

Building Future Generations: The Macroeconomic Consequences of Family Policies

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This Paper: **What are the macroeconomic consequences of family policies?**

- ① Effects on fertility, human capital, social mobility, and welfare
- ② Short-run versus long-run effects, and transition
- ③ Compare in-cash versus in-kind family policies

A quantitative heterogeneous-agent GE-OLG model that incorporates:

- ① Joint determination of **child quantity** and **child quality**
- ② Rich life cycle with **endogenous demographic structure**
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- ② Composition effects (changing composition of parents)
- ③ Demographic structure effects (age distribution)

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Parameter(s) governing the trade-off between child quality and quantity:

- Disciplined by matching cross-sectional data and RCT evidence
- Validated using the Alaska Permanent Fund Dividend and other existing policies

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 - ④ Government needs to finance higher child-related expenditures in transition
- Subsidized childcare and public education are less cost-effective in raising fertility, but offer other advantages

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Fertility, Family Policies, and the Aggregate Economy

- **Empirical:** Milligan (2005), Laroque and Salanié (2008), Drago et al. (2011), Luci-Greulich and Thévenon (2013), González (2013), Raute (2019)...
- **Structural:** [de la Croix and Doepke \(2003\)](#), Kim, Tertilt and Yum (2021)
- **Contribution:** [Develop a structural model tailored to analyzing family policies](#)

Income transfers, Children's Outcomes, and Social Mobility

- Benabou (2002), Heckman and Mosso (2014), Bastian and Michelmore (2018), [Daruich \(2019\)](#), Abbott, Gallipoli, Meghir and Violante (2019), Mullins (2019), [Guner, Kaygusuz and Ventura \(2020\)](#)...
- **Contribution:** [Endogenize fertility choice and demographic structure](#)

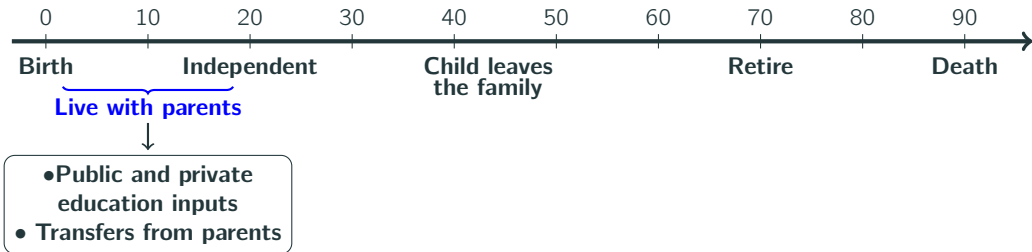
- ① Model
- ② Calibration (2010 USA)
- ③ Validation – the Alaska Permanent Fund Dividend (APFD)
- ④ Counterfactual – Steady-State & Transition
- ⑤ Compare In-Cash vs In-Kind Policy Instruments
- ⑥ Conclusion

Model

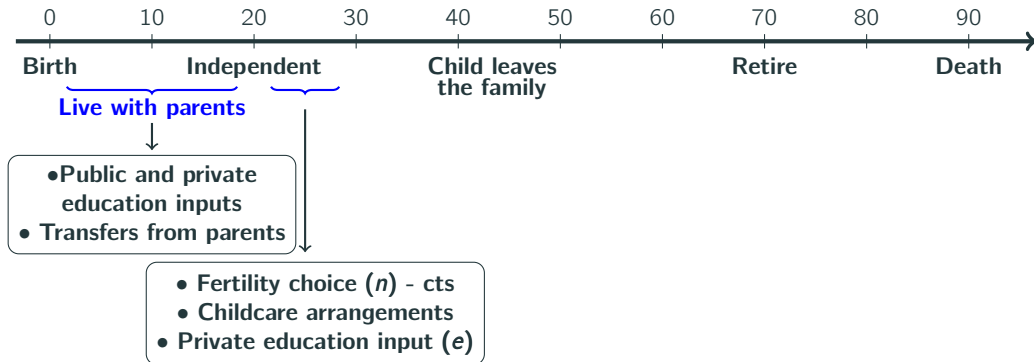
Model: Life Cycle



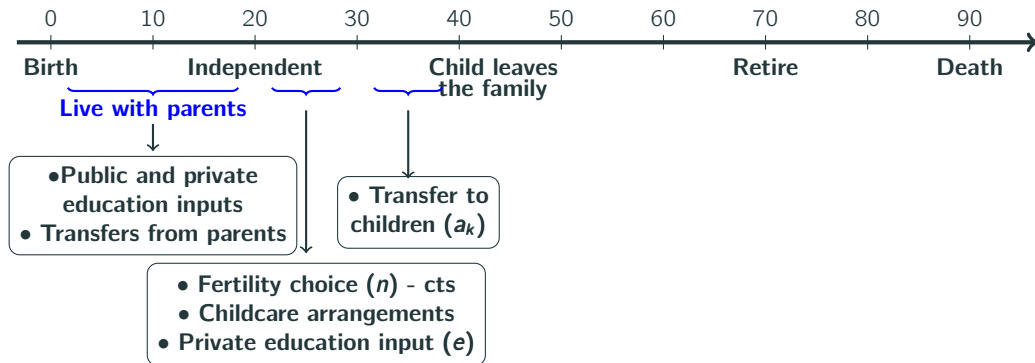
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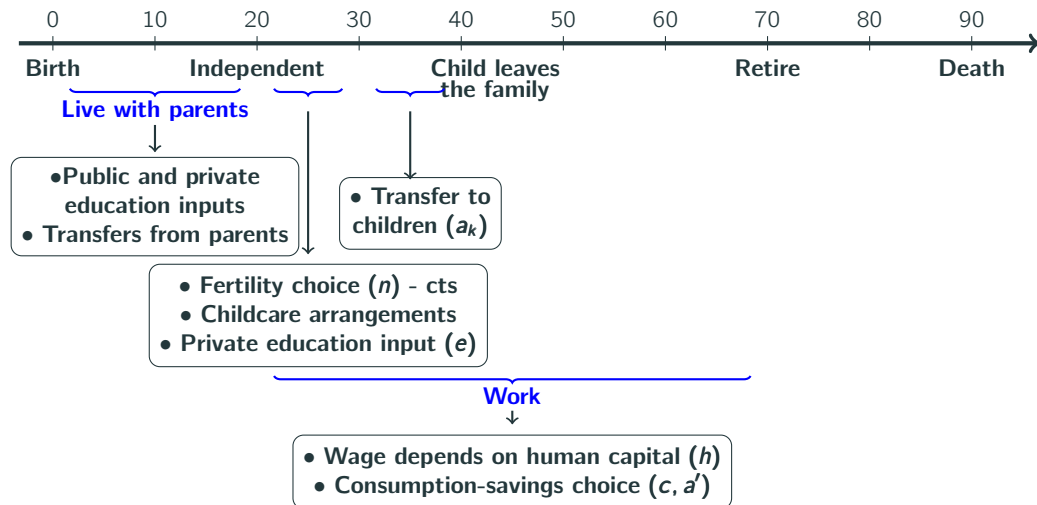
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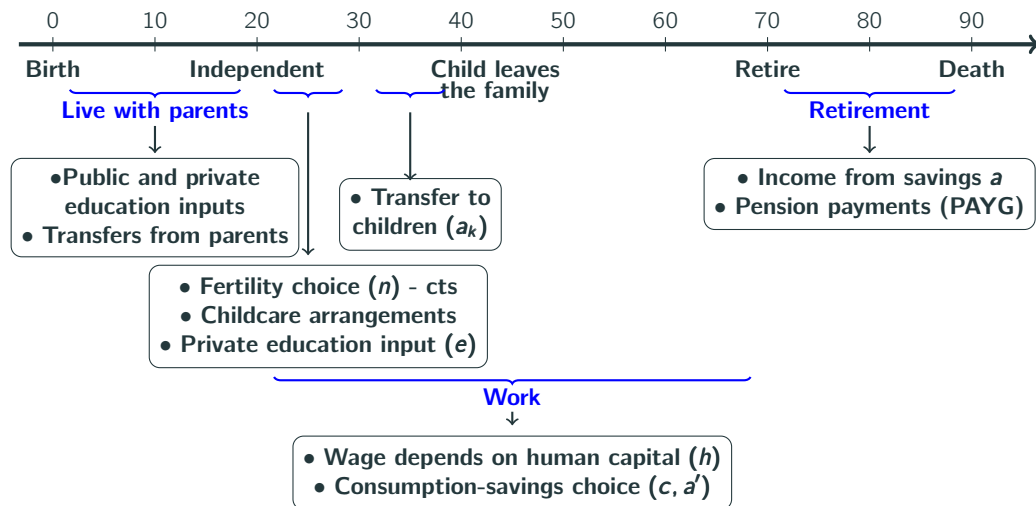
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Fertility, Childcare and Skill Formation



