

# The Fertility Race Between Technology and Social Norms

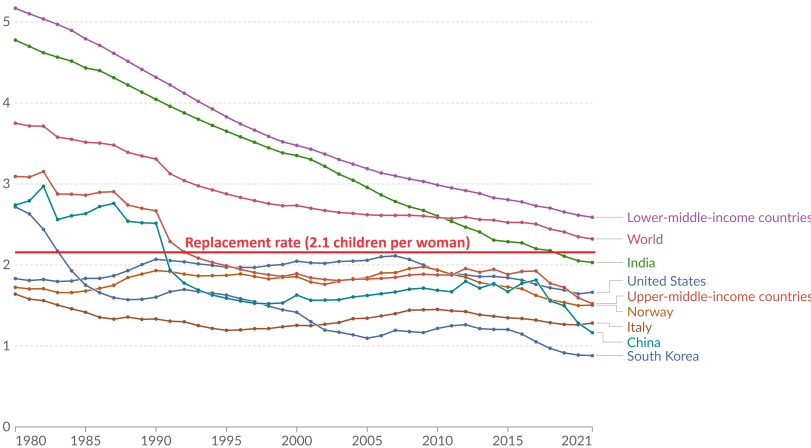
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# Motivation

Fertility rate: children per woman



Data source: United Nations, World Population Prospects (2022)

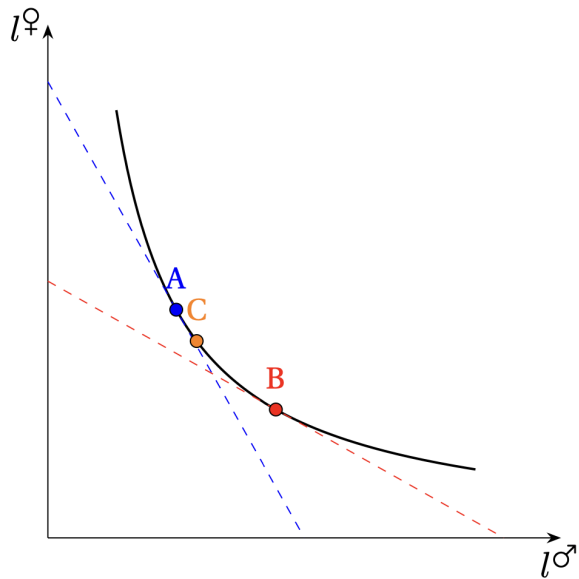
[OurWorldInData.org/fertility-rate](https://OurWorldInData.org/fertility-rate) | CC BY

Note: The total fertility rate is the number of children born to a woman if she were to live to the end of her childbearing years and give birth to children at the current age-specific fertility rates.

# This paper

- A quantitative model of child bargaining
  - Childcare allocation under the influence of social norm
  - Endogenous social norm formation
- A tug-of-war between technological change and social norm
- Document two supporting new facts:
  1. Countries experiencing faster structural change have witnessed more drastic fertility decline
  2. Relationship is stronger in countries with rigid social norms
- Calibrate to the experience of South Korea and conduct counterfactuals

# Mechanism: Social Norm as Endogenous Adjustment Cost



# Key findings

1. In the presence of gender-biased technological change, countries experience steeper fertility decline if there is
  - Intense social pressure, or
  - Reluctance of older cohorts to adapt
2. Slow but eventual fertility recovery as social norm adapt
  - Within-cohort changes – adaptation
  - Between-cohort changes – cohort replacement effects
3. Targeted policies, e.g., subsidies to male childcare, could accelerate the transition and result in larger long-run fertility gains

# Literature

- Goldin (2024)
- Myong et al. (2021)
- Doepke and Kindermann (2019)
- Fernández and Fogli (2009), Fogli and Veldkamp (2013)

Main contribution: new data facts + endogenous social norm

# Roadmap

- Quantitative model
- Supporting facts
- Calibration
- Results
- Conclusion

Model



# Model Setup

- Overlapping generations model with  $J$  periods of life
- Fertility decision at period  $J_f$
- Gender  $g \in \{\text{♀}, \text{♂}\}$  with preference

$$u^g(c^g, n) = c^g + \gamma \cdot \frac{n^{1-\rho} - 1}{1 - \rho} \quad \rho > 0 \quad (1)$$

