

The Macroeconomic Consequences of Family Policies

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UMN-UW International-Macro Student Workshop

Motivation #1 - Social Mobility

- Policy makers are increasingly relying on family policies to reduce child poverty, raise children's human capital and boost social mobility (e.g. **\$3k+ Child Tax Credit through 2025**, **\$1.8 trillion American Families Plan**)

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- **Quality/Quantity trade-off**: More generous child benefits raise fertility. Higher fertility makes investments in children's education more expensive for parents
⇒ Child human capital can fall, reducing social mobility

Motivation #2 - Population Aging

- Understanding the aggregate effects of family policies is important in its own right since these policies are widely adopted to combat population aging (**>2% of GDP** among OECD countries)

▶ example ▶ trend

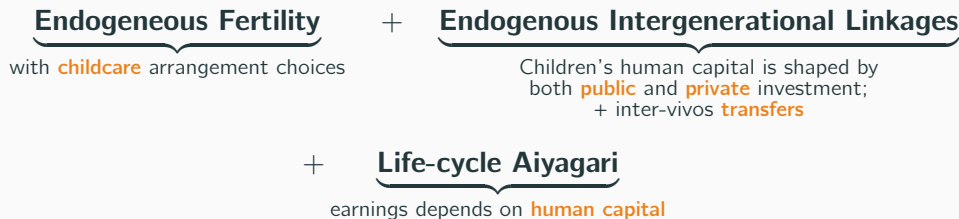
Motivation #2 - Population Aging

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- My paper evaluates the potential benefits of higher fertility on demographic structure and government budget in **general equilibrium**
⇒ Taxes can fall in the long-run, raising social welfare

What are the macroeconomic consequences of large-scale family policies?

Particularly on: average income, intergenerational mobility and welfare. [short-run vs long-run](#)

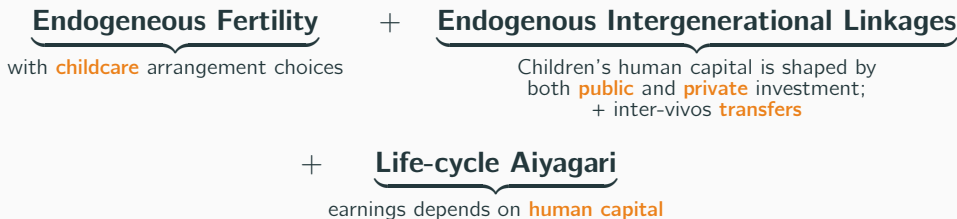
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- **Government:** taxation, pension, baby bonus, childcare subsidy, public education
- **Policy mechanisms:** fertility responses, endogenous human capital, GE effects

Preview of Key Results

- ① With degree of complementarity between quality/quantity that fits data, parents optimally **reduce private education investments** in response to a baby bonus. Baby bonus could **reduce intergenerational mobility** due to heterogeneous responses across households

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¹Average utility of new-born under the veil of ignorance converted to consumption equivalence

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- ③ While average human capital falls by 1.4%, long-run welfare¹ **rises by 3.2%** as changes in demographic structure lead to reduced tax rates in equilibrium
- ④ Among different policy options, expanding **public education** is most effective in improving child human capital and intergenerational mobility

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Fiscal and Education Policies, Income transfers, and Mobility

- Benabou (2002), **de la Croix and Doepke (2003)**, Heckman and Mosso (2014), Bastian and Micheltore (2018), **Daruich (2019)**, Abbott, Gallipoli, Meghir and Violante (2019), Mullins (2019), **Guner, Kaygusuz and Ventura (2020)**...
- **Contribution: Endogenous fertility could reverse policy effects on child human capital and mobility. General equilibrium effects on welfare**

Family Policies and Fertility

- **Empirical:** Milligan (2005), Laroque and Salanié (2008), Drago et al. (2011), Luci-Greulich and Thévenon (2013), González (2013), Raute (2019)...
- **Structural:** Fan and Stark (2008), **Liao (2013)**, Moschini (2020)
- **Contribution: Evaluate large-scale policy counterfactuals with both endogenous fertility and endogenous child skill formation**

① Model

② Calibration (2010 USA)

- **Key moments** on fertility profile (CPS), childcare arrangements (SIPP), parental investments and transfers (PSID) and lifecycle earnings profile (PSID)
- Skill formation based on **RCT evidence** (Garcia, Heckman, Leaf and Prados 2020) and **intergenerational mobility** estimates (Chetty, Hendren, Kline and Saez 2014)

③ Validation

- Model matches **fertility elasticities** estimated for Alaska's Permanent Fund Dividend Program (Kelly, Timilsina and Yonzan 2020, Cowan and Douds 2020)

④ Policy:

