

Software Requirements Specification for Solar Water Heating Systems Incorporating Phase Change Material

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1 Reference Material

This section records information for easy reference.

1.1 Table of Units

Throughout this document SI (Système International d’Unités) is employed as the unit system. In addition to the basic units, several derived units are used as described below. For each unit, the symbol is given followed by a description of the unit with the SI name in parentheses.

symbol	unit	SI
m	length	metre
kg	mass	kilogram
s	time	second
°C	temperature	centigrade
J	energy	Joule
W	power	Watt ($W = J s^{-1}$)

1.2 Table of Symbols

The table that follows summarizes the symbols used in this document along with their units. The choice of symbols was made to be consistent with the heat transfer literature and with existing documentation for solar water heating systems. The symbols are listed in alphabetical order.

symbol	unit	description
A_C	m^2	coil surface area
A_{in}	m^2	surface area over which heat is transferred in
A_P	m^2	phase change material surface area
A_{out}	m^2	surface area over which heat is transferred out
C	$J/(kg\ ^\circ C)$	specific heat capacity
C^L	$J/(kg\ ^\circ C)$	specific heat capacity of a liquid

C_P^L	J/(kg °C)	specific heat capacity of PCM during latent heating phase
C^S	J/(kg °C)	specific heat capacity of a solid
C_P^S	J/(kg °C)	specific heat capacity of PCM during sensible heating phase
C_V	J/(kg °C)	specific heat capacity of a vapour
C_W	J/(kg °C)	specific heat capacity of water
D	m	diameter of tank
E	J	sensible heat energy
E_P	J	heat energy in the PCM
$E_{P_{\text{melt}}}^{\text{init}}$	J	heat energy in the PCM at the instant when melting begins
E_W	J	heat energy in the water
g	W/m ²	volumetric heat generation per unit volume
h	W/(m ² °C)	convective heat transfer coefficient
h_C	W/(m ² °C)	convective heat transfer coefficient between coil and water
H_f	J/kg	specific latent heat of fusion
h_P	W/(m ² °C)	convective heat transfer coefficient between water and PCM
L	m	length of tank
m	kg	mass
m_P	kg	mass of phase change material
m_W	kg	mass of water
$\hat{\mathbf{n}}$	unitless	unit outward normal vector for a surface
q	W/(m ² °C)	heat flux
Q	J	latent heat energy
\mathbf{q}	W/m ²	thermal flux vector
q_C	W/m ²	heat flux from coil
q_{in}	W/m ²	heat flux in
q_P	W/m ²	heat flux into phase change material
Q_P	J	latent heat energy added to PCM
q_{out}	W/m ²	heat flux out
t	s	time
t_{melt}	s	time when melting of the PCM begins
T	°C	temperature
T_{boil}	°C	temperature at boiling point
T_C	°C	temperature of coil
T_{env}	°C	temperature of environment
t_{final}	s	final time

T_{init}	°C	initial temperature
T_{melt}	°C	temperature at melting point
$t_{\text{melt}}^{\text{init}}$	s	time at which melting of PCM begins.
$t_{\text{melt}}^{\text{final}}$	s	time at which melting of PCM ends.
T_{melt}^P	°C	temperature at melting point for PCM
T_W	°C	temperature of water
T_P	°C	temperature of phase change material
ΔT	°C	temperature difference
V	m ³	volume
V_P	m ³	volume of PCM
V_{tank}	m ³	volume of the cylindrical tank
V_W	m ³	volume of water
ρ	kg/m ³	density, mass per unit volume
ρ_P	kg/m ³	density of PCM
ρ_W	kg/m ³	density of water
τ	s	dummy variable for integration over time
ϕ	unitless	melt fraction

1.3 Abbreviations and Acronyms

symbol	description
A	Assumption
DD	Data Definition
GD	General Definition
GS	Goal Statement
IM	Instance Model
LC	Likely Change
ODE	Ordinary Differential Equation
PCM	Phase Change Material
PS	Physical System Description
R	Requirement
SRS	Software Requirements Specification
SWHS	Solar Water Heating System
T	Theoretical Model

2 Introduction

Due to the increasing cost, diminishing availability, and negative environmental impact of fossil fuels, there is a higher demand for renewable energy sources and energy storage technology. Solar water heating systems incorporating Phase Change Material (PCM) use a renewable energy source and provide a novel way of storing energy. Solar water heating systems with PCM improve over the traditional solar heating systems because of their smaller size. The smaller size is possible because of the ability of PCM to store thermal energy as latent heat, which allows higher thermal energy storage capacity per unit weight.