$$V_2(h, a) = \max_{c, a', n, e, t_h, m \geq 0} u(c/\Lambda(n)) + \beta \mathbb{E} V_3(h', a', n, \mathbb{E} h_k)$$

h : parents' skills

t_h : total home care

χ : childcare time

\mathcal{S} : childcare subsidy

a : assets

m : market care

p_m : market care price

\mathcal{B} : baby bonus

n : fertility

e : private educ. input

$\Lambda(n)$: equivalence scale

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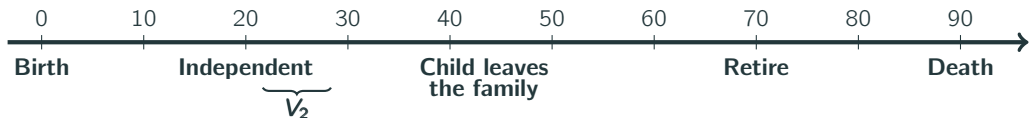
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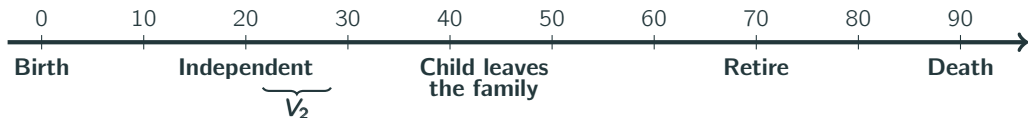
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$$(1 + \tau_c)(c + (p_m \cdot m + e) \cdot n) + a' = (1 + r)a + y - \mathcal{T}(y, a, n) + \mathcal{B} \cdot n \quad \text{[BC]}$$

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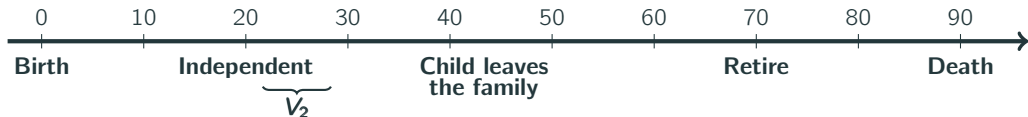
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$$h' = L_2(h, 1 - t_h, z') \quad h_k = G(h, \mathcal{E}, e, \epsilon) \quad [\text{technology}]$$

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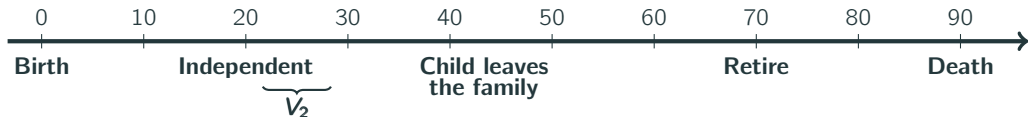
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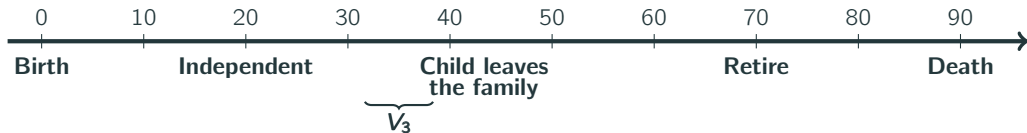
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Two simplifying modeling assumptions:

- ① $G(h, \mathcal{E}, e, \epsilon)$ captures the overall skill formation of children from age 0 to 20
 - ② Time cost χ is non-educational and parents investments are summarized by e .
- High-quality public childcare can be implemented by raising \mathcal{S} and \mathcal{E} jointly in the model

Parent-to-Child Transfer



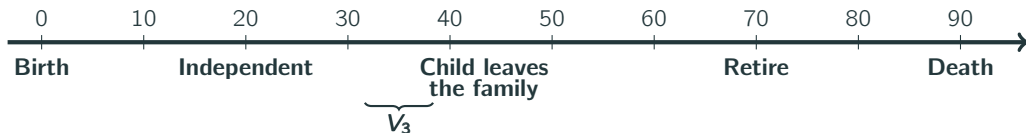
$$V_3(h, a, n, \mathbb{E}h_k) = \max_{c, a', a_k \geq 0} u(c/\Lambda(n)) + \beta \mathbb{E}V_4(h', a') + \underbrace{v(n, \mathbb{E}h_k, a_k)}_{\text{utility from quantity and quality}}$$

$$y = wh$$

$$(1 + \tau_c)c + a' + n \cdot a_k = (1 + r)a + y - \mathcal{T}(y, a, n) \quad [\text{BC}]$$

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Child quantity (n) interacts with child quality ($\mathbb{E}h_k, a_k$) in two ways:

- ① [BC]: higher n raises marginal costs of ($\mathbb{E}h_k, a_k$) à la Becker and Lewis (1973)
- ② Preferences: complements or substitutes – calibrated to match data

Family Policy Mechanisms with Endogenous Fertility

quantity-quality Trade-off

- Consider increase in \mathcal{B} on private educational input e :

$$\underbrace{MU_c \cdot n}_{\text{marginal costs of } e} = \underbrace{\frac{\partial v(n, \mathbb{E}h_k, a_k)}{\partial \mathbb{E}h_k} \cdot \frac{\partial \mathbb{E}h_k}{\partial e}}_{\text{marginal benefits of } e} \quad \text{FOC [e]}$$

- When n is fixed, $\mathcal{B} \uparrow$ (income effect), $MU_c \downarrow \implies e \uparrow$
- When n is endogenous, $\mathcal{B} \uparrow$ ("price" change), $n \uparrow \implies e$ could fall (quantitative prediction depends on calibrated parameters)

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Composition Effects

- Average child human capital:

$$\underbrace{\bar{h}_k}_{\text{average } h_k} = \iint \underbrace{\frac{n^*(h, a)}{N}}_{\text{fertility weight}} \cdot \underbrace{h_k^*(h, a, \cdot)}_{\text{individual child's } h_k} d \underbrace{\mu_2}_{\text{parents' dist.}} d\epsilon$$

- Family policies change the fertility weights, i.e. composition of parents

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- Government fiscal budget:

$$\underbrace{\left(\sum_{j=2}^6 \omega_j \int \mathcal{T}(y_j^*, a_j^*, n_j^*) d\mu_j \right)}_{\text{labor and capital income taxes}} + \underbrace{\tau_c \left(\sum_{j=2}^8 \omega_j \int c_j^* d\mu_j + \omega_2 \int n^* (p_m m^* + e^*) d\mu_2 \right)}_{\text{consumption taxes}} =$$

$$\underbrace{(\omega_0 + \omega_1) \cdot \mathcal{E}}_{\substack{\text{mass of children} \\ \text{public education}}} + \underbrace{\omega_2 \left(\underbrace{\int n^* \cdot \mathcal{B} d\mu_2}_{\text{baby bonus}} + \underbrace{\int (1 + \tau_c) n^* p_m \cdot \mathcal{S} d\mu_2}_{\text{subsidized childcare}} \right)}_{\text{family policy expenditures}} + \underbrace{\pi \left(\sum_{j=7}^8 \omega_j \int wh d\mu_j \right)}_{\text{pension payments}} + \underbrace{\sum_{j=2}^8 \omega_j \cdot \mathcal{X}}_{\text{others}}$$