- Evaluate aggregate impacts of **large-scale** family and education policies

⑤ Conclusion and Next Steps

Model

Model: Timeline



Key Elements

- Life-cycle Aiyagari
- Endogenous Fertility
- Endogenous Child Link

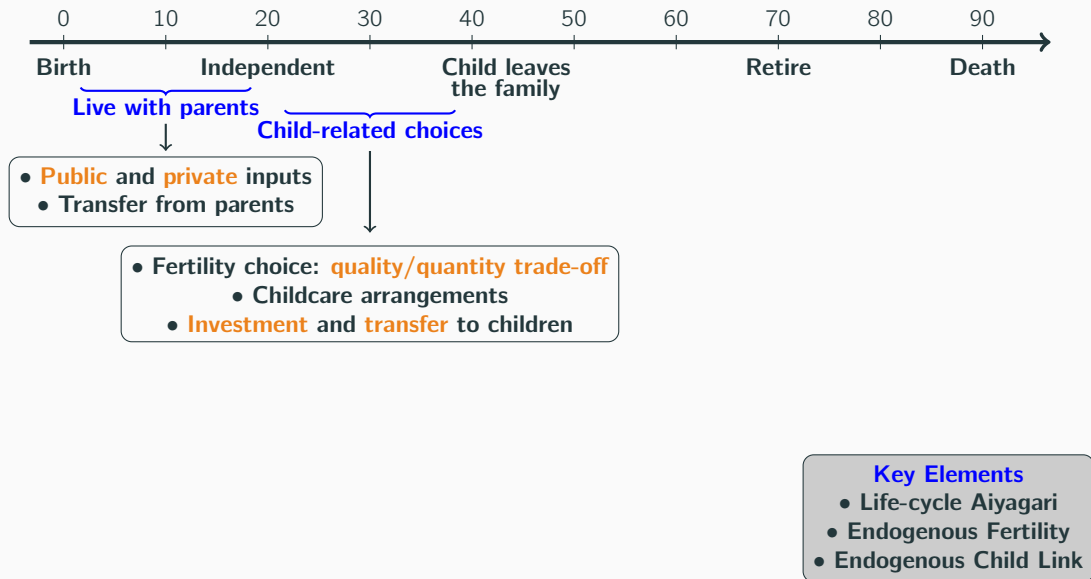
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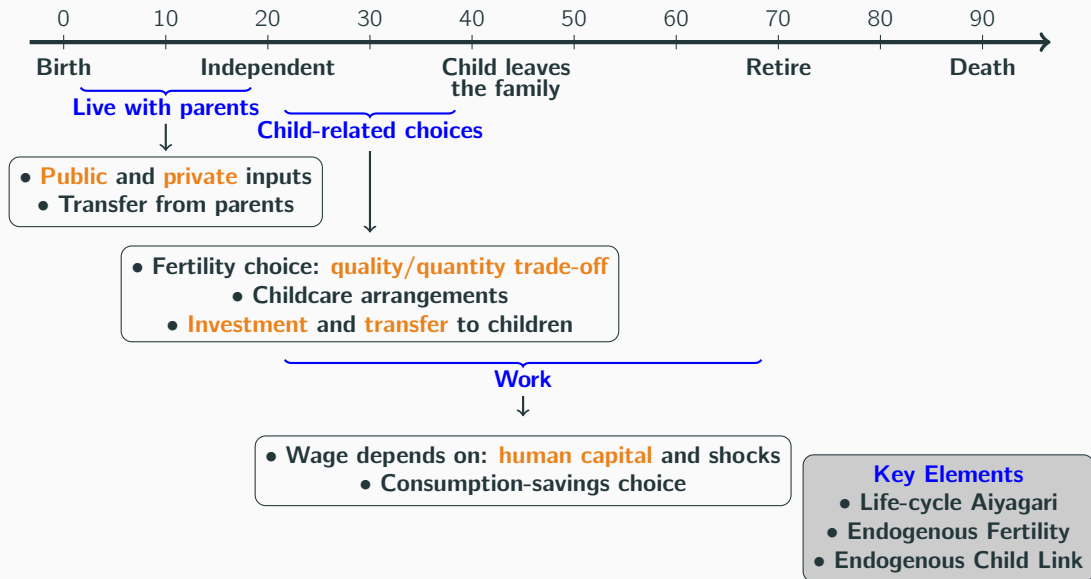
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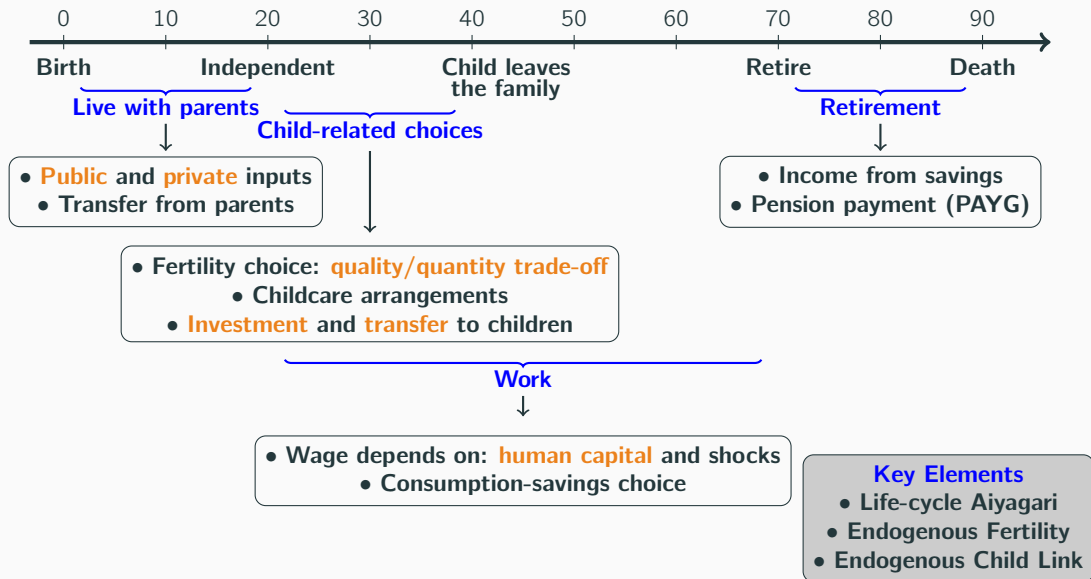
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Fertility, Childcare and Skill Formation



Fertility, Childcare and Skill Formation



$$V_2(h, a) = \max_{c, a', n, t_h, m, e \geq 0} u(c/q_n) + \beta \mathbb{E} V_3(h', a', n, \mathbb{E} h_k)$$

h : parents' skills

a : assets

n : fertility

t_h : home care

m : market care

e : private educ. input

χ : childcare needs

p_m : market care price

q_n : equivalence scale

\mathcal{S} : childcare subsidy

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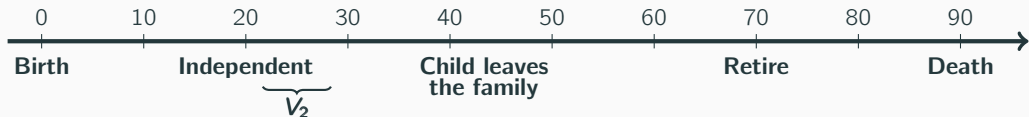
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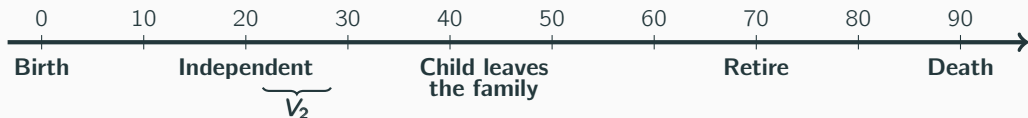
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$$(1 + \tau_c)(c + mp_m(1 - \mathcal{S})n + e \cdot n) + a' = (1 + r)a + y - \mathcal{T}(y, a, n) + \mathcal{B} \cdot n \quad [\text{BC}]$$

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- $G(h, \mathcal{E}, e, \epsilon)$ captures children's skill formation from age 0 to 20 with:
 - Private investment e from age 0 to 10
 - Public education \mathcal{E} from age 0 to 18
 - **Assumption:** childcare arrangement does not affect children's skill formation

Parent-to-Child Transfer



$$V_3(h, a, n, \mathbb{E}h_k) = \max_{c, a', a_k \geq 0} u(c/q_n) + \beta \mathbb{E} V_4(h', a') + \underbrace{v(n, \mathbb{E}h_k, a_k)}_{\text{warm-glow utility}}$$
$$y = wh \cdot 1$$

$$(1 + \tau_c)c + a' + n \cdot a_k = (1 + r)a + y - \mathcal{T}(y, a, n)$$

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- Parents choose a_k received by each child when she becomes independent

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- Parents choose a_k received by each child when she becomes independent
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- To parents, baby bonus \mathcal{B} and childcare subsidy \mathcal{S} reduce the shadow price of child quantity while public education \mathcal{E} raises child quality

- Representative firm with **Cobb-Douglas production function**:

$$Y = AK^{\alpha}H^{1-\alpha}$$

Firms and the Government

- Representative firm with **Cobb-Douglas production function**:

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- Government uses predetermined policy instruments $\{\mathcal{T}(\cdot), \mathcal{B}, \mathcal{S}, \mathcal{E}\}$
- Denote demographic structure as $\{\Omega_j\}_{j=0}^8$ (with $\sum_{j=0}^8 \Omega_j = 1$) and distribution of households across state space as μ . **Government fiscal budget**:

$$\underbrace{\left(\sum_{j=2}^6 \Omega_j \int \mathcal{T}(y_j^*, a_j^*, n_j^*) d\mu \right)}_{\text{labor and capital income taxes}} + \underbrace{\left(\sum_{j=2}^8 \Omega_j \tau_c c_j^* d\mu \right)}_{\text{consumption tax}} = \underbrace{\left(\sum_{j=7}^8 \Omega_j wh \cdot \pi d\mu \right)}_{\text{pension payments}}$$

$$+ \underbrace{(\Omega_0 + \Omega_1)\mathcal{E}}_{\text{public education}} + \underbrace{\int \Omega_2 n^* \cdot \mathcal{B} d\mu}_{\text{baby bonus}} + \underbrace{\int \Omega_2 (1 + \tau_c) m^* n^* p_m \cdot \mathcal{S} d\mu}_{\text{subsidized childcare}} + \underbrace{\mathcal{X}}_{\text{other spendings}}$$

Role for Government Policies

Why may government policies improve welfare?

