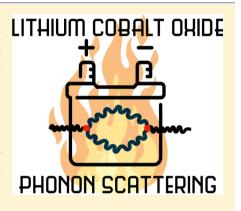


Highly Anisotropic Thermal Transport in LiCoO₂

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Supporting Information

ABSTRACT: LiCoO₂ is the prototypical cathode in lithium-ion batteries. Its crystal structure consists of Li⁺ and CoO₂⁻ layers that alternate along the hexagonal (0001) axis. It is well established that the ionic and electronic conduction are anisotropic, but little is known regarding the heat transport. We analyze the phonon dispersion and lifetimes using anharmonic lattice dynamics based on quantumchemical force constants. Around room temperature, the thermal conductivity in the hexagonal ab plane of the layered cathode is ~6 times higher than that along the c axis. An upper limit to the average thermal conductivity at T = 300 K of 38.5 W m⁻¹ K⁻¹ is set by short phonon lifetimes associated with anharmonic interactions within the octahedral face-sharing CoO2 network. Observations of conductivity <10 W m⁻¹ K⁻¹ can be understood by additional scattering channels including grain boundaries in polycrystalline samples. The impact on thermal processes in lithiumion batteries is discussed.



ithium cobalt oxide, LiCoO2, has been widely used as a ✓ cathode material in lithium-ion batteries (LIBs) following its discovery in 1980¹ and its commercialization in the 1990s. The compound offers a number of attractive features including ease of synthesis, reversible lithium insertion, and high specific energy density.^{2,3} LiCoO₂ crystallizes in a layered structure (space group $R\overline{3}m$, Figure 1a) in which CoO_6 and LiO_6 octahedra form parallel slabs. This layered structure means the material is effectively a 2D ionic and electronic conductor.4,5

Co can be partially replaced by the transition metals Ni and Mn to form the NMC system LiNi, Mn, Co, O, (x + y + z = 1). The Co:Ni:Mn ratio can be tuned to optimize the mechanical and electrochemical performance while reducing cost.^{6,7} Many NMC compositions preserve the same structure type, with some local Jahn-Teller distortions depending on the combination of oxidation states present in the mixed-metal system.6,8

One key challenge for LIBs is to improve lifetimes and safety characteristics without compromising energy and power densities.^{9,10} Thermal management is an important issue and is intimately connected to chemical degradation and battery lifetime. There is a significant gap in knowledge of battery manufacturers and developers on how temperature and thermal management affects capacity/power fade, thermal runaway, and other key characteristics of Li-ion cells. 11 With modern computational techniques many key battery processes can be accurately described by computer simulations, including the defect chemistry and associated ionic and electronic transport. 12 However, little is known regarding heat transport. Very recent work has explored thermal conductivity of battery anode 13,14 and cathode 15 materials using molecular dynamics

In this Letter, we assess the lattice dynamics and thermal transport of LiCoO2 within phonon many-body perturbation theory. For the harmonic phonon dispersion, we find a sensitivity to the choice of the density-functional theory (DFT) electron exchange and correlation functional. Using the HSE06 hybrid functional with the Tkatchenko-Scheffler dispersion correction, we calculate the lifetime and heat conduction of each phonon mode to evaluate the modal contributions to the macroscopic lattice thermal conductivity. We predict values of 53.6 W m⁻¹ K⁻¹ (hexagonal ab plane) and 8.4 W m⁻¹ K⁻¹ (c axis) at room temperature in the pristine

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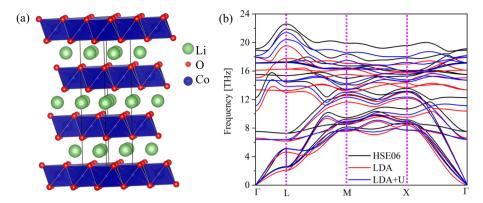


Figure 1. (a) Layered crystal structure of LiCoO₂ with spacegroup $R\overline{3}m$, where the stacking is along the hexagonal c axis. This image was generated using VESTA.¹⁶ (b) Calculated phonon dispersion of LiCoO₂ using three DFT exchange–correlation functionals and a $3 \times 3 \times 3$ supercell to calculate the harmonic force constants.

