#### 1

# Assignment

# Antalene (EE22BTECH11008)

## Question ST 31.2023

Two defective bulbs are present in a set of five bulbs. To remove the two defective bulbs, the bulbs are chosen randomly one by one and tested. If X denotes the minimum number of bulbs that must be tested to find out the two defective bulbs, then Pr(X = 3) (rounded off to two decimal places) equals

### **Solution:**

RV	Values	Description
A	0	1 <sup>st</sup> Bulb defective
	1	1 <sup>st</sup> Bulb non-defective
В	0	2 <sup>nd</sup> Bulb defective
	1	2 <sup>nd</sup> Bulb non-defective
С	0	3 <sup>rd</sup> Bulb defective
	1	3 <sup>rd</sup> Bulb non-defective

TABLE I

RANDOM VARIABLE DECLARATION.

Therefore,

$$p_X(2) = p_{AB}(0,0) (1)$$

$$=\frac{2}{5}\times\frac{1}{4}\tag{2}$$

$$=\frac{1}{10}\tag{3}$$

$$p_X(3) = p_{ABC}(1,0,0) + p_{ABC}(0,1,0) + p_{ABC}(1,1,1)$$
(4)

$$= \frac{3}{5} \times \frac{2}{4} \times \frac{1}{3} + \frac{2}{5} \times \frac{3}{4} \times \frac{1}{3} + \frac{3}{5} \times \frac{2}{4} \times \frac{1}{3}$$
 (5)

$$=\frac{3}{10}\tag{6}$$

$$p_X(4) = p_{ABC}(0, 1, 1) \times \frac{1}{2} + p_{ABC}(1, 0, 1) \times \frac{1}{2} + p_{ABC}(1, 1, 0) \times \frac{1}{2}$$
 (7)

$$= \frac{2}{5} \times \frac{3}{4} \times \frac{2}{3} \times \frac{1}{2} + \frac{3}{5} \times \frac{2}{4} \times \frac{2}{3} \times \frac{1}{2} + \frac{3}{5} \times \frac{2}{4} \times \frac{2}{3} \times \frac{1}{2}$$
 (8)

$$=\frac{3}{10}\tag{9}$$

Hence, The pmf of X is

$$p_X(k) = \begin{cases} 0 & k = 0, 1\\ \frac{1}{10} & k = 2\\ \frac{3}{10} & k = 3, 4\\ 1 & k = 5 \end{cases}$$
 (10)