Long-run welfare: **average value** of newborn under the veil of ignorance:

$$\mathcal{W} = \int V_2 d\mu$$

Pragmatic approach that evaluates whether higher fertility, i.e. additional agents, improves the **average well-being** in the economy²

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Externalities/incompleteness that government could address:

- ① **Fiscal externalities of childbearing and childrearing**
 - Private returns \neq social returns (i.e. $\{\Omega_j\}_{j=0}^8$ and μ)
- ② **Parents cannot borrow against children's future income**
 - Lack of compensation mechanism
- ③ **Life-cycle borrowing constraints**

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Exogenous vs Endogenous Fertility: Policy Implications

Consider an increase in \mathcal{B} (baby bonus) or \mathcal{S} (childcare subsidy)

On child quality h_k for a given parent with human capital h :

- With exogenous fertility, this is a **lump-sum transfer** - $h_k(h)$ rises unambiguously
- With endogenous fertility, $n^*(h)$ increases, **additional channels** on $h_k(h)$:
 - ① **Complementarity/substitutability** via $v(n, \mathbb{E}h_k, a_k)$
 - ② **Higher costs of childrearing** - $n\chi$ and q_n
 - ③ Interactions in budget constraint - **higher shadow price of e**

On aggregate fertility N and average human capital \bar{h} in the economy:

- With exogenous fertility, N is fixed while \bar{h} is boosted
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Policy effects of transfers to families with children cannot predict the aggregate effects of family policies when fertility is endogenous

Calibration

- **Utility from consumption:**

$$u(c) = \frac{c^{1-\gamma_c}}{1-\gamma_c} \quad \gamma_c \in (0, 1)$$

Parametrization: Preferences

- **Utility from consumption:**

$$u(c) = \frac{c^{1-\gamma_c}}{1-\gamma_c} \quad \gamma_c \in (0, 1)$$

- **Utility from child quantity and quality:**

$$v(n, \mathbb{E}h_k, a_k) = \Psi(n) \cdot (\theta \cdot u(\mathbb{E}h_k) + \nu \cdot u(a_k))$$

$$\Psi(n) = 1 - \exp(-\psi n) \quad \psi > 0$$

where parents value child quality via $u(\cdot)$ (Barro and Becker 1989) with exponential child discounting (Córdoba, Ripoll and Liu 2016)

Parametrization: Preferences

- **Utility from consumption:**

$$u(c) = \frac{c^{1-\gamma_c}}{1-\gamma_c} \quad \gamma_c \in (0, 1)$$

- **Utility from child quantity and quality:**

$$v(n, \mathbb{E}h_k, a_k) = \Psi(n) \cdot (\theta \cdot u(\mathbb{E}h_k) + \nu \cdot u(a_k))$$

$$\Psi(n) = 1 - \exp(-\psi n) \quad \psi > 0$$

where parents value child quality via $u(\cdot)$ (Barro and Becker 1989) with exponential child discounting (Córdoba, Ripoll and Liu 2016)

- $v_{12}, v_{13} > 0 \implies$ main results are driven by **quality/quantity trade-off** (Becker and Lewis 1972) rather than assumptions on preferences³

► fit ► V_2 ► V_3 ► intuition ► identification ► results

³Robust to (1) separable preferences (de la Croix and Doepke 2003, Moav 2005), (2) quality and quantity being substitutes (Jones and Schoonbroodt 2010), or (3) dynastic altruism (Daruich and Kozlowski 2020)

Child's Skill Production Function

- Children's skill production function:

$$h_k = \underbrace{Z}_{\text{scalar}} \cdot \underbrace{\epsilon}_{\text{shock}} \cdot \underbrace{h^\rho}_{\text{spillover}} \cdot \left(\underbrace{\mathcal{E}^\omega}_{\text{public education}} + \underbrace{e^\omega}_{\text{private input}} \right)^{\gamma/\omega}$$

$$\log(\epsilon) \sim \mathcal{N}\left(-\frac{\sigma_\epsilon^2}{2}, \sigma_\epsilon^2\right)$$

- $\rho = 0.28$ - rank-rank mobility (Chetty, Hendren, Kline and Saez 2014)
- $\mathcal{E} = 0.165$ - \$12k per pupil per year (NCES)

Child's Skill Production Function Cont'd

Use **RCT evidence** to discipline the productivity of inputs γ :

$$h_k = Z \cdot \epsilon \cdot h^\rho (\mathcal{E}^\omega + e^\omega)^{\gamma/\omega}$$

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- **Garcia, Heckman, Leaf and Prados (2020)**
 - Two US early childhood development programs (ABC, CARE) in 1970s
 - Cost \approx \$13.5k per year for five years - total \$67.5k per child
 - Followed up into adulthood and observe education/income
 - For every dollar invested, children's lifetime labor income increases by **\$1.3**

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 - Followed up into adulthood and observe education/income
 - For every dollar invested, children's lifetime labor income increases by **\$1.3**
- **Apply similar policy in the model: expand existing \mathcal{E} by \$67.5k**
 - **Small scale:** prices and taxes remain unchanged
 - **Target:** children of parents at 10th percentile of earnings
- **Comparing labor income changes with program costs gives $\gamma = 0.16$**

Model Parameters

Table 1: Model Parameters

Preferences				Child human capital production			
Parameter	Interpretation	Value	Source	Parameter	Interpretation	Value	Source
β	discount rate	0.98 ¹⁰	standard	Z	normalizing scalar	2.45	
γ_c	elasticity of substitution	0.55	CPS	σ_ϵ	ability shock dispersion	0.45	PSID
ψ	fertility preference	1.84	CPS	ρ	intergenerational spillover	0.28	Chetty et al. (2014)
θ	quality preference	2.02	PSID	ω	substitution of education	0.9	ATUS
ν	transfer preference	0.42	PSID	\mathcal{E}	public education	0.165	NCES
				γ	input productivity	0.16	Garcia et al. (2020)
Childcare arrangement				Adult human capital evolution			
χ	childcare cost	0.18	Folbre (2008)	η	learning curvature	0.61	PSID
ι	economies of scale at home	0.7	Folbre (2008)	ζ	learning level	0.72	PSID
v	substitutability of care	0.5	SIPP	μ_z	skill depreciation	-0.23	PSID
p_m	price of full-time care	0.13	NACCRRA	σ_z	shock dispersion	0.42	PSID
Taxes and pension				Firm production function			
τ_y^n, λ_y^n	tax levels and progressivity	misc.	TAXSIM	A	total factor productivity	1	normalization
τ_c	consumption tax	0.07	McDaniel (2007)	α	capital share	0.33	standard
τ_a	capital income tax	0.27	McDaniel (2007)	δ_k	capital depreciation	0.04 ¹⁰	standard
π	pension replacement rate	0.40	OECD Database				

- 13 parameters are calibrated within the model using SMM
- Model matches salient features of fertility profile, childcare, parental investment, inter-vivos transfers, intergenerational mobility and lifecycle earnings profile

Validation

Fertility Response to Financial Incentives

Question: Does the model generate responses that match empirical estimates?

Answer: External validation using **Alaska Permanent Fund Dividends (APFD)**

Fertility Response to Financial Incentives

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Answer: External validation using **Alaska Permanent Fund Dividends (APFD)**

- Established in 1982 after discovery of the petroleum. Equal transfer to **all residents** regardless of income, employment or age
- Allows parent to claim dividend on behalf of a child with no requirements on how parents use a child's dividend.

Fertility Response to Financial Incentives

Question: Does the model generate responses that match empirical estimates?