LiCoO₂ crystal. The origin and impact of this large anisotropy is explored.

Phonon Dispersion. The harmonic phonon dispersion of LiCoO₂ is shown in Figure 1b. The positive (real) frequencies across the vibrational Brillouin zone confirm a dynamically stable structure. The four atoms in the primitive (rhombohedral setting) unit cell result in 12 (3N) phonon modes. A group theoretic analysis within the D_{3d} point group assigns the irreducible representations of the acoustic ($A_{2u} + E_u$) and optic branches ($A_{1g} + 2A_{2u} + 2E_u + E_g$). Of these, the $2A_{2u} + 2E_u$ modes are infrared (IR) active and the $A_{1g} + E_g$ modes are Raman active.

The low-spin d^6 configuration of Co(III) in pristine LiCoO₂ avoids the more complex electronic structures associated with the Co(II) and Co(IV) species. However, we still expect some sensitivity to the choice of DFT exchange–correlation functional, as the localized wave functions of 3d transition metals are susceptible to self-interaction errors.¹⁷

The LDA and LDA+U functionals produce qualitatively similar phonon dispersion, in agreement with the work of Du and co-workers. However, the inclusion of nonlocal exchange with HSE06 and the Tkhatchenko–Scheffler dispersion to describe the interlayer interactions results in a stiffening of the frequencies of the optic branches (also observed in other dielectric materials 18). A comparison with available experimental data is given in Table 1. For example, IR measurements place an E_u mode at 7.8 THz, which compares to 7.6 THz from HSE06, while LDA/LDA+U predict a value at \sim 6 THz. Care should, however, be taken with direct comparison

Table 1. Comparison of Phonon Frequencies for Selected Modes at the Γ Point in the Vibrational Brillouin Zone of LiCoO_2^a

method	A_{1g}	$\mathbf{E}_{\mathbf{g}}$	A_{2u}	E_{u}
LDA	18.09	14.30	12.25	7.64
$\mathrm{LDA} + U$	17.95	14.73	11.14	6.42
HSE06	19.12	15.52	12.27	7.53
HSE06+TS	19.17	15.62	12.81	7.56
exp	17.87 ^b	14.57 ^b	12.59 ^c	7.80^{c}

^aThe five rows compare the calculated frequencies (THz) obtained with four different DFT exchange-correlation functionals (TS denotes the Tkatchenko-Scheffler dispersion correction) to room-temperature IR and Raman spectra. ^bRaman active modes. ¹⁹ ^cIR active modes. ²⁰

with experiment as the predictions do not include finite-temperature effects such as thermal expansion and higher-order anharmonic frequency shifts due to phonon—phonon interactions. We would generally expect volume expansion at finite temperature to soften the phonon frequencies, and hence our calculated frequencies to be overestimated compared to the room-temperature measurements.

Lattice Thermal Conductivity. The lattice thermal conductivity of a crystalline material (κ) depends on the nature of its heat-carrying vibrations. Formally, each phonon mode makes a contribution to the macroscopic thermal conductivity given by the product of the modal heat capacity (C_V) , the group velocity (ν) , and the phonon mean-free path $(\nu \times \tau)$, where τ is the phonon lifetime). The macroscopic κ is obtained by summing over band indices (ν) , averaging over wavevectors (q) and normalizing by the cell volume:

$$\kappa = \frac{1}{NV_0} \sum_{q\nu} C_{V,q\nu} \nu_{q\nu} \otimes \nu_{q\nu} \tau_{q\nu} \tag{1}$$

where N is the number of unit cells in the crystal (equivalent to the number of wavevectors included in the Brillouin zone summation) and V_0 is the volume of the crystallographic unit cell. The heat capacity and group velocity can be determined from the harmonic phonon dispersion (Figure 1b), but lifetime is ill-defined (infinite) in the harmonic approximation due to absence of phonon—phonon interactions.

