## Dataset Distillation

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## Background

- Knowledge Distillation
  - large model -> small model
- Datsetset Distillation
  - large dataset -> small dataset
  - coreset & synthetic

### DATASET DISTILLATION

Tongzhou Wang

Facebook AI Research, MIT CSAIL

Antonio Torralba

MIT CSAIL

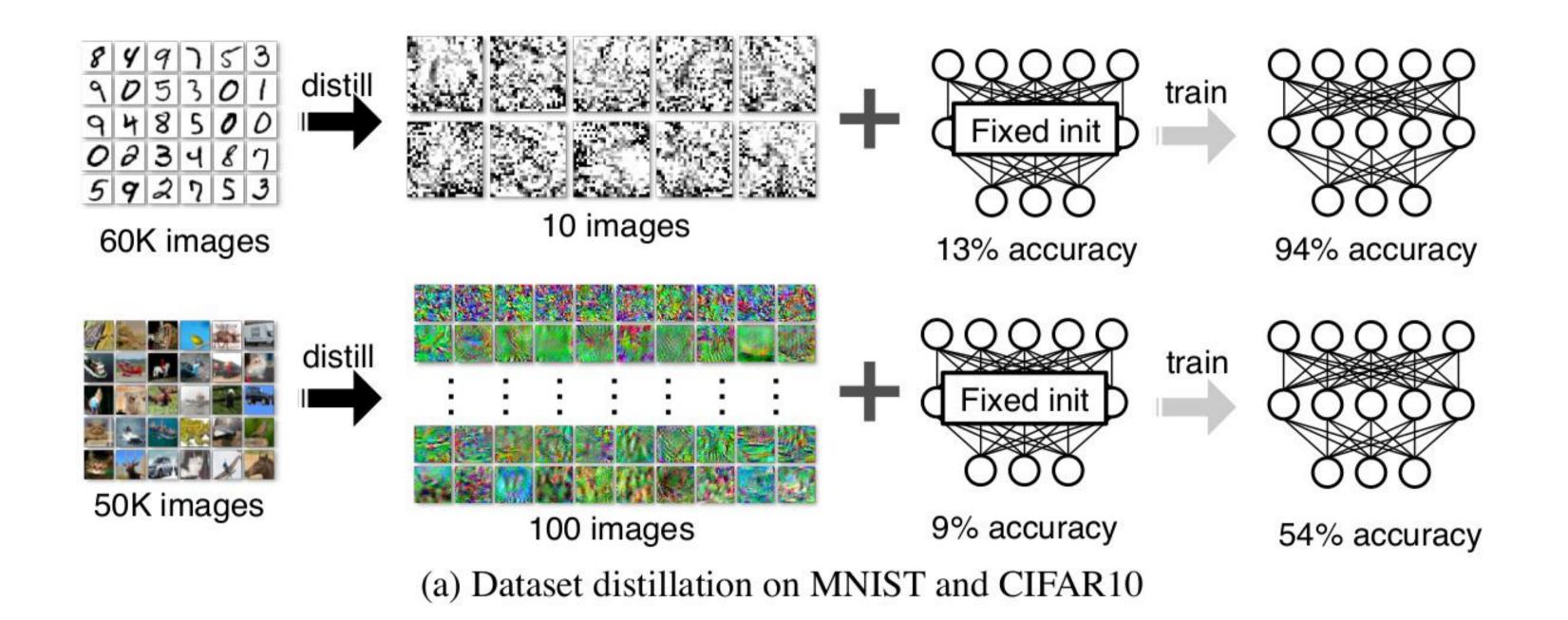
Jun-Yan Zhu

MIT CSAIL

Alexei A. Efros

UC Berkeley

## Motivation



training loss 
$$\theta^* = \operatorname*{arg\,min}_{\theta} \frac{1}{N} \sum_{i=1}^N \ell(x_i, \theta) \triangleq \operatorname*{arg\,min}_{\theta} \ell(\mathbf{x}, \theta), \qquad \mathbf{x} = \{x_i\}_{i=1}^N$$

SGD update

$$\theta_{t+1} = \theta_t - \eta \nabla_{\theta_t} \ell(\mathbf{x}_t, \theta_t),$$

SGD update on syntactic data

$$\theta_1 = \theta_0 - \tilde{\eta} \nabla_{\theta_0} \ell(\tilde{\mathbf{x}}, \theta_0)$$

$$\tilde{\mathbf{x}} = {\{\tilde{x}_i\}_{i=1}^M \text{ with } M \ll N}$$

meta-learning 
$$\tilde{\mathbf{x}}^*, \tilde{\eta}^* = \underset{\tilde{\mathbf{x}}, \tilde{\eta}}{\operatorname{arg\,min}} \, \mathcal{L}(\tilde{\mathbf{x}}, \tilde{\eta}; \theta_0) = \underset{\tilde{\mathbf{x}}, \tilde{\eta}}{\operatorname{arg\,min}} \, \ell(\mathbf{x}, \theta_1) = \underbrace{\left(\underset{\tilde{\mathbf{x}}, \tilde{\eta}}{\operatorname{arg\,min}} \, \ell(\mathbf{x}, \theta_0 - \tilde{\eta} \nabla_{\theta_0} \ell(\tilde{\mathbf{x}}, \theta_0))\right)}_{\text{dependent on } \theta_0},$$

#### Distillation for random initializations

$$\tilde{\mathbf{x}}^*, \tilde{\eta}^* = \underset{\tilde{\mathbf{x}}, \tilde{\eta}}{\operatorname{arg\,min}} \mathbb{E}_{\theta_0 \sim p(\theta_0)} \mathcal{L}(\tilde{\mathbf{x}}, \tilde{\eta}; \theta_0)$$