Answer: External validation using **Alaska Permanent Fund Dividends (APFD)**

- **Ideal policy variation** to test fertility responses:
 - ① **Similar institution and cultural background**
 - ② **Large in scale (\approx \$1.5k per year)** relative to other family policies
 - ③ **Clear implementation:** not tied to labor market status or policy bundles

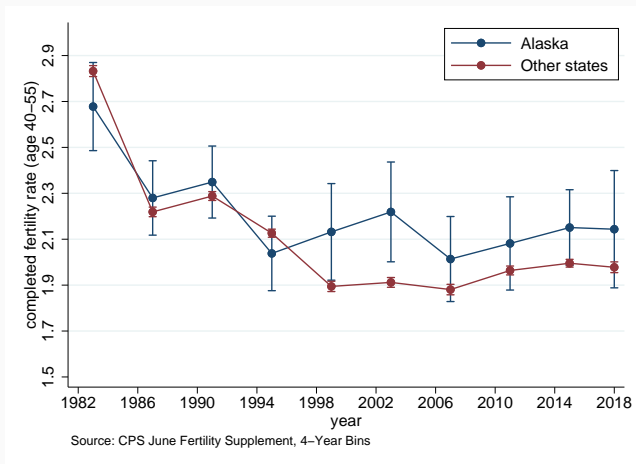
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- **Apply same policy in the model: UBI to all household members by \$1.5k**
(normalized by median income in Alaska relative to the rest of U.S. + partial equilibrium)
 - Completed fertility rises by **4.2%** in the model (Kelly, Timilsina and Yonzan 2020)
 - **Heterogeneous responses:** Larger responses from households with lower opportunity costs of time (model) - larger fertility increases among Alaska Natives and women without high school degree (Cowan and Douds 2020)

Evidence from Completed Fertility Rates



- 95% confidence intervals of sample mean
- Predicted 4.2% (0.08) increase in completed fertility rate is consistent with data

Counterfactuals

Evaluate universal policies of different scale (NPV for \mathcal{B} , \mathcal{E} and % for \mathcal{S})

- **Budget balance:** consumption tax adjusts to balance budget each period
- **General equilibrium:** prices and distributions adjust

Large Scale and Permanent Policy

Evaluate universal policies of different scale (NPV for \mathcal{B} , \mathcal{E} and % for \mathcal{S})

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Outcomes of Interest

- **Aggregate fertility, average human capital, per capita income** and intergenerational mobility ($\frac{1}{TGE}$)
- **Social welfare** in consumption equivalence (changes)

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Outline

- **Long-run effects** - comparing new steady-state economy to baseline economy
- **Transition, alternative funding method** (in progress)

Fertility Effects of Baby Bonus B

Figure 1: Effects on fertility

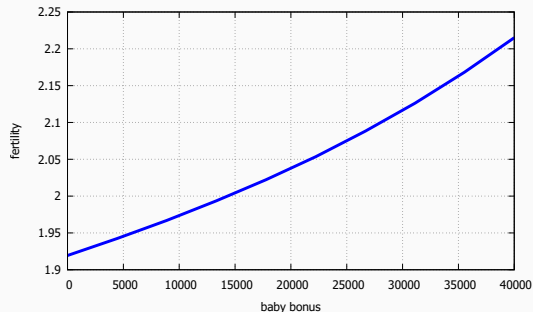
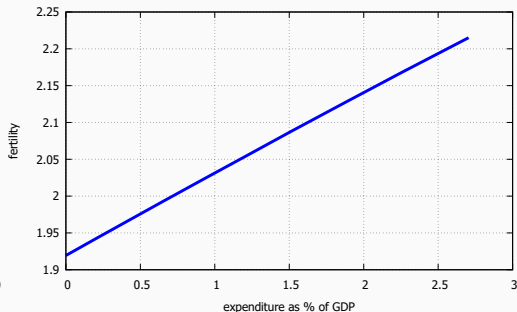


Figure 2: Expenditure share



- Fertility increases as shadow price of child quantity falls
- Baby bonus needs to be greater than **\$28k (NPV)** to raise aggregate fertility rate to **replacement level** (2.1, commonly stated long-run policy goal). The policy costs around **1.6%** of GDP in the new equilibrium

Heterogeneous Response and Effects on Human Capital

Figure 3: Heterogeneous fertility response

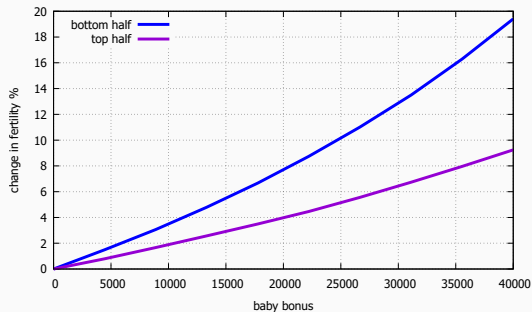
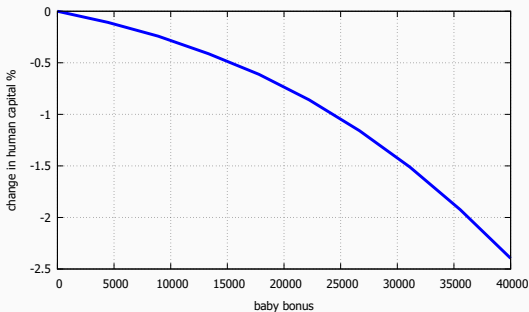


Figure 4: Average human capital



- Households with **lower human capital** respond more to baby bonus
- Recall intergenerational transmission of human capital h^p
- Average human capital **decreases by 1.4%** at replacement rate fertility

Responses in Private Education Investment and Mobility

Figure 5: Average private investment

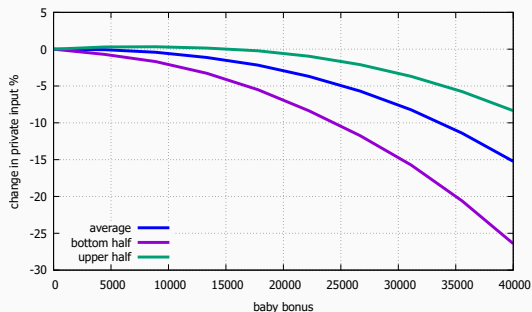
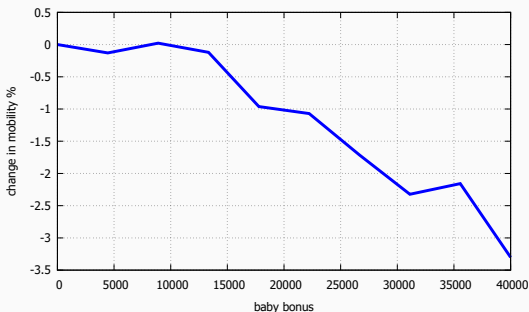


Figure 6: Intergenerational mobility



- Parents **reduce** private investments as higher n increases the shadow price of e
- Predictions consistent with empirical evidence from Australian baby bonus

Responses in Private Education Investment and Mobility

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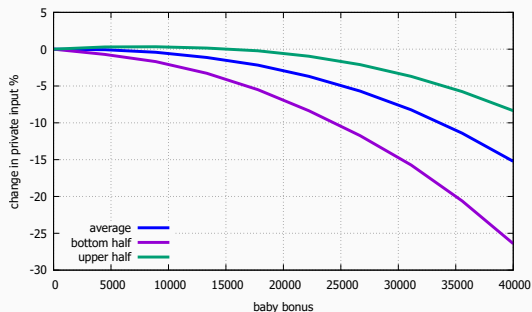
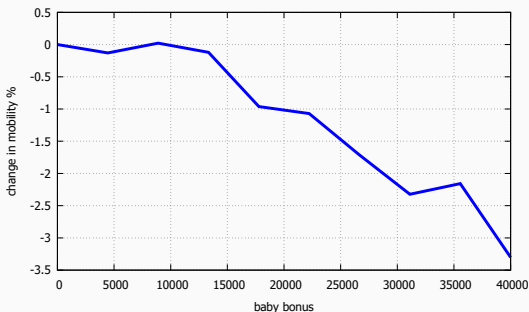


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Responses in Private Education Investment and Mobility

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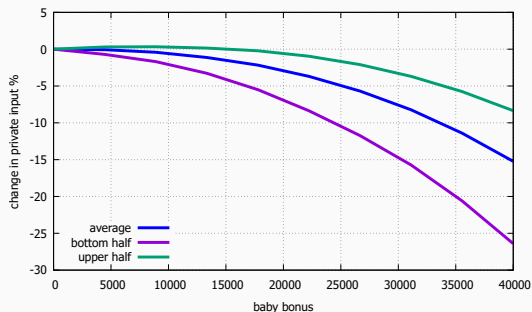
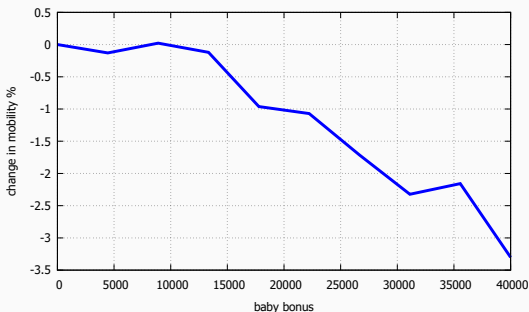