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- **Demographic Structure Effects:** Family policies change $\{\omega_j\}_{j=0}^8$. Effects on fiscal burden depends on relative costs of old versus child

Calibration

Model Parameters

Table 1: Model Parameters

Interpretation		Value	Source	Interpretation		Value	Source
Preferences				Child human capital production			
β	discount rate	0.98 ¹⁰	standard	Z	normalizing scalar	2.50	median income =1
γ	elasticity of substitution	0.73	CPS	σ_ϵ	ability shock dispersion	0.58	PSID
ψ	fertility preference	2.30	CPS	ρ	intergenerational spillover	0.30	Chetty et al. (2014)
θ	human capital preference	2.85	PSID	ξ	substitution of education	0.9	CEX
ν	transfer preference	0.29	PSID	\mathcal{E}	public education	\$12,000	NCES
Childcare arrangement				κ	input productivity	0.13	Gárcia et al. (2020)
χ	childcare cost	0.18	ATUS	Adults' human capital evolution			
ι	economies of scale at home	0.7	ATUS	η	learning curvature	1.22	PSID
υ	substitutability of care	0.38	SIPP	$\{\zeta\}_{j=2}^5$	learning level	misc.	PSID
p_m	price of full-time care	\$6,860	NACCRRA	μ_z	skill depreciation	-0.23	PSID
Taxes and pension				σ_z	shock dispersion	0.38	PSID
τ_y^0, λ_y^0	tax levels and progressivity	misc.	TAXSIM	Firm production function			
τ_c	consumption tax	0.07	McDaniel (2007)	A	total factor productivity	1	normalization
τ_a	capital income tax	0.27	McDaniel (2007)	α	capital share	0.33	standard
π	pension replacement rate	0.40	OECD Database	δ_k	capital depreciation	0.04 ¹⁰	standard

- 14 parameters are **calibrated** within the model

► moment fit

► childcare ► adult skill ► firm and gov.

Utility from child quantity and quality:

$$v(n, \mathbb{E}h_k, a_k) = \underbrace{\Psi(n)}_{\text{child discounting}} \cdot \underbrace{(\theta \cdot u(\mathbb{E}h_k) + \nu \cdot u(a_k))}_{\text{utility from child quality}}$$

$$\underbrace{\Psi(n) = 1 - \exp(-\psi n)}_{\text{increasing \& concave in } n} \quad u(x) = \frac{x^{1-\gamma}}{1-\gamma} \quad \gamma \in (0, 1) \quad x \in \{\mathbb{E}h_k, a_k, c\}$$

- Results robust to dynastic altruism and separable preferences

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- γ - elasticity of intergenerational substitution (EGS) (Córdoba and Ripoll 2019)

Utility from child quantity and quality:

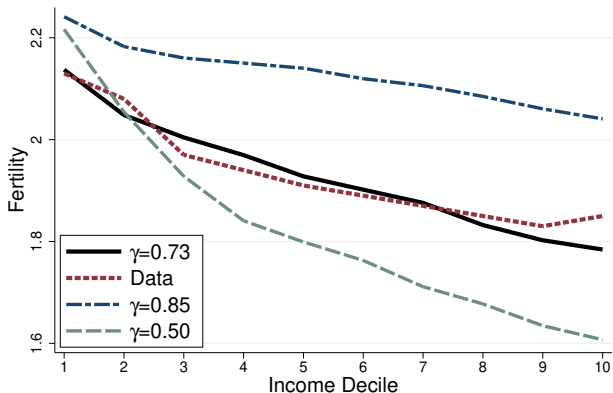
$$v(n, \mathbb{E}h_k, a_k) = \underbrace{\Psi(n)}_{\text{child discounting}} \cdot \underbrace{(\theta \cdot u(\mathbb{E}h_k) + \nu \cdot u(a_k))}_{\text{utility from child quality}}$$

$$\underbrace{\Psi(n) = 1 - \exp(-\psi n)}_{\text{increasing \& concave in } n} \quad u(x) = \frac{x^{1-\gamma}}{1-\gamma} \quad \gamma \in (0, 1) \quad x \in \{\mathbb{E}h_k, a_k, c\}$$

- Results robust to dynastic altruism and separable preferences
- $\{\psi, \theta, \nu\}$ matches aggregate fertility and average spendings on quality
- γ - elasticity of intergenerational substitution (EGS) (Córdoba and Ripoll 2019)
- Conditional on other parameters, **γ determines fertility elasticity**. Higher $\gamma \implies$ smaller fertility responses, larger quality responses (c.f. Soares 2005) ▶ intuition

Identification of γ

- γ identified by **fertility-income profile** (Córdoba, Ripoll and Liu 2016). Higher $\gamma \implies$ Higher MRS of quantity for quality \implies flatter profile



- Calibrated γ generates realistic life-cycle profile of net worth

► net worth

Children's Skill Production Function

- Children's skill production function:

$$h_k = \underbrace{Z}_{\text{scalar}} \cdot \underbrace{\epsilon}_{\text{shock}} \cdot \underbrace{h^\rho}_{\text{spillover}} \cdot \left(\underbrace{\mathcal{E}^\xi}_{\text{public education}} + \underbrace{e^\xi}_{\text{private input}} \right)^{\kappa/\xi}$$

$$\log(\epsilon) \sim \mathcal{N}\left(-\frac{\sigma_\epsilon^2}{2}, \sigma_\epsilon^2\right)$$

- Highlight of parameters:
 - $\rho = 0.3$ - rank-rank mobility (Chetty, Hendren, Kline and Saez 2014)
 - $\mathcal{E} = 0.16$ - \$12k per pupil per year (NCES)
 - $\kappa = 0.13$ - **RCT evidence** from García, Heckman, Leaf and Prados (2020)

Validation

Does the model generate responses that match empirical estimates?

External validation using **Alaska Permanent Fund Dividends (APFD)**

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 - ① Large in scale (\approx \$1.5k per year) relative to other family policies
 - ② Simple implementation that is income- or work-tested

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- Ideal setting to test fertility responses:
 - ① Large in scale (\approx \$1.5k per year) relative to other family policies
 - ② Simple implementation that is income- or work-tested
- Re-calibrate, then implement APFD in the model: universal basic income (UBI) to parents and children by \$1.5k. The model predicts:
 - ① Completed fertility rises by **0.16** children per women
 - ② Larger responses from households with lower human capital

Difference-in-Difference Analysis

- CPS June Fertility Supplement 1982-2018, Alaskan women aged 40-55 divided into “not treated”, “partially treated” ($T_1 = 1$), and “fully treated” ($T_2 = 1$)

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- Estimate on full sample, and subsamples by education (at least 1 year of college)

$$\text{fertility} = \beta_0 + \beta_1 T_1 + \beta_2 T_2 + \text{State FE} + \text{Year FE} + \epsilon$$

Difference-in-Difference Analysis

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$$\text{fertility} = \beta_0 + \beta_1 T_1 + \beta_2 T_2 + \text{State FE} + \text{Year FE} + \epsilon$$

- Regression results confirm model predictions:

	(1) Full Sample	(2) Low Educ.	(3) High Educ.	Average	Model Low Educ.	High Educ.
β_1	0.098*** (0.027)	0.216*** (0.036)	0.074*** (0.021)			
β_2	0.172*** (0.032)	0.296*** (0.041)	0.105*** (0.025)	0.16	0.31	0.09
# Obs.	146,804	69,511	77,293			

Counterfactual

Main Counterfactual

- Evaluate **baby bonuses** \mathcal{B} of different sizes
 - Timing: unexpected and permanent policy change
 - Source of funds: τ_c balances budget each period