#### Algorithm 1 Dataset Distillation

```
Input: p(\theta_0): distribution of initial weights; M: the number of distilled data
Input: \alpha: step size; n: batch size; T: the number of optimization iterations; \tilde{\eta}_0: initial value for \tilde{\eta}
 1: Initialize \tilde{\mathbf{x}} = {\{\tilde{x}_i\}_{i=1}^{M} \text{ randomly, } \tilde{\eta} \leftarrow \tilde{\eta}_0}
 2: for each training step t = 1 to T do
             Get a minibatch of real training data \mathbf{x}_t = \{x_{t,j}\}_{j=1}^n
 3:
             Sample a batch of initial weights \theta_0^{(j)} \sim p(\theta_0)
            for each sampled \theta_0^{(j)} do
                   Compute updated parameter with GD: \theta_1^{(j)} = \theta_0^{(j)} - \tilde{\eta} \nabla_{\theta_0^{(j)}} \ell(\tilde{\mathbf{x}}, \theta_0^{(j)})
 6:
                   Evaluate the objective function on real training data: \mathcal{L}^{(j)} = \ell(\mathbf{x}_t, \theta_1^{(j)})
 8:
             end for
            Update \tilde{\mathbf{x}} \leftarrow \tilde{\mathbf{x}} - \alpha \nabla_{\tilde{\mathbf{x}}} \sum_{i} \mathcal{L}^{(j)}, and \tilde{\eta} \leftarrow \tilde{\eta} - \alpha \nabla_{\tilde{\eta}} \sum_{i} \mathcal{L}^{(j)}
10: end for
Output: distilled data \tilde{\mathbf{x}} and optimized learning rate \tilde{\eta}
```

# Analysis

origin loss

$$\ell(\mathbf{x}, \theta) = \ell((\mathbf{d}, \mathbf{t}), \theta) = \frac{1}{2N} \|\mathbf{d}\theta - \mathbf{t}\|^2.$$
 d-> N×D

DD loss

$$\ell(\mathbf{x}, \theta_0 - \tilde{\eta} \nabla_{\theta_0} \ell(\tilde{\mathbf{x}}, \theta_0))$$

$$\widetilde{d} \rightarrow M \times D$$

$$\theta_1 = \theta_0 - \tilde{\eta} \nabla_{\theta_0} \ell(\tilde{\mathbf{x}}, \theta_0) = \theta_0 - \frac{\tilde{\eta}}{M} \tilde{\mathbf{d}}^T (\tilde{\mathbf{d}} \theta_0 - \tilde{\mathbf{t}}) = (\mathbf{I} - \frac{\tilde{\eta}}{M} \tilde{\mathbf{d}}^T \tilde{\mathbf{d}}) \theta_0 + \frac{\tilde{\eta}}{M} \tilde{\mathbf{d}}^T \tilde{\mathbf{t}}.$$

•  $\mathbf{d}^T \mathbf{d} \theta^* = \mathbf{d}^T \mathbf{t}$  for global minimum

$$\mathbf{d}^T \mathbf{d} (\mathbf{I} - \frac{\tilde{\eta}}{M} \tilde{\mathbf{d}}^T \tilde{\mathbf{d}}) \theta_0 + \frac{\tilde{\eta}}{M} \mathbf{d}^T \mathbf{d} \tilde{\mathbf{d}}^T \tilde{\mathbf{t}} = \mathbf{d}^T \mathbf{t}$$

Mild assumption: columns of d are independent (i.e. d<sup>T</sup>d has full rank)

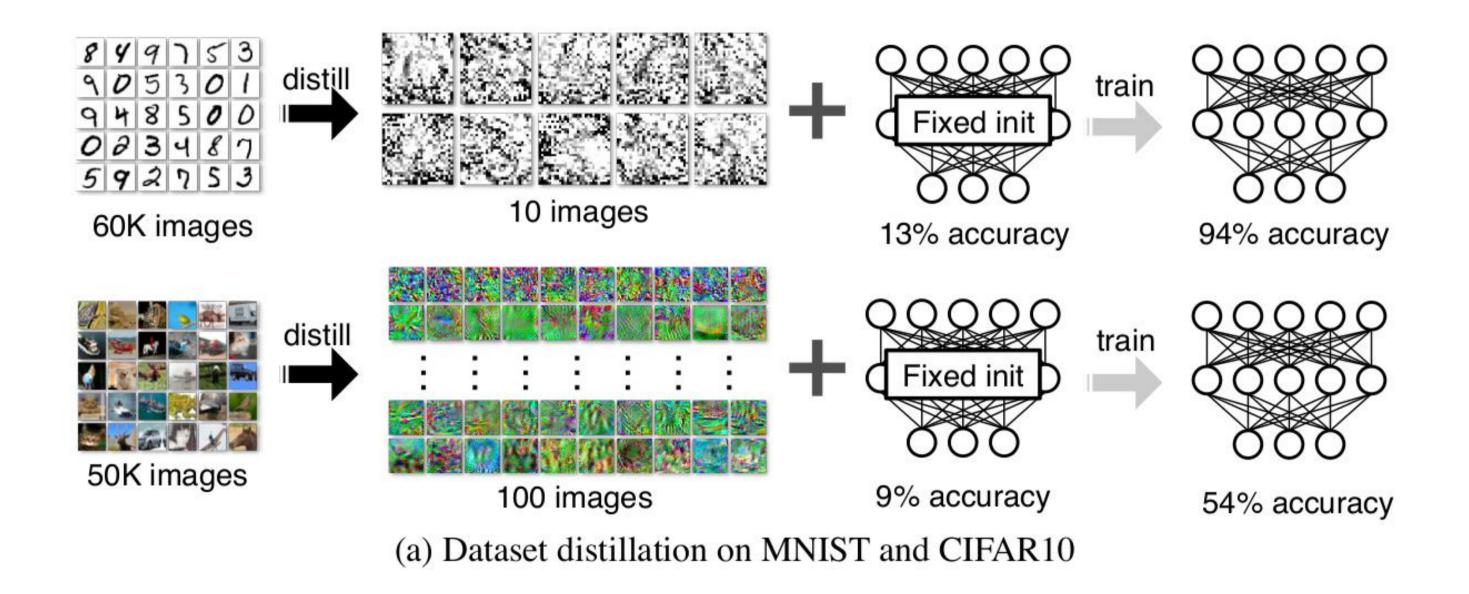
Satisfy for any 
$$\theta_0 \longrightarrow \mathbf{I} - \frac{\tilde{\eta}}{M} \tilde{\mathbf{d}}^T \tilde{\mathbf{d}} = \mathbf{0}, \longrightarrow \tilde{\mathbf{d}}^T \tilde{\mathbf{d}}$$
 has full rank and  $M \geq D$ .