Figure 6: Intergenerational mobility



- Parents **reduce** private investments as higher n increases the shadow price of e
- Predictions consistent with empirical evidence from Australian baby bonus
- Intergenerational mobility **decreases by 2%** at replacement fertility
- Results are **stronger** when cash transfers are targeted at low-income households

Output Response and Change in Consumption Tax

Figure 7: Per capita output

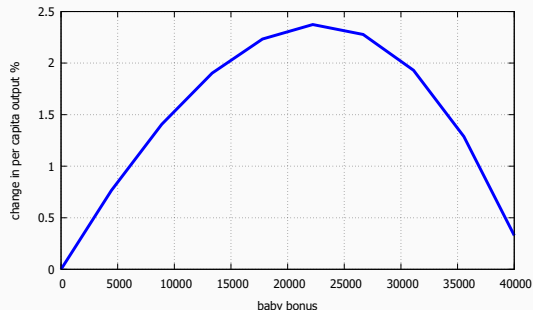
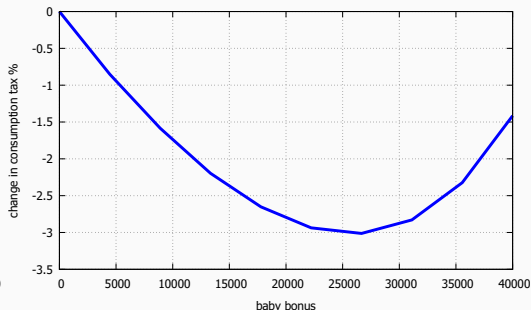


Figure 8: Change in consumption tax



- **Per capita output** increases initially due to changes in **demographic structure**

Output Response and Change in Consumption Tax

Figure 7: Per capita output

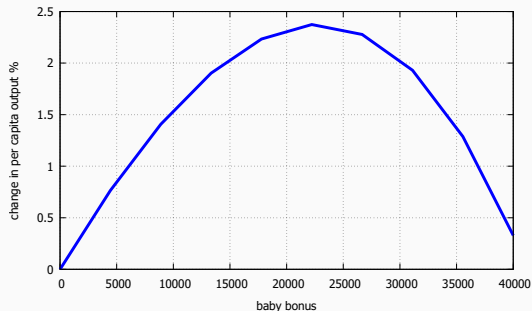
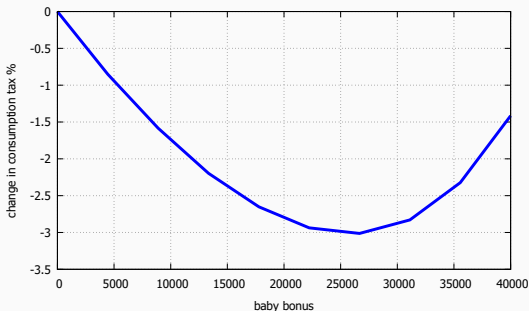


Figure 8: Change in consumption tax



- **Per capita output** increases initially due to changes in **demographic structure**
- Consumption tax could be **reduced** while keeping government budget satisfied
- Larger baby bonus is **not always beneficial** as average human capital worsens

Social Welfare under Baby Bonus \mathcal{B}

Figure 9: Change in welfare

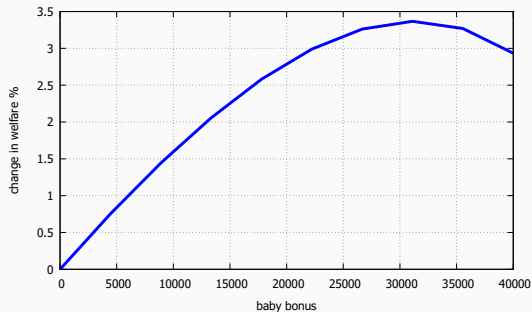
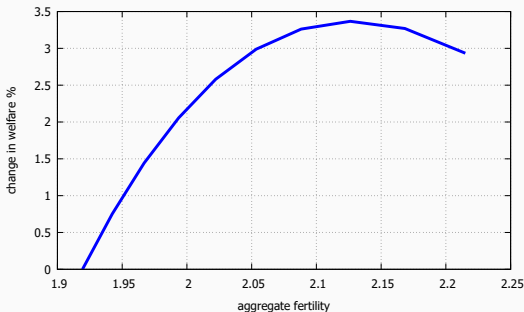


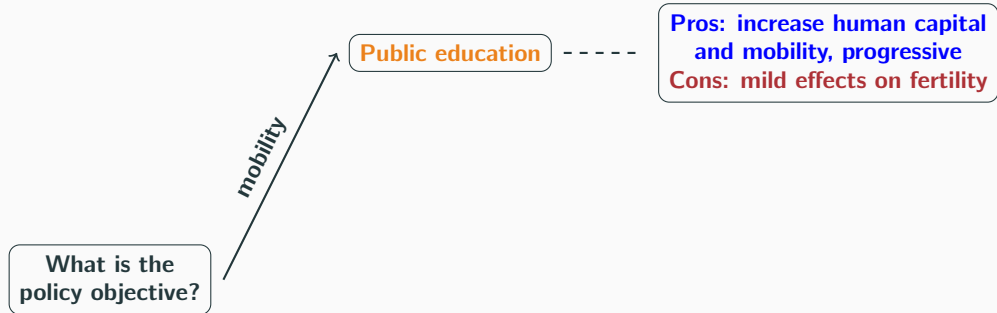
Figure 10: Fertility Possibility Frontier



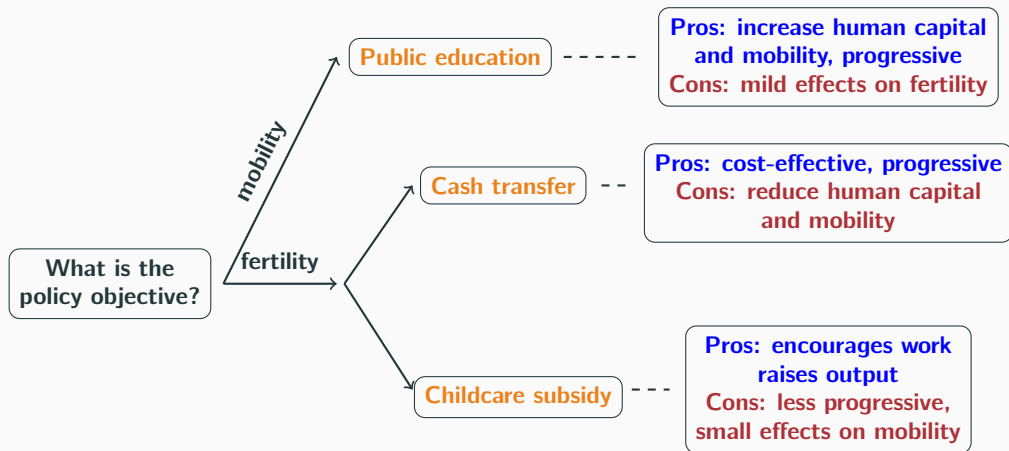
- Welfare effects are **not monotonic** in the size of baby bonus
- Welfare maximized around replacement fertility. Consumption equivalence increases by **3.2%**. Sources: (1) higher n , (2) lower τ_c , (3) change in μ
- **Progressive** policy with large welfare improvement for low-income households

