Software Requirements Specification for GlassBR

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1 Reference Material

This section records information for easy reference.

1.1 Table of Units

The unit system used throughout is SI (Système International d'Unités). In addition to the basic units, several derived units are also used. For each unit, the Table of Units lists the symbol, a description and the SI name.

| Symbol | Description | SI Name |
|--------------|-------------|----------|
| kg | mass | kilogram |
| \mathbf{m} | length | metre |
| N | force | newton |
| Pa | pressure | pascal |
| S | time | second |

Table 1: Table of Units

1.2 Table of Symbols

The symbols used in this document are summarized in the Table of Symbols along with their units. The symbols are listed in alphabetical order.

| Symbol | Description | Units |
|----------------|------------------------------------------------------------|-------|
| \overline{a} | Plate length (long dimension) | m |
| AR | Aspect ratio | _ |
| $AR_{ m max}$ | Maximum aspect ratio | _ |
| B | Risk of failure | _ |
| b | Plate width (short dimension) | m |
| capacity | Capacity or load resistance | Pa |
| $d_{ m max}$ | Maximum value for one of the dimensions of the glass plate | m |
| d_{\min} | Minimum value for one of the dimensions of the glass plate | m |
| E | Modulus of elasticity of glass | Pa |
| g | Glass type | _ |
| GTF | Glass type factor | _ |
| h | Minimum thickness | m |
| interpY | InterpY | _ |
| interpZ | InterpZ | _ |
| is-safeLoad | Load resistance safety requirement | _ |

| Symbol | Description | Units |
|---------------------------|-----------------------------------------------------------------------------|------------------------------------------|
| is-safeLR | 3 second load equivalent resistance safety requirement | |
| is-safePb | Probability of glass breakage safety requirement | _ |
| is-safe Prob | Probability of failure safety requirement | - |
| J | Stress distribution factor (Function) | _ |
| $J_{ m max}$ | Maximum value for the stress distribution factor | _ |
| $J_{ m min}$ | Minimum value for the stress distribution factor | _ |
| $J_{ m tol}$ | Stress distribution factor (Function) based on Pbtol | _ |
| k | Surface flaw parameter | $\frac{\mathrm{m}^{12}}{\mathrm{N}^7}$ |
| LDF | Load duration factor | _ |
| Load | Applied load (demand) or pressure | Pa |
| LR | Load resistance | Pa |
| LSF | Load share factor | _ |
| m | Surface flaw parameter | $\frac{\mathrm{m}^{12}}{\mathrm{N}^{7}}$ |
| NFL | Non-factored load | Pa |
| $P_{ m b}$ | Probability of breakage | _ |
| $P_{ m btol}$ | Tolerable probability of breakage | _ |
| $P_{ m f}$ | Probability of failure | _ |
| $P_{ m ftol}$ | Tolerable probability of failure | - |
| q | Applied load (demand) | Pa |
| \widehat{q} | Dimensionless load | _ |
| $\widehat{q}_{	ext{tol}}$ | Tolerable load | _ |
| SD | Stand off distance | m |
| SD_{max} | Maximum stand off distance permissible for input | \mathbf{m} |
| SD_{\min} | Minimum stand off distance permissible for input | m |
| $SD_{ m x}$ | Stand off distance $(x$ -component) | \mathbf{m} |
| $SD_{ m y}$ | Stand off distance $(y$ -component) | \mathbf{m} |
| $SD_{ m z}$ | Stand off distance $(z$ -component) | m |
| t | Nominal thickness | mm |
| | $t \in \{2.5, 2.7, 3.0, 4.0, 5.0, 6.0, 8.0, 10.0, 12.0, 16.0, 19.0, 22.0\}$ | |
| $t_{ m d}$ | Duration of load | S |
| TNT | TNT equivalent factor | _ |
| w | Charge weight | kg |
| $w_{ m max}$ | Maximum permissible input charge weight | kg |
| $w_{ m min}$ | Minimum permissible input charge weight | kg |

| Symbol | Description | Units |
|-----------|----------------------------|-------|
| w_{TNT} | Equivalent TNT charge mass | kg |

Table 2: Table of Symbols

1.3 Abbreviations and Acronyms

| Abbreviation | Full Form |
|---------------------|-------------------------------------|
| A | Assumption |
| AN | Annealed |
| AR | Aspect Ratio |
| DD | Data Definition |
| FT | Fully Tempered |
| GS | Goal Statement |
| GTF | Glass Type Factor |
| HS | Heat Strengthened |
| IG | Insulating Glass |
| IM | Instance Model |
| LC | Likely Change |
| LG | Laminated Glass |
| LR | Load Resistance |
| LSF | Load Share Factor |
| N/A | Not Applicable |
| NFL | Non-Factored Load |
| PS | Physical System Description |
| R | Requirement |
| SD | Stand Off Distance |
| SRS | Software Requirements Specification |
| TM | Theoretical Model |
| UC | Unlikely Change |
| Uncert. | Typical Uncertainty |

Table 3: Abbreviations and Acronyms

2 Introduction

Software is helpful to efficiently and correctly predict the blast risk involved with the glass slab. The blast under consideration is any kind of man-made explosion. The software, herein called GlassBR, aims to predict the blast risk involved with the glass slab using an intuitive interface.

The following section provides an overview of the Software Requirements Specification (SRS) for GlassBR. This section explains the purpose of this document, the scope of the requirements, the characteristics of the intended reader, and the organization of the document.

2.1 Purpose of Document

The primary purpose of this document is to record the requirements of the GlassBR. Goals, assumptions, theoretical models, definitions, and other model derivation information are specified, allowing the reader to fully understand and verify the purpose and scientific basis of GlassBR. With the exception of system constraints, this SRS will remain abstract, describing what problem is being solved, but not how to solve it.

