

Dynamic Scope

The way in which names are looked up in Scheme and Python is called lexical scope (or static scope) [You can see what names are in scope by inspecting the definition]

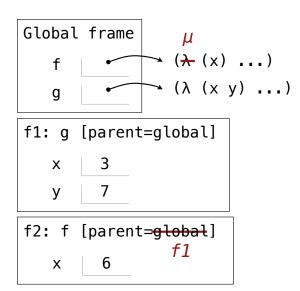
Lexical scope: The parent of a frame is the environment in which a procedure was *defined*

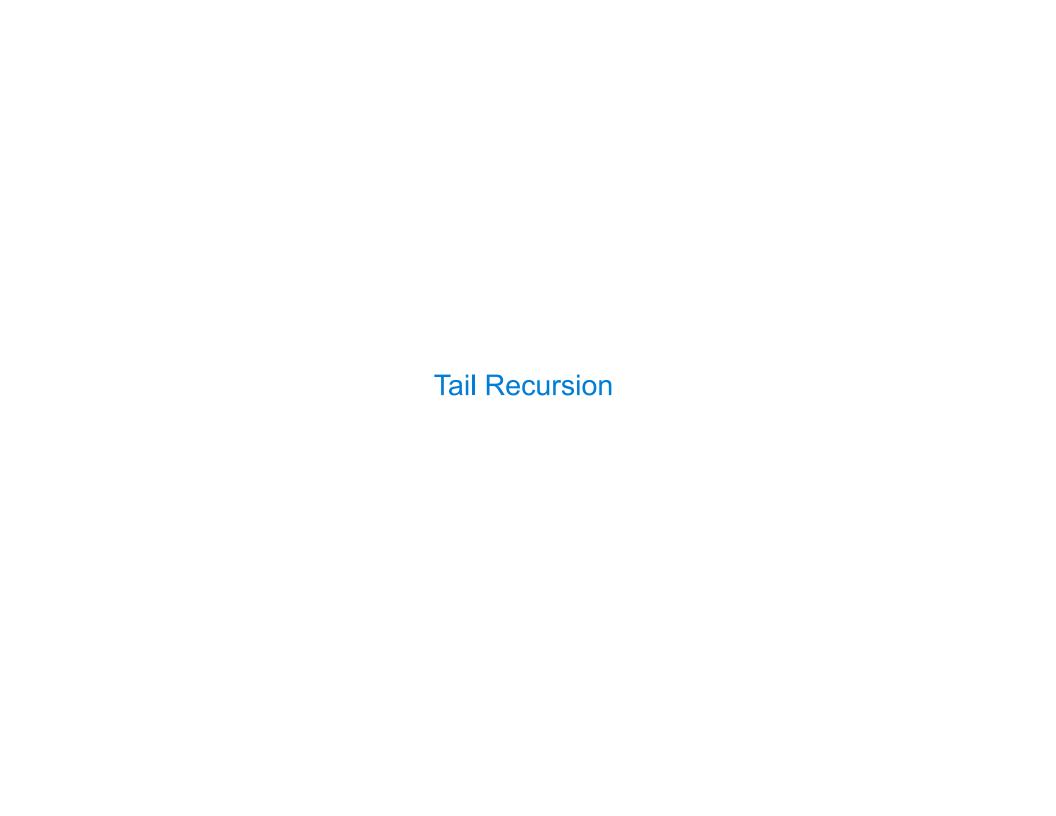
Dynamic scope: The parent of a frame is the environment in which a procedure was *called*

```
Special form to create dynamically
                       scoped procedures (mu special form
                        only exists in Project 4 Scheme)
 (define f (\frac{lambda}{x} (x) (+ x y)))
 (define g (lambda (x y) (f (+ x x))))
 (q \ 3 \ 7)
Lexical scope: The parent for f's frame is the global frame
                  Error: unknown identifier: v
```

Dynamic scope: The parent for f's frame is g's frame

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Functional Programming

All functions are pure functions

No re-assignment and no mutable data types

Name-value bindings are permanent

Advantages of functional programming:

- The value of an expression is independent of the order in which sub-expressions are evaluated
- Sub-expressions can safely be evaluated in parallel or only on demand (lazily)
- **Referential transparency:** The value of an expression does not change when we substitute one of its subexpression with the value of that subexpression

But... no for/while statements! Can we make basic iteration efficient? Yes!