**What is the
policy objective?**

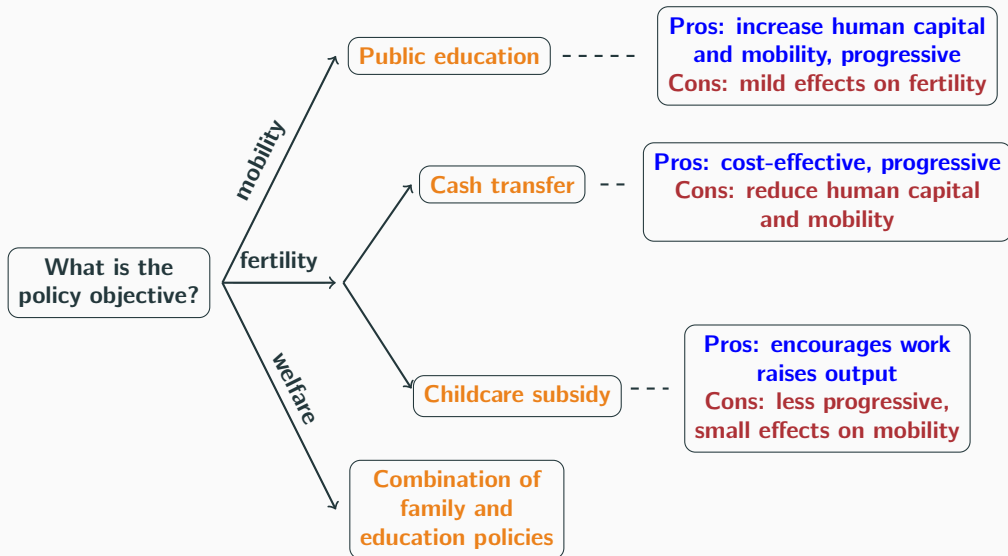
Taking Stock



Taking Stock



Taking Stock



Macroeconomic consequences of large-scale family policies depend on:

- Fertility responses, endogenous skill formation and **GE** effects

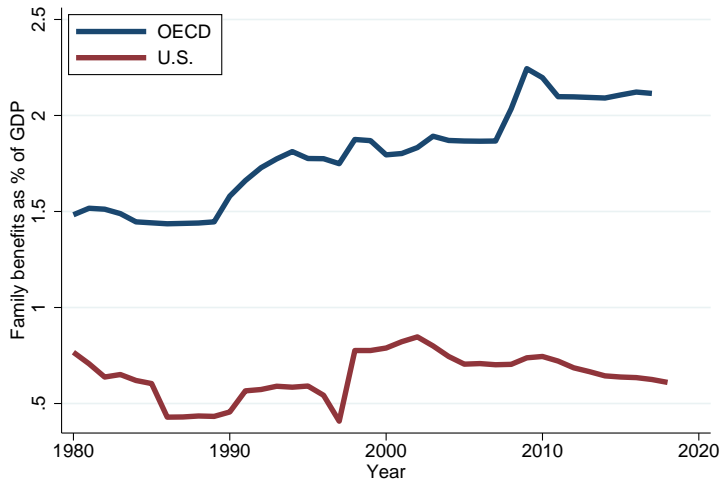
Model

- Introduce **quality/quantity trade-off** into a GE-OLG model with incomplete market and distortionary taxes

Results:

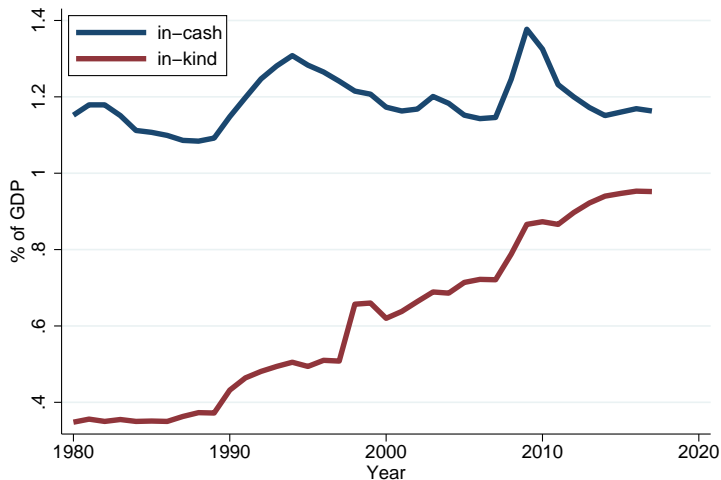
- ① Compared with models where fertility is fixed, introducing endogenous fertility reverses several key policy implications under conservative parametrization
- ② Despite having negative effects on average human capital and social mobility, a **\$28k** baby bonus raises fertility to replacement level and improves welfare by **3.2%** via effects on **demographic structure** and taxes in general equilibrium
- ③ Public education raises output, mobility and welfare, but has mild effects on fertility

Time Trend of Public Expenditures on Child Benefits



Source: OECD database

Expenditure Breakdown



Source: OECD database

Working Without Children and Retirement

- For households working without children:

$$V_j(h, a) = \max_{c, a' \geq 0} u(c) + \beta \mathbb{E} V_{j+1}(h', a')$$

$$(1 + \tau_c)c + a' = (1 + r)a + y - \mathcal{T}(y, a, 0)$$

$$h' = L(h, 1, z)$$

- For retired households:

$$V_j(h, a) = \max_{c, a' \geq 0} u(c) + \beta V_{j+1}(h, a')$$

$$(1 + \tau_c)c + a' = (1 + r - r\tau_a)a + \pi \cdot wh$$

$$V_9(\cdot) \equiv 0$$

where π is pension replacement rate

Stationary Equilibrium

- **Distributions:**

- Demographic structure $\{\Omega_j\}_{j=0}^8$ and distribution of agents over states μ are invariant over time periods
- Distribution of initial states is determined by older generations and shock processes

- **Households Optimize:** Households choose consumption, savings, fertility, childcare arrangements, child investments and inter-vivos transfers such that utility is maximized

- **Firms maximize profits**

- **Prices clear markets**

- **Government balances budget in period to period**

Identification

- Recall parametric assumptions:

$$u(c) = \frac{c^{1-\gamma_c}}{1-\gamma_c} \quad \gamma_c \in (0, 1)$$

$$v(n, \mathbb{E}h_k, a_k) = \Psi(n) \cdot (\theta \cdot u(\mathbb{E}h_k) + \nu \cdot u(a_k))$$

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- Córdoba, Ripoll and Liu (2016): **γ_c (EGS) governs quality/quantity trade-off.**
Higher $\gamma_c \Rightarrow$ higher MRS of quantity for quality \Rightarrow MB_n rises faster with h than $MC_n \Rightarrow$ flatter or even positive **income-fertility profile**
- Calibrate $\gamma_c = 0.54$ to match income-fertility profile (CPS)

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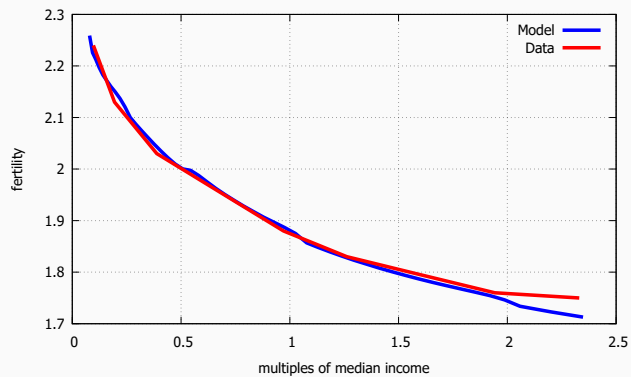
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- Calibrate $\gamma_c = 0.54$ to match income-fertility profile (CPS)
- Córdoba and Ripoll (2019) disentangles EIS from EGS. To fit data:
 - EGS is significantly larger than one (c.f. $\gamma_c < 1$)
 - EIS is at most one (c.f. risk-aversion to fit wealth accumulation)

Model Fit: Fertility-Income Profile



Childcare Arrangement

- **Childcare arrangements:**

$$n \cdot \chi = \left(t_h^{v/\iota} + (n \cdot m)^v \right)^{1/v}$$

Set $\chi = 0.18$. Returns to scale within family $\iota = 0.7$ (Folbre 2008)