This document will be used as a starting point for subsequent development phases, including writing the design specification and the software verification and validation plan. The design document will show how the requirements are to be realized, including decisions on the numerical algorithms and programming environment. The verification and validation plan will show the steps that will be used to increase confidence in the software documentation and the implementation. Although the SRS fits in a series of documents that follow the so-called waterfall model, the actual development process is not constrained in any way. Even when the waterfall model is not followed, as Parnas and Clements point out [7], the most logical way to present the documentation is still to "fake" a rational design process.

2.2 Scope of Requirements

The scope of the requirements includes determining the safety of a glass slab under a blast loading following the ASTM standard ([1]).

2.3 Characteristics of Intended Reader

Reviewers of this documentation should have an understanding of second year calculus, structural mechanics, glass breakage, blast risk, computer applications in civil engineering, and applicable standards for constructions using glass from [1], [3], and [2] in references. The users of GlassBR can have a lower level of expertise, as explained in Sec:User Characteristics.

2.4 Organization of Document

The organization of this document follows the template for an SRS for scientific computing software proposed by [6] and [9], with some aspects taken from Volere template 16 [8]. The presentation follows the standard pattern of presenting goals, theories, definitions, and assumptions. For readers that would like a more bottom up approach, they can start reading the data definitions and trace back to find any additional information they require.



Figure 1: System Context

The goal statements are refined to the theoretical models and the theoretical models to the instance models. The data definitions are used to support the definitions of the different models.

3 Stakeholders

This section describes the stakeholders: the people who have an interest in the product.

3.1 The Client

The client for GlassBR is a company named Entuitive. It is developed by Dr. Manuel Campidelli. The client has the final say on acceptance of the product.

3.2 The Customer

The customers are the end user of GlassBR.

4 General System Description

This section provides general information about the system. It identifies the interfaces between the system and its environment, describes the user characteristics, and lists the system constraints.

4.1 System Context

Fig:sysCtxDiag shows the system context. A circle represents an external entity outside the software, the user in this case. A rectangle represents the software system itself (GlassBR). Arrows are used to show the data flow between the system and its environment.

The interaction between the product and the user is through a user interface. The responsibilities of the user and the system are as follows:

• User Responsibilities

- Provide the input data related to the glass slab and blast type, ensuring no errors in the data entry.
- Ensure that consistent units are used for input variables.
- Ensure required software assumptions are appropriate for any particular problem input to the software.

• GlassBR Responsibilities

- Detect data type mismatch, such as a string of characters input instead of a floating point number.
- Determine if the inputs satisfy the required physical and software constraints.
- Predict whether the glass slab is safe or not.

4.2 User Characteristics

- The end user of GlassBR is expected to have completed at least the equivalent of the second year of an undergraduate degree in civil engineering or structural engineering.
- The end user is expected to have an understanding of theory behind glass breakage and blast risk.
- The end user is expected to have basic computer literacy to handle the software.

4.3 System Constraints

There are no system constraints.

5 Specific System Description

This section first presents the problem description, which gives a high-level view of the problem to be solved. This is followed by the solution characteristics specification, which presents the assumptions, theories, and definitions that are used.

5.1 Problem Description

A system is needed to efficiently and correctly predict whether a glass slab can withstand a blast under given conditions.

5.1.1 Terminology and Definitions

This subsection provides a list of terms that are used in the subsequent sections and their meaning, with the purpose of reducing ambiguity and making it easier to correctly understand the requirements. All of the terms are extracted from [1].

- 1. Glass breakage The fracture or breakage of any lite or ply in monolithic, laminated, or insulating glass.
- 2. Lateral Perpendicular to the glass surface.
- 3. Lite Pieces of glass that are cut, prepared, and used to create the window or door.
- 4. Specifying authority The design professional responsible for interpreting applicable regulations of authorities having jurisdiction and considering appropriate site specific factors to determine the appropriate values used to calculate the specified design load, and furnishing other information required to perform this practice.
- 5. Blast resistant glazing Glazing that provides protection against air blast pressure generated by explosions.
- 6. Equivalent TNT charge mass Mass of TNT placed on the ground in a hemisphere that represents the design explosive threat.

7. Glass Type:

- Annealed (AN) A flat, monolithic, glass lite which has uniform thickness where the residual surface stresses are almost zero, as defined in [2].
- Fully tempered (FT) A flat, monolithic, glass lite of uniform thickness that has been subjected to a special heat treatment process where the residual surface compression is not less than 69 MPa (10 000 psi) or the edge compression not less than 67 MPa (9700 psi), as defined in [3].
- Heat strengthened (HS) A flat, monolithic, glass lite of uniform thickness that has been subjected to a special heat treatment process where the residual surface compression is not less than 24 MPa (3500psi) or greater than 52 MPa (7500 psi), as defined in [3].
- 8. Applied load (demand) or pressure A uniformly distributed lateral pressure.
 - Load resistance (LR) The uniform lateral load that a glass construction can sustain based upon a given probability of breakage and load duration as defined in [1, (pp. 1 and 53)].
 - Non-factored load (NFL) Three second duration uniform load associated with a probability of breakage less than or equal to 8 lites per 1000 for monolithic AN glass.