Main Counterfactual

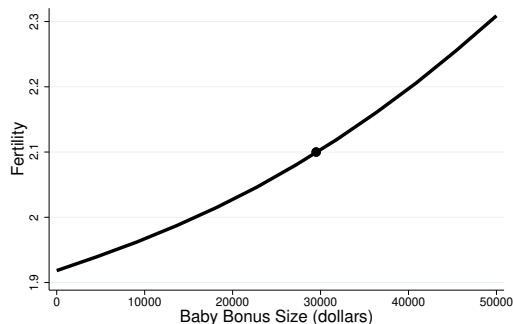
- Evaluate **baby bonuses** \mathcal{B} of different sizes
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 - ① Long-run welfare $\mathcal{W} = \int V_2 d\mu_2$ – average value of newborn
 - ② Welfare of existing households and those born in transition
- Roadmap of results:
 - Long-run effects
 - Transition and distributional effects across generations
- Other policies: subsidized childcare \mathcal{S} and public education \mathcal{E}

Fertility Effects of Cash Rewards to Childbirth

Figure 1: Effects on aggregate fertility



- **$B = \$30k$** raises aggregate fertility rate to the replacement level (benchmark policy), costing around 1.8% of GDP in the new equilibrium

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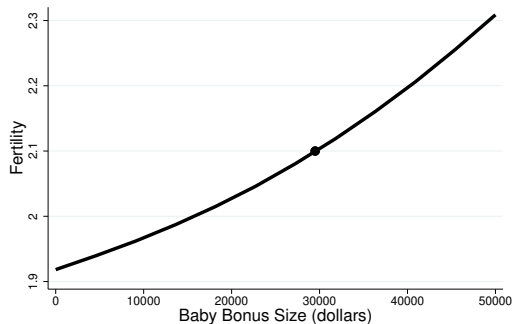
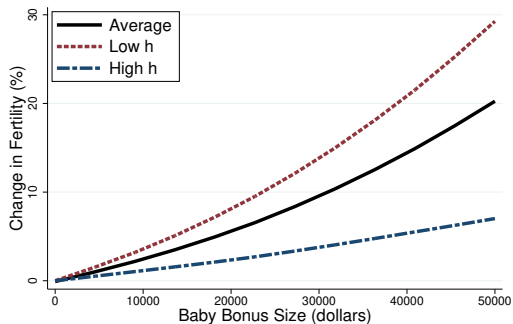


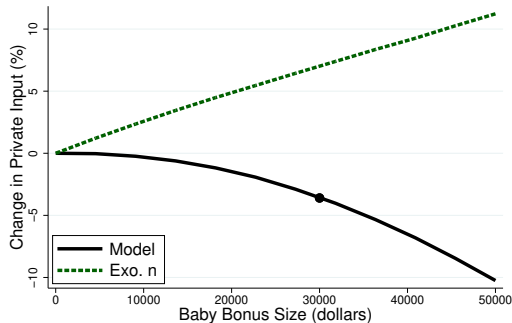
Figure 2: Heterogeneous fertility response



- **$B = \$30k$** raises aggregate fertility rate to the replacement level (benchmark policy), costing around 1.8% of GDP in the new equilibrium
- Parents with lower human capital respond more in fertility – larger proportional change in the shadow price of child ($e^*(h)$ and wh)

Effects on e and Average Human Capital

Figure 3: Average private input e



- Average private input (e) **falls by 4%** – **quantity-quality trade-off**

Effects on e and Average Human Capital

Figure 3: Average private input e

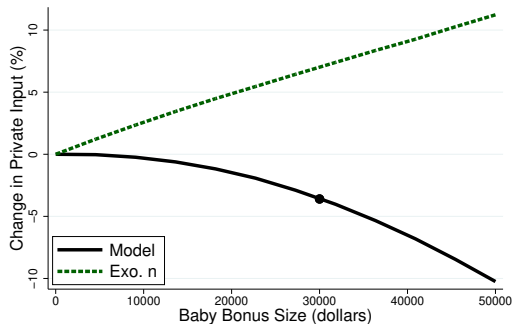
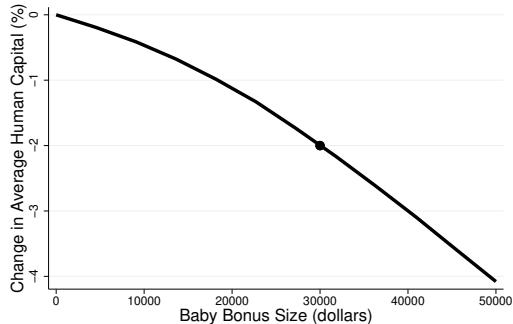


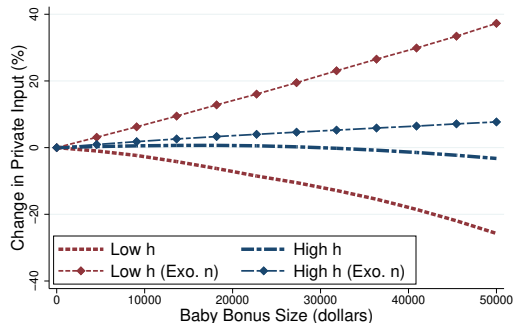
Figure 4: Average human capital



- Average private input (e) **falls by 4%** – **quantity-quality trade-off**
- Average human capital **falls by 2%** – **composition effects** and reduced private input e

Average Human Capital and Social Mobility

Figure 5: Heterogeneous response in e



- Larger reductions in e among parents with low h as their n increases more

Average Human Capital and Social Mobility

Figure 5: Heterogeneous response in e

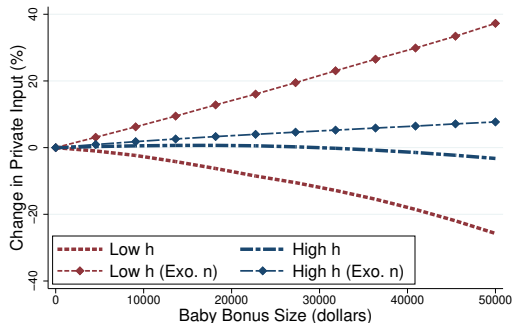
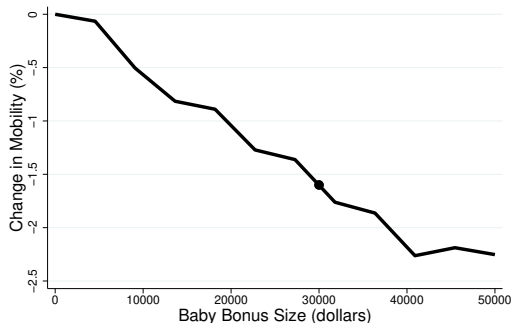


Figure 6: Intergenerational mobility



- Larger reductions in e among parents with low h as their n increases more
- Intergenerational mobility **decreases by 1.8%**

Average Human Capital and Social Mobility

Figure 5: Heterogeneous response in e

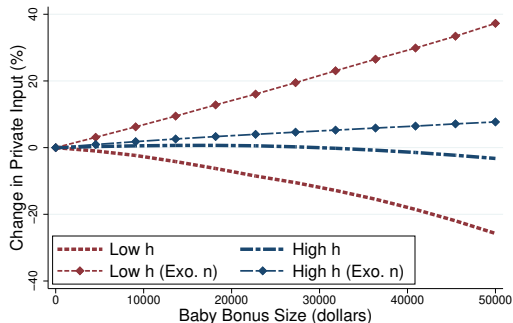
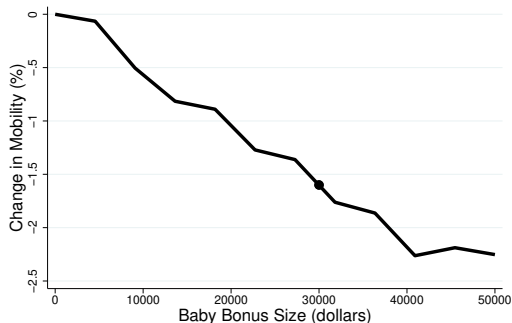
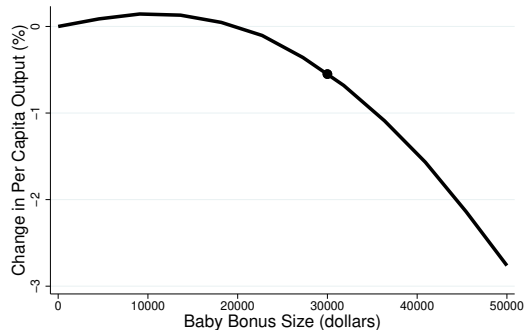