- Elasticity of substitution: $v = 0.5$ - average share of income spent on childcare by education (SIPP) (Malik 2019)
- **Price of full-time childcare:** $p_m = \$6,860$ per year for child aged 0-10 (The National Association of Child Care Resource & Referral Agencies 2011)

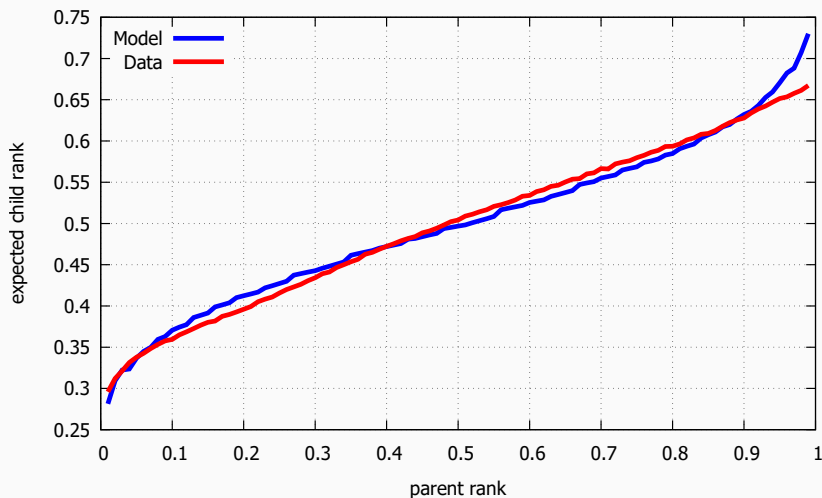
- **Human capital of working adults** evolves:

$$h_{j+1} = \exp(z) (h_j + \zeta(h_j t))^\eta$$

$$\log(z) \sim \mathcal{N}(\mu_z, \sigma_z)$$

- $\eta = 0.61, \zeta = 0.72$ - lifecycle earnings (PSID) (Huggett, Ventura and Yaron 2011)
- $\mu_z = -0.23, \sigma_z = 0.42$ - 2% skill depreciation and lifecycle Gini coefficient of earnings (Huggett, Ventura and Yaron 2011)

Intergenerational Mobility: Model vs Data



- Rank-rank slope = 0.34 (Chetty, Hendren, Kline and Saez 2014)

- **Firms' production function:** capital share $\alpha = 0.33$ and 4% capital depreciation
- **Government taxes**

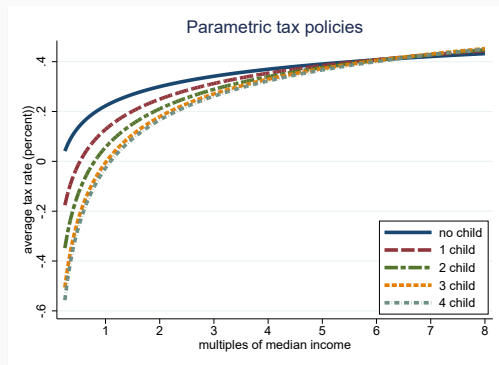
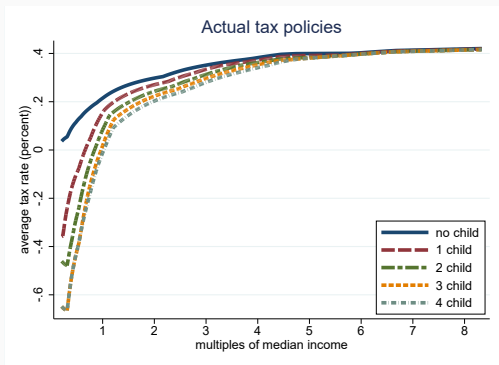
- **Income taxes:**

$$\mathcal{T}(y, a, n) = y \cdot (1 - \tau_y^n y^{-\lambda_y^n}) + \tau_a r a$$

where $\{\tau_y^n, \lambda_y^n\}_{n=0}^6$ estimated using TAXSIM

- **Tax rates** from McDaniel (2014): $\tau_c = 0.07$ and $\tau_a = 0.27$
- **Pension replacement rate:** $\pi = 40\%$

Income Taxes: Model vs Data



- Child tax benefits (reduction in tax rates) are larger for low-income households

Baby Bonus in Australia

- **A\$3,000 baby bonus**⁴ to every child born on or after July 1st 2004
- Peter Costello (Treasurer of Australia): "One (baby) for the Mum, one for the Dad, and one for the country"
- $tfr_{AUS,2004} = 1.77 > 1.73 = tfr_{USA,2018}$ before the Covid Baby Bust [▶ other](#)
- Drago et al. (2011) finds:
 - Significant fertility responses and evidence for long-term/quantum effects
 - Marginal cost for an additional birth to be at least A\$126,000⁵
 - Larger fertility responses from low-income households
- Gaitz and Schurer (2017) finds that the baby bonus was **ineffective** in boosting learning, socio-emotional or physical health outcomes of pre-school children

[▶ back to intro](#)[▶ back to results](#)

⁵More details: (1) Announced on Mar.12th 2004, (2) universal coverage, lump-sum payment, (3) Equivalent to 4 times average weekly earnings, (4) Equivalent to \$2,800 in 2010 USD.

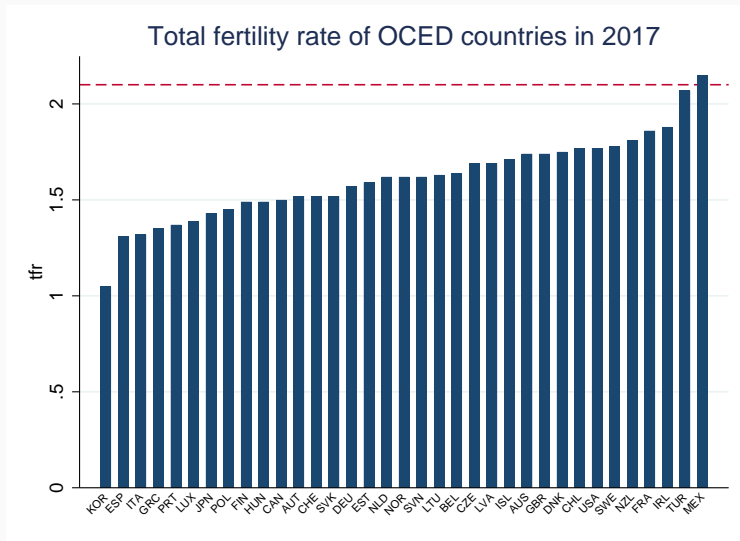
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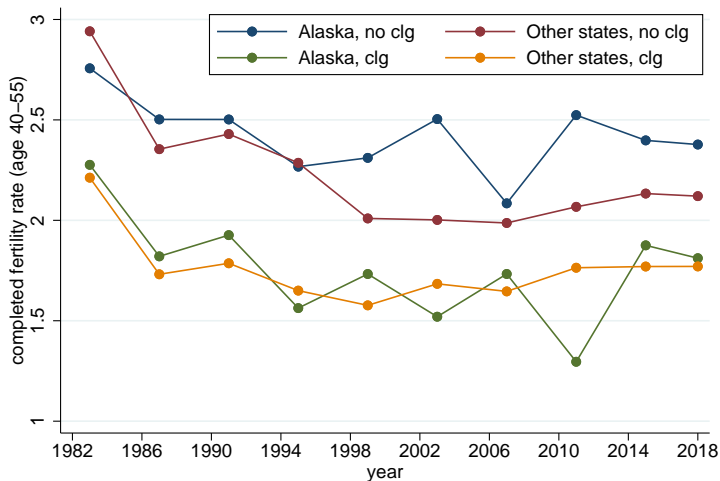
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⁵Equivalent to \$117,600 in 2010 USD. Quantitative model predicts \$130,000 is needed for an additional birth (for the U.S.).