- Raising each child incurs a time cost  $\phi$ . Parents need to satisfy the childcare provision constraint:

$$n\phi = \left( \beta \cdot (l^{\text{♀}})^{\frac{\sigma-1}{\sigma}} + (1 - \beta) \cdot (l^{\text{♂}})^{\frac{\sigma-1}{\sigma}} \right)^{\frac{\sigma}{\sigma-1}}, \quad \sigma > 1 \quad (2)$$

- Bargaining under limited commitment (Doepke and Kindermann 2019)

# Stage 1: Childcare Decision

- For all  $n$ , the couple solves:

$$\min_{l_t^{\text{♀}}, l_t^{\text{♂}}} w_t^{\text{♀}} l_t^{\text{♀}} + w_t^{\text{♂}} l_t^{\text{♂}} + \lambda \cdot w_t^{\text{♂}} \cdot \left( \frac{l_t^{\text{♀}}}{l_t^{\text{♂}}} - \eta_t \right)^2, \quad (3)$$

- Exogenous wages  $w_t^{\text{♂}}$  and  $w_t^{\text{♀}}$  affected by structural transformation (Ngai and Petrongolo 2017)
- Prevailing social norm  $\eta_t$
- Parameter  $\lambda$  governs social pressure
- Parents can commit to the solution  $l_t^{\text{♀}}(n)$  and  $l_t^{\text{♂}}(n)$

## Stage 2: Fertility Decision

- Only mutually agreed-upon fertility is realized, defined as:

$$n_t = \min\{n_t^{\text{♀}}, n_t^{\text{♂}}\}, \quad (4)$$

- $n_t^g$  is the fertility level that maximizes the ex-post utility

$$n_t^g = \arg \max_n u^g(c_t^g(n), n) \quad g \in \{\text{♀}, \text{♂}\} \quad (5)$$

where  $c_t^g(n)$  comes from the bargaining problem in the third stage

## Stage 3: Consumption Allocation

- With  $n$  children, outside option in the non-cooperative case

$$\bar{u}^g(n) = w_t^g(1 - l_t^g(n)) + \gamma \cdot \frac{n^{1-\rho} - 1}{1 - \rho}, \quad \rho > 0, \quad (6)$$

- Nash bargaining of consumption

$$\max_{c^{\ominus}, c^{\oslash}} \left( u^{\ominus}(c^{\ominus}, n) - \bar{u}^{\ominus}(n) \right)^{1/2} \cdot \left( u^{\oslash}(c^{\oslash}, n) - \bar{u}^{\oslash}(n) \right)^{1/2}, \quad (7)$$

subject to the budget constraint:

$$c^{\ominus} + c^{\oslash} = (1 + \alpha) \cdot [w_t^{\ominus}(1 - l_t^{\ominus}(n)) + w_t^{\oslash}(1 - l_t^{\oslash}(n))], \quad (8)$$

# Social Norm

- The prevailing social norm at time  $t$  is defined as:

$$\eta_t = \sum_{j=1}^{J-J_f} \phi_{J_f+j,t} \cdot \tilde{\eta}_{J_f+j}, \quad \sum_{j=1}^{J-J_f} \phi_{J_f+j,t} = 1, \quad (9)$$

- Weights reflect population shares:

$$\phi_{j,t} = \frac{\pi_{j,t}}{\sum_{k=J_f+1}^J \pi_{k,t}}, \quad (10)$$

where  $\pi_{j,t}$  denotes the population share of the cohort aged  $j$  at time  $t$

# Older Cohorts' Re-evaluation

- Older cohorts form opinions by solving:

$$\tilde{\eta}_{J_f+j} = \arg \min_{\eta} w_t^{\text{♀}} \cdot \eta + w_t^{\text{♂}} + \psi \cdot \left( \eta - \frac{l_{t-j}^{\text{♀}}}{l_{t-j}^{\text{♂}}} \right)^2. \quad (11)$$

- $\frac{l_{t-j}^{\text{♀}}}{l_{t-j}^{\text{♂}}}$  is the childcare practice adopted by these agents  $j$  periods ago
- Parameter  $\psi$  governs the “stubbornness”
- Social norm evolution reflects:
  1. Within-cohort effects from re-evaluation
  2. Between-cohort effects from entry and exit