Figure 6: Intergenerational mobility



- Larger reductions in e among parents with low h as their n increases more
- Intergenerational mobility **decreases by 1.8%**
- Results will be **stronger** when baby bonus is targeted at low-income households

Figure 7: Per capita output



- Per capita output **falls by 0.6%**

Output and Tax

Figure 7: Per capita output

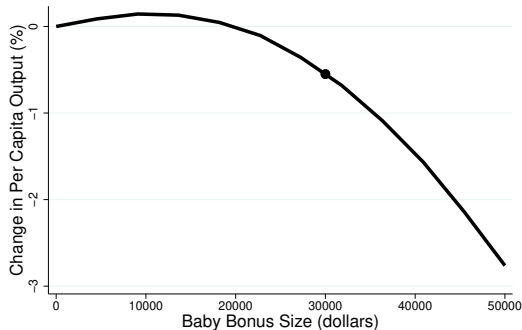
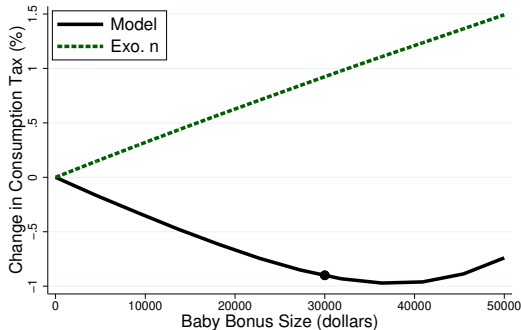
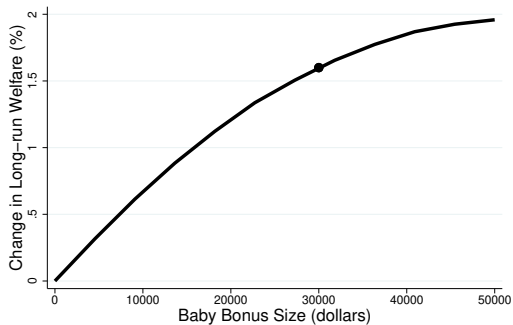


Figure 8: Change in consumption tax



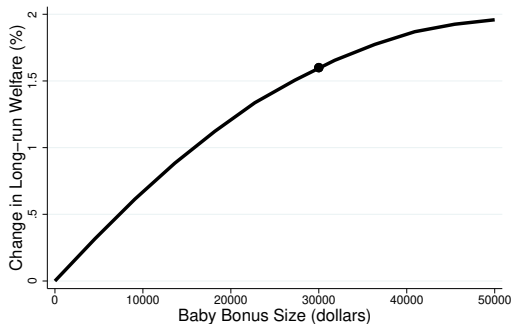
- Per capita output **falls by 0.6%**
- **Demographic structure effects:** consumption taxes **reduces by 0.9%**

Figure 9: Change in welfare



- Long-run welfare \mathcal{W} increases by 1.6%, mostly due to lower taxes (0.9%)

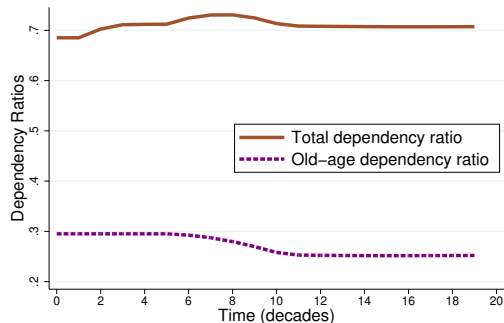
Figure 9: Change in welfare



- Long-run welfare \mathcal{W} increases by 1.6%, mostly due to lower taxes (0.9%)
- FSD in μ is **neither necessary nor sufficient** for better policies - need to consider ω (c.f. Chu and Koo 1990)

Transition Path of $\mathcal{B} = \$30,000$ - Replacement Fertility

Figure 10: Change in dependency ratios



- Higher child-related government expenditures in the first few decades beyond the direct policy costs (\mathcal{E} and $\mathcal{T}(n, \cdot)$)

Transition Path of $\mathcal{B} = \$30,000$ - Replacement Fertility

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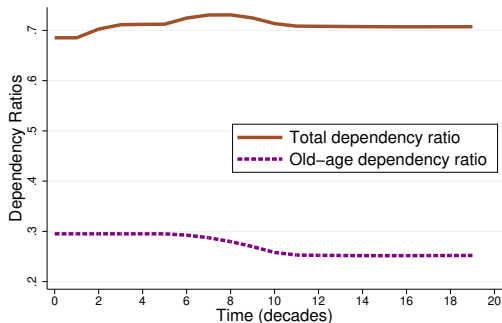
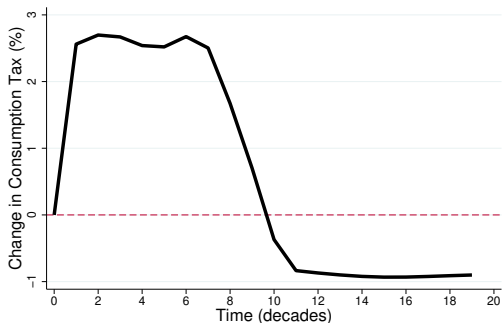


Figure 11: Change in consumption tax

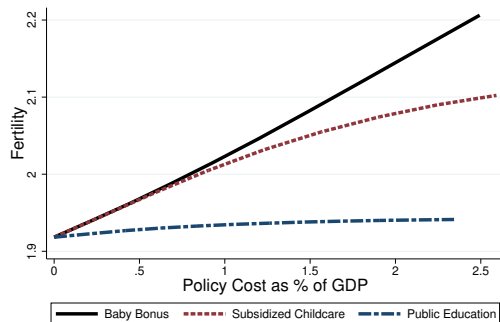


- Higher child-related government expenditures in the first few decades beyond the direct policy costs (\mathcal{E} and $\mathcal{T}(n, \cdot)$)
- With τ_c changing to balance the budget, welfare effects for:
 - Newborns in transition – positive but smaller than 1.6%
 - Existing baby bonus recipients – positive, existing non-recipients – negative

► plot

Highlights of Policy Comparisons

Figure 12: Effects on Fertility



- \mathcal{S} and \mathcal{E} are less cost-effective in raising fertility

Highlights of Policy Comparisons

Figure 12: Effects on Fertility

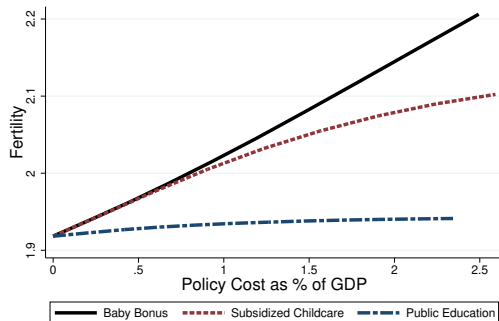
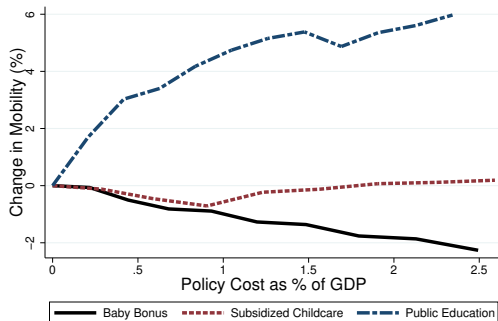


Figure 13: Effects on Mobility



- \mathcal{S} and \mathcal{E} are less cost-effective in raising fertility
- \mathcal{E} is most effective in improving mobility - larger effects when targeted at low-income families

What I do:

- Develop a quantitative GE-OLG model to study the macroeconomic consequences of family policies
- Calibrate the model to match U.S. data and validate using empirical evidence

