

# Software Requirements Specification for Solar Water Heating Systems

Thulasi Jegatheesan

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# 1 Reference Material

This section records information for easy reference.

## 1.1 Table of Units

The unit system used throughout is SI (Système International d'Unités). In addition to the basic units, several derived units are also used. For each unit, the table lists the symbol, a description and the SI name.

Symbol	Description
°C	temperature (centigrade)
J	energy (joule)
kg	mass (kilogram)
m	length (metre)
s	time (second)
W	power (watt)

Table 1

## 1.2 Table of Symbols

The table that follows summarizes the symbols used in this document along with their units. The choice of symbols was made to be consistent with the heat transfer literature and with existing documentation for solar water heating systems. The symbols are listed in alphabetical order.

Symbol	Description	Units
$A_C$	Heating coil surface area	$\text{m}^2$
$A_{in}$	Surface area over which heat is transferred in	$\text{m}^2$
$A_{out}$	Surface area over which heat is transferred out	$\text{m}^2$
$C$	Specific heat capacity	$\frac{\text{J}}{(\text{kg}^\circ\text{C})}$
$C^L$	Specific heat capacity of a liquid	$\frac{\text{J}}{(\text{kg}^\circ\text{C})}$
$C_W$	Specific heat capacity of water	$\frac{\text{J}}{(\text{kg}^\circ\text{C})}$
$D$	Diameter of tank	$\text{m}$
$E$	Sensible heat	$\text{J}$
$E_W$	Change in heat energy in the water	$\text{J}$
$g$	Volumetric heat generation per unit volume	$\frac{\text{W}}{\text{m}^3}$

Symbol	Description	Units
$h$	Convective heat transfer coefficient	$\frac{\text{W}}{(\text{m}^2 \cdot ^\circ\text{C})}$
$h_C$	Convective heat transfer coefficient between coil and water	$\frac{\text{W}}{(\text{m}^2 \cdot ^\circ\text{C})}$
$L$	Length of tank	m
$m$	Mass	kg
$m_W$	Mass of water	kg
$\mathbf{n}$	Normal Vector	—
$q$	Heat flux	$\frac{\text{W}}{\text{m}^2}$
$q_C$	Heat flux into the water from the coil	$\frac{\text{W}}{\text{m}^2}$
$q_{in}$	Heat flux input	$\frac{\text{W}}{\text{m}^2}$
$q_{out}$	Heat flux output	$\frac{\text{W}}{\text{m}^2}$
$\mathbf{q}$	Thermal flux vector	$\frac{\text{W}}{\text{m}^2}$
$S$	Surface	$\text{m}^2$
$T$	Temperature	$^\circ\text{C}$
$t$	Time	s
$\Delta T$	Change in temperature	$^\circ\text{C}$
$T_C$	Temperature of the heating coil	$^\circ\text{C}$
$T_{env}$	Temperature of the environment	$^\circ\text{C}$
$t_{final}$	Final time	s
$T_{init}$	Initial temperature	$^\circ\text{C}$
$t_{step}$	Time step for simulation	s
$T_W$	Temperature of the water	$^\circ\text{C}$
$V$	Volume	$\text{m}^3$
$V_W$	Volume of water	$\text{m}^3$
$\pi$	Circumference to diameter ratio	—
$\rho$	Density	$\frac{\text{kg}}{\text{m}^3}$
$\rho_W$	Density of water	$\frac{\text{kg}}{\text{m}^3}$
$\tau_W$	ODE parameter for water	s
$\nabla$	Gradient	—

Table 2

### 1.3 Abbreviations and Acronyms

Abbreviation	Full Form
A	Assumption
DD	Data Definition
GD	General Definition
GS	Goal Statement
IM	Instance Model
LC	Likely Change
ODE	Ordinary Differential Equation
PS	Physical System Description
R	Requirement
SRS	Software Requirements Specification
SWHS	Solar Water Heating System
TM	Theoretical Model
UC	Unlikely Change
Uncert.	Typical Uncertainty

Table 3

## 2 Introduction

Due to increasing cost, diminishing availability, and negative environmental impact of fossil fuels, there is a higher demand for renewable energy sources and energy storage technology. Solar water heating systems provide a novel way of storing energy. The following section provides an overview of the Software Requirements Specification (SRS) for solar water heating systems. The developed program will be referred to as Solar Water Heating System (SWHS). This section explains the purpose of this document, the scope of the system, the characteristics of the intended reader, and the organization of the document.