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Recursion and Iteration in Python

In Python, recursive calls always create new active frames

factorial(n, k) computes: n! * k

		Time	Space
def	<pre>factorial(n, k): if n == 0: return k else:</pre>	Linear	Linear
	return factorial(n-1, k*n)		
	<pre>factorial(n, k): while n > 0: n, k = n-1, k*n return k</pre>	Linear	Constant

Tail Recursion

From the Revised⁷ Report on the Algorithmic Language Scheme:

"Implementations of Scheme <u>are required to be properly tail-recursive</u>. This allows the execution of an iterative computation <u>in constant space</u>, even if the iterative computation is described by a syntactically recursive procedure."

How? Eliminate the middleman!

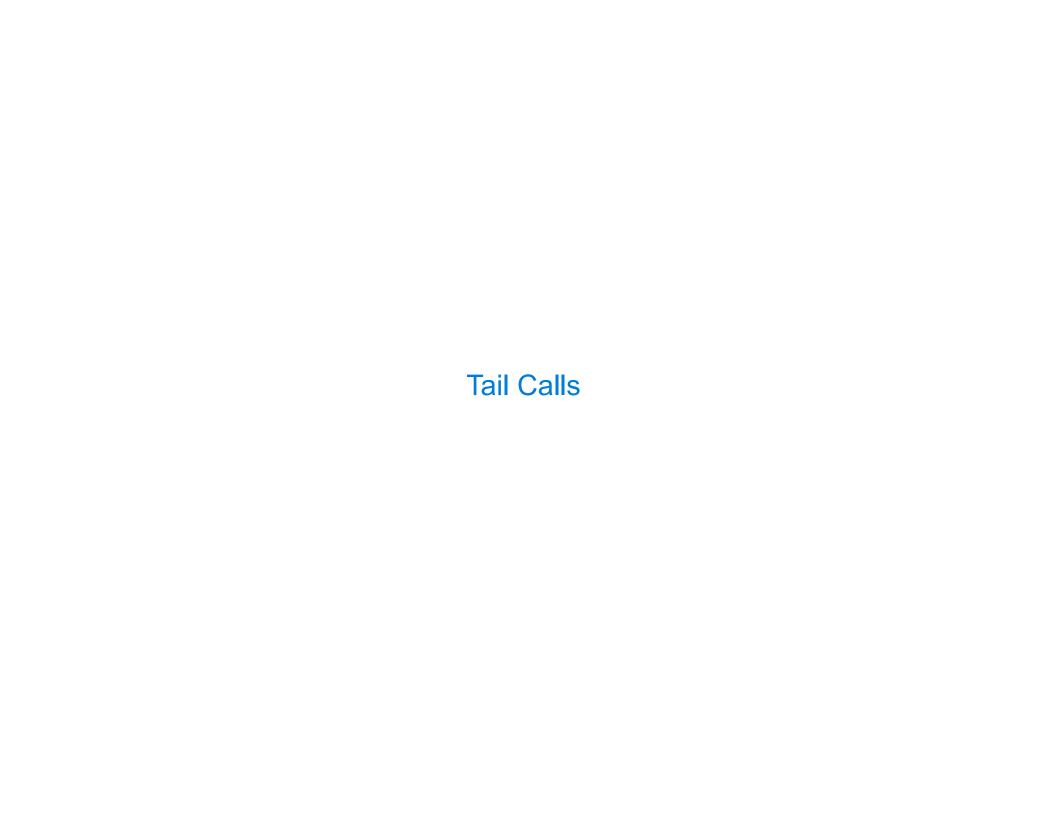
Should use resources like

Time Space
Linear Constant

def	factori	lal(n, k)	:
	while r	n > 0:	
	n,	k = n-1,	k∗n
	return	k	

(Demo)

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Tail Calls

A procedure call that has not yet returned is active. Some procedure calls are tail calls. A Scheme interpreter should support an unbounded number of active tail calls using only a constant amount of space.