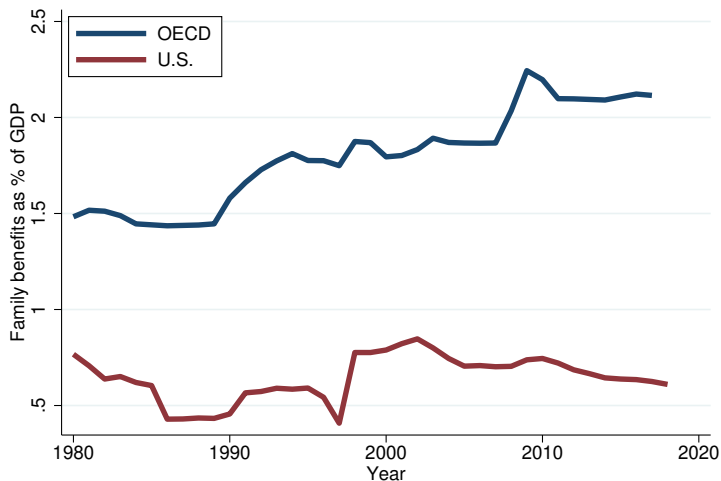
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What I Find:

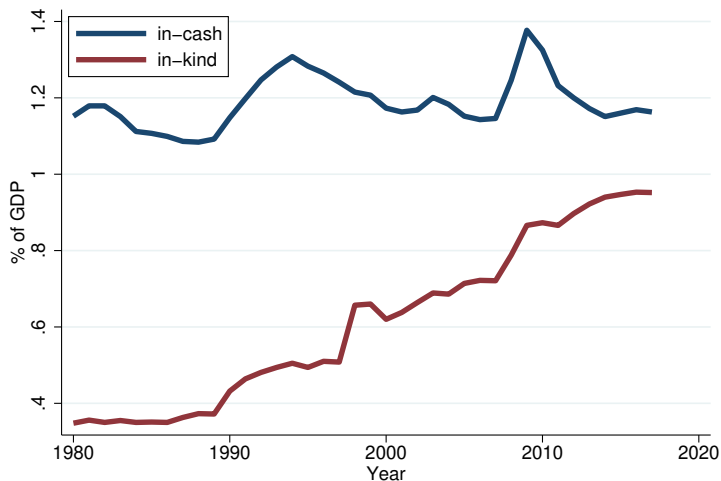
- ① \$30k cash benefit at birth raises fertility to the replacement level, but reduces average human capital and social mobility by 2%
- ② Long-run welfare rises 1.6% due to endogenous demographic structure changes
- ③ Government needs to finance higher child-related expenditures in transition
- ④ In-kind policies have smaller fertility effects, but offer other advantages

Time Trend of Public Expenditures on Child Benefits



Source: OECD database

Expenditure Breakdown



Source: OECD database

Working Without Children and Retirement

- For households working without children, $j \in \{4, 5, 6\}$:

$$V_j(h, a) = \max_{c, a' \geq 0} u(c/\Lambda(0)) + \beta \delta_j \mathbb{E} V_{j+1}(h', a')$$

$$(1 + \tau_c)c + a' = (1 + r)a + y - \mathcal{T}(y, a, 0)$$

$$h' = L_j(h, 1, z)$$

- For retired households, $j \in \{7, 8\}$:

$$V_j(h, a) = \max_{c, a' \geq 0} u(c/\Lambda(0)) + \beta \delta_j V_{j+1}(h, a')$$

$$(1 + \tau_c)c + a' = (1 + r)a + \pi \cdot wh - \mathcal{T}(0, a, 0)$$

$$V_9(\cdot) \equiv 0$$

where π is pension replacement rate

Stationary Equilibrium

- Invariant distribution: Demographic structure $\{\omega_j\}_{j=0}^8$ and distribution of agents over states $\{\mu_j\}_{j=0}^8$ are invariant over time periods
- Households optimize utility and firms maximize profits
- Prices clear markets
- Government balances budget in period to period
- Externalities/incompleteness that government could address:
 - ① **Fiscal externalities of childbearing and childrearing**
 - Private returns \neq social returns (i.e. $\{\omega_j\}_{j=0}^8$ and $\{\mu_j\}_{j=0}^8$)
 - ② **Borrowing constraints** (Daruich 2019, Abbott et al. 2019 ...)

Endogenous Childcare Arrangements

- Standard models where a child costs fixed amount of time, total income y :

$$y = wh \underbrace{(1 - (\underbrace{\chi - \mathcal{S}}_{\text{time cost}}) \cdot n)}_{\text{labor supply}} + n \cdot \mathcal{B}$$

which implies \mathcal{S} is equivalent to a baby bonus $\frac{\mathcal{B}}{wh}$

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 - Subsidized childcare: labor supply \uparrow market care enrollment \uparrow (Baker et al. 2008)
 - Baby bonus: labor supply \downarrow market care enrollment \downarrow (González 2013)

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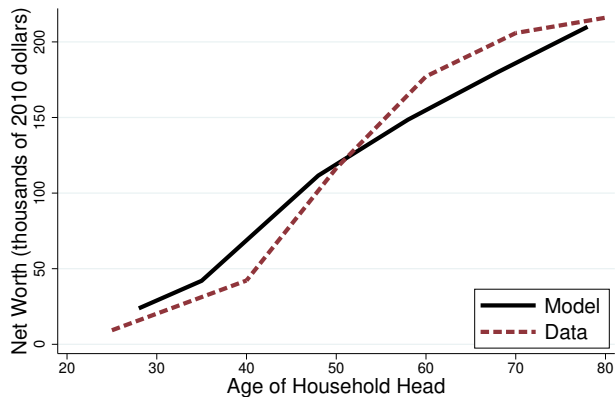
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- Empirical evidence indicates the opposite:
 - Subsidized childcare: labor supply \uparrow market care enrollment \uparrow (Baker et al. 2008)
 - Baby bonus: labor supply \downarrow market care enrollment \downarrow (González 2013)
- Endogenous childcare arrangements:** (in-kind) subsidized childcare induces more labor supply from parents with $m^*(h, a) \leq \mathcal{S}$
- Affects inequalities in wage growth since $h_{j+1} = L_j(\cdot, t_w)$

Model Fit

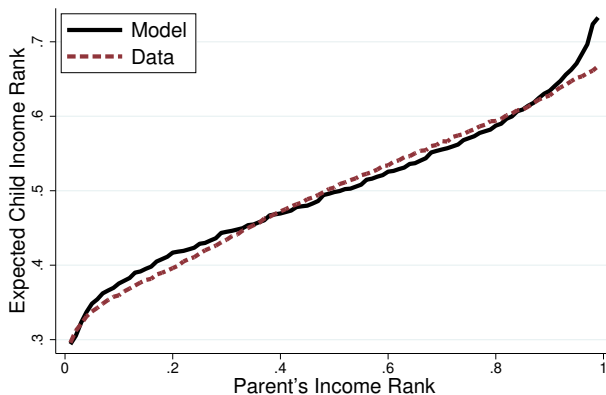
Parameter	Interpretation	Moment	Data	Model
γ	elasticity of substitution	fertility differential	0.12	0.12
ψ	fertility preference	average fertility	1.92	1.92
θ	human capital preference	average investment as % of income	13.4	13.5
ν	transfer preference	average transfer	\$48,381	\$48,400
ι	economies of scale at home	childcare time by # children	1.5	1.5
υ	substitutability of care	average care spending as % of income	16	16
Z	normalizing scalar	median income = 1	N/A	N/A
σ_{ϵ}	ability shock dispersion	Gini of earnings at $j = 2$	0.29	0.29
ρ	intergenerational spillover	intergenerational elasticity of earnings	0.34	0.33
ξ	substitution of education	investment by parents' education	misc.	misc.
κ	input productivity	return on per dollar investment (NPV)	\$1.3	\$1.29
η	learning curvature	income growth by initial decile	0.1	0.09
$\{\zeta\}_{j=2}^5$	learning level	income growth by age	misc.	misc.
σ_z	shock dispersion	Gini of earnings at $j = 6$	0.39	0.39