### 2.1 Purpose of Document

The main purpose of this document is to describe the modelling of solar water heating system. The goals and theoretical models used in the SWHS code are provided, with an emphasis on explicitly identifying assumptions and unambiguous definitions. This document is intended to be used as a reference to provide ad hoc access to all information necessary to understand and verify the model. The SRS is abstract because the contents say what problem is being solved, but do not say how to solve it. This document will be used as a starting point for subsequent development phases, including writing the design specification and the software verification and validation plan. The design document will show how the requirements are to be realized, including decisions on the numerical algorithms and programming environment. The verification and validation plan will show the steps that will be used to increase confidence in the software documentation and the implementation. Although the SRS fits in a series of documents that follow the so-called waterfall model, the

actual development process is not constrained in any way. Even when the waterfall model is not followed, as Parnas and Clements point out [4], the most logical way to present the documentation is still to “fake” a rational design process.

## 2.2 Scope of Requirements

The scope of the requirements includes thermal analysis of a single solar water heating tank. Given the appropriate inputs, SWHS predicts the temperature and thermal energy histories for the water.

## 2.3 Characteristics of Intended Reader

Reviewers of this documentation should have an understanding of heat transfer theory from level 3 or 4 mechanical engineering and differential equations from level 1 and 2 calculus. The users of SWHS can have a lower level of expertise, as explained in [Section: User Characteristics](#).

## 2.4 Organization of Document

The organization of this document follows the template for an SRS for scientific computing software proposed by [dParnas1972] and [parnasClements1984]. The presentation follows the standard pattern of presenting goals, theories, definitions, and assumptions. For readers that would like a more bottom up approach, they can start reading the instance models in [Section: Instance Models](#) and trace back to find any additional information they require. The goal statements ([Section: Goal Statements](#)) are refined to the theoretical models and the theoretical models ([Section: Theoretical Models](#)) to the instance models ([Section: Instance Models](#)). The instance model to be solved is referred to as [IM: eBalanceOnWtr](#). The instance model provides the Ordinary Differential Equation (ODE) that model the solar water heating system. SWHS solves this ODE.

# 3 General System Description

This section provides general information about the system. It identifies the interfaces between the system and its environment, describes the user characteristics, and lists the system constraints.

## 3.1 System Context

[Fig:SysCon](#) shows the system context. A circle represents an external entity outside the software, the user in this case. A rectangle represents the software system itself (SWHS). Arrows are used to show the data flow between the system and its environment. SWHS



Figure 1: **Fig:SysCon:** System Context

is mostly self-contained. The only external interaction is through the user interface. The responsibilities of the user and the system are as follows:

- User Responsibilities:
  - Provide the input data to the system, ensuring no errors in the data entry
  - Take care that consistent units are used for input variables
- SWHS Responsibilities:
  - Detect data type mismatch, such as a string of characters instead of a floating point number
  - Determine if the inputs satisfy the required physical and software constraints
  - Calculate the required outputs

### 3.2 User Characteristics

The end user of SWHS should have an understanding of undergraduate Level 1 Calculus and Physics.

### 3.3 System Constraints

There are no system constraints.

## 4 Specific System Description

This section first presents the problem description, which gives a high-level view of the problem to be solved. This is followed by the solution characteristics specification, which presents the assumptions, theories, and definitions that are used.

## 4.1 Problem Description

SWHS is a computer program developed to investigate the heating of water in a solar water heating tank.

### 4.1.1 Terminology and Definitions

This subsection provides a list of terms that are used in the subsequent sections and their meaning, with the purpose of reducing ambiguity and making it easier to correctly understand the requirements.

- Heat flux: The rate of thermal energy transfer through a given surface per unit time
- Specific heat capacity: The amount of energy required to raise the temperature of the unit mass of a given substance by a given amount
- Thermal conduction: The transfer of heat energy through a substance
- Transient: Changing with time

### 4.1.2 Physical System Description

The physical system of SWHS, as shown in [Fig:Tank](#), includes the following elements:

PS1: Tank containing water.

PS2: Heating coil at bottom of tank. ( $q_C$  represents the heat flux into the water from the coil.)

### 4.1.3 Goal Statements

Given the temperature of the heating coil, the initial temperature of the water, and the material properties, the goal statements are:

Water-Temperature: Predict the temperature of the water over time.

Heat-Water-Energy: Predict the change in heat energy in the water over time.

## 4.2 Solution Characteristics Specification

The instance models that govern SWHS are presented in [Section: Instance Models](#). The information to understand the meaning of the instance models and their derivation is also presented, so that the instance models can be verified.