- Glass weight load The dead load component of the glass weight.
- Short duration load Any load lasting 3 seconds or less.
- Specified design load The magnitude in Pa (psf), type (for example, wind or snow) and duration of the load given by the specifying authority.
- Long duration load Any load lasting approximately 30 days.
- 9. Stand off distance (SD) The distance from the glazing surface to the centroid of a hemispherical high explosive charge. It is represented by the coordinates (SD_x, SD_y, SD_z) .
- 10. Load share factor (LSF) A multiplying factor derived from the load sharing between the double glazing, of equal or different thicknesses and types (including the layered behaviour of LG under long duration loads), in a sealed IG unit.
- 11. Glass type factor (GTF) A multiplying factor for adjusting the LR of different glass type, that is, AN, FT, or HS, in monolithic glass, LG (Laminated Glass), or IG (Insulating Glass) constructions.
- 12. Aspect ratio (AR) The ratio of the long dimension of the glass to the short dimension of the glass. For glass supported on four sides, the aspect ratio is always equal to or greater than 1.0. For glass supported on three sides, the ratio of the length of one of the supported edges perpendicular to the free edge, to the length of the free edge, is equal to or greater than 0.5.
- 13. Probability of breakage $(P_{\rm b})$ The fraction of glass lites or plies that would break at the first occurrence of a specified load and duration, typically expressed in lites per 1000 ([2]).

5.1.2 Physical System Description

The physical system of GlassBR, as shown in the Fig:physSystImage below, includes the following elements:

PS1: The glass slab.

PS2: The point of explosion. Where the bomb, or any kind of man-made explosion, is located. The stand off distance is the distance between the point of explosion and the glass.

5.1.3 Goal Statements

Given the dimensions of the glass plane, the glass type, the characteristics of the explosion, and the tolerable probability of breakage, the goal statements are:

hstands-Explosion: Analyze and predict whether the glass slab under consideration will be able to withstand the explosion of a certain degree which is calculated based on user input.



Figure 2: The physical system

5.2 Solution Characteristics Specification

The instance models that govern GlassBR are presented in the Instance Model Section. The information to understand the meaning of the instance models and their derivation is also presented, so that the instance models can be verified.

5.2.1 Assumptions

This section simplifies the original problem and helps in developing the theoretical models by filling in the missing information for the physical system. The assumptions refine the scope by providing more detail.

glassType: The standard E1300-09a for calculation applies only to monolithic, laminated, or insulating glass constructions of rectangular shape with continuous lateral support along one, two, three, or four edges. This practice assumes that: (1) the supported glass edges for two, three and four-sided support conditions are simply supported and free to slip in plane; (2) glass supported on two sides acts as a simply supported beam; and (3) glass supported on one side acts as a cantilever.

glassCondition: Following [1, (pg. 1)], this practice does not apply to any form of wired, patterned, etched, sandblasted, drilled, notched, or grooved glass with surface and edge treatments that alter the glass strength. (RefBy: UC:Accommodate-Altered-Glass.)

explainScenario: This system only considers the external explosion scenario for its calculations. (RefBy: LC:Calculate-Internal-Blask-Risk.)

standard Values: The values provided in Sec:Values of Auxiliary Constants are assumed for the duration of load $(t_{\rm d})$, and the material properties of m, k, and E. (RefBy: LC:Variable-Values-of-m,k,E, DD:sdfTol, DD:nFL, DD:load DurFactor, DD:dimlessLoad, and A:ldfConstant.)

glassLite: Glass under consideration is assumed to be a single lite; hence, the value of LSF is equal to 1 for all calculations in GlassBR. (RefBy: LC:Accomodate-More-than-Single-Lite.)

bundaryConditions: Boundary conditions for the glass slab are assumed to be 4-sided support for calculations. (RefBy: LC:Accomodate-More-Boundary-Conditions.)

responseType: The response type considered in GlassBR is flexural. (RefBy: LC:Consider-More-than-Flexure-Glass.)

ldfConstant: With reference to A:standardValues, the value of load duration factor (LDF) is a constant in GlassBR. (RefBy: LC:Variable-Values-of-m,k,E and DD:loadDurFactor.)

5.2.2 Theoretical Models

This section focuses on the general equations and laws that GlassBR is based on.

| Refname | TM:isSafeProb |
|-------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Label | Safety Probability |
| Equation | $is-safeProb = P_{\rm f} < P_{\rm ftol}$ |
| Description | $is-safe Prob$ is the probability of failure safety requirement (Unitless) $P_{\rm f}$ is the probability of failure (Unitless) $P_{\rm ftol}$ is the tolerable probability of failure (Unitless) |
| Notes | If $is-safeProb$, the structure is considered safe. |
| Source | [1] |
| RefBy | FR:Check-Glass-Safety |

| Refname | TM:isSafeLoad |
|-------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Label | Safety Load |
| Equation | is-safeLoad = capacity > Load |
| Description | is-safeLoad is the load resistance safety requirement (Unitless) $capacity$ is the capacity or load resistance (Pa) $Load$ is the applied load (demand) or pressure (Pa) |
| Notes | If $is-safeLoad$, the structure is considered safe. |
| Source | [1] |
| RefBy | FR:Check-Glass-Safety |

5.2.3 General Definitions

There are no general definitions.

5.2.4 Data Definitions

This section collects and defines all the data needed to build the instance models.

| Refname | DD:riskFun |
|-------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Label | Risk of failure |
| Symbol | B |
| Units | Unitless |
| Equation | $B = \frac{k}{\left(ab\right)^{m-1}} \left(Eh^2\right)^m LDFe^J$ |
| Description | B is the risk of failure (Unitless) k is the surface flaw parameter $\left(\frac{m^{12}}{N^7}\right)$ a is the plate length (long dimension) (m) b is the plate width (short dimension) (m) m is the surface flaw parameter $\left(\frac{m^{12}}{N^7}\right)$ E is the modulus of elasticity of glass (Pa) h is the minimum thickness (m) LDF is the load duration factor (Unitless) J is the stress distribution factor (Function) (Unitless) |
| Notes | a and b are the dimensions of the plate, where $(a \ge b)$. b is defined in DD:minThick and is based on the nominal thicknesses. b is defined in DD:loadDurFactor. b is defined in DD:stressDistFac. |
| Source | [1], [4, (Eqs. 4-5)], and [5, (Eq. 14)] |
| RefBy | DD:probOfBreak |