# Demographic Evolution

- The demographic structure of this economy  $\pi_t$  evolves

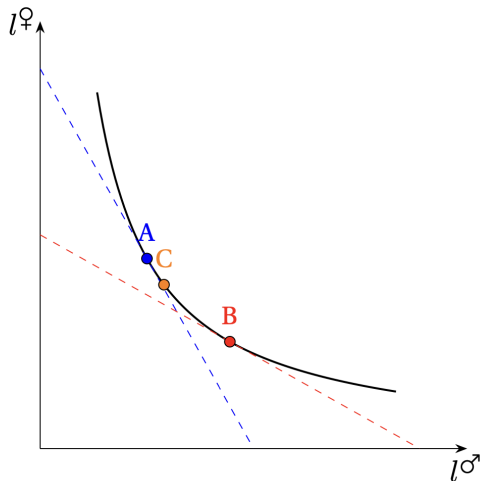
$$\pi_{t+1} = \frac{\mathbf{\Pi}_t \cdot \pi_t}{\|\mathbf{\Pi}_t \cdot \pi_t\|_{L^2}}, \quad (12)$$

where  $\mathbf{\Pi}_t$  is a  $J \times J$  demographic transition matrix

- The element in the first row and  $J_f$ -th column of  $\mathbf{\Pi}_t$  equals  $n_t/2.1$

# Model Predictions

- **Prediction 1:** Economies experiencing faster gender-biased technological changes exhibit more rapid fertility declines.
- **Prediction 2:** The impact of gender-biased technological changes on fertility is stronger in economies with more stringent social norms.





## Supporting Facts

# Data Source

- Fertility data from the United Nations
- Sectoral employment data from the Groningen Growth and Development Centre (GGDC)
- GDP data from the Penn World Table 10.01
- Cultural tightness data from Uz (2019)
  - The dispersion of opinions: in a tight culture, people's values, norms, and behavior are similar to each other because deviations are sanctioned
- Gender attitudes data from the International Social Survey Programme (ISSP) Family and Changing Gender Roles modules
- 23 countries spanning all levels of development

# Variable Definition

- Speed of fertility change for country  $i$ :

$$\text{tfr}_{i,\text{year}} = \alpha_i^{\text{tfr}} + \text{speed\_tfr}_i \times \text{year} + u_i \quad (13)$$

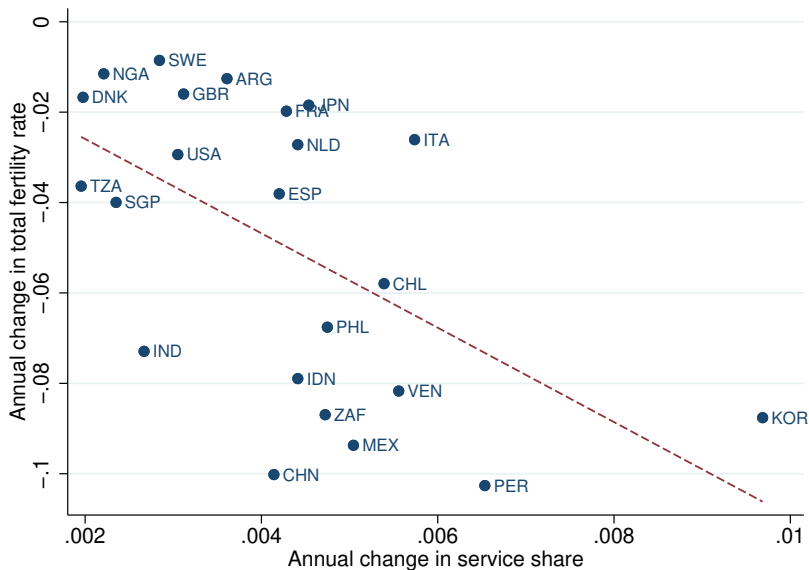
- Speed of structural change for country  $i$ :

$$\text{service share}_{i,\text{year}} = \alpha_i^{\text{ser}} + \text{speed\_ser}_i \times \text{year} + v_i \quad (14)$$