Figure 2: Solar water heating tank, with heat flux from heating coil of  $q_C$

### 4.2.1 Assumptions

This section simplifies the original problem and helps in developing the theoretical model by filling in the missing information for the physical system. The numbers given in the square brackets refer to the Theoretical Models [Section: Theoretical Models](#), General Definitions [Section: General Definitions](#), Data Definitions [Section: Data Definitions](#), Instance Models [Section: Instance Models](#), Likely Changes [Section: Likely Changes](#), or Unlikely Changes [Section: Unlikely Changes](#), in which the respective assumption is used.

- Thermal-Energy-Only: The only form of energy that is relevant for this problem is thermal energy. All other forms of energy, such as mechanical energy, are assumed to be negligible. [TM: consThermE](#).
- Heat-Coeffs-Constant: All heat transfer coefficients are constant over time. [GD: nwtmCooling](#).
- Temp-Across-Tank: The water in the tank is fully mixed, so the temperature of the water is the same throughout the entire tank. [GD: rocTempSimp](#).
- Density-Constant-over-Volume: The density of water has no spatial variation; that is, it is constant over their entire volume. [GD: rocTempSimp](#).
- Specific-Heat-Constant-over-Volume: The specific heat capacity of water has no spatial variation; that is, it is constant over its entire volume. [GD: rocTempSimp](#).
- Cooling-Coil-Water: Newton's law of convective cooling applies between the heating coil and the water. [DD: htFluxC](#).
- Coil-Temperature-Constant-over-Time: The temperature of the heating coil is constant over time. [LC: Temperature-Coil-Variable-Over-Day](#) [DD: htFluxC](#).
- Coil-Temperature-Constant-over-Length: The temperature of the heating coil does not vary along its length. [LC: Temperature-Coil-Variable-Over-Length](#).
- No-Temp-Discharge: The model only accounts for charging of the tank, not discharging. The temperature of the water can only increase, or remain constant; it cannot decrease. This implies that the initial temperature is less than (or equal to) the temperature of the heating coil. [LC: Discharging-Tank](#).
- Water-Always-Liquid: The operating temperature range of the system is such that the material (water in this case) is always in liquid state. That is, the temperature will not drop below the melting point temperature of water, or rise above its boiling point temperature. [UC: Water-Fixed-States](#) [TM: sensHtE](#) [IM: heatEInWtr](#) [IM: eBalanceOnWtr](#).
- Perfect-Insulation-Tank: The tank is perfectly insulated so that there is no heat loss from the tank. [LC: Tank-Lose-Heat](#) [IM: eBalanceOnWtr](#).
- Heat-Generation-By-Water: No internal heat is generated by the water; therefore, the volumetric heat generation per unit volume is zero. [UC: No-Internal-Heat-Generation](#) [IM: eBalanceOnWtr](#).

eric-Pressure-Tank: The pressure in the tank is atmospheric, so the melting point temperature and boiling point temperature of water are 0°C and 100°C, respectively **IM: heatEInWtr**.

### 4.2.2 Theoretical Models

This section focuses on the general equations and laws that SWHS is based on.

Refname	TM:consThermE
Label	Conservation of thermal energy
Equation	$-\nabla \cdot \mathbf{q} + g = \rho C \frac{\partial T}{\partial t}$
Description	<p><math>\nabla</math> is the gradient (Unitless)</p> <p><math>\mathbf{q}</math> is the thermal flux vector (<math>\frac{\text{W}}{\text{m}^2}</math>)</p> <p><math>g</math> is the volumetric heat generation per unit volume (<math>\frac{\text{W}}{\text{m}^3}</math>)</p> <p><math>\rho</math> is the density (<math>\frac{\text{kg}}{\text{m}^3}</math>)</p> <p><math>C</math> is the specific heat capacity (<math>\frac{\text{J}}{(\text{kg}^\circ\text{C})}</math>)</p> <p><math>t</math> is the time (s)</p> <p><math>T</math> is the temperature (°C)</p>
Notes	<p>The above equation gives the law of conservation of energy for transient heat transfer in a material of specific heat capacity <math>C</math> (<math>\frac{\text{J}}{(\text{kg}^\circ\text{C})}</math>) and density, <math>\rho</math> (<math>\frac{\text{kg}}{\text{m}^3}</math>), where <math>\mathbf{q}</math> is the thermal flux vector (<math>\frac{\text{W}}{\text{m}^2}</math>), <math>g</math> is the volumetric heat generation per unit volume (<math>\frac{\text{W}}{\text{m}^3}</math>), <math>T</math> is the temperature (°C), <math>t</math> is time (s), and <math>\nabla</math> is the degree of steepness of a graph at any point. For this equation to apply, other forms of energy, such as mechanical energy, are assumed to be negligible in the system (<b>A: Thermal-Energy-Only</b>).</p>
Source	<a href="#">Fourier Law of Heat Conduction and Heat Equation</a>
RefBy	<b>GD: rocTempSimp</b> .