| Refname | DD:minThick |
|-------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Label | Minimum thickness |
| Symbol | h |
| Units | m |
| Equation | $h = \frac{1}{1000} \begin{cases} 2.16, & t = 2.5 \\ 2.59, & t = 2.7 \\ 2.92, & t = 3.0 \\ 3.78, & t = 4.0 \\ 4.57, & t = 5.0 \\ 5.56, & t = 6.0 \\ 7.42, & t = 8.0 \\ 9.02, & t = 10.0 \\ 11.91, & t = 12.0 \\ 15.09, & t = 16.0 \\ 18.26, & t = 19.0 \\ 21.44, & t = 22.0 \end{cases}$ |
| Description | $h \text{ is the minimum thickness (m)} \\ t \text{ is the nominal thickness} \\ t \in \{2.5, 2.7, 3.0, 4.0, 5.0, 6.0, 8.0, 10.0, 12.0, 16.0, 19.0, 22.0\} \text{ (mm)}$ |
| Notes | t is a function that maps from the nominal thickness (h) to the minimum thickness. |
| Source | [1] |
| RefBy | DD:sdfTol, DD:riskFun, DD:nl@L, and DD:dimlessLoad |

| Refname | DD:loadDurFactor |
|-------------|-------------------------------------------------------------------------------------------------------------------------------------------------------|
| Label | Load duration factor |
| Symbol | LDF |
| Units | Unitless |
| Equation | $LDF = \left(\frac{t_{\rm d}}{60}\right)^{\frac{m}{16}}$ |
| Description | LDF is the load duration factor (Unitless) $t_{\rm d}$ is the duration of load (s) m is the surface flaw parameter $(\frac{\rm m^{12}}{\rm N^7})$ |
| Notes | $t_{\rm d}$ and m come from A:standard Values. LDF is assumed to be constant (from A:ldf Constant). |
| Source | [1] |
| RefBy | DD:sdfTol and DD:riskFun |

| Refname | DD:stressDistFac |
|-------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Label | Stress distribution factor (Function) |
| Symbol | J |
| Units | Unitless |
| Equation | $J = interpZ (\text{``SDF.txt''}, AR, \hat{q})$ |
| Description | J is the stress distribution factor (Function) (Unitless) $interpZ$ is the interpZ (Unitless) AR is the aspect ratio (Unitless) \hat{q} is the dimensionless load (Unitless) |
| Notes | J is obtained by interpolating from data shown in Fig:dimlessloadVSaspect. AR is defined in DD:aspectRatio. \hat{q} is defined in DD:dimlessLoad. |
| Source | [1] |
| RefBy | DD:riskFun |

| Refname | DD:nFL |
|-------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Label | Non-factored load |
| Symbol | NFL |
| Units | Pa |
| Equation | $NFL = rac{\widehat{q}_{ m tol}Eh^4}{\left(ab ight)^2}$ |
| Description | NFL is the non-factored load (Pa) \hat{q}_{tol} is the tolerable load (Unitless) E is the modulus of elasticity of glass (Pa) h is the minimum thickness (m) a is the plate length (long dimension) (m) b is the plate width (short dimension) (m) |
| Notes | \hat{q}_{tol} is defined in DD:tolLoad. E comes from A:standardValues. h is defined in DD:minThick and is based on the nominal thicknesses. a and b are the dimensions of the plate, where $(a \geq b)$. |
| Source | [1] |
| RefBy | DD:calofCapacity |

| Refname | DD:gTF |
|-------------|--------------------------------------------------------------------------------------------------------------|
| Label | Glass type factor |
| Symbol | GTF |
| Units | Unitless |
| Equation | $GTF = \begin{cases} 1, & g = \text{``AN''} \\ 4, & g = \text{``FT''} \\ 2, & g = \text{``HS''} \end{cases}$ |
| Description | GTF is the glass type factor (Unitless) g is the glass type (Unitless) |
| Notes | AN is annealed glass. FT is fully tempered glass. HS is heat strengthened glass. |
| Source | [1] |
| RefBy | DD:calofCapacity and DD:dimlessLoad |

| Refname | DD:dimlessLoad |
|-------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Label | Dimensionless load |
| Symbol | \widehat{q} |
| Units | Unitless |
| Equation | $\hat{q} = \frac{q \left(a b\right)^2}{E h^4 G T F}$ |
| Description | \hat{q} is the dimensionless load (Unitless) q is the applied load (demand) (Pa) a is the plate length (long dimension) (m) b is the plate width (short dimension) (m) E is the modulus of elasticity of glass (Pa) h is the minimum thickness (m) GTF is the glass type factor (Unitless) |
| Notes | q is the 3 second duration equivalent pressure, as given in DD:calofDemand. a and b are the dimensions of the plate, where $(a \ge b)$. E comes from A:standardValues. h is defined in DD:minThick and is based on the nominal thicknesses. GTF is defined in DD:gTF. |
| Source | [1] and [5, (Eq. 7)] |
| RefBy | DD:stressDistFac |

| Refname | DD:tolLoad |
|-------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Label | Tolerable load |
| Symbol | $\widehat{q}_{\mathrm{tol}}$ |
| Units | Unitless |
| Equation | $\hat{q}_{\rm tol} = interpY(\text{``SDF.txt''}, AR, J_{\rm tol})$ |
| Description | \hat{q}_{tol} is the tolerable load (Unitless) $interpY \text{ is the interpY (Unitless)}$ AR is the aspect ratio (Unitless) J_{tol} is the stress distribution factor (Function) based on Pbtol (Unitless) |
| Notes | \hat{q}_{tol} is obtained by interpolating from data shown in Fig:dimlessloadVSaspect. AR is defined in DD:aspectRatio. J_{tol} is defined in DD:sdfTol. |
| Source | [1] |
| RefBy | DD:nFL |