We calculate the lifetime of each phonon mode within phonon many-body perturbation theory by taking into account the leading term of three-phonon scattering processes. ²¹ Our calculated thermal conductivity is plotted in Figure 2. The conductivity decays exponentially with increasing temperature and is found to be highly anisotropic: around room temperature, the thermal conductivity in the hexagonal ab plane is 53.6 W m⁻¹ K⁻¹, while the value along the c axis is 8.4 W m⁻¹ K⁻¹.

The experimentally measured thermal conductivity is as low as 4 W m $^{-1}$ K $^{-1}$ at 280 K, 22 which is slightly below our calculated result along the c axis. Our predictions should represent an upper limit for pristine single crystals, as in real, imperfect samples other scattering processes occur due to extended (e.g., dislocations and grain boundaries) and point (e.g., Li_{Co} antisite) defects. Indeed, recent classical molecular dynamics simulations using empirical potentials predict that polycrystalline LiCoO $_2$ has a greatly reduced thermal conductivity. We find that the experimental value of thermal

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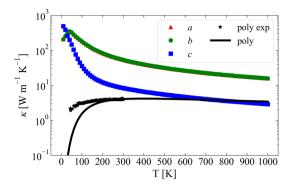


Figure 2. Calculated lattice thermal conductivity (κ) of LiCoO₂ along the a, b, and c axes. The corresponding modal accumulation functions are presented in the Supporting Information. The experimental data²² were measured on polycrystalline samples using a steady-state technique (poly exp). The black line is a simulation of a polycrystalline (poly) sample of LiCoO₂ with $\kappa_{\rm average} = \frac{1}{3}(\kappa_a + \kappa_b + \kappa_c)$ and a boundary-scattering model that limits the mean-free path to an average grain size; the experimental measurements are well reproduced with a limit of 2 nm.

conductivity in polycrystalline samples can be reproduced if the phonon mean-free path length is limited to a threshold value of 2 nm (see Figure 2).

Original of Anisotropic Transport. Phonon lifetimes and mean-free paths have only recently become accessible to firstprinciples calculations, and the majority of available data is on face-centered cubic systems. 21,23,24 In comparison to tetrahedral semiconductors with simpler structures such as GaAs and CdTe, 25 the average strength of the three-phonon interactions in LiCoO₂ is 3 orders of magnitude larger, and the associated phonon lifetimes of LiCoO₂ are correspondingly 3 orders of magnitude shorter (see Figure 3). To investigate the origin of the directional anisotropy, we analyzed separately the model contributions to the thermal conductivity. The analysis in Figure 3 shows that the modes that make the largest contributions to the thermal transport are those that have faster group velocities (panel a and b) and longer modal lifetimes (panels c and d), and hence longer mean-free paths (panels e and f). The longest calculated mean-free path of the heat carrying modes is 44 nm in the ab plane and 446 nm along the c axis in the perfect crystal. However, the thermal conductivity is a summation over the phonon Brillouin zone (cf. eq 1), and the lower density of long-lived modes along the c axis results results in shorter average path lengths of 1.6 nm compared to 3.9 nm in the ab plane.

Heat generation during the charge—discharge process of a battery can exceed 1 W/cm³ depending on the cycling rate. This is due to a combination of resistive heating from ion and electron transport together with changes in entropy. Simulations of battery components typically assume isotropic thermal transport, which we have shown is not the case. The thermal stability of LiCoO₂ is known to be poor, which can lead to thermal runaway under high-temperature operation or overcharging. This could be avoided by tuning the grain size distributions in combination with active binders that act as heat sinks in a composite electrode structure.

