

We thus know the price of the security now.
Now recall the price of a caplet with
Bachelier's formula:

$$C_{PI Bach}(t, T_0, T_1) = \delta P(t, T_1) \sigma_{Bach} \sqrt{T_0 - t} \\ (D \Phi(D) + \phi(D)) \text{ with} \\ D = \frac{F(t, T_0, T_1) - K}{\sigma \sqrt{T_0 - t}}$$

If the caplet is ATM, i.e. $F(t, T_0, T_1) = K$, this
simplifies to

$$C_{PI Bach}(t, T_0, T_1) = \delta P(t, T_1) \sigma_{Bach} \sqrt{T_0 - t} \phi(0)$$

Plugging the price we found for $C_{PI Black}$ and
solving for σ_{Bach} gives:

$$\sigma_{Bach} = \frac{0.13049947392014823}{1 \cdot e^{-0.03 \cdot 5} \sqrt{4} \phi(0)} = 0.019002593220489485 \\ = \frac{1}{\sqrt{27}}$$