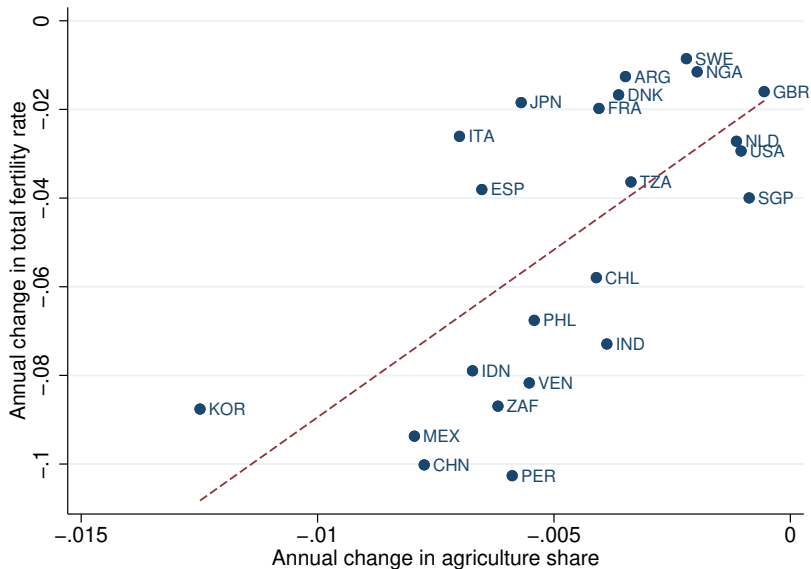
$$\text{agriculture share}_{i,\text{year}} = \alpha_i^{\text{agr}} + \text{speed\_agr}_i \times \text{year} + v_i \quad (15)$$

- Define tight = 1 if tightness score in upper half

# Service Expansion and Fertility Decline



# Agriculture Shrinkage and Fertility Decline



# Regression Results: Cross-Section

- Correlation is driven by countries with tight social norms

|                | Dependent Variable: Fertility Change |                     |                  |                  |                   |                   |                  |                  |
|----------------|--------------------------------------|---------------------|------------------|------------------|-------------------|-------------------|------------------|------------------|
|                | Service                              |                     |                  |                  | Agriculture       |                   |                  |                  |
|                | (1)                                  | (2)                 | (3)              | (4)              | (5)               | (6)               | (7)              | (8)              |
| speed_SC       | -10.44***<br>(3.38)                  | -11.82***<br>(3.78) | -5.48<br>(4.02)  | -6.89<br>(4.27)  | 7.56***<br>(1.90) | 8.39***<br>(2.06) | 5.03**<br>(2.38) | 5.80**<br>(2.41) |
| tight×speed_SC |                                      |                     | -5.11*<br>(2.56) | -5.23*<br>(2.56) |                   |                   | 3.23<br>(1.95)   | 3.51*<br>(1.93)  |
| speed_gdp      |                                      | 0.30<br>(0.35)      |                  | 0.33<br>(0.33)   |                   | 0.32<br>(0.31)    |                  | 0.38<br>(0.30)   |
| Observations   | 23                                   | 23                  | 23               | 23               | 23                | 23                | 23               | 23               |
| R-squared      | 0.31                                 | 0.34                | 0.43             | 0.46             | 0.43              | 0.46              | 0.50             | 0.54             |