any small number of distilled data fail to generalize to arbitrary initial  $heta_0$ 

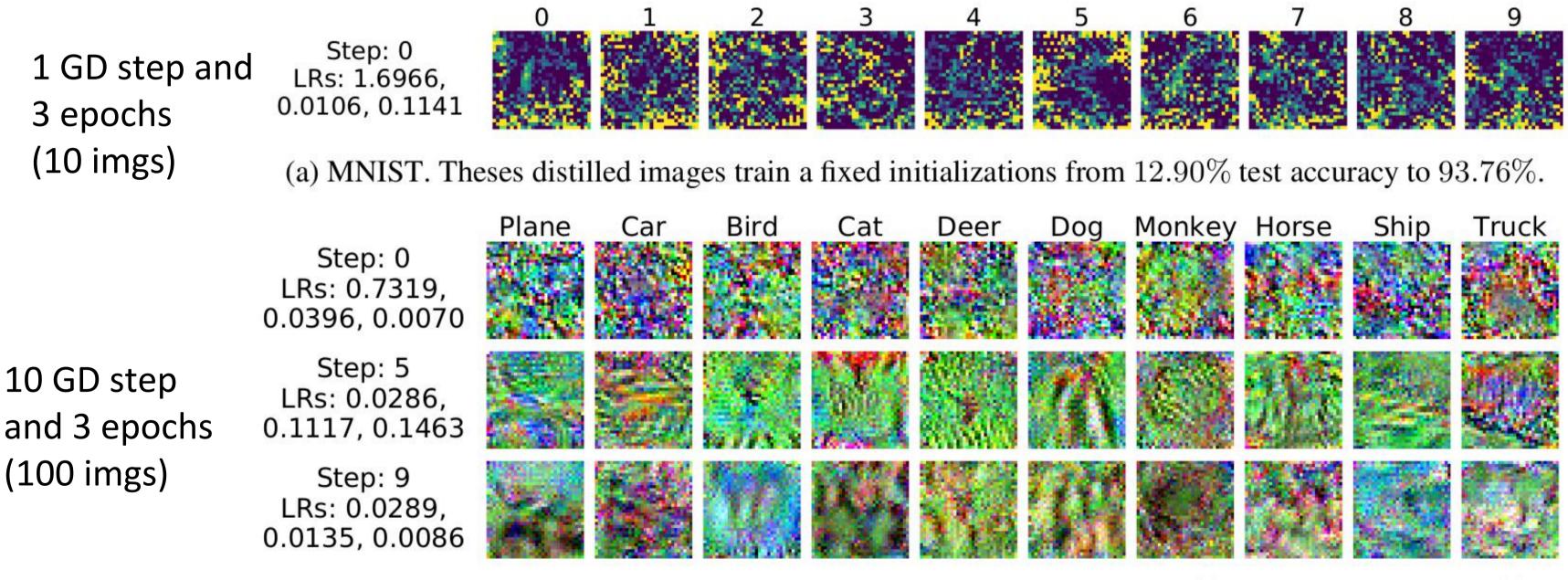
### Multiple GD steps and epochs

```
Algorithm 1 Dataset Distillation
Input: p(\theta_0): distribution of initial weights; M: the number of distilled data
Input: \alpha: step size; n: batch size; T: the number of optimization iterations; \tilde{\eta}_0: initial value for \tilde{\eta}
 1: Initialize \tilde{\mathbf{x}} = {\{\tilde{x}_i\}_{i=1}^{M} \text{ randomly, } \tilde{\eta} \leftarrow \tilde{\eta}_0}
                                                                                        multiple epochs over the same sequence of distilled data
 2: for each training step t = 1 to T do
            Get a minibatch of real training data \mathbf{x}_t = \{x_{t,j}\}_{j=1}^n
 3:
            Sample a batch of initial weights \theta_0^{(j)} \sim p(\theta_0)
 4:
           for each sampled \theta_0^{(j)} do
 5:
                  Compute updated parameter with GD: \theta_1^{(j)} = \theta_0^{(j)} - \tilde{\eta} \nabla_{\theta_0^{(j)}} \ell(\tilde{\mathbf{x}}, \theta_0^{(j)})  \theta_{i+1} = \theta_i - \tilde{\eta}_i \nabla_{\theta_i} \ell(\tilde{\mathbf{x}}_i, \theta_i),
 6:
                  Evaluate the objective function on real training data: \mathcal{L}^{(j)} = \ell(\mathbf{x}_t, \theta_1^{(j)})
 8:
           end for
            Update \tilde{\mathbf{x}} \leftarrow \tilde{\mathbf{x}} - \alpha \nabla_{\tilde{\mathbf{x}}} \sum_{j} \mathcal{L}^{(j)}, and \tilde{\eta} \leftarrow \tilde{\eta} - \alpha \nabla_{\tilde{\eta}} \sum_{i} \mathcal{L}^{(j)}
                                                                                                                                   back propagate through all steps, using
 9:
                                                                                                                                   HVP to accelerate
10: end for
Output: distilled data \tilde{\mathbf{x}} and optimized learning rate \tilde{\eta}
```