Net Worth by Age: Model and Data



- Net worth by age of household head from SCF summary tables

Intergenerational Mobility: Model vs Data



- Rank-rank slope = 0.34 (Chetty, Hendren, Kline and Saez 2014)

Child's Skill Production Function Cont'd

Use **RCT evidence** to estimate the productivity of inputs κ :

$$h_k = Z \cdot \epsilon \cdot h^\rho (\mathcal{E}^\xi + e^\xi)^{\kappa/\xi}$$

- García, Heckman, Leaf and Prados (2020)
 - Two US early childhood development programs (ABC, CARE) in 1970s
 - Cost \approx \$13.5k per year for five years - total \$67.5k per child
 - Followed up into adulthood and observe education/income
 - For every dollar invested, children's lifetime labor income increases by **\$1.3**
- Apply similar policy in the model: expand existing \mathcal{E} by \$67.5k
 - **Small scale**: prices and taxes remain unchanged
 - **Target**: children of parents at 10th percentile of earnings
- Comparing labor income changes with program costs gives $\kappa = 0.13$

Costs of Child and Childcare

- OECD equivalence scale:

$$\Lambda(n) = 1.7 + 0.5 \cdot n$$

- **Childcare arrangements:**

$$n \cdot \chi = \left(t_h^{v/\iota} + (n \cdot m)^v \right)^{1/v}$$

Set $\chi = 0.18$ (Folbre 2008). Returns to scale within family calibrated to be $\iota = 0.7$

- Elasticity of substitution: $v = 0.38$ - average share of income spent on childcare by education (SIPP) (Herbst 2018)
- **Price of full-time childcare:** $p_m = \$6,860$ per year for child aged 0-10 (The National Association of Child Care Resource & Referral Agencies 2011)

Fertility Response

- Consider simplified problem for low- h parents, i.e. quality margin not operative

$$\max_{c,n} \quad u(c) + \Psi(n)u(\mathcal{E})$$
$$c + n \cdot \chi = 1$$

- First-order condition for n :

$$\underbrace{\Psi'(n) \cdot u(\mathcal{E})}_{\text{MB of } n} = \underbrace{\lambda \cdot \chi}_{\text{MC of } n}$$

- Plug in $u(c) = \frac{c^{1-\gamma}}{1-\gamma}$, we have

$$\Psi'(n) = (1-\gamma) \cdot \chi \cdot \frac{\lambda}{\mathcal{E}^{1-\gamma}} \implies \Delta \Psi'(n) \propto (1-\gamma) \cdot \Delta \chi$$

Conditional on other parameters, higher $\gamma \implies$ smaller n response

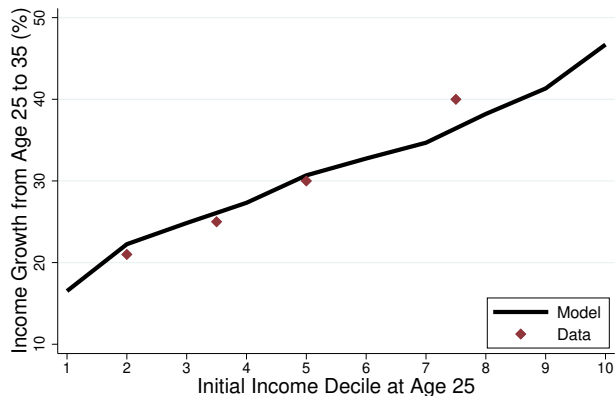
- **Human capital of working adults** evolves:

$$h_{j+1} = L_j(h_j, t_w, z') = \exp(z') [h_j + \zeta_j (h_j \cdot t_w)^\eta]$$

$$\log(z) \sim \mathcal{N}(\mu_z, \sigma_z)$$

- $\{\zeta_j\}_{j=2}^5$ - age-earnings profile (CPS)
- $\eta = 1.22$ - inequality in wage growth (CPS)
- $\mu_z = -0.23$ - 2% skill depreciation
- $\sigma_z = 0.38$ - life-cycle Gini coefficient of earnings (Huggett, Ventura and Yaron 2011)

Inequality in Wage Growth: Model vs Data



- Growth rate of average income from age 25 to 35 by education in CPS-ASEC data (2008-2014)

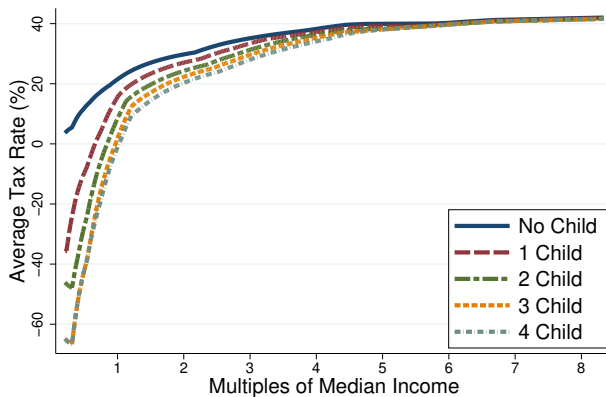
- **Firms' production function:** capital share $\alpha = 0.33$ and 4% capital depreciation
- **Government taxes**
 - **Income taxes:**

$$\mathcal{T}(y, a, n) = y \cdot (1 - \tau_y^n y^{-\lambda_y^n}) + \tau_a r a$$

where $\{\tau_y^n, \lambda_y^n\}_{n=0}^6$ estimated using TAXSIM

- **Tax rates** from McDaniel (2014): $\tau_c = 0.07$ and $\tau_a = 0.27$
- **Pension replacement rate:** $\pi = 40\%$

Income Taxes: Model vs Data



- Child tax benefits (reduction in tax rates) are larger for low-income households

APFD and Completed Fertility Rate

Figure 14: Completed Fertility Rate (CFR)

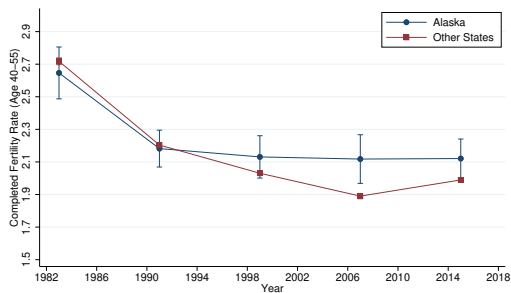
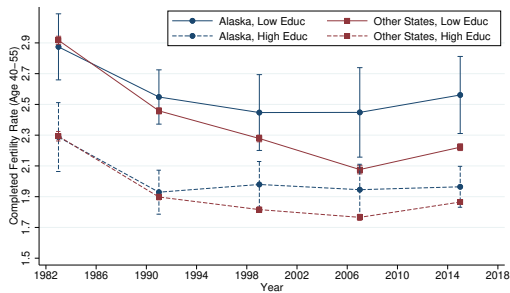


Figure 15: CFR by Education



Australian Baby Bonus

- **A\$3,000 baby bonus**¹ to every child born on or after July 1st 2004
- Risse (2010) and Drago et al. (2011) find:
 - Significant fertility responses and evidence for long-term/quantum effects
 - Baby bonus needed for additional birth around A\$126,000 $\approx 4 \times \text{GDPPC}$
 - Larger fertility responses from low-income households
- Gaitz and Schurer (2017) finds that the baby bonus was **ineffective** in boosting learning, socio-emotional or physical health outcomes of pre-school children

¹More details: (1) Announced on Mar 12th 2004, (2) universal coverage, lump-sum payment, (3) Equivalent to 4 times average weekly earnings, (4) Equivalent to \$2,800 in 2010 USD.