The following section provides an overview of the Software Requirements Specification (SRS) for a solar water heating system that incorporates PCM. The developed program will be referred to as Solar Water Heating System (SWHS). This section explains the purpose of this document, the scope of the system, the organization of the document and the characteristics of the intended readers.

2.1 Purpose of Document

The main purpose of this document is to describe the modelling of solar water heating systems incorporating PCM. The goals and theoretical models used in the SWHS code are provided, with an emphasis on explicitly identifying assumptions and unambiguous definitions. This document is intended to be used as a reference to provide ad hoc access to all information necessary to understand and verify the model. The SRS is abstract because the contents say *what* problem is being solved, but do not say *how* to solve it.

This document will be used as a starting point for subsequent development phases, including writing the design specification and the software verification and validation plan. The design document will show how the requirements are to be realized, including decisions on the numerical algorithms and programming environment. The verification and validation plan will show the steps that will be used to increase confidence in the software documentation and the implementation. Although the SRS fits in a series of documents that follow the so-called waterfall model, the actual development process is not constrained in any way. Even when the process is not waterfall, as Parnas and Clements [5] point out, the most logical way to present the documentation is still to “fake” a rational design process.

2.2 Scope of Requirements

The scope of the requirements is limited to thermal analysis of a single solar water heating tank incorporating PCM. Given the appropriate inputs, the code for SWHS is intended to predict the temperature and energy histories for the water and the PCM. This entire document is written assuming that the substances inside the heating tank are water and PCM.

2.3 Organization of Document

The organization of this document follows the template for an SRS for scientific computing software proposed by [3] and [6]. The presentation follows the standard pattern of presenting goals, theories, definitions, and assumptions. For readers that would like a more bottom up approach, they can start reading the instance models in Section 4.2.5 and trace back to find any additional information they require. The instance models provide the Ordinary Differential Equations (ODEs) and algebraic equations that model the solar water heating system with PCM. SWHS solves these ODEs.

The goal statements are refined to the theoretical models, and theoretical models to the instance models. The instance models (Section 4.2.5) to be solved are referred to as IM1 to IM4.

3 General System Description

This section provides general information about the system, identifies the interfaces between the system and its environment, and describes the user characteristics and the system constraints.

3.1 User Characteristics

The end user of SWHS should have an understanding of undergraduate Level 1 Calculus and Physics.

3.2 System Constraints

There are no system constraints.

4 Specific System Description

This section first presents the problem description, which gives a high-level view of the problem to be solved. This is followed by the solution characteristics specification, which presents the assumptions, theories, definitions and finally the instance models (ODEs) that model the solar water heating tank with PCM.

4.1 Problem Description

SWHS is a computer program developed to investigate the effect of employing PCM within a solar water heating tank.

4.1.1 Terminology and Definitions

This subsection provides a list of terms that are used in the subsequent sections and their meaning, with the purpose of reducing ambiguity and making it easier to correctly understand the requirements:

- Heat Flux: The rate of heat energy transfer per unit area.
- Phase Change Material (PCM): A substance that uses phase changes (melting) to absorb or release large amounts of heat at a constant temperature.
- Specific Heat: heat capacity per unit mass.
- Thermal Conduction: the transfer of heat energy through a substance.
- Transient: Changing with time.

4.1.2 Physical System Description

The physical system of SWHS, as shown in Figure 1, includes the following elements:

PS1: Tank containing water.

PS2: Heating coil at bottom of tank. (q_C represents the heat flux from the coil into the water.)

4.1.3 Goal Statements

Given the temperature of the coil, initial conditions for the temperature of the water and the PCM, and material properties, the goal statements are:

GS1: predict the water temperature over time;

4.2 Solution Characteristics Specification

The instance models (ODEs) that govern SWHS are presented in Subsection 4.2.5. The information to understand the meaning of the instance models and their derivation is also presented, so that the instance models can be verified.