A tail call is a call expression in a tail context:

- The last body sub-expression in a lambda expression (or procedure definition)
- Sub-expressions 2 & 3 in a tail context if expression whole "if" expression in tail context
- All non-predicate sub-expressions in a tail context cond
- The last sub-expression in a tail context and, or, begin, or let

Example: Length of a List

A call expression is **not a tail call** if more computation <u>is still required</u> <u>in the calling procedure</u>

Linear recursive procedures can often be re-written to use tail calls

this is the last body sub-expression, is tail call

Eval with Tail Call Optimization

The return value of the tail call is the return value of the current procedure call

Therefore, tail calls shouldn't increase the environment size

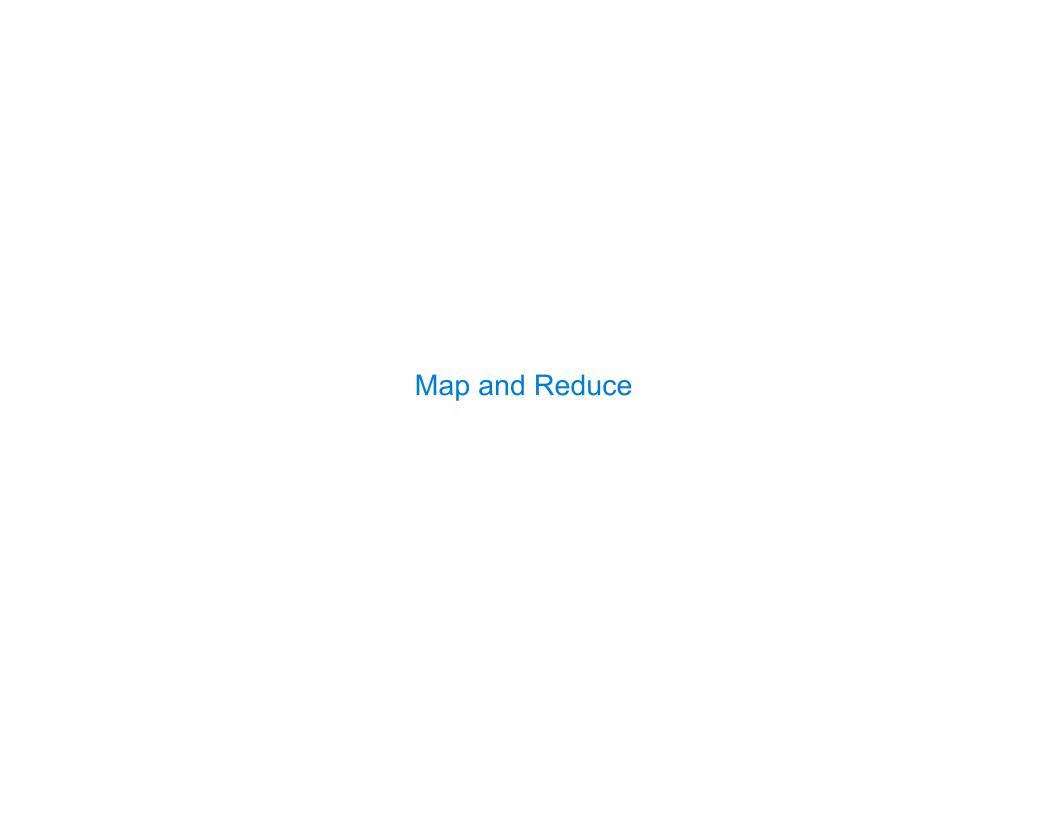
(Demo)



Which Procedures are Tail Recursive?

Which of the following procedures run in constant space?

```
;; Return whether s contains v.
(define (contains s v)
 (if (null? s)
     false
     (if (= v (car s))
         (contains (cdr s) v))))
;; Return whether s has any repeated elements.
(define (has-repeat s)
 (if (null? s)
     false
     (if (contains? (cdr s) (car s))
          true
         ((has-repeat (cdr s)))
```