Refname	TM:sensHtE
Label	Sensible heat energy (no state change)
Equation	$E = C^L m \Delta T$
Description	<p><math>E</math> is the sensible heat (J)</p> <p><math>C^L</math> is the specific heat capacity of a liquid (<math>\frac{\text{J}}{(\text{kg}^\circ\text{C})}</math>)</p> <p><math>m</math> is the mass (kg)</p> <p><math>\Delta T</math> is the change in temperature (<math>^\circ\text{C}</math>)</p>
Notes	$E$ occurs as long as the material does not reach a temperature where a phase change occurs, as assumed in <a href="#">A: Water-Always-Liquid</a> .
Source	<a href="#">Definition of Sensible Heat</a>
RefBy	<a href="#">IM: heatEInWtr</a> .

#### 4.2.3 General Definitions

This section collects the laws and equations that will be used to build the instance models.

Refname	GD:nwtnCooling
Label	Newton's law of cooling
Units	$\frac{\text{W}}{\text{m}^2}$
Equation	$q(t) = h\Delta T(t)$
Description	<p><math>q</math> is the heat flux (<math>\frac{\text{W}}{\text{m}^2}</math>)</p> <p><math>t</math> is the time (s)</p> <p><math>h</math> is the convective heat transfer coefficient (<math>\frac{\text{W}}{\text{m}^2\text{°C}}</math>)</p> <p><math>\Delta T</math> is the change in temperature (°C)</p>
Notes	<p>Newton's law of cooling describes convective cooling from a surface. The law is stated as: the rate of heat loss from a body is proportional to the difference in temperatures between the body and its surroundings. <math>\mathbf{q}(t)</math> is the thermal flux (<math>\frac{\text{W}}{\text{m}^2}</math>). <math>h</math> is the heat transfer coefficient, assumed independant of <math>T</math> (<b>A: Heat-Transfer-Coeffs-Constant</b>) (<math>\frac{\text{W}}{\text{m}^2\text{°C}}</math>). <math>\Delta T(t) = T(t) - T_{env}(t)</math> is the time-dependant thermal gradient between the environment and the object (°C).</p>
Source	[1, (pg. 8)]
RefBy	

Refname	GD:rocTempSimp
Label	Simplified rate of change of temperature
Equation	$mC \frac{dT}{dt} = q_{in}A_{in} - q_{out}A_{out} + gV$
Description	<p> <math>m</math> is the mass (kg)  <math>C</math> is the specific heat capacity (<math>\frac{J}{(kg^{\circ}C)}</math>)  <math>t</math> is the time (s)  <math>T</math> is the temperature (<math>^{\circ}C</math>)  <math>q_{in}</math> is the heat flux input (<math>\frac{W}{m^2}</math>)  <math>A_{in}</math> is the surface area over which heat is transferred in (<math>m^2</math>)  <math>q_{out}</math> is the heat flux output (<math>\frac{W}{m^2}</math>)  <math>A_{out}</math> is the surface area over which heat is transferred out (<math>m^2</math>)  <math>g</math> is the volumetric heat generation per unit volume (<math>\frac{W}{m^3}</math>)  <math>V</math> is the volume (<math>m^3</math>) </p>
Notes	<p>The basic equation governing the rate of change of temperature, for a given volume <math>V</math>, with time. <math>m</math> is the mass (kg). <math>C</math> is the specific heat capacity (<math>\frac{J}{(kg^{\circ}C)}</math>). <math>T</math> is the temperature (<math>^{\circ}C</math>) and <math>t</math> is the time (s). <math>q_{in}</math> and <math>q_{out}</math> are the in and out heat transfer rates, respectively (<math>\frac{W}{m^2}</math>). <math>A_{in}</math> and <math>A_{out}</math> are the surface areas over which the heat is being transferred in and out, respectively (<math>m^2</math>). <math>g</math> is the volumetric heat generated (<math>\frac{W}{m^3}</math>). <math>V</math> is the volume (<math>m^3</math>).</p>
Source	—
RefBy	GD: rocTempSimp IM: eBalanceOnWtr.
Detailed derivation of simplified rate of change of temperature. Integrating TM: consThermE over a volume ( $V$ ), we have:	

$$-\int_V \nabla \cdot \mathbf{q} dV + \int_V g dV = \int_V \rho C \frac{\partial T}{\partial t} dV$$