#### Fixed initialization



#### Fixed initialization

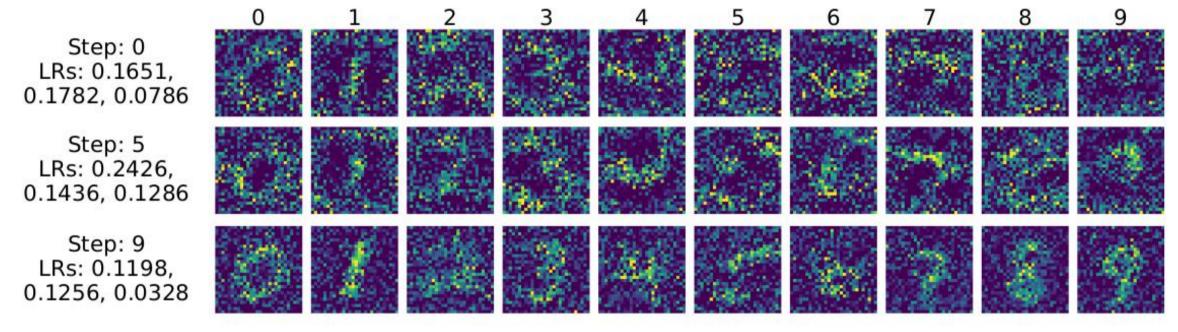


(b) CIFAR10. These distilled images train a fixed initialization from 8.82% test accuracy to 54.03%.

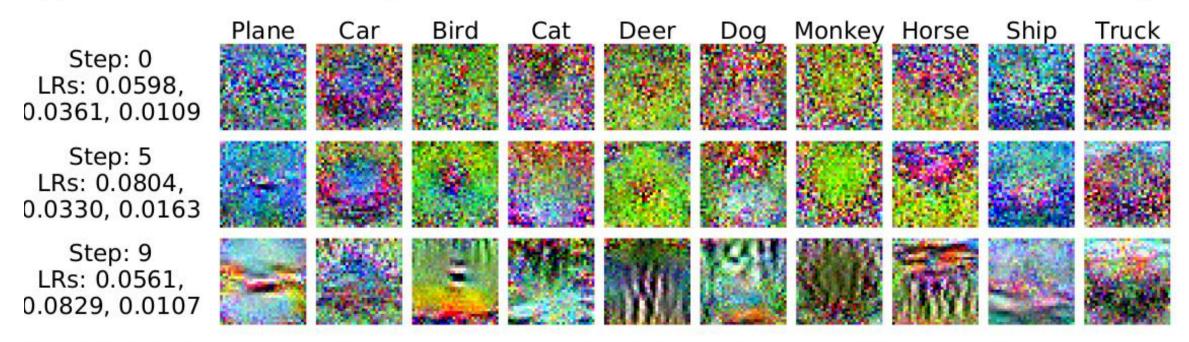
look like random noise as it encodes x and  $\theta_0$ 

Random initialization (Xavier Initialization)

10 GD step and 3 epochs (100 imgs)



(a) MNIST. These distilled images unknown random initializations to  $79.50\% \pm 8.08\%$  test accuracy.



(b) CIFAR10. These distilled images unknown random initializations to  $36.79\% \pm 1.18\%$  test accuracy.

each step containing one image per category.

Images used in early steps tend to look noisier

Compare with baseline (Lenet)

	Ours		Baselines							
	Fixed init.	Random init.	Used as t	raining data in sar	Used in K-NN classification					
	Tixed iiit.		Random real	Optimized real	k-means	Average real	Random real	k-means		
MNIST	96.6	$79.5 \pm 8.1$	$68.6 \pm 9.8$	$73.0 \pm 7.6$	$76.4 \pm 9.5$	$77.1 \pm 2.7$	$71.5 \pm 2.1$	$92.2 \pm 0.1$		
CIFAR10	54.0	$36.8 \pm 1.2$	$21.3 \pm 1.5$	$23.4 \pm 1.3$	$22.5 \pm 3.1$	$22.3 \pm 0.7$	$18.8 \pm 1.3$	$29.4 \pm 0.3$		

99% 80%

- Random real images
- Optimized real images -> top 20% from random sets
- k-means -> use cluster centroids for each category
- Average real images -> average image
- All methods use ten images per category (100 in total) except average real

Hyper-parameter sensitivity studies

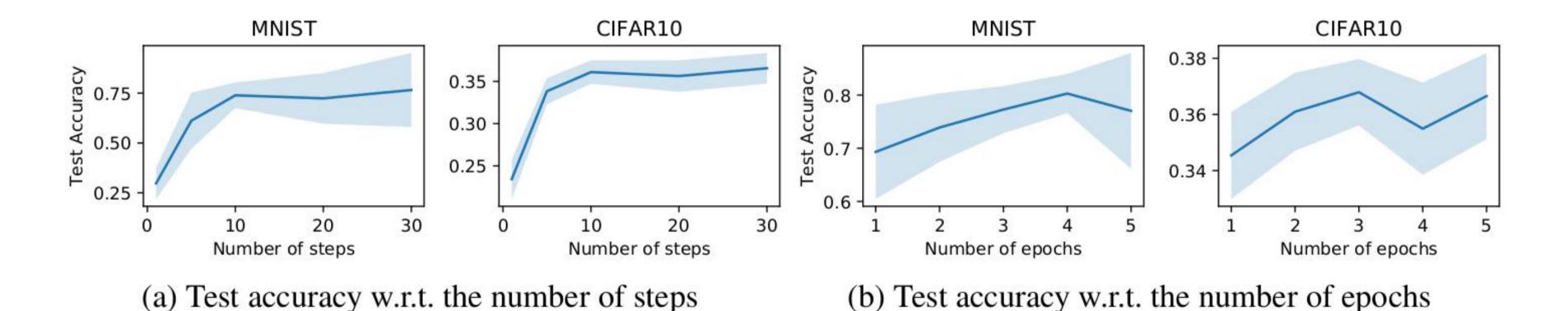


Figure 4: Hyper-parameter sensitivity studies: we evaluate models in *random initialization* settings. (a) Average test accuracy w.r.t. the number of GD steps. We use two epochs. (b) Average test accuracy w.r.t. the number of epochs. We use 10 steps, with each step containing 10 images.