Example: Reduce

```
Recursive call is a tail call

Space depends on what procedure requires

(reduce * '(3 4 5) 2)

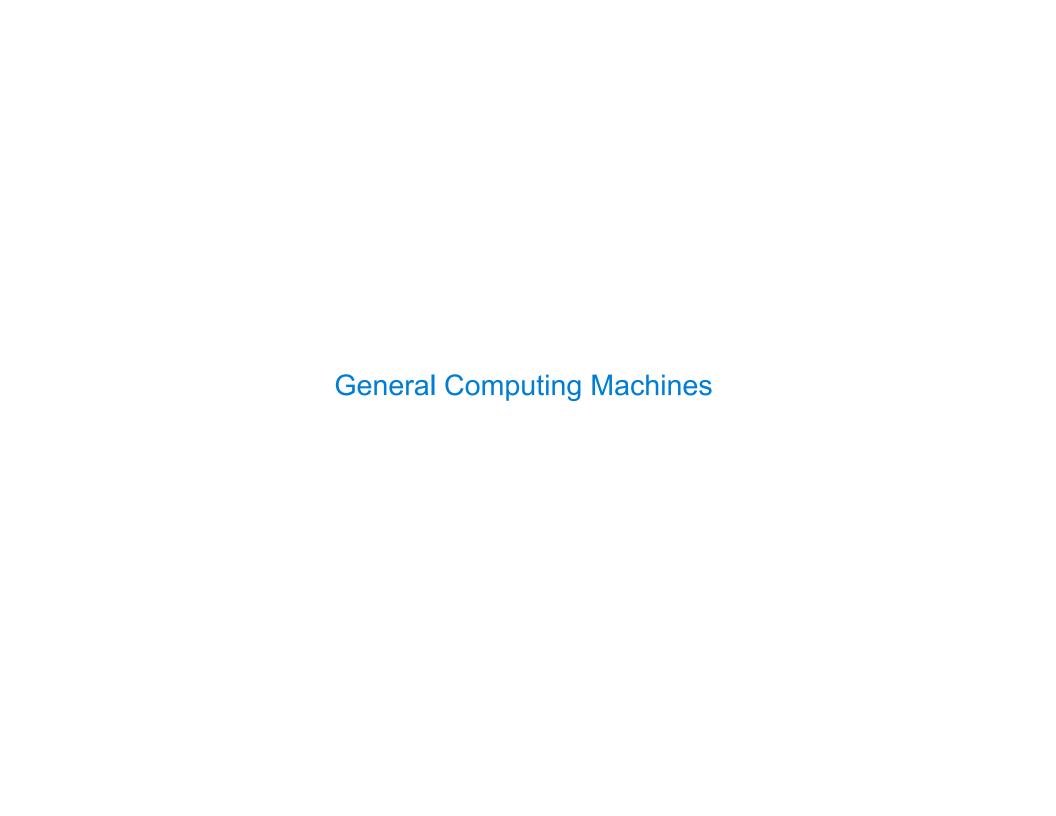
(reduce (lambda (x y) (cons y x)) '(3 4 5) '(2))

(5 4 3 2)
```

Example: Map with Only a Constant Number of Frames

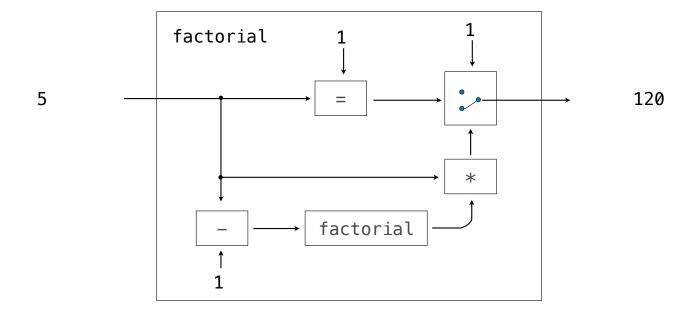
```
(define (map procedure s)
 (if (null? s)
      nil
      (cons (procedure (car s))
            (map procedure (cdr s)))
(map (lambda (x) (-5 x)) (list 1 2))
                      Pair
                                Pair
                      Pair
                                Pair
                                        nil
```

```
(define (map procedure s)
  (define (map-reverse s m)
    (if (null? s)
        (map-reverse (cdr s)
                     (cons (procedure (car s))
  (reverse (map-reverse s nil)))
(define (reverse s)
  (define (reverse-iter s r)
   (if (null? s)
        (reverse-iter (cdr s)
                      (cons (car s) r))))
  (reverse-iter s nil))
```



An Analogy: Programs Define Machines

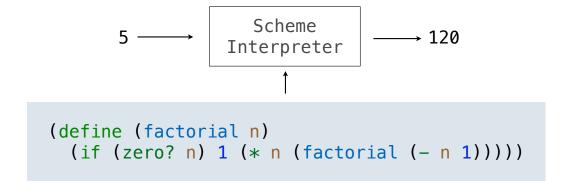
Programs specify the logic of a computational device



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Interpreters are General Computing Machine

An interpreter can be parameterized to simulate any machine



Our Scheme interpreter is a universal machine

A bridge between the data objects that are manipulated by our programming language and the programming language itself

Internally, it is just a set of evaluation rules