Australian Baby Bonus

- **A\$3,000 baby bonus**¹ to every child born on or after July 1st 2004
- Risse (2010) and Drago et al. (2011) find:
 - Significant fertility responses and evidence for long-term/quantum effects
 - Baby bonus needed for additional birth around A\$126,000 $\approx 4 \times \text{GDPPC}$
 - Larger fertility responses from low-income households
- Gaitz and Schurer (2017) finds that the baby bonus was **ineffective** in boosting learning, socio-emotional or physical health outcomes of pre-school children
- Results from baby bonus counterfactual are consistent with above findings:
 - Significant fertility effects that are larger among low-income households
 - Baby bonus needed for additional birth = $3.5 \times \text{GDPPC}$
 - Child human capital reduces due to quantity-quality trade-off

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[▶ back to results](#)

¹More details: (1) Announced on Mar 12th 2004, (2) universal coverage, lump-sum payment, (3) Equivalent to 4 times average weekly earnings, (4) Equivalent to \$2,800 in 2010 USD.

Spanish Baby Bonus

- **€\$2,500 baby bonus**² to every child born on or after July 1st 2007
- González (2013) finds:
 - Total fertility rate increased
 - Mothers reduced labor supply
 - Fewer children were enrolled in formal childcare

²More details: (1) Announced on July 3rd 2007, (2) universal coverage, lump-sum payment, (3) Equivalent to 4.5 times the monthly gross minimum wage for full-time worker, (4) Equivalent to \$3,500 in 2010 USD.

Spanish Baby Bonus

- **€\$2,500 baby bonus**² to every child born on or after July 1st 2007
- González (2013) finds:
 - Total fertility rate increased
 - Mothers reduced labor supply
 - Fewer children were enrolled in formal childcare
- Results from model are consistent with above findings:
 - Baby bonus needed for additional birth / GDPPC = 3.6 (data) vs 3.5 (model)
 - Parents reduce labor supply as fertility raises → more childcare needs
 - Parents demand less market care as relative costs of home care falls due to economies of scale in home production of childcare

► back to validation

²More details: (1) Announced on July 3rd 2007, (2) universal coverage, lump-sum payment, (3) Equivalent to 4.5 times the monthly gross minimum wage for full-time worker, (4) Equivalent to \$3,500 in 2010 USD.

Georgia's Cherokee Land Lottery in 1832

- Georgia allocated more than 18,000 parcels of land via large-scale lottery in 1832. More than 98% of eligible man participated
- Shock in wealth rather than change in price of child
- Winners were about \$748 wealthier than losers by 1850³
- Bleakley and Ferrie (2016) finds:
 - Parents increase fertility slightly
 - Decedents of winners have no better adult outcomes than the sons of nonwinners

³Equivalent to 1,010 days of earnings for an unskilled laborer in the South

Georgia's Cherokee Land Lottery in 1832

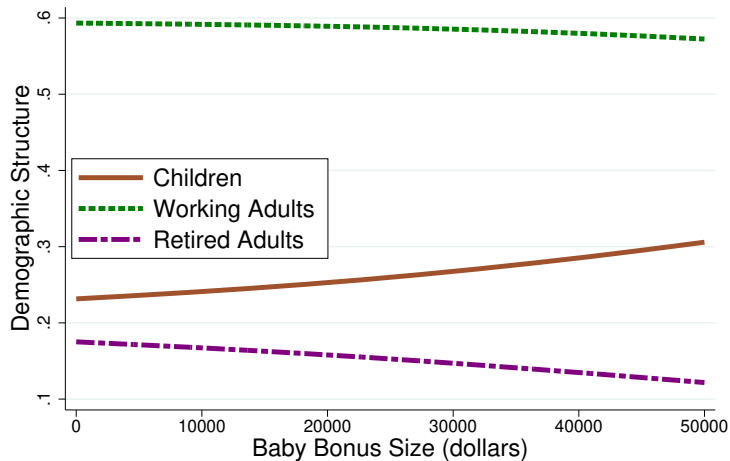
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- Winners were about \$748 wealthier than losers by 1850³
- Bleakley and Ferrie (2016) finds:
 - Parents increase fertility slightly
 - Decedents of winners have no better adult outcomes than the sons of nonwinners
- As skill price increases, Cherokee results provides:
 - ① Upper bound for fertility responses
 - ② Lower bound for child quality responses
- Model predictions consistent with these predictions:

$$n^*(h, a') \leq n^*(h, a) \quad e^*(h, a') \gg e^*(h, a)$$

for fixed h and $a' > a$

³Equivalent to 1,010 days of earnings for an unskilled laborer in the South

Change in Demographic Structure



Distributional Welfare Consequences

Figure 16: Newborns in Transition

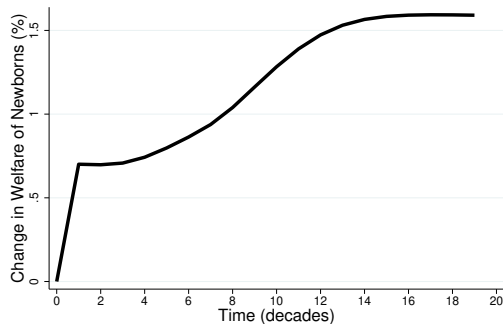
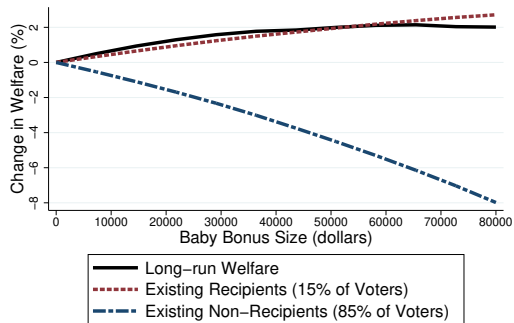


Figure 17: Long-run and Existing Households



Baby Bonus versus Subsidized Childcare

Figure 18: Effects on Income Growth

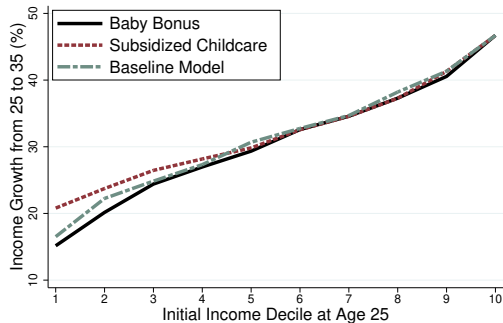
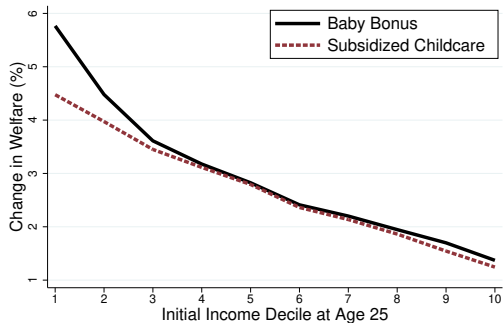


Figure 19: Effects on Welfare



- Subsidized childcare reduces inequality in income growth

Baby Bonus versus Subsidized Childcare

Figure 18: Effects on Income Growth

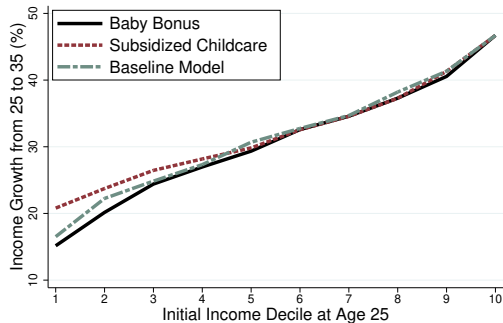
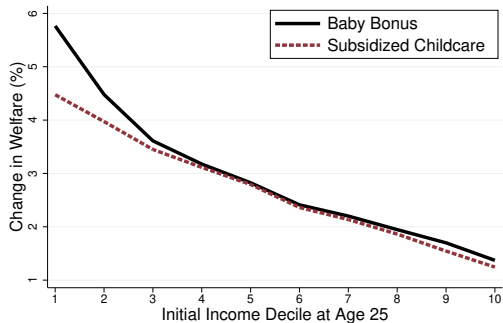


Figure 19: Effects on Welfare



- Subsidized childcare reduces inequality in income growth
- Low-income households prefer cash transfers of the same face value