

# Week 8

I used online calculators to calculate entropy, entropy average, weighted entropy average, Information Gain, Gini Impurity, Gini Impurity average, and weighted Gini Impurity average.

## 1. Calculate Entropy and Information Gain:

### Calculate Entropy for Entire Dataset:

$$E(D) = 1$$

### Calculate Entropy for Each Attribute:

Weather Condition

$$E(\text{Rain}) = 0.92$$

$$E(\text{Snow}) = 0.92$$

$$E(\text{Clear}) = 1$$

Road Condition

$$E(\text{Bad}) = 0.81$$

$$E(\text{Average}) = 1$$

$$E(\text{Good}) = 0.81$$

Traffic Condition

$$E(\text{High}) = 0.82$$

$$E(\text{Normal}) = 0.92$$

$$E(\text{Light}) = 0.92$$

Engine Problem

$$E(\text{Yes}) = 0.81$$

$$E(\text{No}) = 0.92$$

### Calculate the Weighted Entropy Average for Each Attribute:

Weather Condition = 0.95

Road Condition = 0.85

Traffic Condition = 0.88

Engine Problem Condition = 0.88

Calculate the Information Gain for Each Attribute:

Weather Condition = 0.05

Road Condition = 0.15

Traffic Condition = 0.12

Engine Problem = 0.12

Choose Best Attribute as Root Node:

Road Condition has highest information gain value.

Road Condition is root node.

**2. Calculate Gini Impurity:**

Calculate Gini Impurity for Entire Dataset:

$Gini(D) = 0.5$

Calculate Gini Impurity for Each Attribute:

Weather Condition

$Gini(Rain) = 0.44$

$Gini(Snow) = 0.44$

$Gini(Clear) = 5$

Road Condition

$Gini(Bad) = 0.38$

$Gini(Average) = 0.5$

$Gini(Good) = 0.38$

Traffic Condition

$Gini(High) = 0.38$

$Gini(Normal) = 0.44$

$Gini(Light) = 0.44$

Engine Problem

$Gini(Yes) = 0.5$

$Gini(No) = 0.5$

Calculate the Weighted Gini Impurity Average for Each Attribute:

Weather Condition = 0.47

Road Condition = 0.4

Traffic Condition = 0.42

Engine Problem Condition = 0.5

Choose Best Attribute as Root Node:

Road Condition has lowest Gini impurity value.

Road Condition is root node.

**3. Construct the Decision Tree:**

Determine first layer:

Root node = Road Condition

Branch 1 = Bad

Branch 2 = Average

Branch 3 = Good

Determine Branch 1 with Information Gain:

Weather Condition = 0.31

Traffic Condition = 0

Engine Problem = 0.31

Use Weather or Engine

Intermediate node = Weather Condition

Branch 1.1 = Rain

Branch 1.2 = Snow

Branch 1.3 = Clear

Determine Branch 2 with Information Gain:

Weather Condition = 0

Traffic Condition = 0

Engine Problem = 1

Intermediate node = Engine Problem

Branch 2.1 = Yes

Branch 2.2 = No

Determine Branch 3 with Information Gain:

Weather Condition = 0.31

Traffic Condition = 0

Engine Problem = 0.81

Intermediate node = Engine Problem

Branch 3.1 = No

Branch 3.2 = Yes

Final Decision Tree:

