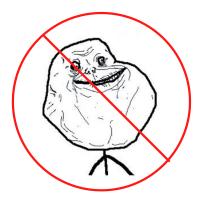


Office Hours: You Should Go!

You are not alone!



https://cs61a.org/office-hours/

Example: Prime Factorization

Prime Factorization

Each positive integer n has a set of prime factors: primes whose product is n

```
8 = 2 * 2 * 2

9 = 3 * 3

10 = 2 * 5

11 = 11

12 = 2 * 2 * 3
```

One approach: Find the smallest prime factor of n, then divide by it

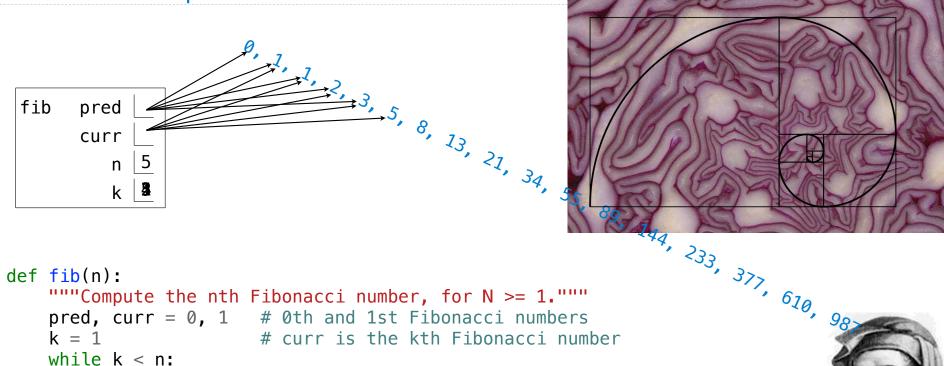
$$858 = 2 * 429 = 2 * 3 * 143 = 2 * 3 * 11 * 13$$

Example: Iteration

The Fibonacci Sequence

k = k + 1

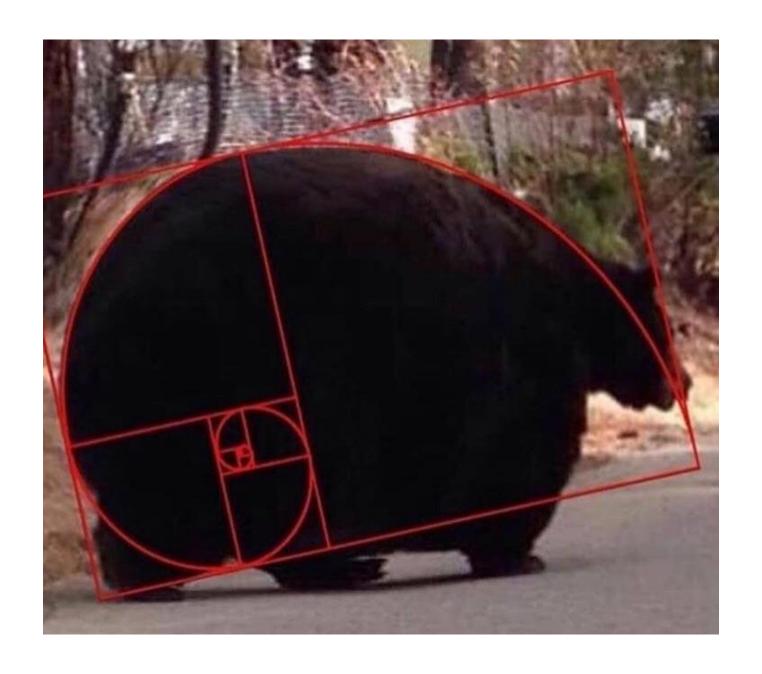
return curr



The next Fibonacci number is the sum of the current one and its predecessor

pred, curr = curr, pred + curr

Go Bears!



Designing Functions

Describing Functions

A function's *domain* is the set of all inputs it might possibly take as arguments.

A function's *range* is the set of output values it might possibly return.

A pure function's *behavior* is the relationship it creates between input and output.

def square(x):
 """Return X * X."""

x is a number

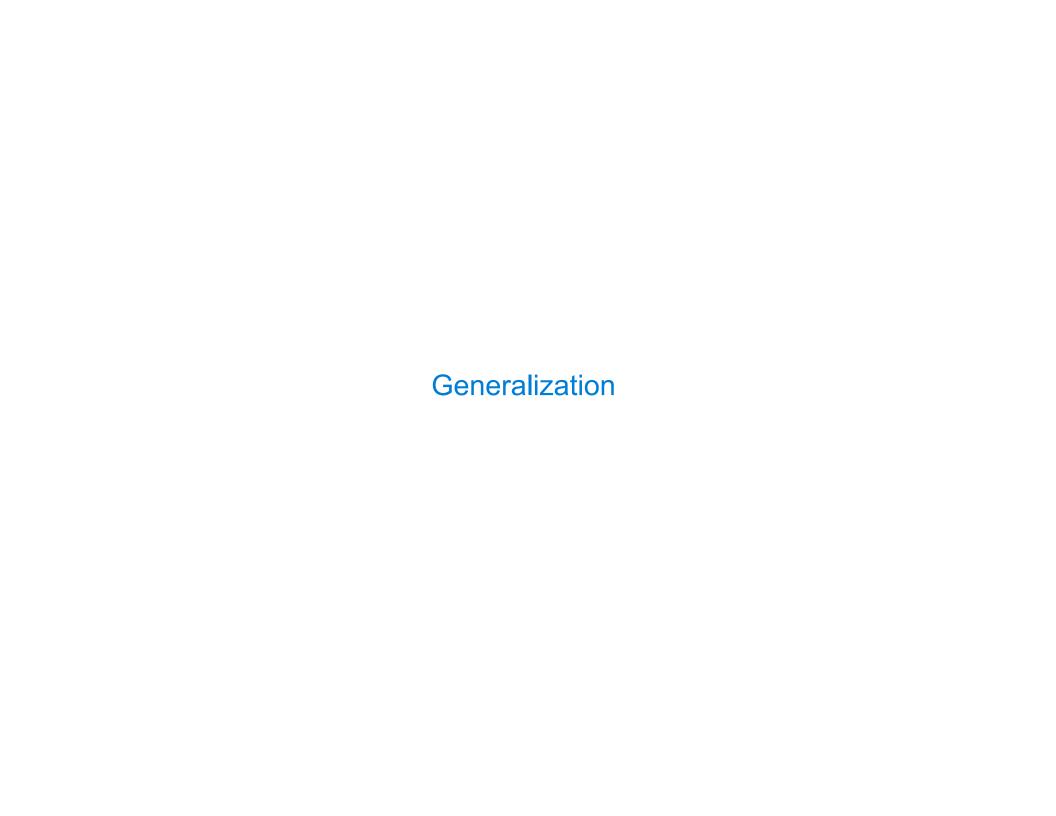
square returns a nonnegative real number

square returns the square of x

A Guide to Designing Function

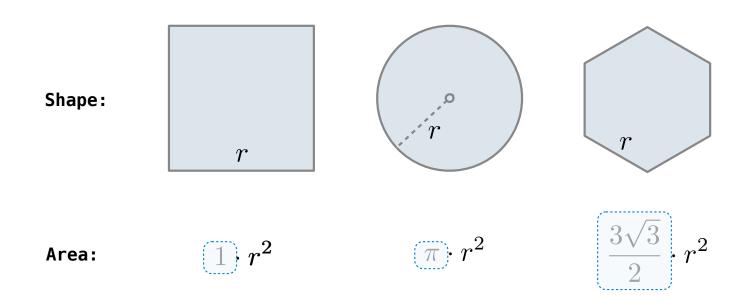
Give each function exactly one job, but make it apply to many related situations

Don't repeat yourself (DRY): Implement a process just once, but execute it many times