# Regression Results: Panel

- Same patterns using panel regressions

|                             | Dependent Variable: Fertility Change |                    |                     |                    |                   |                   |                   |                     |
|-----------------------------|--------------------------------------|--------------------|---------------------|--------------------|-------------------|-------------------|-------------------|---------------------|
|                             | Service                              |                    |                     |                    | Agriculture       |                   |                   |                     |
|                             | (1)                                  | (2)                | (3)                 | (4)                | (5)               | (6)               | (7)               | (8)                 |
| Speed.SC                    | -6.64***<br>(0.70)                   | -7.32***<br>(0.74) | -10.40***<br>(1.57) | -7.23***<br>(0.91) | 7.66***<br>(0.53) | 8.91***<br>(0.62) | 9.58***<br>(0.92) | 9.61**<br>(0.63)    |
| Speed.SC×Norm Change Total  |                                      |                    | 5.35**<br>(2.40)    |                    |                   |                   | -1.94<br>(1.98)   |                     |
| Speed.SC×Norm Change Recent |                                      |                    |                     | 0.59<br>(0.38)     |                   |                   |                   | -0.49<br>(0.31)     |
| Norm Change Recent          |                                      |                    |                     | 0.59<br>(0.38)     |                   |                   |                   | -19.42***<br>(4.09) |
| Controls                    | Yes                                  | Yes                | Yes                 | Yes                | Yes               | Yes               | Yes               | Yes                 |
| Country FEs                 | No                                   | Yes                | Yes                 | Yes                | Yes               | Yes               | Yes               | Yes                 |
| Year Trend                  | No                                   | Yes                | Yes                 | Yes                | Yes               | Yes               | Yes               | Yes                 |
| Observations                | 785                                  | 785                | 785                 | 785                | 785               | 785               | 785               | 785                 |
| R-squared                   | 0.26                                 | 0.38               | 0.39                | 0.39               | 0.35              | 0.45              | 0.45              | 0.47                |

# Calibration



# Calibration Strategy (1)

- The parameters to be calibrated are:

$$\underbrace{J, J_f}_{\text{demographics}}, \quad \underbrace{\gamma, \rho, \psi, \lambda}_{\text{preferences}}, \quad \underbrace{\beta, \phi, \sigma, \alpha}_{\text{technologies}}.$$

- Some parameters exogenously set:
  - Each period as 5 years, set  $J = 16$  (total lifespan of 80 years) and  $J_f = 6$  (childbearing between 25 to 30)
  - $\alpha = 1.2$  following Doepke and Kindermann (2019)
  - $\sigma = 3.0$  following Knowles (2013)
  - $\phi = 0.15$  following de La Croix and Doepke (2003)

## Calibration Strategy (2)

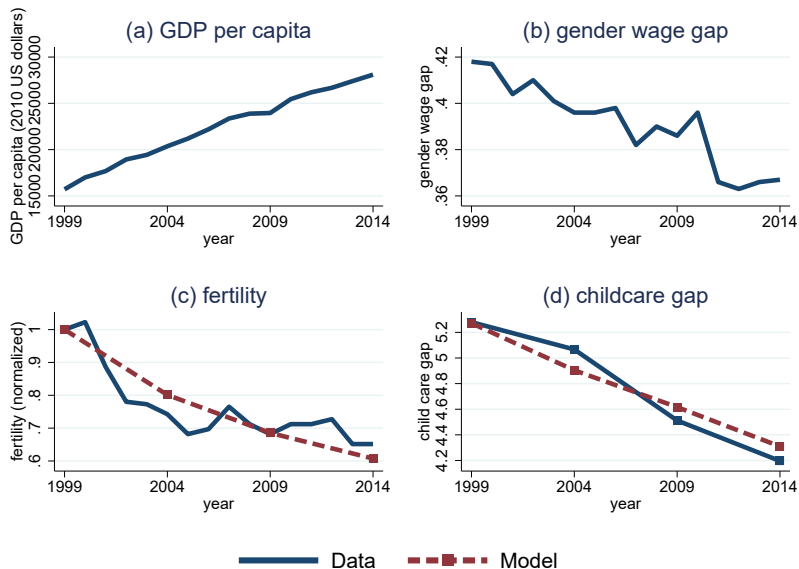
- The fertility weight,  $\gamma$ , is inferred from the initial fertility level
- The fertility curvature,  $\rho$ , governs the trade-off between consumption and fertility, identified by the fertility response to rising opportunity costs
- The relative childcare productivity,  $\beta$ , is determined by the initial gender gap in childcare time.
- The weight of individual's own experience in the formation of opinions, i.e., "stubbornness",  $\psi$ , is calibrated to match the share of between-cohort component in driving social norm changes
- The social pressure parameter,  $\lambda$ , is calibrated to the persistence of gender gaps in childcare over time

# Data Source

Calibrate to match South Korea from 1999 to 2014

- Gendered wage path from the World Bank
- Fertility path from the United Nations
- Childcare time by gender from the Korea Time Use Survey
- Opinion change from the Korean General Social Survey