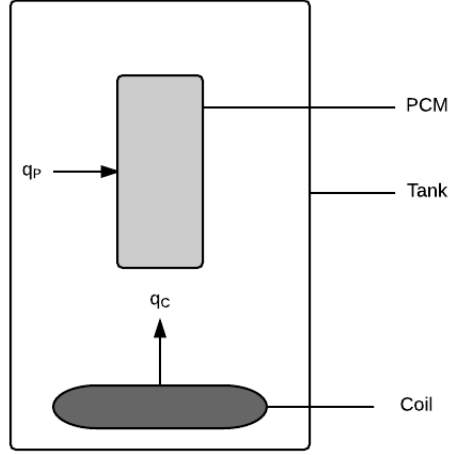


Figure 1: Solar water heating tank, with heat flux from coil and to the PCM of q_C and q_P , respectively

4.2.1 Assumptions

This section simplifies the original problem and helps in developing the theoretical model by filling in the missing information for the physical system. The numbers given in the square brackets refer to the theoretical model [T], general definition [GD], data definition [DD], instance model [IM], or likely change [LC], in which the respective assumption is used.

- A1: The only form of energy that is relevant for this problem is thermal energy. All other forms of energy, such as mechanical energy, are assumed to be negligible [T1].
- A2: All heat transfer coefficients are constant over time [GD1].
- A3: The water in the tank is fully mixed, so the temperature is the same throughout the entire tank [GD2, DD??].
- A4: The PCM has the same temperature throughout [GD2, DD??, LC1].
- A5: Density of the water and PCM have not spatial variation; that is, they are each constant over their entire volume [GD2].
- A6: Specific heat capacity of the water and PCM have no spatial variation; that is, they are each constant over their entire volume [GD2].
- A7: Newton's law of convective cooling applies between the coil and the water [DD1].

- A8: The temperature of the heating coil is constant over time [DD1, LC2].
- A9: The temperature of the heating coil does not vary along its length [DD1, LC3].
- A10: Newton's law of convective cooling applies between the water and the PCM [DD??].
- A11: The model only accounts for charging of the tank, not discharging. The temperature of the water and PCM can only increase, or remain constant; they do not decrease. This implies that the initial temperature (A12) is less than (or equal) to the temperature of the coil [IM1, LC4].
- A12: The initial temperature of the water and the PCM is the same [IM1, IM2, LC5].
- A13: The simulation will start with the PCM in solid form [IM2, IM4].
- A14: The operating temperature range of the system is such that the water is always in liquid form. That is, the temperature will not drop below the melting point of water, or rise above its boiling point [IM1, IM3].
- A15: The tank is perfectly insulated so that there is no heat loss from the tank [IM1, LC6].
- A16: No internal heat is generated by either the water or the PCM; therefore, the volumetric heat generation is zero [IM1, IM2].
- A17: The volume change of the PCM due to melting is negligible [IM2].
- A18: The PCM is in either in a liquid or solid state, but not a gas [IM2, IM4].

4.2.2 Theoretical Models

This section focuses on the general equations and laws that SWHS is based on.

Number	T1
Label	Conservation of thermal energy
Equation	$-\nabla \cdot \mathbf{q} + g = \rho C \frac{\partial T}{\partial t}$
Description	The above equation gives the conservation of energy for time varying heat transfer in a material of specific heat capacity C and density ρ , where \mathbf{q} is the thermal flux vector, g is the volumetric heat generation, T is the temperature, t is time, and ∇ is the gradient operator. For this equation to apply, other forms of energy, such as mechanical energy, as assumed to be negligible in the system (A1).
Source	http://www.efunda.com/formulae/heat_transfer/conduction/overview_cond.cfm
Ref. By	GD2

4.2.3 General Definitions

This section collects the laws and equations that will be used in deriving the data definitions, which in turn are used to build the instance models.

Number	GD1
Label	Newton's law of cooling
SI Units	W m^{-2}
Equation	$q(t) = h\Delta T(t)$
Description	<p>Newton's law of cooling describes convective cooling from a surface. The law is stated as: the rate of heat loss from a body is proportional to the difference in temperatures between the body and its surroundings.</p> <p>$q(t)$ is the thermal flux (W m^{-2}).</p> <p>h is the heat transfer coefficient, assumed independent of T (A2) ($\text{W m}^{-2} \text{ }^{\circ}\text{C}^{-1}$).</p> <p>$\Delta T(t) = T(t) - T_{\text{env}}(t)$ is the time-dependent thermal gradient between the environment and the object ($^{\circ}\text{C}$).</p>
Source	[2, p. 8]
Ref. By	DD1, DD??