### Few-shot domain adaptation

	Ours w/ fixed pre-trained	Ours w/ random pre-trained	Random real	Optimized real	k-means	Average real	Adaptation Motiian et al. (2017)	No adaptation	Train on <b>full</b> target dataset
$\mathcal{M}  o \mathcal{U}$	97.9	$95.4 \pm 1.8$	$94.9 \pm 0.8$	$95.2 \pm 0.7$	$92.2 \pm 1.6$	$93.9 \pm 0.8$	$96.7 \pm 0.5$	$90.4 \pm 3.0$	$97.3 \pm 0.3$
$\mathcal{U}  o \mathcal{M}$	93.2	$92.7 \pm 1.4$	$87.1 \pm 2.9$	$87.6 \pm 2.1$	$85.6 \pm 3.1$	$78.4 \pm 5.0$	$89.2 \pm 2.4$	$67.5 \pm 3.9$	$98.6 \pm 0.5$
$\mathcal{S}  o \mathcal{M}$	96.2	$85.2 \pm 4.7$	$84.6 \pm 2.1$	$85.2 \pm 1.2$	$85.8 \pm 1.2$	$74.9 \pm 2.6$	$74.0 \pm 1.5$	$51.6 \pm 2.8$	$98.6 \pm 0.5$

Table 2: Performance of our method and baselines in adapting models among MNIST  $(\mathcal{M})$ , USPS  $(\mathcal{U})$ , and SVHN  $(\mathcal{S})$ . 100 distilled images are trained for ten GD steps and three epochs. Our method outperforms few-shot domain adaptation (Motiian et al., 2017) and other baselines in most settings.

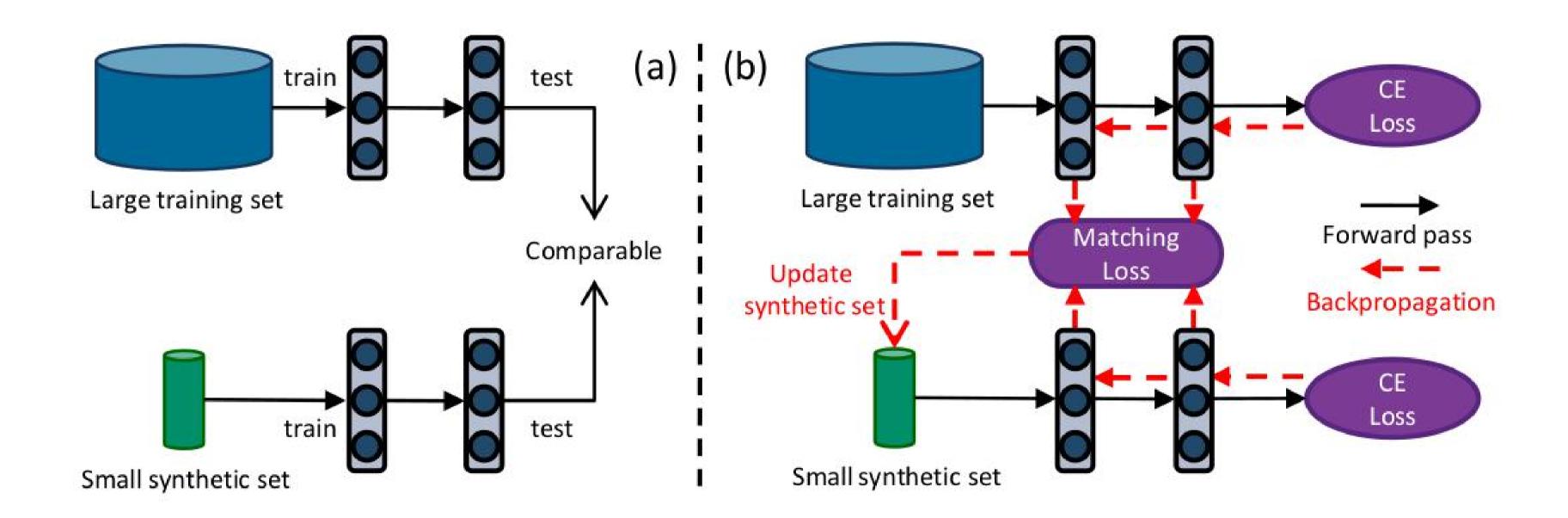
#### DATASET CONDENSATION WITH GRADIENT MATCHING

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ICLR 2021

## Motivation

- Coreset construction
  - continual learning, active learning ...
  - compactness, diversity, forgetfulness ...
  - not guarantee for downstream tasks and presence of representative samples
- Datset Distillation
  - synthesize informative samples by optimization



learning a synthetic set such that a deep network trained on it and the large set produces similar gradients w.r.t. its weights.

$$\boldsymbol{\theta}^{\mathcal{T}} = \underset{\boldsymbol{\theta}}{\operatorname{arg\,min}} \mathcal{L}^{\mathcal{T}}(\boldsymbol{\theta}) \qquad |\mathcal{S}| \ll |\mathcal{T}|$$

$$\mathcal{L}^{\mathcal{T}}(\boldsymbol{\theta}) = \frac{1}{|\mathcal{T}|} \sum_{(\boldsymbol{x}, y) \in \mathcal{T}} \ell(\phi_{\boldsymbol{\theta}}(\boldsymbol{x}), y) \qquad |\mathcal{S}| \ll |\mathcal{T}|$$

$$\mathcal{L}^{\mathcal{S}}(\boldsymbol{\theta}) = \frac{1}{|\mathcal{S}|} \sum_{(\boldsymbol{s}, y) \in \mathcal{S}} \ell(\phi_{\boldsymbol{\theta}}(\boldsymbol{s}), y)$$