| Refname | DD:sdfTol |
|-------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Label | Stress distribution factor (Function) based on Pbtol |
| Symbol | $J_{ m tol}$ |
| Units | Unitless |
| Equation | $J_{\rm tol} = \ln \left(\ln \left(\frac{1}{1 - P_{\rm btol}} \right) \frac{(ab)^{m-1}}{k \left(Eh^2 \right)^m LDF} \right)$ |
| Description | J_{tol} is the stress distribution factor (Function) based on Pbtol (Unitless) P_{btol} is the tolerable probability of breakage (Unitless) a is the plate length (long dimension) (m) b is the plate width (short dimension) (m) m is the surface flaw parameter $\left(\frac{\mathrm{m}^{12}}{\mathrm{N}^{7}}\right)$ k is the surface flaw parameter $\left(\frac{\mathrm{m}^{12}}{\mathrm{N}^{7}}\right)$ E is the modulus of elasticity of glass (Pa) h is the minimum thickness (m) LDF is the load duration factor (Unitless) |
| Notes | P_{btol} is entered by the user. a and b are the dimensions of the plate, where $(a \geq b)$. m, k , and E come from A:standardValues. h is defined in DD:minThick and is based on the nominal thicknesses. LDF is defined in DD:loadDurFactor. |
| Source | [1] |
| RefBy | DD:tolLoad |

| Refname | DD:standOffDist |
|-------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Label | Stand off distance |
| Symbol | SD |
| Units | m |
| Equation | $SD = \sqrt{S{D_{\mathrm{x}}}^2 + S{D_{\mathrm{y}}}^2 + S{D_{\mathrm{z}}}^2}$ |
| Description | SD is the stand off distance (m) $SD_{\rm x}$ is the stand off distance (x-component) (m) $SD_{\rm y}$ is the stand off distance (y-component) (m) $SD_{\rm z}$ is the stand off distance (z-component) (m) |
| Source | [1] |
| RefBy | DD:calofDemand |

| Refname | DD:aspectRatio |
|-------------|-------------------------------------------------------------------------------------------------------------------------------|
| Label | Aspect ratio |
| Symbol | AR |
| Units | Unitless |
| Equation | $AR = \frac{a}{b}$ |
| Description | AR is the aspect ratio (Unitless) a is the plate length (long dimension) (m) b is the plate width (short dimension) (m) |
| Notes | a and b are the dimensions of the plate, where $(a \ge b)$. |
| Source | [1] |
| RefBy | DD:tolLoad and DD:stressDistFac |

| Refname | DD:eqTNTW |
|-------------|------------------------------------------------------------------------------------------------------------------------------|
| Label | Equivalent TNT charge mass |
| Symbol | w_{TNT} |
| Units | kg |
| Equation | $w_{TNT} = wTNT$ |
| Description | w_{TNT} is the equivalent TNT charge mass (kg) w is the charge weight (kg) TNT is the TNT equivalent factor (Unitless) |
| Source | [1] |
| RefBy | DD:calofDemand |

| Refname | DD:probOfBreak |
|-------------|----------------------------------------------------------------------------------------------|
| Label | Probability of breakage |
| Symbol | $P_{ m b}$ |
| Units | Unitless |
| Equation | $P_{\rm b}=1-e^{-B}$ |
| Description | $P_{\rm b}$ is the probability of breakage (Unitless) B is the risk of failure (Unitless) |
| Notes | B is defined in $\overline{\mathrm{DD:riskFun}}$. |
| Source | [1] and [4] |
| RefBy | IM:isSafePb |

| Refname | DD:calofCapacity |
|-------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------|
| Label | Load resistance |
| Symbol | LR |
| Units | Pa |
| Equation | LR=NFLGTFLSF |
| Description | LR is the load resistance (Pa) NFL is the non-factored load (Pa) GTF is the glass type factor (Unitless) LSF is the load share factor (Unitless) |
| Notes | LR is also called capacity. NFL is defined in $\frac{\text{DD:nFL}}{\text{DTF}}$ is defined in $\frac{\text{DD:gTF}}{\text{DD:gTF}}$. |
| Source | [1] |
| RefBy | IM:isSafeLR |

| Refname | DD:calofDemand |
|-------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Label | Applied load (demand) |
| Symbol | q |
| Units | Pa |
| Equation | $q = interpY(\text{``TSD.txt''}, SD, w_{TNT})$ |
| Description | q is the applied load (demand) (Pa) $interpY$ is the interpY (Unitless) SD is the stand off distance (m) w_{TNT} is the equivalent TNT charge mass (kg) |
| Notes | q , or applied load (demand), is the 3 second duration equivalent pressure obtained from Fig:demandVSsod by interpolation using stand off distance (SD) and w_{TNT} as parameters. w_{TNT} is defined in DD:eqTNTW. SD is the stand off distance as defined in DD:standOffDist. |
| Source | [1] |
| RefBy | IM:isSafeLR and DD:dimlessLoad |

5.2.5 Instance Models

This section transforms the problem defined in the problem description into one which is expressed in mathematical terms. It uses concrete symbols defined in the data definitions to replace the abstract symbols in the models identified in theoretical models and general

definitions.