Total Fertility Rate Across Countries

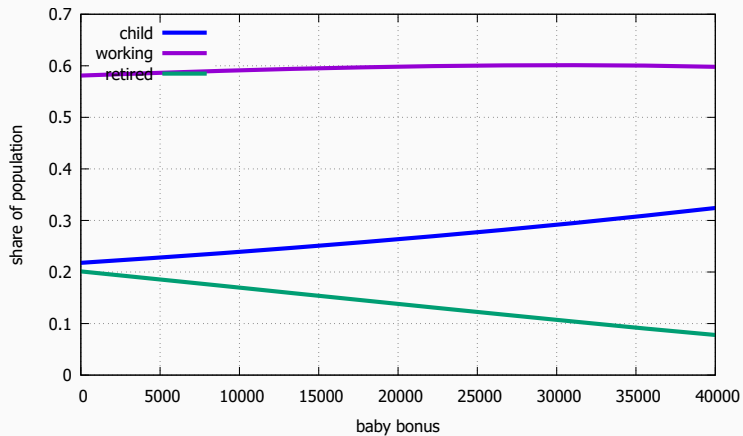


Evidence from Completed Fertility Rates



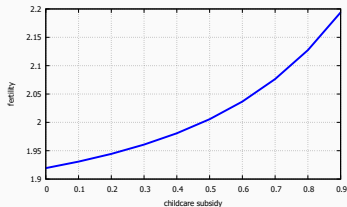
Source: CPS June Fertility Supplement, 4-Year Bins

Change in Demographic Structure

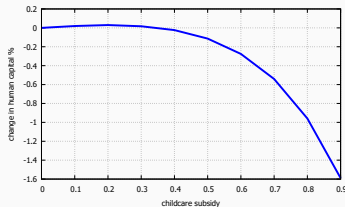


Highlights for Subsidized Childcare \mathcal{S}

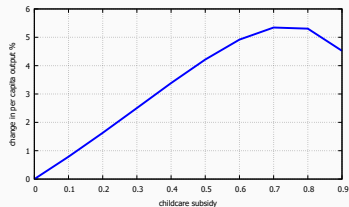
Fertility



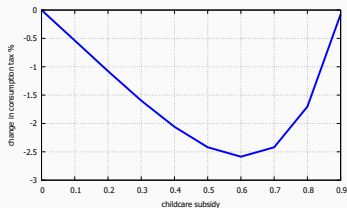
Average human capital



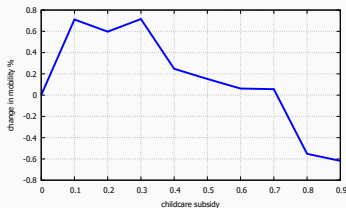
Per capita output



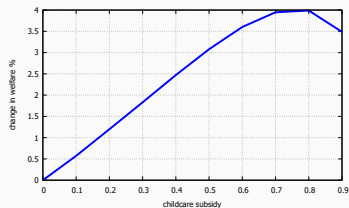
Change in consumption tax



Intergenerational Mobility



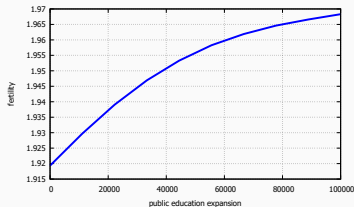
Welfare



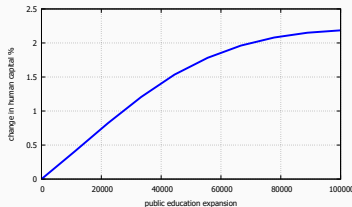
- Need **78%** refund to reach 2.1 fertility, **50%** less cost-effective than baby bonus
- Impacts of subsidized childcare are qualitatively similar to baby bonus except that **it encourages work** (Guner, Kaygusuz and Ventura 2020) and **mobility effect is small**
- **Less progressive** because subsidy amount depends on childcare expenditures

Highlights for Public Education Expansion \mathcal{E}

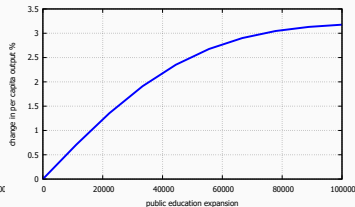
Fertility



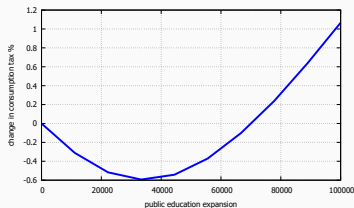
Average human capital



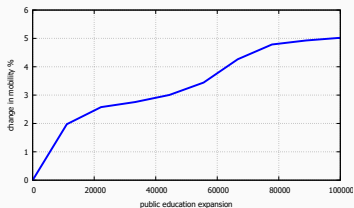
Per capita output



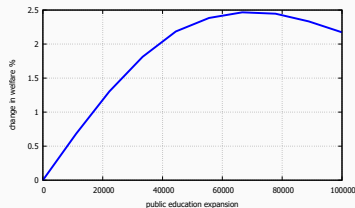
Change in consumption tax



Intergenerational Mobility

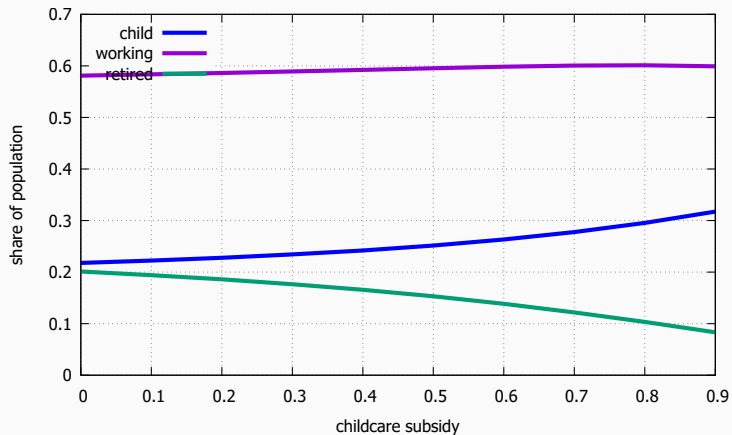


Welfare

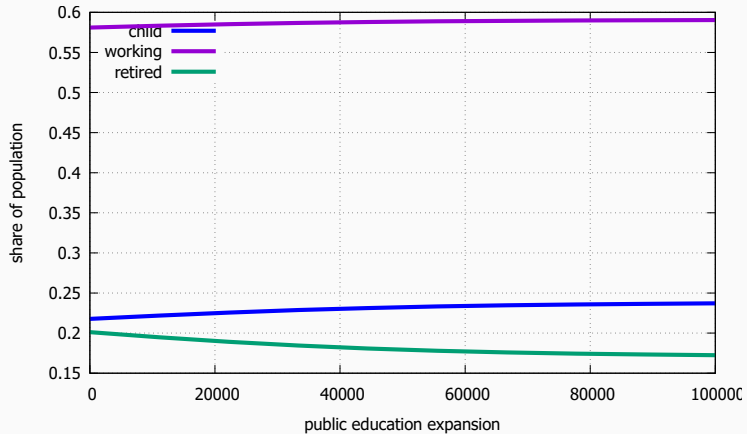


- **Mildest fertility effects** (0.035 boost vs 0.3 boost using \$40k baby bonus)
- **Most effective in improving mobility** (4% increase using \$65k)
- **Progressive** policy with large welfare improvement for low-income households

Change in Demographic Structure



Change in Demographic Structure



Transition path

- **Question:** How long do we need to wait for aggregate effects to take place? What are the distributional consequences for households in the original steady-state? Majority support for policy reform?
- **Conjecture:** Majority support may requires transfers **within cohorts**

Alternative ways of financing

- **Question:** How will things change if the policy could be funded via government deficits or labor/capital taxes?

Optimal policies

- **Question:** What is the optimal policy combination to maximize welfare?