Discussion

$$\mathcal{S}^* = \underset{\mathcal{S}}{\operatorname{arg\,min}} \mathcal{L}^{\mathcal{T}}(\boldsymbol{\theta}^{\mathcal{S}}(\mathcal{S}))$$
 subject to  $\boldsymbol{\theta}^{\mathcal{S}}(\mathcal{S}) = \underset{\boldsymbol{\theta}}{\operatorname{arg\,min}} \mathcal{L}^{\mathcal{S}}(\boldsymbol{\theta}).$ 

- nested loop optimization
- unrolling the recursive computation graph over multiple steps

- Optimization
  - lacktriangle comparable performance && similar in parameter space  $m{ heta}^{\mathcal{S}} pprox m{ heta}^{\mathcal{T}}$
  - assume similar weights imply similar performance

$$\min_{\mathcal{S}} D(\boldsymbol{\theta}^{\mathcal{S}}, \boldsymbol{\theta}^{\mathcal{T}}) \quad \text{subject to} \quad \boldsymbol{\theta}^{\mathcal{S}}(\mathcal{S}) = \arg\min_{\boldsymbol{\theta}} \mathcal{L}^{\mathcal{S}}(\boldsymbol{\theta})$$

 $oldsymbol{ heta}^{\mathcal{T}}$  depends on  $oldsymbol{ heta}_0$ 

$$\min_{\mathcal{S}} \mathrm{E}_{\boldsymbol{\theta}_0 \sim P_{\boldsymbol{\theta}_0}} [D(\boldsymbol{\theta}^{\mathcal{S}}(\boldsymbol{\theta}_0), \boldsymbol{\theta}^{\mathcal{T}}(\boldsymbol{\theta}_0))] \quad \text{subject to} \quad \boldsymbol{\theta}^{\mathcal{S}}(\mathcal{S}) = \arg\min_{\boldsymbol{\theta}} \mathcal{L}^{\mathcal{S}}(\boldsymbol{\theta}(\boldsymbol{\theta}_0))$$

• back-optimization approach (fixed steps  $(\varsigma)$ )

$$oldsymbol{ heta}^{\mathcal{S}}(\mathcal{S}) = ext{opt-alg}_{oldsymbol{ heta}}(\mathcal{L}^{\mathcal{S}}(oldsymbol{ heta}), arsigma)$$

distance can be large and fixed steps may be not enough

- Curriculum based approach
  - follow a similar path throughout the optimization

$$\min_{\mathcal{S}} \mathrm{E}_{\boldsymbol{\theta}_0 \sim P_{\boldsymbol{\theta}_0}} [\sum_{t=0}^{T-1} D(\boldsymbol{\theta}_t^{\mathcal{S}}, \boldsymbol{\theta}_t^{\mathcal{T}})] \quad \text{subject to}$$
 
$$\boldsymbol{\theta}_{t+1}^{\mathcal{S}}(\mathcal{S}) = \mathrm{opt-alg}_{\boldsymbol{\theta}}(\mathcal{L}^{\mathcal{S}}(\boldsymbol{\theta}_t^{\mathcal{S}}), \varsigma^{\mathcal{S}}) \quad \text{and} \quad \boldsymbol{\theta}_{t+1}^{\mathcal{T}} = \mathrm{opt-alg}_{\boldsymbol{\theta}}(\mathcal{L}^{\mathcal{T}}(\boldsymbol{\theta}_t^{\mathcal{T}}), \varsigma^{\mathcal{T}})$$

• In preliminary experiments  $D(\boldsymbol{\theta}_t^{\mathcal{S}}, \boldsymbol{\theta}_t^{\mathcal{T}}) \rightarrow \mathbf{0}$ 

$$\boldsymbol{\theta}_{t+1}^{\mathcal{S}} \leftarrow \boldsymbol{\theta}_{t}^{\mathcal{S}} - \eta_{\boldsymbol{\theta}} \nabla_{\boldsymbol{\theta}} \mathcal{L}^{\mathcal{S}}(\boldsymbol{\theta}_{t}^{\mathcal{S}}) \quad \text{and} \quad \boldsymbol{\theta}_{t+1}^{\mathcal{T}} \leftarrow \boldsymbol{\theta}_{t}^{\mathcal{T}} - \eta_{\boldsymbol{\theta}} \nabla_{\boldsymbol{\theta}} \mathcal{L}^{\mathcal{T}}(\boldsymbol{\theta}_{t}^{\mathcal{T}}),$$

$$\min_{\mathcal{S}} \mathrm{E}_{\boldsymbol{\theta}_0 \sim P_{\boldsymbol{\theta}_0}} [\sum_{t=0}^{T-1} D(\nabla_{\boldsymbol{\theta}} \mathcal{L}^{\mathcal{S}}(\boldsymbol{\theta}_t), \nabla_{\boldsymbol{\theta}} \mathcal{L}^{\mathcal{T}}(\boldsymbol{\theta}_t))].$$