Applying Gauss's Divergence Theorem to the first term over the surface  $S$  of the volume, with  $\mathbf{q}$  as the thermal flux vector for the surface and  $\mathbf{n}$  as a unit outward normal vector for

a surface:

$$-\int_S \mathbf{q} \cdot \mathbf{n} dS + \int_V g dV = \int_V \rho C \frac{\partial T}{\partial t} dV$$

We consider an arbitrary volume. The volumetric heat generation per unit volume is assumed constant. Then (1) can be written as:

$$q_{in}A_{in} - q_{out}A_{out} + gV = \int_V \rho C \frac{\partial T}{\partial t} dV$$

Where  $q_{in}$ ,  $q_{out}$ ,  $A_{in}$ , and  $A_{out}$  are explained in [GD: rocTempSimp](#). Assuming  $\rho$ ,  $C$  and  $T$  are constant over the volume, which is true in our case by [A: Constant-Water-Temp-Across-Tank](#), [A: Density-Water-Constant-over-Volume](#), and [A: Specific-Heat-Energy-Constant-over-Volume](#), we have:

$$\rho CV \frac{dT}{dt} = q_{in}A_{in} - q_{out}A_{out} + gV$$

Using the fact that  $\rho=m/V$ , (2) can be written as:

$$mC \frac{dT}{dt} = q_{in}A_{in} - q_{out}A_{out} + gV$$

#### 4.2.4 Data Definitions

This section collects and defines all the data needed to build the instance models.

Refname	DD:htFluxC
Label	Heat flux into the water from the coil
Symbol	$q_C$
Units	$\frac{\text{W}}{\text{m}^2}$
Equation	$q_C = h_C (T_C - T_W(t))$
Description	$q_C$ is the heat flux into the water from the coil ( $\frac{\text{W}}{\text{m}^2}$ ) $h_C$ is the convective heat transfer coefficient between coil and water ( $\frac{\text{W}}{\text{m}^2\text{C}}$ ) $T_C$ is the temperature of the heating coil ( $^{\circ}\text{C}$ ) $T_W$ is the temperature of the water ( $^{\circ}\text{C}$ ) $t$ is the time (s)
Notes	A: Newton-Law-Convective-Cooling-Coil-Water A: Temp-Heating-Coil-Constant-over-Time
Source	[2]
RefBy	IM: eBalanceOnWtr IM: eBalanceOnWtr.

#### 4.2.5 Instance Models

This section transforms the problem defined in [Section: Problem Description](#) into one which is expressed in mathematical terms. It uses concrete symbols defined in [Section: Data Definitions](#) to replace the abstract symbols in the models identified in [Section: Theoretical Models](#) and [Section: General Definitions](#). The goal [GS: Predict-Water-Temperature](#) is met by [IM: eBalanceOnWtr](#) and the goal [GS: Predict-Water-Energy](#) is met by [IM: heatElInWtr](#).



Refname	IM:eBalanceOnWtr	
Label	Energy balance on water to find the temperature of the water	
Input	$T_C, T_{init}, t_{final}, A_C, h_C, C_W, m_W$	
Output	$T_W$	
Input Constraints	$T_{init} \leq T_C$	
Output constraints	Con-	$0 < t < t_{final}$
Equation	$\frac{dT_W}{dt} = \frac{1}{\tau_W} (T_C - T_W(t))$	
Description	<p><math>t</math> is the time (s)</p> <p><math>T_W</math> is the temperature of the water (°C)</p> <p><math>\tau_W</math> is the ODE parameter for water (s)</p> <p><math>T_C</math> is the temperature of the heating coil (°C)</p>	
Notes	<p><math>T_W</math> is the temperature of the water (°C). <math>T_C</math> is the temperature of the heating coil (°C). <math>\tau_W = \frac{m_W C_W}{h_C A_C}</math> is a constant (s). The above equation applies as long as the water is in liquid form, <math>0 &lt; T_W &lt; 100</math> (°C) where 0 (°C) and 100 (°C) are the melting and boiling point temperatures of water, respectively (<b>A: Water-Always-Liquid</b>).</p>	
Source	[2, (with PCM removed)]	
RefBy	<p>UC: No-Internal-Heat-Generation FR: Output-Input-Derived-Quantities FR: Find-Mass FR: Calculate-Temperature-Water-Over-Time.</p>	