The goal GS:Predict-Glass-Withstands-Explosion is met by IM:isSafePb, IM:isSafeLR.

| Refname | IM:isSafePb |
|-----------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Label | Safety Req-Pb |
| Input | $P_{ m b},P_{ m btol}$ |
| Output | is-safePb |
| Input Constraints | $P_{ m b}>0$ $P_{ m btol}>0$ |
| Output Constraints | |
| Equation | $is-safePb=P_{\rm b} < P_{\rm btol}$ |
| Description | $is-safePb$ is the probability of glass breakage safety requirement (Unitless) $P_{\rm b} \ \ {\rm is\ the\ probability\ of\ breakage\ (Unitless)}$ $P_{\rm btol} \ \ {\rm is\ the\ tolerable\ probability\ of\ breakage\ (Unitless)}$ |
| Notes | If $is-safePb$, the glass is considered safe. $is-safePb$ and $is-safePb$ (from IM:isSafeLR) are either both True or both False. $P_{\rm b}$ is defined in DD:probOfBreak. $P_{\rm btol}$ is entered by the user. |
| Source | [1] |
| RefBy | IM:isSafeLR 31 |

| Refname | IM:isSafeLR |
|-----------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Label | Safety Req-LR |
| Input | LR,q |
| Output | is-safeLR |
| Input Constraints | LR > 0 $q > 0$ |
| Output Constraints | |
| Equation | is-safeLR=LR>q |
| Description | is-safeLR is the 3 second load equivalent resistance safety requirement (Unitless) LR is the load resistance (Pa) q is the applied load (demand) (Pa) |
| Notes | If $is-safeLR$, the glass is considered safe. $is-safePb$ (from IM:isSafePb) and $is-safeLR$ are either both True or both False. LR is defined in DD:calofCapacity and is also called capacity. q is the 3 second duration equivalent pressure, as given in DD:calofDemand. |
| Source | [1] |
| RefBy | 32 IM:isSafePb |

5.2.6 Data Constraints

The Data Constraints Table shows the data constraints on the input variables. The column for physical constraints gives the physical limitations on the range of values that can be taken by the variable. The uncertainty column provides an estimate of the confidence with which the physical quantities can be measured. This information would be part of the input if one were performing an uncertainty quantification exercise. The constraints are conservative, to give the user of the model the flexibility to experiment with unusual situations. The column of typical values is intended to provide a feel for a common scenario. The auxiliary constants give the values of the specification parameters used in the Data Constraints Table.

| Var | Physical Constraints | Software Constraints | Typical Value | Uncert. |
|----------------|---------------------------------|----------------------------------|------------------|---------|
| \overline{a} | $a > 0 \land a \ge b$ | $d_{\min} \le a \le d_{\max}$ | 1.5 m | 10% |
| AR | $AR \ge 1$ | $AR \le AR_{\max}$ | 1.5 | 10% |
| b | $0 < b \le a$ | $d_{\min} \le b \le d_{\max}$ | $1.2 \mathrm{m}$ | 10% |
| $P_{ m btol}$ | $0 \le P_{\mathrm{btol}} \le 1$ | _ | 0.008 | 0.1% |
| SD | SD > 0 | $SD_{\min} \le SD \le SD_{\max}$ | 45 m | 10% |
| TNT | TNT > 0 | _ | 1 | 10% |
| w | w > 0 | $w_{\min} \leq w \leq w_{\max}$ | 42 kg | 10% |

Table 4: Input Data Constraints

5.2.7 Properties of a Correct Solution

The Data Constraints Table shows the data constraints on the output variables. The column for physical constraints gives the physical limitations on the range of values that can be taken by the variable.

| Var | Physical Constraints |
|-------------|---------------------------------|
| $P_{\rm b}$ | $0 \le P_{\rm b} \le 1$ |
| J | $J_{\min} \leq J \leq J_{\max}$ |

Table 5: Output Data Constraints

6 Requirements

This section provides the functional requirements, the tasks and behaviours that the software is expected to complete, and the non-functional requirements, the qualities that the software is expected to exhibit.

6.1 Functional Requirements

This section provides the functional requirements, the tasks and behaviours that the software is expected to complete.

Input-Values: Input the values from Tab:ReqInputs, which define the glass dimensions, type of glass, tolerable probability of failure, and the characteristics of the blast.

wing-Assumptions: The system shall set the known values as described in the table for Required Assignments.

Data_Constraints: The system shall check the entered input values to ensure that they do not exceed the data constraints. If any of the input values are out of bounds, an error message is displayed and the calculations stop.

and-Known-Values: Output the input values from FR:Input-Values and the known values from FR:System-Set-Values-Following-Assumptions.

Check-Glass-Safety: If $is - safePb \land is - safeLR$ (from TM:isSafeProb and TM:isSafeLoad), output the message "For the given input parameters, the glass is considered safe." If the condition is false, then output the message "For the given input parameters, the glass is NOT considered safe."

Output-Values: Output the values from the table for Required Outputs.

| Symbol | Description | Units |
|-------------------|-----------------------------------------------------------------------------|--------------|
| \overline{a} | Plate length (long dimension) | m |
| b | Plate width (short dimension) | m |
| g | Glass type | _ |
| $P_{ m btol}$ | Tolerable probability of breakage | _ |
| $SD_{\mathbf{x}}$ | Stand off distance $(x$ -component) | \mathbf{m} |
| $SD_{ m y}$ | Stand off distance $(y$ -component) | m |
| SD_{z} | Stand off distance $(z$ -component) | m |
| t | Nominal thickness | mm |
| | $t \in \{2.5, 2.7, 3.0, 4.0, 5.0, 6.0, 8.0, 10.0, 12.0, 16.0, 19.0, 22.0\}$ | |
| TNT | TNT equivalent factor | _ |
| w | Charge weight | kg |