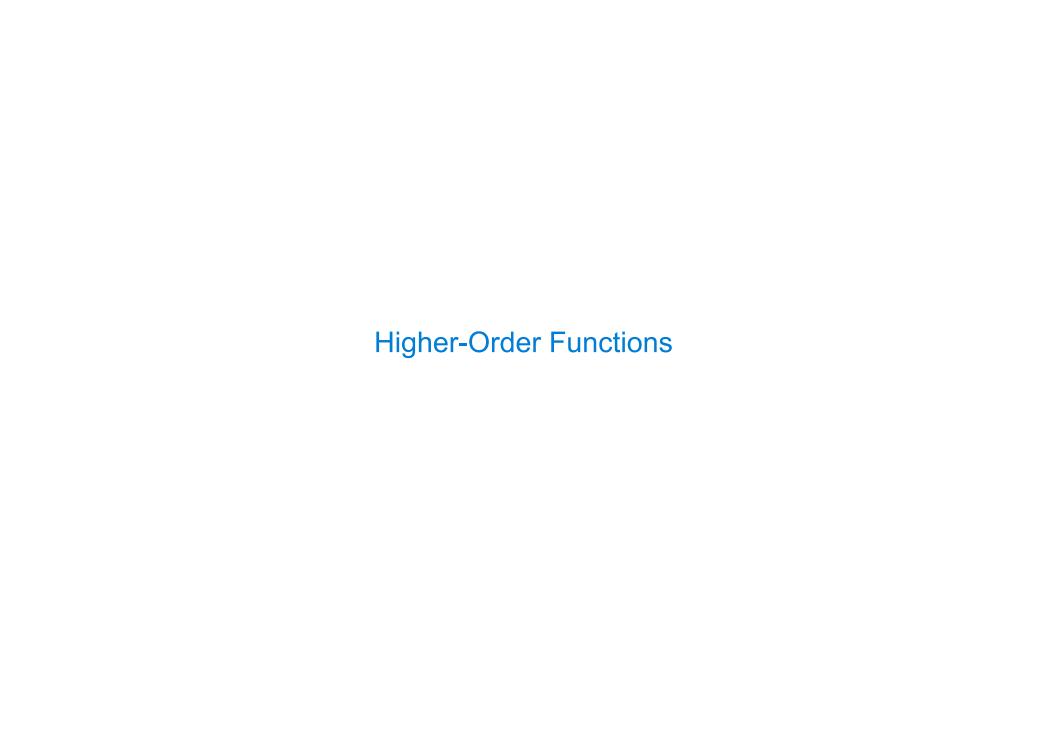


Generalizing Patterns with Arguments

Regular geometric shapes relate length and area.



Finding common structure allows for shared implementation



Generalizing Over Computational Processes

The common structure among functions may be a computational process, rather than a number.

$$\sum_{k=1}^{5} (k) = 1 + 2 + 3 + 4 + 5 = 15$$

$$\sum_{k=1}^{5} k^{3} = 1^{3} + 2^{3} + 3^{3} + 4^{3} + 5^{3} = 225$$

$$\sum_{k=1}^{5} \frac{8}{(4k-3)\cdot(4k-1)} = \frac{8}{3} + \frac{8}{35} + \frac{8}{99} + \frac{8}{195} + \frac{8}{323} = 3.04$$

Summation Example

```
Function of a single argument
def cube(k):
                                 (not called "term")
     return pow(k, 3)
                            A formal parameter that will
def summation(n, term)
                               be bound to a function
     """Sum the first n terms of a sequence.
     >>> summation(5, cube)
     225
                           The cube function is passed
     11 11 11
                              as an argument value
     total, k = 0, 1
     while k <= n:
          total, k = total + term(k), k + 1
     return total
                             The function bound to term
  0 + 1 + 8 + 27 + 64 + 125
                                 gets called here
```

Functions as Return Values

Locally Defined Functions

Functions defined within other function bodies are bound to names in a local frame

```
A function that returns a function

def make adder(n):

"""Return a function that takes one argument k and returns k + n.

>>> add three = make_adder(3)

>>> add_three(4)

The name add_three is bound to a function

7

"""

def adder(k):
    return (k + n)
    A def statement within another def statement

Can refer to names in the enclosing function
```

Call Expressions as Operator Expressions