Derivation of the energy balance on water: To find the rate of change of  $T_W$ , we look at the energy balance on water. The volume being considered is the volume of water in the tank  $V_W$ , which has mass  $m_W$  and specific heat capacity,  $C_W$ . Heat transfer occurs in the water from the heating coil as  $q_C$  (DD: htFluxC), over area  $A_C$ . No heat transfer occurs to the outside of the tank, since it has been assumed to be perfectly insulated (A: Perfect-Insulation-Tank). Since the assumption is made that no internal heat is generated (A: No-Internal-Heat-Generation-By-Water),  $g = 0$ . Therefore, the equation for GD: rocTempSimp can be written as:

$$m_W C_W \frac{dT_W}{dt} = q_C A_C$$

Using DD: htFluxC , this can be written as:

$$m_W C_W \frac{dT_W}{dt} = h_C A_C (T_C - T_W)$$

Dividing (3) by  $m_W C_W$ , we obtain:

$$\frac{dT_W}{dt} = \frac{h_C A_C}{m_W C_W} (T_C - T_W)$$

Setting  $\tau_W = m_W C_W / h_C A_C$  , Equation (4) can be written in its final form as:

$$\frac{dT_W}{dt} = \frac{1}{\tau_W} (T_C - T_W)$$

Refname	IM:heatEInWtr		
Label	Heat energy in the water		
Input	$T_{init}, m_W, C_W, m_W$		
Output	$E_W$		
Input Constraints			
Output constraints	Con-	$0 < t < t_{final}$	
Equation			
$E_W(t) = C_W m_W (T_W(t) - T_{init})$			
Description			
$E_W$ is the change in heat energy in the water (J) $t$ is the time (s) $C_W$ is the specific heat capacity of water ( $\frac{\text{J}}{(\text{kg}^\circ\text{C})}$ ) $m_W$ is the mass of water (kg) $T_W$ is the temperature of the water ( $^\circ\text{C}$ ) $T_{init}$ is the initial temperature ( $^\circ\text{C}$ )			
Notes			
The above equation is derived using <b>TM: sensHtE</b> . $E_W$ is the change in thermal energy of the liquid water relative to the energy at the initial temperature ( $T_{init}$ ) (J). $C_W$ is the specific heat capacity of liquid water ( $\frac{\text{J}}{(\text{kg}^\circ\text{C})}$ ) and $m_W$ is the mass of the water (kg). The change in temperature is the difference between the temperature at time $t$ (s), $T_W$ and the initial temperature, $T_{init}$ ( $^\circ\text{C}$ ). This equation applies as long as $0 < T_W < 100^\circ\text{C}$ ( <b>A: Water-Always-Liquid, A: Atmospheric-Pressure-Tank</b> ).			
Source	[2]		
RefBy	FR: Calculate-Change-Heat_Energy-Water-Over-Time.		

#### 4.2.6 Data Constraints

[Table:InDataConstraints](#) and [Table:OutDataConstraints](#) show the data constraints on the input and output variables, respectively. The column for physical constraints gives the physical limitations on the range of values that can be taken by the variable. The uncertainty column provides an estimate of the confidence with which the physical quantities can be measured. This information would be part of the input if one were performing an uncertainty quantification exercise. The constraints are conservative, to give the user of the model the flexibility to experiment with unusual situations. The column of typical values is intended to provide a feel for a common scenario. The column for software constraints restricts the range of inputs to reasonable values.

Var	Physical Constraints	Software Constraints	Typical Value	Uncert.
$A_C$	$A_C > 0$	$A_C \leq A_C^{max}$	0.12 m <sup>2</sup>	10%
$C_W$	$C_W > 0$	$C_W^{min} < C_W < C_W^{max}$	$4.186 \cdot 10^3 \frac{\text{J}}{(\text{kg}^\circ\text{C})}$	10%
$D$	$D > 0$	–	0.412 m	10%
$h_C$	$h_C > 0$	$h_C^{min} \leq h_C \leq h_C^{max}$	$1.0 \cdot 10^3 \frac{\text{W}}{(\text{m}^2^\circ\text{C})}$	10%
$L$	$L > 0$	$L_{min} \leq L \leq L_{max}$	1.5 m	10%
$T_C$	$0 < T_C < 100$	–	50.0 °C	10%
$t_{final}$	$t_{final} > 0$	$t_{final} < t_{final}^{max}$	$50.0 \cdot 10^3 \text{ s}$	10%
$T_{init}$	$0 < T_{init} < 100$	–	40.0 °C	10%
$t_{step}$	$0 < t_{step} < t_{final}$	–	0.01 s	10%
$\rho_W$	$\rho_W > 0$	$\rho_W^{min} < \rho_W \leq \rho_W^{max}$	$1.0 \cdot 10^3 \frac{\text{kg}}{\text{m}^3}$	10%