The lattice thermal conductivity of NMC compositions will be even lower than LiCoO₂ owing to the additional phonon scattering from cation disorder and the associated spatial inhomogeneity in the phonon frequencies and lifetimes. This also introduces a technical challenge for modeling, which

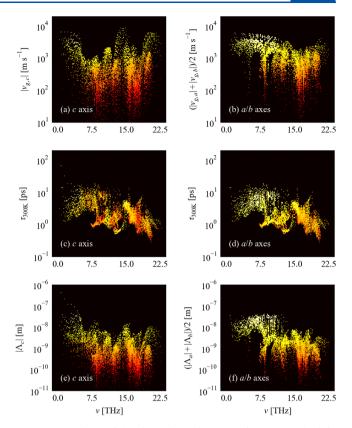


Figure 3. Analysis of the thermal conductivity of LiCoO₂. The left-and right-hand columns show transport along the c direction and in the ab plane, respectively. Subplots (a) and (b) show the spectrum of group velocities, subplots (c) and (d) show the modal lifetimes, and subplots (e) and (f) show the mean-free paths. The heat maps are color coded by the modal contributions to κ , from red (low) to yellow (high).

would need to consider an ensemble of transition metal and oxidation state distributions for force constant calculations. Beyond shorter phonon lifetimes, however, cation disorder may also provide a kinetic barrier to the formation of secondary phases, which could account for the overall improved stability of the NMC compositions.

The impact of thermal effects on anion redox has recently been highlighted, where heat dissipation contributes to voltage hysteresis upon battery cycling.²⁸ Investigation of the coupling between the vibrational modes of defects with bulk phonon transport is a worthwhile direction for future research.

To conclude, the thermal conductivity in $LiCoO_2$ is highly anisotropic, with a 6 times larger κ in the in-plane direction. First-principles analysis of the harmonic phonon dispersion and anharmonic phonon—phonon interactions reveal that the anisotropy largely originates from differences in the group velocity of the heat-carrying phonon modes, in particular the number of modes with larger in-plane than out-of-plane velocities. We found that the hybrid HSE06 exchange—correlation functional provides a good description of the vibrational properties of $LiCoO_2$ and will likely be essential for the commercial NMC system where the mixed-oxidation states of Ni, Mn, and Co exhibit strong electron correlation. Our study provides a robust foundation for advancing our understanding of thermal processes in battery materials.

■ COMPUTATIONAL METHODS

The starting point for the structural relaxation was the experimentally determined structure of LiCoO_2 from the work of Cava and co-workers. The total energy and electronic structure calculations were performed using planewave density-functional theory as implemented in the Vienna Ab initio Simulation Package. A plane-wave basis set with a 600 eV cutoff was used to expand the electronic wave functions. Structural relaxation was performed with a $6 \times 6 \times 6$ k-point mesh, for which the total energy was converged to within 1 meV per atom, and a force tolerance of 0.001 eV/Å was set for convergence of the ion positions to ensure accurate atomic positions and lattice parameters.

To account for the weak interlayer interactions in $LiCoO_2$ we also tested the Tkatchenko–Scheffler dispersion³¹ with Hirshfeld partitioning,³² which has been shown to reproduce the experimental lattice parameters²⁹ as well as the Lintercalation energies.^{33,34} For LDA+U, a representative U value of 3.9 V was applied to the Co d orbitals. The hybrid HSE06³⁵ functional was used in both harmonic and anharmonic lattice-dynamics calculations.

The second-order (harmonic) force constants were computed using a $3 \times 3 \times 3$ supercell expansion and a finite-difference displacement step of 10^{-2} Å. The third-order (anharmonic) force constants were also computed using $3 \times 3 \times 3$ expansion but using a larger 3×10^{-2} Å step. The lattice thermal conductivity of LiCoO₂ was obtained by solving the phonon Boltzmann transport equation within the relaxation-time approximation using the Phono3py package.³⁶

ASSOCIATED CONTENT

S Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.jp-clett.9b02073.

Harmonic phonon dispersion; thermal conductivity accumulation functions with phonon frequency (PDF)

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Notes

The authors declare no competing financial interest.

The associated structure files and input/output of the phonon calculations are available in an online data repository at https://doi.org/10.5281/zenodo.3385124.

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