does not require the expensive unrolling

#### Algorithm 1: Dataset condensation with gradient matching

**Input:** Training set  $\mathcal{T}$ 

**Required**: Randomly initialized set of synthetic samples S for C classes, probability distribution over randomly initialized weights  $P_{\theta_0}$ , deep neural network  $\phi_{\theta}$ , number of outer-loop steps K, number of inner-loop steps T, number of steps for updating weights  $\varsigma_{\theta}$  and synthetic samples  $\varsigma_{S}$  in each inner-loop step respectively, learning rates for updating weights  $\eta_{\theta}$  and synthetic samples  $\eta_{S}$ .

```
2 for k=0,\cdots,K-1 do Loop for initialization
              Initialize \theta_0 \sim P_{\theta_0}
3
              for t = 0, \dots, T - 1 do steps
4
                       for c = 0, \dots, C - 1 do class
5
                                 Sample a minibatch pair B_c^{\mathcal{T}} \sim \mathcal{T} and B_c^{\mathcal{S}} \sim \mathcal{S} \triangleright B_c^{\mathcal{T}} and B_c^{\mathcal{S}} are of the same class c.
6
                               Compute \mathcal{L}_c^{\mathcal{T}} = \frac{1}{|B_c^{\mathcal{T}}|} \sum_{(\boldsymbol{x},y) \in B_c^{\mathcal{T}}} \ell(\phi_{\boldsymbol{\theta}_t}(\boldsymbol{x}), y) and \mathcal{L}_c^{\mathcal{S}} = \frac{1}{|B_c^{\mathcal{S}}|} \sum_{(\boldsymbol{s},y) \in B_c^{\mathcal{S}}} \ell(\phi_{\boldsymbol{\theta}_t}(\boldsymbol{s}), y)
7
                          Update S_c \leftarrow \text{opt-alg}_{S}(D(\nabla_{\theta}\mathcal{L}_c^{S}(\theta_t), \nabla_{\theta}\mathcal{L}_c^{T}(\theta_t)), \varsigma_{S}, \eta_{S})
8
                       Update \boldsymbol{\theta}_{t+1} \leftarrow \text{opt-alg}_{\boldsymbol{\theta}}(\mathcal{L}^{\mathcal{S}}(\boldsymbol{\theta}_t), \varsigma_{\boldsymbol{\theta}}, \eta_{\boldsymbol{\theta}})
                                                                                                                                                                                                          \triangleright Use the whole S
9
```

Output: S

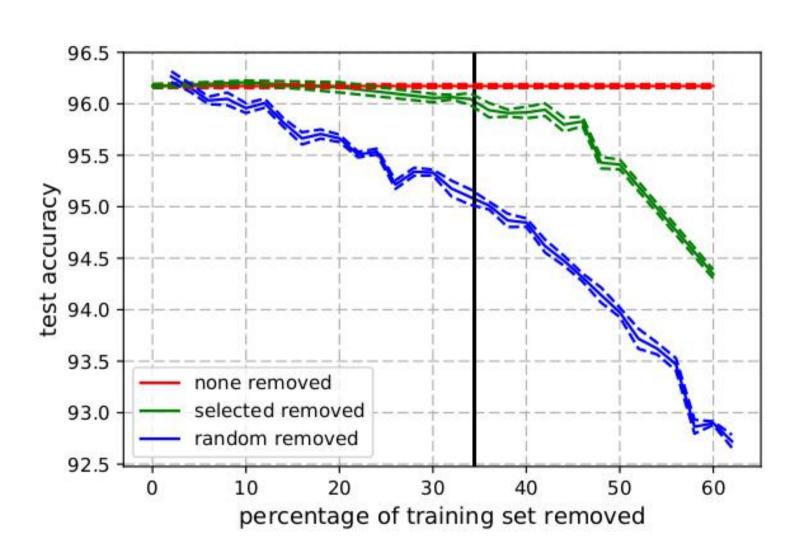
- Matching loss  $D(\cdot, \cdot)$ 
  - different layers -> different parameter shape
  - MLP: 2D (out×in), CNN: 4D (out×in×h×w)

$$D(\nabla_{\boldsymbol{\theta}} \mathcal{L}^{\mathcal{S}}, \nabla_{\boldsymbol{\theta}} \mathcal{L}^{\mathcal{T}}) = \sum_{l=1}^{L} d(\nabla_{\boldsymbol{\theta}^{(l)}} \mathcal{L}^{\mathcal{S}}, \nabla_{\boldsymbol{\theta}^{(l)}} \mathcal{L}^{\mathcal{T}})$$
$$d(\mathbf{A}, \mathbf{B}) = \sum_{i=1}^{\text{out}} \left( 1 - \frac{\mathbf{A_{i\cdot}} \cdot \mathbf{B_{i\cdot}}}{\|\mathbf{A_{i\cdot}}\| \|\mathbf{B_{i\cdot}}\|} \right)$$
$$\text{cosine similarity}$$

 ${f A}_i$  and  ${f B}_i$  are flattened gradients corresponding to each output node i

- Baseline
  - random, DD
  - Herding baseline-> nearest to cluster center
  - K-Center-> multiple center points
  - Forgetting method [1]

the unforgettable examples contain less information



[1] An Empirical Study of Example Forgetting during Deep Neural Network Learning, Mariya Toneva, Alessandro Sordoni, Remi Tachet des Combes, Adam Trischler, Yoshua Bengio, Geoffrey J. Gordon, ICLR 2019.

	Img/Cls	Ratio %	Random	Coreset Herding	Selection K-Center	Forgetting	Ours	Whole Dataset
MNIST	1 10 50	0.017 0.17 0.83	64.9±3.5 95.1±0.9 97.9±0.2	89.2±1.6 93.7±0.3 94.9±0.2	89.3±1.5 84.4±1.7 97.4±0.3	35.5±5.6 68.1±3.3 88.2±1.2	$91.7{\pm}0.5$ $97.4{\pm}0.2$ $98.8{\pm}0.2$	99.6±0.0
FashionMNIST	1 10 50	0.017 0.17 0.83	51.4±3.8 73.8±0.7 82.5±0.7	$67.0\pm1.9$ $71.1\pm0.7$ $71.9\pm0.8$	66.9±1.8 54.7±1.5 68.3±0.8	42.0±5.5 53.9±2.0 55.0±1.1	$70.5\pm0.6\ 82.3\pm0.4\ 83.6\pm0.4$	93.5±0.1
SVHN	1 10 50	0.014 0.14 0.7	14.6±1.6 35.1±4.1 70.9±0.9	$20.9\pm1.3$ $50.5\pm3.3$ $72.6\pm0.8$	$21.0\pm1.5$ $14.0\pm1.3$ $20.1\pm1.4$	$12.1\pm1.7$ $16.8\pm1.2$ $27.2\pm1.5$	31.2±1.4 76.1±0.6 82.3±0.3	95.4±0.1
CIFAR10	1 10 50	0.02 0.2 1	14.4±2.0 26.0±1.2 43.4±1.0	$21.5\pm1.2$ $31.6\pm0.7$ $40.4\pm0.6$	$21.5\pm1.3$ $14.7\pm0.9$ $27.0\pm1.4$	$13.5\pm1.2$ $23.3\pm1.0$ $23.3\pm1.1$	28.3±0.5 44.9±0.5 53.9±0.5	84.8±0.1