Number	GD2
Label	Simplified rate of change of temperature
Equation	$mC\frac{dT}{dt} = q_{\text{in}}A_{\text{in}} - q_{\text{out}}A_{\text{out}} + gV$
Description	<p>The basic equation governing the rate of change of temperature, for a given volume V, with time.</p> <p>m is the mass (kg).</p> <p>C is the specific heat capacity ($\text{J kg}^{-1} \text{ } ^\circ\text{C}^{-1}$).</p> <p>$T$ is the temperature ($^\circ\text{C}$) and t is the time (s).</p> <p>q_{in} and q_{out} are the in and out heat transfer rates, respectively (W m^{-2}).</p> <p>A_{in} and A_{out} are the surface areas over which the heat is being transferred in and out, respectively (m^2).</p> <p>g is the volumetric heat generated (W m^{-3}).</p> <p>V is the volume (m^3).</p>
Ref. By	IM1, IM2

Detailed derivation of simplified rate of change of temperature

Integrating (T1) over a volume (V), we have

$$-\int_V \nabla \mathbf{q} dV + \int_V g dV = \int_V \rho C \frac{\partial T}{\partial t} dV.$$

Applying Gauss's Divergence theorem to the first term over the surface S of the volume, with \mathbf{q} as the thermal flux vector for the surface, and $\hat{\mathbf{n}}$ is a unit outward normal for the surface,

$$-\int_S \mathbf{q} \cdot \hat{\mathbf{n}} dS + \int_V g dV = \int_V \rho C \frac{\partial T}{\partial t} dV. \quad (1)$$

We consider an arbitrary volume. The volumetric heat generation is assumed constant. Then (1) can be written as

$$q_{\text{in}}A_{\text{in}} - q_{\text{out}}A_{\text{out}} + gV = \int_V \rho C \frac{\partial T}{\partial t} dV,$$

where q_{in} , q_{out} , A_{in} , and A_{out} are explained in GD2. Assuming ρ , C and T are constant over the volume, which is true in our case by assumption (A3), (A4), (A5), and (A6), we have

$$\rho CV \frac{dT}{dt} = q_{\text{in}} A_{\text{in}} - q_{\text{out}} A_{\text{out}} + gV. \quad (2)$$

Using the fact that $\rho = m/V$, (2) can be written as

$$mC \frac{dT}{dt} = q_{\text{in}} A_{\text{in}} - q_{\text{out}} A_{\text{out}} + gV.$$

4.2.4 Data Definitions

This section collects and defines all the data needed to build the instance models. The dimension of each quantity is also given.

Number	DD1
Label	Heat flux out of coil
Symbol	q_C
SI Units	W m^{-2}
Equation	$q_C(t) = h_C(T_C - T_W(t))$, over area A_C
Description	T_C is the temperature of the coil. T_W is the temperature of the water. The heat flux out of the coil, q_C , is found by assuming that Newton's Law of Cooling applies (A7). This law (GD1) is used on the surface of the coil, which has area A_C and heat transfer coefficient h_C . This equation assumes that the temperature of the coil is constant over time (A8) and that it does not vary along the length of the coil (A9).
Sources	[4]
Ref. By	IM1

4.2.5 Instance Models

This section transforms the problem defined in the Section 4.1 into one which is expressed in mathematical terms. It uses concrete symbols defined in Section 4.2.4 to replace the abstract symbols in the models identified in the Sections 4.2.2 and 4.2.3.

The goals GS1 to GS?? are solved by IM1 to IM4. The solutions for IM1 and IM2 are coupled since the solution for T_W and T_P depend on one another. IM3 can be solved once IM1 has been solved. The solution of IM2 and IM4 are also coupled, since the temperature and energy of the PCM depend on the phase change.

Number	IM1
Label	Energy balance on water to find T_W
Input	$m_W, C_W, h_C, A_C, t_{\text{final}}, T_C, T_{\text{init}}$ The input is constrained so that $T_{\text{init}} \leq T_C$ (A11)
Output	$T_W(t), 0 \leq t \leq t_{\text{final}}$, such that $\frac{dT_W}{dt} = \frac{1}{\tau_W}(T_C - T_W(t))$, $T_W(0) = T_{\text{init}}$ (A12)
Description	T_W is the water temperature ($^{\circ}\text{C}$). T_C is the coil temperature ($^{\circ}\text{C}$). $\tau_W = \frac{m_W C_W}{h_C A_C}$ is a constant (s). The above equation applies as long as the water is in liquid form, $0 < T_W < 100^{\circ}\text{C}$, where 0°C and 100°C are the melting and boiling points of water, respectively (A14).
Sources	Original SRS with PCM removed
Ref. By	IM2

Derivation of the energy balance on water

To find the rate of change of T_W , we look at the energy balance on water. The volume being considered is the volume of water in the tank V_W , which has mass m_W and specific heat capacity, C_W . Heat transfer occurs in the water from the coil as q_C , over area A_C . No heat transfer occurs to the outside of the tank, since it has been assumed to be perfectly insulated (A15). Assuming no internal heat is generated (A16), $g = 0$. Therefore, the equation for GD2 can be written as:

$$m_W C_W \frac{dT_W}{dt} = q_C A_C.$$

Using DD1 and DD?? for q_C and q_P respectively, this can be written as

$$m_W C_W \frac{dT_W}{dt} = h_C A_C (T_C - T_W). \quad (3)$$

Dividing (3) by $m_W C_W$, we obtain

$$\frac{dT_W}{dt} = \frac{h_C A_C}{m_W C_W} (T_C - T_W). \quad (4)$$

Setting $\tau_W = \frac{m_W C_W}{h_C A_C}$, Equation (4) can be written in its final form as:

$$\frac{dT_W}{dt} = \frac{1}{\tau_W}(T_C - T_W).$$

Number	IM2
Label	Energy balance on PCM to find T_P
Input	$m_P, C_P^S, C_P^L, h_P, A_P, t_{\text{final}}, T_{\text{init}}, T_{\text{melt}}^P, T_W(t)$ from IM1 The input is constrained so that $T_{\text{init}} < T_{\text{melt}}^P$ (A13)
Output	$T_P(t), 0 \leq t \leq t_{\text{final}}$, with initial conditions, $T_W(0) = T_P(0) = T_{\text{init}}$ (A12), and $T_W(t)$ from IM1, such that the following governing ODE is satisfied. The specific ODE depends on T_P as follows: $\frac{dT_P}{dt} = \begin{cases} \frac{dT_P}{dt} = \frac{1}{\tau_P^S}(T_W(t) - T_P(t)) & \text{if } T_P < T_{\text{melt}}^P \\ \frac{dT_P}{dt} = \frac{1}{\tau_P^L}(T_W(t) - T_P(t)) & \text{if } T_P > T_{\text{melt}}^P \\ 0 & \text{if } T_P = T_{\text{melt}}^P \text{ and } 0 < \phi < 1 \end{cases}$ <p>The temperature remains constant at T_{melt}^P, even with the heating (or cooling), until the phase change has occurred for all of the material; that is as long as $0 < \phi < 1$. ϕ (from DD??) is determined as part of the heat energy in the PCM, as given in IM4</p> <p>$t_{\text{melt}}^{\text{init}}$, the temperature at which melting begins.</p> <p>$t_{\text{melt}}^{\text{final}}$, the temperature at which melting end.</p>
Description	T_W is water temperature ($^{\circ}\text{C}$). T_P is the PCM temperature ($^{\circ}\text{C}$). $\tau_P^S = \frac{m_P C_P^S}{h_P A_P}$ is a constant (s). $\tau_P^L = \frac{m_P C_P^L}{h_P A_P}$ is a constant (s).
Sources	[4]
Ref. By	IM1, IM4

Detailed derivation of the energy balance on the PCM during sensible heating phase

To find the rate of change of T_P , we look at the energy balance on the PCM. The volume being considered is the volume of the PCM, V_P . The derivation that follows is initially for the solid PCM. The PCM in the tank has mass m_P and specific heat capacity C_P^S . Heat input from the water to the PCM is q_P over area A_P . There is no heat flux output. Assuming

no internal heat generated (A16), $g = 0$, the equation for GD2 can be written as:

$$m_P C_P^S \frac{dT_P}{dt} = q_P A_P$$

Using DD?? for q_P , this equation can be written as

$$m_P C_P^S \frac{dT_P}{dt} = h_P A_P (T_W - T_P).$$

Dividing by $m_P C_P^S$ we obtain,

$$\frac{dT_P}{dt} = \frac{h_P A_P}{m_P C_P^S} (T_W - T_P).$$

Setting $\tau_P^S = \frac{m_P C_P^S}{h_P A_P}$, this can be written as

$$\frac{dT_P}{dt} = \frac{1}{\tau_P^S} (T_W - T_P). \quad (5)$$

Equation (5) applies for the solid PCM. In the case where all the PCM is melted, the same derivation applies, except that C_P^S is replaced by C_P^L , and thus τ_P^S is replaced by τ_P^L . Although a small change in surface area would be expected with melting, this is not included, since the volume change of the PCM with melting is assumed to be negligible (A17).

In the case where $T_P = T_{\text{melt}}^P$ and not all of the PCM is melted, the temperature does not change. Therefore, in this case $\frac{dT_P}{dt} = 0$.

This derivation does not consider the boiling of the PCM, as the PCM is assumed to either be in a solid or liquid state (A18).

Number	IM3
Label	Heat energy in the water
Input	$C_W, m_W, T_{\text{init}}, T_W(t)$
Output	$E_W(t), 0 \leq t \leq t_{\text{final}}$, such that $E_W(t) = C_W m_W (T_W(t) - T_{\text{init}})$
Description	The above equation is derived using T??. E_W is the change in thermal energy of the liquid water relative to the energy at the initial temperature (T_{init}). C_W is the specific heat capacity of liquid water and m_W is the mass of the water. The change in temperature is the difference between the temperature at time t, T_W , and the initial temperature, T_{init} , this equation applies as long as $0 < T_W < 100^\circ\text{C}$ (A14).
Sources	[4]
Ref. By	–

Number	IM4
Label	Heat energy in the PCM
Input	$C_P^S, C_P^L, H_f, T_P(t), T_{\text{init}}, m_P, T_{\text{melt}}^P, h_P, A_P, t_{\text{melt}}^{\text{init}}$ (from IM2), t_{final} The input is constrained so that $T_{\text{init}} < T_{\text{melt}}^P$ (A13)
Output	$E_P(t), 0 \leq t \leq t_{\text{final}}$, such that $E_P = \begin{cases} C_P^S m_P (T_P(t) - T_{\text{init}}) & \text{if } T_P < T_{\text{melt}}^P \\ E_{P_{\text{melt}}}^{\text{init}} + H_f m_p + C_P^L m_P (T_P(t) - T_{\text{melt}}^P) & \text{if } T_P > T_{\text{melt}}^P \\ E_{P_{\text{melt}}}^{\text{init}} + Q_P(t) & \text{if } T_P = T_{\text{melt}}^P, (0 < \phi < 1) \end{cases}$ $E_{P_{\text{melt}}}^{\text{init}} = C_P^S m_p (T_{\text{melt}}^P - T_{\text{init}})$ Here $Q_P(t)$ is found with the initial condition that $Q_P(t_{\text{melt}}^{\text{init}}) = 0$ and $\frac{dQ_P(t)}{dt} = q_P(t) A_P = h_P A_P (T_W(t) - T_{\text{melt}}^P),$ with the heat flux q_P from DD??, over area A_P , $\phi = \frac{Q_P}{H_f m_P}$ (DD??)
Description	<p>The above equation is derived using T?? and T??. E_P is the change in thermal energy of the PCM relative to the energy at the initial temperature (T_{init}).</p> <p>E_P for the solid PCM is found using T?? for sensible heating, with the specific heat capacity of the solid PCM, C_P^S, and the change in the PCM temperature from the initial temperature.</p> <p>E_P for the melted PCM ($T_P > T_{\text{melt}}^P$) is found using T?? for sensible heating of the liquid PCM, plus the energy when melting starts, plus the energy required to melt all of the PCM. The energy when melting starts is $E_{P_{\text{melt}}}^{\text{init}}$. The energy required to melt all of the PCM is $H_f m_p$ (DD??). The specific heat capacity of the liquid PCM is C_P^L and the change in temperature is $T_P - T_{\text{melt}}^P$.</p> <p>E_P during melting of the PCM is found using the energy required at the instant melting of the PCM begins, $E_{P_{\text{melt}}}^{\text{init}}$, plus the latent heat energy added to the PCM, Q_P, since the time when melting began ($t_{\text{melt}}^{\text{init}}$).</p> <p>The heat energy for boiling of the PCM is not detailed, since the PCM is assumed to either be in a solid or liquid state (A18).</p>
Sources	[4]
Ref. By	IM2

4.2.6 Data Constraints

Table 1 and 3 show the data constraints on the input and output variables, respectively. The column physical constraints gives the physical limitations on the range of values that can be taken by the variable. The column for software constraints restricts the range of inputs to reasonable values. The constraints are conservative, to give the user of the model the flexibility to experiment with unusual situations. The column of typical values is intended to provide a feel for a common scenario. The uncertainty column provides an estimate of the confidence with which the physical quantities can be measured. This information would be part of the input if one were performing an uncertainty quantification exercise.