# Calibration Results (1)



# Calibration Results (2)

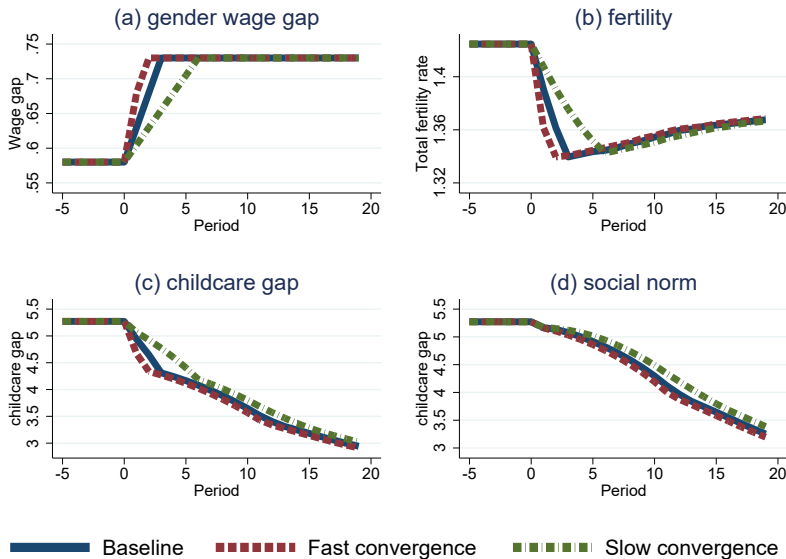
|           | Parameter                  | Value  | Data moment                    | Source                        | Model fit    |
|-----------|----------------------------|--------|--------------------------------|-------------------------------|--------------|
| $\gamma$  | Fertility weight           | 0.24   | $n_{1999} = 1.42$              | United Nations                | 1.42         |
| $\sigma$  | Childcare substitutability | 3.0    |                                | Knowles (2013)                |              |
| $\beta$   | Childcare productivity     | 0.57   | $\eta_{1999} = 5.25$           | Park (2021)                   | 5.25         |
| $\rho$    | Fertility curvature        | 2.4    | $n_{1999} \sim n_{2014}$       | United Nations                | See Figure 3 |
| $\psi$    | Stubbornness               | 3.0    | Within-cohort effects          | KGSS                          | 80%          |
| $\lambda$ | Social pressure            | 0.0006 | $\eta_{1999} \sim \eta_{2014}$ | Park (2021)                   | See Figure 3 |
| $\alpha$  | Economies of scale         | 1.2    |                                | Doepke and Kindermann (2019)  |              |
| $\phi$    | Time costs per child       | 0.15   |                                | de La Croix and Doepke (2003) |              |
| $J$       | Total number of periods    | 16     | 80 years                       | World Health Organization     |              |
| $J_f$     | The fertile period         | 6      | 25 to 30 yo                    | Statista                      |              |

## Calibration Results (3)

|                          | Old tech. & old norm | New tech. & new norm | New tech. & old norm |
|--------------------------|----------------------|----------------------|----------------------|
| $w^{\varphi}/w^{\sigma}$ | 0.58                 | 0.74                 | 0.74                 |
| $\eta$                   | 5.25                 | 2.53                 | 5.25                 |
| $l^{\varphi}/l^{\sigma}$ | 5.25                 | 2.53                 | 4.66                 |
| $n$                      | 1.43                 | 1.37                 | 1.32                 |