Table 4: Input Data Constraints

Var	Physical Constraints
$T_W$	$T_{init} \leq T_W \leq T_C$
$E_W$	$E_W \geq 0$

Table 5: Output Data Constraints

#### 4.2.7 Properties of a Correct Solution

FIXME.

## 5 Requirements

This section provides the functional requirements, the tasks and behaviours that the software is expected to complete, and the non-functional requirements, the qualities that the software

is expected to exhibit.

## 5.1 Functional Requirements

This section provides the functional requirements, the tasks and behaviours that the software is expected to complete.

**Initial-Quantities:** Input the following quantities described in [Table:ReqInputs](#), which define the tank parameters, material properties and initial conditions.

**Find-Mass:** Use the inputs in [FR: Input-Initial-Quantities](#) to find the mass needed for [IM: eBalanceOnWtr](#), using  $m_W = V_W \rho_W = \pi \left(\frac{D}{2}\right)^2 L \rho_W$ , where  $V_W$  is the volume of water.

**Physical\_Constraints:** Verify that the inputs satisfy the required physical constraints shown in [Table:InDataConstraints](#).

**Derived-Quantities:** Output the input quantities and derived quantities in the following list: the quantities from [FR: Input-Initial-Quantities](#), the mass from [FR: Find-Mass](#), and  $\tau_W$  (from [IM: eBalanceOnWtr](#)).

**Water-Over-Time:** Calculate and output the temperature of the water ( $T_W(t)$ ) over the simulation time (from [IM: eBalanceOnWtr](#)).

**Water-Over-Time:** Calculate and output the change in heat energy in the water ( $E_W(t)$ ) over the simulation time (from [IM: heatEInWtr](#)).

Symbol	Description	Units
$A_C$	Heating coil surface area	$\text{m}^2$
$A_{tol}$	Absolute tolerance	—
$C_W$	Specific heat capacity of water	$\frac{\text{J}}{(\text{kg}^\circ\text{C})}$
$D$	Diameter of tank	$\text{m}$
$h_C$	Convective heat transfer coefficient between coil and water	$\frac{\text{W}}{(\text{m}^2^\circ\text{C})}$
$L$	Length of tank	$\text{m}$
$R_{tol}$	Relative tolerance	—
$T_C$	Temperature of the heating coil	$^\circ\text{C}$
$t_{final}$	Final time	$\text{s}$
$T_{init}$	Initial temperature	$^\circ\text{C}$
$t_{step}$	Time step for simulation	$\text{s}$
$\rho_W$	Density of water	$\frac{\text{kg}}{\text{m}^3}$

Table 6: Required Inputs following [FR: Input-Initial-Quantities](#)

## 5.2 Non-Functional Requirements

This section provides the non-functional requirements, the qualities that the software is expected to exhibit.

Correct: The outputs of the code have the properties described in [Section: Properties of a Correct Solution](#).

Verifiable: The code is tested with complete verification and validation plan.

Understandable: The code is modularized with complete module guide and module interface specification.

Reusable: The code is modularized.

Maintainable: The traceability between requirements, assumptions, theoretical models, general definitions, data definitions, instance models, likely changes, unlikely changes, and modules is completely recorded in traceability matrices in the SRS and module guide.

## 6 Likely Changes

Variable-Over-Day: [A: Temp-Heating-Coil-Constant-over-Time](#) - The temperature of the heating coil will change over the course of the day, depending on the energy received from the sun.

Variable-Over-Length: [A: Temp-Heating-Coil-Constant-over-Length](#) - The temperature of the heating coil will actually change along its length as the water within it cools.

Discharging-Tank: [A: Charging-Tank-No-Temp-Discharge](#) - The model currently only accounts for charging of the tank. That is, increasing the temperature of the water to match the temperature of the coil. A more complete model would also account for discharging of the tank.

Tank-Lose-Heat: [A: Perfect-Insulation-Tank](#) - Any real tank cannot be perfectly insulated and will lose heat.

## 7 Unlikely Changes

Water-Fixed-States: [A: Water-Always-Liquid](#) - It is unlikely for the change of water from liquid to a solid, or from liquid to gas to be considered.

Internal-Heat-Generation: [A: No-Internal-Heat-Generation-By-Water](#) - Is used for the derivations of [IM: eBalanceOnWtr](#).

## 8 Traceability Matrices and Graphs

The purpose of the traceability matrices is to provide easy references on what has to be additionally modified if a certain component is changed. Every time a component is changed, the items in the column of that component that are marked with an “X” should be modified as well. [Table:TraceMatAvsAll](#) shows the dependencies of data definitions, theoretical models, general definitions, instance models, requirements, likely changes, and unlikely changes on the assumptions. [Table:TraceMatRefvsRef](#) shows the dependencies of data definitions, theoretical models, general definitions, and instance models with each other. [Table:TraceMatAllvsR](#) shows the dependencies of requirements, goal statements on the data definitions, theoretical models, general definitions, and instance models.

	A: Thermal-Energy-Only	A: Heat-Transfer-C
DD: htFluxC		
TM: consThermE	X	
TM: sensHtE		
GD: nwtNCooling		X
GD: rocTempSimp		
IM: eBalanceOnWtr		
IM: heatEInWtr		
FR: Input-Initial-Quantities		
FR: Find-Mass		
FR: Check-Input-with-Physical_Constraints		
FR: Output-Input-Derived-Quantities		
FR: Calculate-Temperature-Water-Over-Time		
FR: Calculate-Change-Heat_Energy-Water-Over-Time		
LC: Temperature-Coil-Variable-Over-Day		
LC: Temperature-Coil-Variable-Over-Length		
LC: Discharging-Tank		
LC: Tank-Lose-Heat		
UC: Water-Fixed-States		
UC: No-Internal-Heat-Generation		

  

	DD: htFluxC	TM: consThermE	TM: sensHtE	GD: nwtNCooling	GD: rocTe
DD: htFluxC					
TM: consThermE					
TM: sensHtE					
GD: nwtNCooling					

	DD: htFluxC	TM: consThermE	TM: sensHtE	GD: nwtNCooling	GD: rocTe
GD: rocTempSimp		X			X
IM: eBalanceOnWtr	X				X
IM: heatEInWtr			X		

Table 8: Traceability Matrix Showing the Connections Between Items and

	DD: htFluxC	TM: consThermE	TM: sensHtE
GS: Predict-Water-Temperature			
GS: Predict-Water-Energy			
FR: Input-Initial-Quantities			
FR: Find-Mass			
FR: Check-Input-with-Physical_Constraints			
FR: Output-Input-Derived-Quantities			
FR: Calculate-Temperature-Water-Over-Time			
FR: Calculate-Change-Heat_Energy-Water-Over-Time			

## 9 Values of Auxiliary Constants

This section contains the standard values that are used for calculations in SWHS.

Symbol	Description	Value	Unit
$A_C^{max}$	maximum surface area of coil	100000	m <sup>2</sup>
$C_{tol}$	relative tolerance for conservation of energy	1.0e − 3%	–
$C_W^{max}$	maximum specific heat capacity of water	4210	$\frac{J}{(kg^{\circ}C)}$
$C_W^{min}$	minimum specific heat capacity of water	4170	$\frac{J}{(kg^{\circ}C)}$
$h_C^{max}$	maximum convective heat transfer coefficient between coil and water	10000	$\frac{W}{(m^2^{\circ}C)}$
$h_C^{min}$	minimum convective heat transfer coefficient between coil and water	10	$\frac{W}{(m^2^{\circ}C)}$
$L_{max}$	maximum length of tank	50	m
$L_{min}$	minimum length of tank	0.1	m
$t_{final}^{max}$	maximum final time	86400	s
$\rho_W^{max}$	maximum density of water	1000	$\frac{kg}{m^3}$



Symbol	Description	Value	Unit
$\rho_W^{min}$	minimum density of water	950	$\frac{\text{kg}}{\text{m}^3}$

Table 10: Auxiliary Constants

## 10 References

- [1] F. P. Incropera et al. *Fundamentals of Heat and Mass Transfer*. 6th ed. Hoboken, New Jersey: John Wiley and Sons, 2007.
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