, b = 0;      ----- 1 unit
-      for (i = 0; i < n; i++)      ----- (1; n + 1; n)
-      {
n      a = a + i; ----- 1 unit
-      }
-      for (j = 0; j < n; j++)      ----- (1; n + 1; n)
-      {
n      b = b + j; ----- 1 unit
-      }
```

Solution: = 1 + 1 + n + 1 + n + n * (1) + 1 + n + 1 + n + n * (1)

$$T(n) = 6n + 5$$

2.

```
1      int a = 0;      ----- 1 unit
-      for (i = 0; i < n; i++)      ----- (1; n + 1; n) unit
-      {
n          for (j = n; j > 0; j--)----- (1, n + 1; n) unit
-          {
n              a = a + i + j; ----- 1 unit
-              }
-      }
```

Solution: = 1 + 1 + n + 1 + n + n * (1 + n + 1 + n + n)

$$T(n) = 3n^2 + 4n + 3$$

3.

```
1      int sum = 0; ----- 1 unit
-      for (int i = 1; i < n; i *= 2) ----- (1; log2n + 1; log2n)
-      {
log2n          for (int j = 0; j < n; j++) ----- (1; n + 1; n)
-              {
log2n          sum++; ----- 1 unit
-              }
-      }
```

Solution: = 1 + 1 + log₂n + 1 + log₂n + log₂n * (1 + n + 1 + n + n)

$$T(n) = 3n \log_2 n + 4 \log_2 n + 3$$

4.

```
1      int a = 0, i = n;
-      while (i > 0) ----- (log2n + 2)
    {
log2n + 1      a += i;          ----- 1 unit
log2n + 1      i /= 2;          ----- 1 unit
    }
```

Solution: = 1 + log₂n + 2 + (log₂n + 1) * (2)

T(n) = 3log₂n + 5

5.

```
-      for (int i = n; i > 0; i--) ----- (1; n + 1; n)
-      {
n          for (int j = 1; j < n; j *= 2) ----- (1; log2n + 1; log2n)
-          {
n      log2n      cout << i; ----- 1 unit
-          }
-      }
```

Solution: = 1 + n + 1 + n + n * (1 + log₂n + 1 + log₂n + log₂n)

T(n) = 3nlog₂n + 4n + 2

TASK – 02

1.

```
1      int i, j, k = 0; ----- 1 unit
-      for (i = n / 2; i <= n; i++) ----- (1; n / 2 + 1; n / 2)
-      {
n / 2      for (j = 2; j <= n; j = j * 3) ----- (1; log3n + 1; log3n)
-          {
n / 2  log3n      k = k + n / 2; ----- 1 unit
-          }
-      }
```

Solution: = (n / 2) * (log₃n)

Big - Oh = O(nlog₃n)

2.

```
1      int count = 0;          ----- 1 unit
-      for (int i = n / 2; i <= n; i++) ----- (1; n/2 + 1; n/2)
n/2      for (int j = 1; j <= n; j = 2 * j) ----- (1; log2n + 1; log2n)
n/2  log2n      for (int k = 1; k <= n; k = k * 2) ----- (1; log2n + 1; log2n)
n/2  log2n  log2n      count++;          ----- 1 unit
```

Solution: = (n / 2) * (log₂n) * (log₂n)

Big - Oh = O(n(log₂n)²)

```

3.
1      int count = 0; ----- 1 unit
-      for (int i = n; i > 0; i /= 2) ----- (1; log2n + 1; log2n)
-      {
log2n          for (int j = 0; j < i; j++) ----- (1; i + 1; i)
-              {
log2n                  count++; ----- 1 unit
-              }
-      }

```

Solution: = $(\log_2 n) * (\sum_{i=0}^{\log_2 n} n(1/2)^i)$

Big - Oh = $O(\sum_{i=0}^{\log_2 n} n(1/2)^i * (\log_2 n))$

TASK – 03

```

1.
-      void function(int n)
-      {
1          if (n == 1) ----- 1 unit
1              return; ----- 1 unit
-          for (int i = 1; i <= n; i++) ----- (1; n + 1; n)
-          {
n              for (int j = 1; j <= n; j++) ----- (1; n + 1; n)
-              {
n                  cout << "*"; ----- 1 unit
n                  break; ----- 1 unit
1              }
-          }
-      }

```

Best - Case = Omega = $\Omega(2)$

Worst - Case = Big Oh = $O(n)$ //Because of break statement

2.

```
void function(int n)
{
    if (n % 2 == 0) ----- 1 unit
    {
        for (int i = 1; i < n; i *= 2) ----- (1; log2n + 1; log2n)
        {
            cout << i << endl; ----- 1 unit
        }
    }
    else
    {
        for (int i = 0; i < n; i++) ----- (1; n + 1; n)
        {
            for (int j = 0; j < i; j++) ----- (1; i + 1; i)
            {
                cout << i + j << endl; ----- 1 unit
            }
        }
    }
}
```

Best - Case = $\Omega(3)$ // $T(n) = 3\log_2 n + 3$, put $n = 1$.

Worst - Case = Big Oh = $O(n * \sum_{i=0}^{\log_2 n} n(1/2)^i)$

TASK – 04

```
int main()
{
    int num; ----- 1 unit
    char ch; ----- 1 unit
    cout << "Enter a number: "; ----- 1 unit
    cin >> num; ----- 1 unit
    cout << "If you wish to check whether the input number is "; ----- 1 unit
    cout << "prime or not? enter 1"; ----- 1 unit
    cout << "enter 2 to see fibonacci series till the input number."; ----- 1 unit
    cin >> ch; ----- 1 unit
    if (ch == '1') ----- 1 unit
    {
        if (isPrime(num) == true) -----  $3n^{1/2} + 1$  unit
        cout << num << " is a Prime number" << endl; ----- 1 unit
    }
    else
        cout << num << " is not a Prime number" << endl; ----- 1 unit
    if (ch == '2') ----- 1 unit
    {
        printFibonacci(num); ----- (6n - 2) unit
    }
    return 0; ----- 1 unit
}
```

```

void printFibonacci(int n)
{
    int fib1 = 0; ----- 1 unit
    int fib2 = 1; ----- 1 unit
    for (int i = 2; i <= n; i = i + 1) ----- (1; n; n -1)
    {
        int temp = fib1 + fib2; ----- 1 unit
        fib1 = fib2; ----- 1 unit
        fib2 = temp; ----- 1 unit
        cout << temp << endl; ----- 1 unit
    }
}

bool isPrime(int n)
{
    for (int i = 2; i <= sqrt(n); i++) ----- (1; sqrt(n); sqrt(n) - 1) unit
    {
        if (n % i == 0) ----- 1 unit
        {
            return false; ----- 1 unit
        }
    }
    return true; ----- 1 unit
}

```

- 1) printFibonacci : $= 2 + 1 + n + n - 1 + 4n - 4 = 6n - 2$
- 2) isPrime : $= 1 + n^{1/2} + n^{1/2} - 1 + n^{1/2} - 1 + 1 = 3n^{1/2}$
- 3) main : $= 9 + 1 + 6n - 2 + 1 \Rightarrow T(n) = 6n + 9$