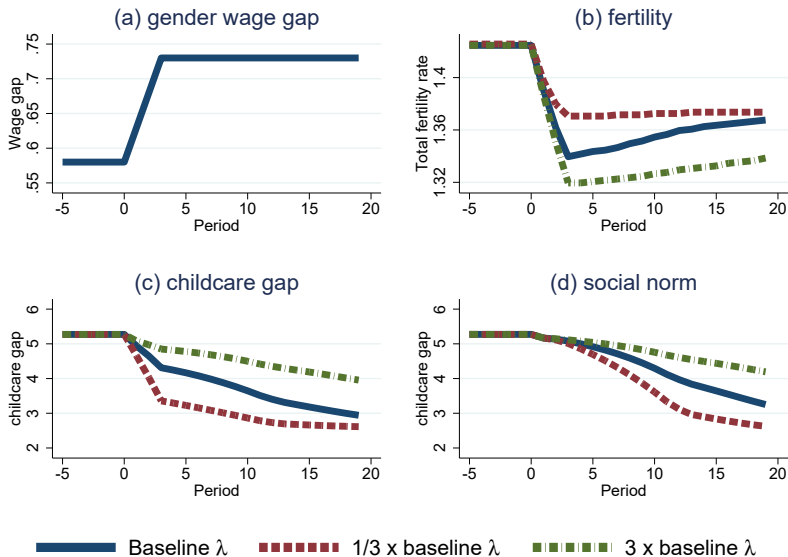
Counterfactual

# Counterfactual 1: The Speed of Technological Change

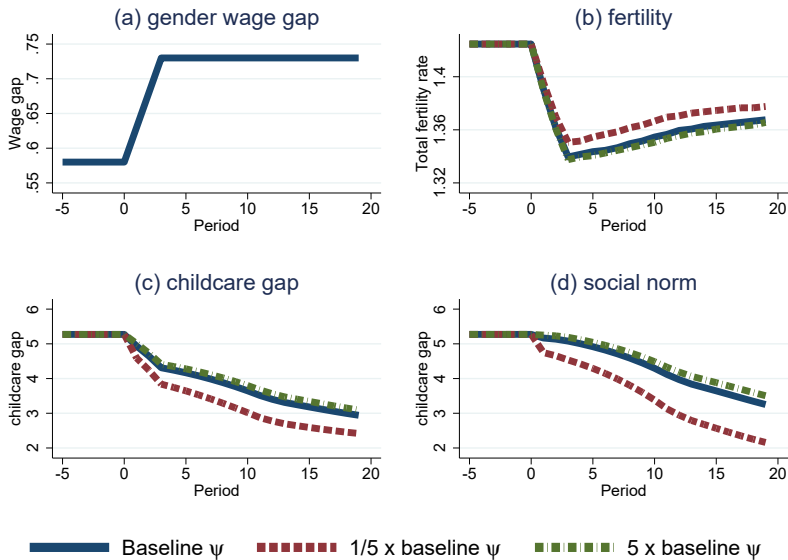




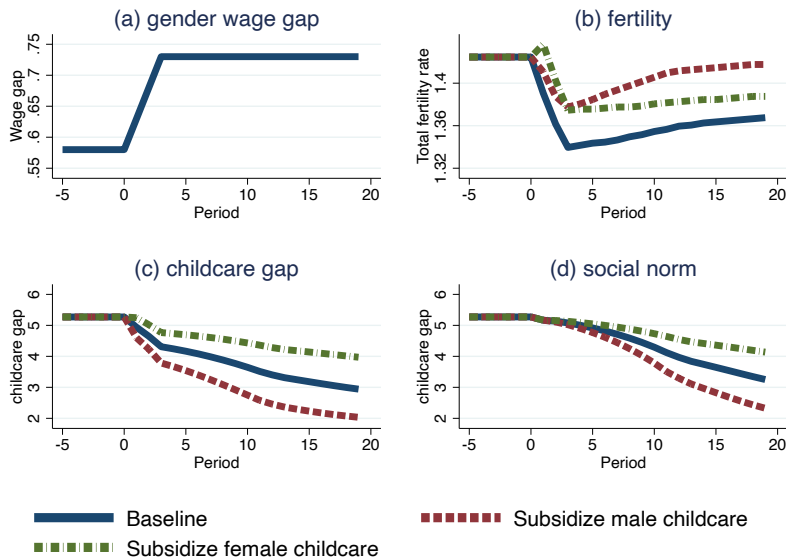
# Counterfactual 2: The Role of Social Pressure