The specification parameters in Table 1 are listed in Table 2.

Table 1: Input Variables

Var	Physical Constraints	Software Constraints	Typical Value	Uncertainty
L	$L > 0$	$L_{\min} \leq L \leq L_{\max}$	1.5 m	10%
D	$D > 0$	$\frac{D}{L_{\min}} \leq \frac{D}{L} \leq \frac{D}{L_{\max}}$	0.412 m	10%
V_P	$V_P > 0$ (*) $V_P < V_{\text{tank}}(D, L)$	$V_P \geq \text{minfract} \cdot V_{\text{tank}}(D, L)$	0.05 m ³	10%
A_P	$A_P > 0$ (*)	$V_P \leq A_P \leq \frac{2}{h_{\min}} V_P$ (#)	1.2 m ²	10%
ρ_P	$\rho_P > 0$	$\rho_P^{\min} < \rho_P < \rho_P^{\max}$	1007 kg/m ³	10%
T_{melt}^P	$0 < T_{\text{melt}}^P < T_C$		44.2 °C	10%
C_P^S	$C_P^S > 0$	$C_{P\min}^S < C_P^S < C_{P\max}^S$	1760 J/(kg °C)	10%
C_P^L	$C_P^L > 0$	$C_{P\min}^L < C_P^L < C_{P\max}^L$	2270 J/(kg °C)	10%
H_f	$H_f > 0$	$H_f^{\min} < H_f < H_f^{\max}$	211600 J/kg	10%
A_C	$A_C > 0$ (*)	$A_C \leq A_C^{\max}$	0.12 m ²	10%
T_C	$0 < T_C < 100$ (+)		50 °C	10%
ρ_W	$\rho_W > 0$	$\rho_W^{\min} < \rho_W \leq \rho_W^{\max}$	1000 kg/m ³	10%
C_W	$C_W > 0$	$C_W^{\min} < C_W < C_W^{\max}$	4186 J/(kg °C)	10%
h_C	$h_C > 0$	$h_C^{\min} \leq h_C \leq h_C^{\max}$	1000 W/(m ² °C)	10%
h_P	$h_P > 0$	$h_P^{\min} \leq h_P \leq h_P^{\max}$	1000 W/(m ² °C)	10%
T_{init}	$0 < T_{\text{init}} < T_{\text{melt}}$ (+)		40 °C	10%
t_{final}	$t_{\text{final}} > 0$	$t_{\text{final}} < t_{\text{final}}^{\max}$ (**)	50000 s	10%

(*) These quantities cannot be equal to zero, or there will be a divide by zero in the model.

- (+) These quantities cannot be zero, or there would be freezing (A14).
- (#) The constraints on the surface area are calculated by considering the surface area to volume ratio. The assumption is that the lowest ratio is 1 and the highest possible is $2/h_{\min}$, where h_{\min} is the thickness of a “sheet” of PCM. A thin sheet has the greatest surface area to volume ratio.
- (**) The constraint on the maximum time at the end of the simulation is the total number of seconds in one day.

Table 2: Specification Parameter Values

Var	Value
L_{\min}	0.1 m
L_{\max}	50 m
$\frac{D}{L}_{\min}$	0.002
$\frac{D}{L}_{\max}$	200
minfrac	10^{-6}
h_{\min}	0.001 m
ρ_P^{\min}	500 kg m^{-3}
ρ_P^{\max}	20000 kg m^{-3}
$C_{P\min}^S$	$100 \text{ J kg}^{-1} \text{ }^\circ\text{C}^{-1}$
$C_{P\max}^S$	$4000 \text{ J kg}^{-1} \text{ }^\circ\text{C}^{-1}$
$C_{P\min}^L$	$100 \text{ J kg}^{-1} \text{ }^\circ\text{C}^{-1}$
$C_{P\max}^L$	$5000 \text{ J kg}^{-1} \text{ }^\circ\text{C}^{-1}$
A_C^{\max}	$\pi(\frac{D}{2})^2 \text{ m}^2$
ρ_W^{\min}	950 kg m^{-3}
ρ_W^{\max}	1000 kg m^{-3}
C_W^{\min}	$4170 \text{ J kg}^{-1} \text{ }^\circ\text{C}^{-1}$
C_W^{\max}	$4210 \text{ J kg}^{-1} \text{ }^\circ\text{C}^{-1}$
h_C^{\min}	$10 \text{ W m}^{-2} \text{ }^\circ\text{C}^{-1}$
h_C^{\max}	$10000 \text{ W m}^{-2} \text{ }^\circ\text{C}^{-1}$
h_P^{\min}	$10 \text{ W m}^{-2} \text{ }^\circ\text{C}^{-1}$
h_P^{\max}	$10000 \text{ W m}^{-2} \text{ }^\circ\text{C}^{-1}$
t_{final}^{\max}	86400 s

Table 3: Output Variables

Var	Physical Constraints
T_W	$T_{\text{init}} \leq T_W \leq T_C$ (by A11)
T_P	$T_{\text{init}} \leq T_P \leq T_C$ (by A11)
E_W	$E_W \geq 0$
E_P	$E_P \geq 0$

5 Requirements

This section provides the functional requirements, the business tasks that the software is expected to complete, and the nonfunctional requirements, the qualities that the software is expected to exhibit.

5.1 Functional Requirements

R1: Input the following quantities, which define the tank parameters, material properties and initial conditions:

symbol	unit	description
L	m	length of tank
D	m	diameter of tank
V_P	m ³	volume of PCM
A_P	m ²	phase change material surface area
ρ_P	kg/m ³	density of PCM
T_{melt}^P	°C	temperature at melting point for PCM
C_P^S	J/(kg °C)	specific heat capacity of PCM during sensible heating phase
C_P^L	J/(kg °C)	specific heat capacity of PCM during latent heating phase
H_f	J/kg	specific latent heat of fusion
A_C	m ²	coil surface area
T_C	°C	temperature of coil
ρ_W	kg/m ³	density of water
C_W	J/(kg °C)	specific heat capacity of water
h_C	W/(m ² °C)	convective heat transfer coefficient between coil and water
h_P	W/(m ² °C)	convective heat transfer coefficient between water and PCM

T_{init}	°C	initial temperature of water and PCM
t_{final}	s	time at end of simulation

R2: Use the inputs in R1 to find the mass needed for IM1 to IM4, as follows:

$$m_W = V_W \rho_W = (V_{\text{tank}} - V_P) \rho_W = (\pi(D/2)^2 L - V_P) \rho_W$$

$$m_P = V_P \rho_P,$$

where V_W is the volume of water in the tank and V_{tank} is the volume inside of the cylindrical tank.

R3: Verify that the inputs satisfy the required physical constraints shown in Table 1.

R4: Output the input quantities and derived quantities in the following list: the quantities from R1, the masses from R2, τ_W (from IM1), η (from IM1), τ_P^S (from IM2) and τ_P^L (from IM2).

R5: Calculate and output the temperature of the water ($T_W(t)$) over the simulation time (from IM1).

R6: Calculate and output the temperature of the PCM ($T_P(t)$) over the simulation time (from IM2).

R7: Calculate and output the energy in the water ($E_W(t)$) over the simulation time (from IM3).

R8: Calculate and output the energy in the PCM ($E_P(t)$) over the simulation time (from IM4).

R9: Calculate and output the time at which the PCM begins to melt $t_{\text{melt}}^{\text{init}}$ (from IM2).

R10: Calculate and output the time at which the PCM stops melting $t_{\text{melt}}^{\text{final}}$ (from IM2).

5.2 Nonfunctional Requirements

Given the small size, and relative simplicity, of this problem, performance is not a priority. Any reasonable implementation will be very quick and use minimal storage. Rather than performance, the priority nonfunctional requirements are correctness, verifiability, understandability, reusability and maintainability.

6 Likely Changes

- LC1: A4 - PCM is actually a poor thermal conductor, so the assumption of uniform PCM temperature is not likely.
- LC2: A8 - The temperature of the heating coil will change over the course of the day, depending on the energy received from the sun.
- LC3: A9 - The temperature of the water in the coil will actually change along its length as the water cools.
- LC4: A11 - The model currently only accounts for charging of the tank. A more complete model would also account for discharging of the tank.
- LC5: A12 - To add more flexibility to the simulation, the initial temperature of the water and the PCM could be allowed to have different values.
- LC6: A15 - Any real tank cannot be perfectly insulated and will lose heat.

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