ConvNet is used for training and testing, commonly used in fewshot learning

### Comapre with DD

Dataset	Img/Cls	DD	Ours	Whole Dataset
MNIST	1 10	- 79.5±8.1	85.0±1.6 <b>93.9±0.6</b>	99.5±0.0
CIFAR10	1 10	- 36.8±1.2	24.2±0.9 39.1±1.2	83.1±0.2

Table 3: Comparison to DD (Wang et al., 2018) in terms of testing accuracy (%).

2 times faster and more consistent results over multiple runs

#### Visualization

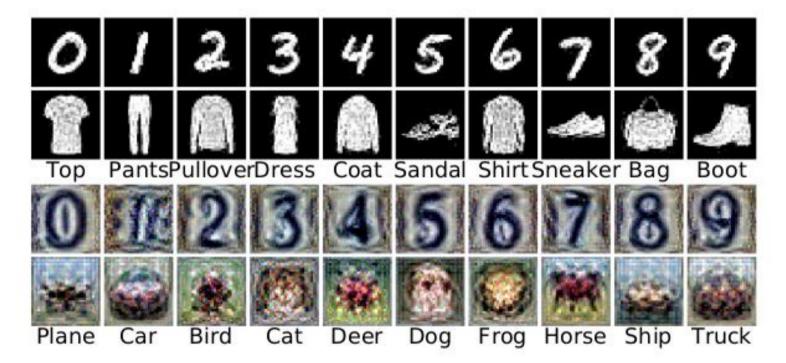


Figure 2: Visualization of condensed 1 image/class with ConvNet for MNIST, Fashion-MNIST, SVHN and CIFAR10.

### Cross-architecture performance

C\T	MLP	ConvNet	LeNet	AlexNet	VGG	ResNet
MLP	$70.5 \pm 1.2$	$63.9 \pm 6.5$	77.3±5.8	$70.9 \pm 11.6$	53.2±7.0	80.9±3.6
ConvNet	$69.6 \pm 1.6$	$91.7 \pm 0.5$	$85.3 \pm 1.8$	$85.1 \pm 3.0$	$83.4 \pm 1.8$	$90.0 \pm 0.8$
LeNet	$71.0 \pm 1.6$	$90.3 \pm 1.2$	$85.0 \pm 1.7$	$84.7 \pm 2.4$	$80.3 \pm 2.7$	$89.0 \pm 0.8$
AlexNet	$72.1 \pm 1.7$	$87.5 \pm 1.6$	$84.0 \pm 2.8$	$82.7 \pm 2.9$	$81.2 \pm 3.0$	$88.9 \pm 1.1$
VGG	$70.3 \pm 1.6$	$90.1 \pm 0.7$	$83.9 \pm 2.7$	$83.4 \pm 3.7$	$81.7 \pm 2.6$	$89.1 \pm 0.9$
ResNet	$73.6 \pm 1.2$	$91.6 \pm 0.5$	$86.4 \pm 1.5$	85.4±1.9	$83.4 \pm 2.4$	$89.4 \pm 0.9$

Table 2: Cross-architecture performance in testing accuracy (%) for condensed 1 image/class in MNIST.

mlp generated pics performs badly for cnn, while cnn generated pics perform well for other mlp

### Continual Learning

testing accuracies are computed by averaging performance after each stage (SVHN→MNIST→USPS)

10 images/class

KD: regularize output vs previous

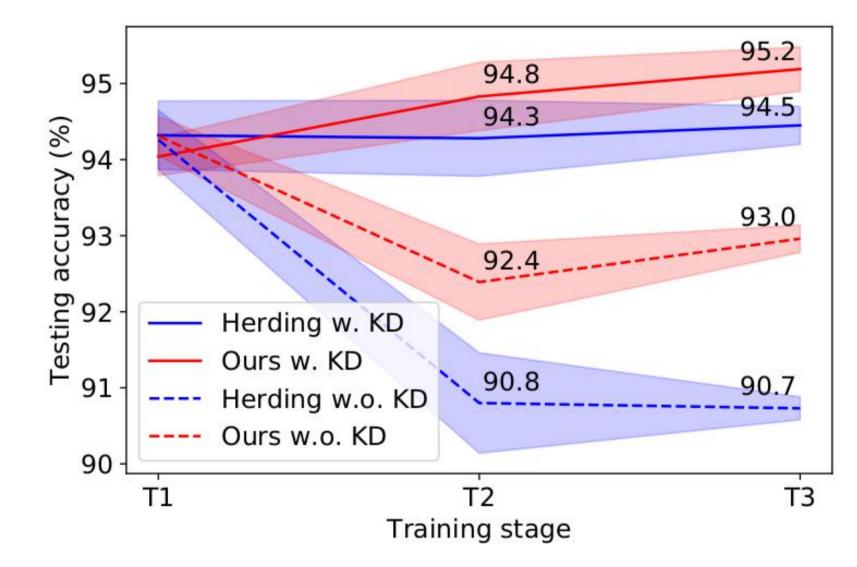


Figure 4: Continual learning performance in accuracy (%). Herding denotes the original E2E (Castro et al. 2018). T1, T2, T3 are three learning stages. The performance at each stage is the mean testing accuracy on all learned tasks.