# Counterfactual 3: The Role of Older Cohorts' Reevaluation



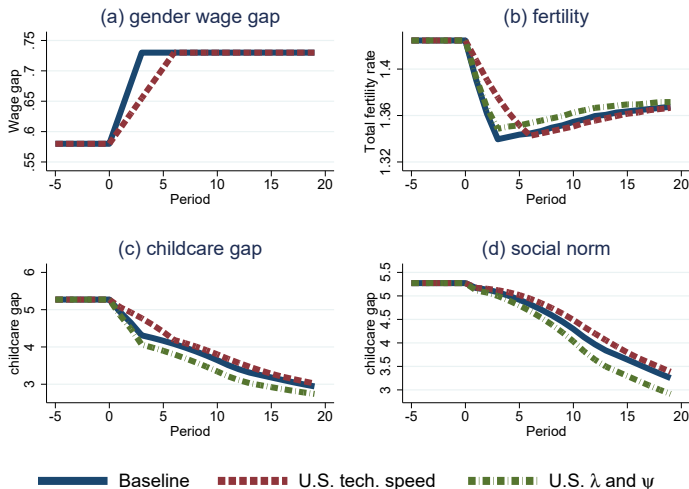
# Counterfactual 4: Gender-Specific Childcare Subsidy



# Counterfactual 5: U.S. Parameters

[details](#)

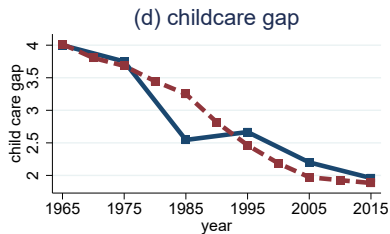
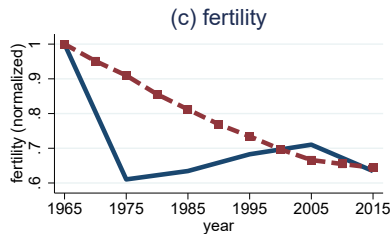
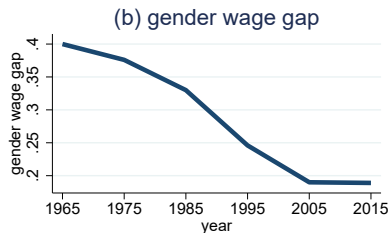
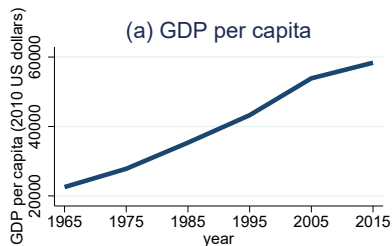
- U.S. has slower structural change, less social pressure, and less stubbornness



# Conclusion

- A quantitative model to study the fertility impacts of gender-biased technological change with endogenous social norm
- Slow but eventual fertility recovery
- Intense social pressure and reluctance to adapt result in steep fertility decline and entrenched traditional norms
- Targeted policies, e.g., subsidies to male childcare, could accelerate the transition and result in larger long-run fertility gains

# Calibration Results - U.S. (1)

[back](#)

— Data    - - - Model

# Calibration Results - U.S. (2)

[back](#)

|           | Parameter                  | Value  | Data moment                    | Source                        | Model fit    |
|-----------|----------------------------|--------|--------------------------------|-------------------------------|--------------|
| $\gamma$  | Fertility weight           | 1.27   | $n_{1965} = 2.90$              | United Nations                | 2.90         |
| $\sigma$  | Childcare substitutability | 3.0    |                                | Knowles (2013)                |              |
| $\beta$   | Childcare productivity     | 0.55   | $\eta_{1965} = 4.0$            | Egerton et al. (2005)         | 4.0          |
| $\rho$    | Fertility curvature        | 2.4    | $n_{1965} \sim n_{2015}$       | United Nations                | See Figure 9 |
| $\psi$    | Stubbornness               | 2.0    | Within-cohort effects          | GSS                           | 30%          |
| $\lambda$ | Social pressure            | 0.0005 | $\eta_{1965} \sim \eta_{2015}$ | Egerton et al. (2005)         | See Figure 9 |
| $\alpha$  | Economies of scale         | 1.2    |                                | Doepke and Kindermann (2019)  |              |
| $\phi$    | Time costs per child       | 0.15   |                                | de La Croix and Doepke (2003) |              |
| $J$       | Total number of periods    | 16     | 80 years                       | World Health Organization     |              |
| $J_f$     | The fertile period         | 6      | 25 to 30 yo                    | Statista                      |              |