## Quantitative Risk Management Assignment 9

Due: December 3, 2019

Question 1: Let  $(X_i)_{i\in\mathbb{N}}$  be independent with distribution F.

- 1. Let  $F(x) = 1 \exp(-\beta x)$  for  $\beta > 0$  and  $x \ge 0$  so that  $X_i$  is exponentially distributed. Show that  $F \in MDA(H_0)$  by using the sequences  $c_n = \frac{\log(n)}{\beta}$  and  $d_n = \frac{1}{\beta}$ .
- 2. Let  $F(x) = 1 (\frac{\kappa}{\kappa + x})^{\alpha}$  for  $\alpha > 0$ ,  $\kappa > 0$ , and  $x \ge 0$  so that  $X_i$  has Pareto distribution. Show that  $F \in MDA(H_{1/\alpha})$  by using the sequences  $c_n = \kappa n^{1/\alpha} \kappa$  and  $d_n = \frac{\kappa n^{1/\alpha}}{\alpha}$ .

Question 2: Suppose X has excess distribution over the threshold u of  $F_u = G_{\xi,\beta}$ . Show that the excess distribution over the threshold v is equal to  $F_v = G_{\xi,\beta+(v-u)\xi}$  for  $v \ge u$ .

Question 3: Download 5 years of Microsoft stock prices beginning on November 26, 2011.

- 1. Compute the negative log returns and reproduce the sample mean excess plot shown in the lecture.
- 2. Select a threshold of 0.01 for the negative log returns and fit a GPD model to the excess distribution over the threshold by maximum likelihood estimation. The Matlab function gppdf may be useful.