Table 6: Required Inputs following FR:Input-Values

| Symbol | Description | Source | Units |
|------------|--------------------------------|------------------|----------------------------------------|
| AR | Aspect ratio | DD:aspectRatio | _ |
| E | Modulus of elasticity of glass | A:standardValues | Pa |
| GTF | Glass type factor | DD:gTF | _ |
| h | Minimum thickness | DD:minThick | m |
| k | Surface flaw parameter | A:standardValues | $\frac{\mathrm{m}^{12}}{\mathrm{N}^7}$ |
| LDF | Load duration factor | DD:loadDurFactor | _ |
| LSF | Load share factor | A:glassLite | _ |
| m | Surface flaw parameter | A:standardValues | $\frac{\text{m}^{12}}{\text{N}^{7}}$ |
| SD | Stand off distance | DD:standOffDist | m |
| $t_{ m d}$ | Duration of load | A:standardValues | S |

Table 7: Required Assignments following FR:System-Set-Values-Following-Assumptions

| Symbol | Description | Source | Units |
|-----------------------|------------------------------------------------------|------------------|-------|
| \overline{AR} | Aspect ratio | DD:aspectRatio | _ |
| B | Risk of failure | DD:riskFun | _ |
| GTF | Glass type factor | DD:gTF | _ |
| h | Minimum thickness | DD:minThick | m |
| is-safeLR | Safety Req-LR | IM: is SafeLR | _ |
| is-safePb | Safety Req-Pb | IM:isSafePb | |
| J | Stress distribution factor (Function) | DD:stressDistFac | _ |
| $J_{ m tol}$ | Stress distribution factor (Function) based on Pbtol | DD:sdfTol | _ |
| NFL | Non-factored load | DD:nFL | Pa |
| \widehat{q} | Dimensionless load | DD:dimlessLoad | _ |
| $\hat{q}_{	ext{tol}}$ | Tolerable load | DD:tolLoad | _ |

Table 8: Required Outputs following FR:Output-Values

${\bf 6.2}\quad {\bf Non\text{-}Functional\ Requirements}$

This section provides the non-functional requirements, the qualities that the software is expected to exhibit.

Correct: The outputs of the code have the properties described in Sec:Properties of a Correct Solution.

Verifiable: The code is tested with complete verification and validation plan.

Understandable: The code is modularized with complete module guide and module interface specifica-

tion

Reusable: The code is modularized.

Maintainable: The traceability between requirements, assumptions, theoretical models, general defini-

tions, data definitions, instance models, likely changes, unlikely changes, and modules

is completely recorded in traceability matrices in the SRS and module guide.

Portable: The code is able to be run in different environments.

7 Likely Changes

This section lists the likely changes to be made to the software.

nternal-Blask-Risk: A:explainScenario - The system currently only calculates for external blast risk. In the

future, calculations can be added for the internal blast risk.

le-Values-of-m,k,E: A:standardValues, A:ldfConstant - Currently, the values for m, k, and E are assumed

to be the same for all glass. In the future, these values can be changed to variable

inputs.

e-than-Single-Lite: A:glassLite - The software may be changed to accommodate more than a single lite.

indary-Conditions: A:boundaryConditions - The software may be changed to accommodate more boundary

conditions than 4-sided support.

han-Flexure-Glass: A:responseType - The software may be changed to consider more than just flexure of

the glass.

8 Unlikely Changes

This section lists the unlikely changes to be made to the software.

-of-Certain-Degree: The goal of the system is to predict whether the glass slab under consideration can

withstand an explosion of a certain degree.

late-Altered-Glass: A:glassCondition requires that the glass is not altered in any way. Therefore, this

cannot be used on altered glass.

9 Traceability Matrices and Graphs

The purpose of the traceability matrices is to provide easy references on what has to be additionally modified if a certain component is changed. Every time a component is changed, the items in the column of that component that are marked with an "X" should be modified as well. Tab:TraceMatAvsA shows the dependencies of assumptions on the assumptions. Tab:TraceMatAvsAll shows the dependencies of data definitions, theoretical models, general definitions, instance models, requirements, likely changes, and unlikely changes on the assumptions. Tab:TraceMatRefvsRef shows the dependencies of data definitions, theoretical models, general definitions, and instance models with each other. Tab:TraceMatAllvsR shows the dependencies of requirements, goal statements on the data definitions, theoretical models, general definitions, and instance models.

| | A:glassType | A:glassCondition | A:explainScenario | A:standardValu |
|----------------------|-------------|------------------|-------------------|----------------|
| A:glassType | | | | |
| A:glassCondition | | | | |
| A:explainScenario | | | | |
| A:standardValues | | | | |
| A:glassLite | | | | |
| A:boundaryConditions | | | | |
| A:responseType | | | | |
| A:ldfConstant | | | | X |

Table 9: Traceability Matrix Showing the Connection Assumptions

A:glassType A:glassCondition A:explainScena

DD:riskFun
DD:minThick
DD:loadDurFactor
DD:stressDistFac
DD:nFL

DD:gTF

DD:dimlessLoad

DD:tolLoad

DD:sdfTol

DD:standOffDist

DD:aspectRatio

DD:eqTNTW

DD:probOfBreak

DD:calofCapacity

| | A:glassType | A.glassCondition | A toyplain Scoper |
|--------------------------------------------|-------------|------------------|-------------------|
| | A.glassType | A:glassCondition | Atexplainscena |
| DD:calofDemand | | | |
| TM:isSafeProb | | | |
| TM:isSafeLoad | | | |
| IM:isSafePb | | | |
| IM:isSafeLR | | | |
| FR:Input-Values | | | |
| FR:System-Set-Values-Following-Assumptions | | | |
| FR:Check-Input-with-Data_Constraints | | | |
| FR:Output-Values-and-Known-Values | | | |
| FR:Check-Glass-Safety | | | |
| FR:Output-Values | | | |
| NFR:Correct | | | |
| NFR:Verifiable | | | |
| NFR:Understandable | | | |
| NFR:Reusable | | | |
| NFR:Maintainable | | | |
| NFR:Portable | | | |
| LC:Calculate-Internal-Blask-Risk | | | X |
| LC:Variable-Values-of-m,k,E | | | |
| LC:Accomodate-More-than-Single-Lite | | | |
| LC:Accomodate-More-Boundary-Conditions | | | |
| LC:Consider-More-than-Flexure-Glass | | | |
| UC:Predict-Withstanding-of-Certain-Degree | | | |
| UC:Accommodate-Altered-Glass | | X | |

