Question 12.13.2.9 If A and B are two events such that $\Pr\left(A\right)=\frac{1}{4}, \Pr\left(B\right)=\frac{1}{2}$ and $\Pr\left(AB\right)=\frac{1}{8}$. Find Pr(A'B').

solution: Since,

$$A'B' = (A+B)' \tag{1}$$

$$\implies \Pr(A'B') = \Pr((A+B)')$$
 (2)

$$=1-\Pr\left(\left(A+B\right)\right)\tag{3}$$

we also know that,

$$Pr((A+B)) = Pr(A) + Pr(B) - Pr(AB)$$
(4)

$$= \frac{1}{4} + \frac{1}{2} - \frac{1}{8}$$

$$= \frac{5}{8}$$
(5)
(6)

$$=\frac{5}{8}\tag{6}$$

Hence, we get

$$\Pr(A'B') = 1 - \frac{5}{8}$$
 (7)
= $\frac{3}{8}$ (8)

$$=\frac{3}{8}\tag{8}$$