Table 10: Traceability Matrix Showing the Items

| | DD:riskFun | DD:minThick | DD:loadDurFactor | DD:stressDistFac | DD |
|------------------|------------|-------------|------------------|------------------|----|
| DD:riskFun | | X | X | X | |
| DD:minThick | | | | | |
| DD:loadDurFactor | | | | | |
| DD:stressDistFac | | | | | |
| DD:nFL | | X | | | |
| DD:gTF | | | | | |
| DD:dimlessLoad | | X | | | |
| DD:tolLoad | | | | | |
| DD:sdfTol | | X | X | | |
| DD:standOffDist | | | | | |
| DD:aspectRatio | | | | | |

| | DD:riskFun | DD:minThick | DD:loadDurFactor | ${\bf DD:} {\bf stressDistFac}$ | DD |
|------------------|------------|-------------|------------------|---------------------------------|----|
| DD:eqTNTW | | | | | |
| DD:probOfBreak | X | | | | |
| DD:calofCapacity | | | | | X |
| DD:calofDemand | | | | | |
| TM:isSafeProb | | | | | |
| TM:isSafeLoad | | | | | |
| IM:isSafePb | | | | | |
| IM:isSafeLR | | | | | |

| | DD:riskFun | DD:minThick | DD:loadDurFactor |
|--------------------------------------------|------------|-------------|------------------|
| GS:Predict-Glass-Withstands-Explosion | | | |
| FR:Input-Values | | | |
| FR:System-Set-Values-Following-Assumptions | | | |
| FR:Check-Input-with-Data_Constraints | | | |
| FR:Output-Values-and-Known-Values | | | |
| FR:Check-Glass-Safety | | | |
| FR:Output-Values | | | |

NFR:Understandable NFR:Reusable NFR:Maintainable

NFR:Portable

NFR:Correct NFR:Verifiable

The purpose of the traceability graphs is also to provide easy references on what has to be additionally modified if a certain component is changed. The arrows in the graphs represent dependencies. The component at the tail of an arrow is depended on by the component at the head of that arrow. Therefore, if a component is changed, the components that it points to should also be changed. Fig:TraceGraphAvsA shows the dependencies of assumptions on the assumptions. Fig:TraceGraphAvsAll shows the dependencies of data definitions, theoretical models, general definitions, instance models, requirements, likely changes, and unlikely changes on the assumptions. Fig:TraceGraphRefvsRef shows the dependencies of data definitions, theoretical models, general definitions, and instance models with each other. Fig:TraceGraphAllvsR shows the dependencies of requirements, goal statements on the data definitions, theoretical models, general definitions, and instance models. Fig:Trace-



Figure 3: TraceGraphAvsA



Figure 4: TraceGraphAvsAll

GraphAllvsAll shows the dependencies of dependencies of assumptions, models, definitions, requirements, goals, and changes with each other.

For convenience, the following graphs can be found at the links below:

- TraceGraphAvsA
- TraceGraphAvsAll
- $\bullet \quad Trace Graph Refvs Ref$
- TraceGraphAllvsR
- TraceGraphAllvsAll

10 Values of Auxiliary Constants

This section contains the standard values that are used for calculations in GlassBR.

| Symbol | Description | Value | Unit |
|--------------------|------------------------------------------------------------|------------------|------|
| AR_{\max} | maximum aspect ratio | 5 | |
| $d_{\rm max}$ | maximum value for one of the dimensions of the glass plate | 5 | m |
| d_{\min} | minimum value for one of the dimensions of the glass plate | 0.1 | m |
| E | modulus of elasticity of glass | $71.7\cdot 10^9$ | Pa |
| J_{max} | maximum value for the stress distribution factor | 32 | _ |
| $J_{ m min}$ | minimum value for the stress distribution factor | 1 | _ |



Figure 5: TraceGraphRefvsRef

| Symbol | Description | Value | Unit |
|---------------------|--------------------------------------------------|-----------------------|------------------------------------------|
| k | surface flaw parameter | $28.6 \cdot 10^{-54}$ | $\frac{\text{m}^{12}}{\text{N}^7}$ |
| LSF | load share factor | 1 | _ |
| m | surface flaw parameter | 7 | $\frac{\mathrm{m}^{12}}{\mathrm{N}^{7}}$ |
| SD_{max} | maximum stand off distance permissible for input | 130 | m |
| SD_{\min} | minimum stand off distance permissible for input | 6 | m |
| $t_{ m d}$ | duration of load | 3 | S |
| w_{max} | maximum permissible input charge weight | 910 | kg |
| w_{min} | minimum permissible input charge weight | 4.5 | kg |

Table 13: Auxiliary Constants

11 References

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Figure 7: TraceGraphAllvsAll

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12 Appendix

This appendix holds the graphs (Fig:demandVSsod and Fig:dimlessloadVSaspect) used for interpolating values needed in the models.



Figure 8: 3 second duration equivalent pressure (q) versus Stand off distance (SD) versus Charge weight (w)



Figure 9: Non dimensional lateral applied load (demand) or pressure (\hat{q}) versus Aspect Ratio (AR) versus Stress distribution factor (Function) (J)