1500011370_Poisson

December 31, 2018

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In [12]: import numpy as np
         import matplotlib.pyplot as plt
         from math import *
In [28]: # Set maximum iteration
         maxIter = 100
         TOL = 1e-5
         # Set Dimension and delta
         lenX = 6
         lenY = 5 #we set it rectangular
         delta = 1
         # Boundary condition
         Ttop = 100
         Tright = 0
         def Tbottom(x):
             if x \le 6 and x \ge 0:
                 return x(6-x)
             else:
                 return 0
         def Tleft(y):
             if y \le 5 and y \ge 0:
                 return y(5-y)
             else:
                 return 0
         # heat
         q = 1.5
         K = 1.04
         h = 0.4
         k = 1/3
         n = int(lenX/h) # n = 15
         m = int(lenY/k) # m = 15
In [29]: x = np.arange(n)
         y = np.arange(m)
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w = np.zeros((n, m))
         for i in range(1, n):
             x[i] = i * h
             y[i] = i * k
In [30]: _{lambda} = h* h / k* k
         mu = 2*(1+k)
         1 = 1
In [27]: while(1<=maxIter):</pre>
             z = (-pow(h, 2)*(-q/K)+y[m-1]*(5-y[m-1])+
                   _{\rm lambda} * w[1][m-2]+w[2][m-1])/mu
             NORM = abs(z-w[1][m-1])
             w[1][m-1] = z
             for i in range(2, n-1):
                  z = (-pow(h, 2)*(-q/K)+ 0 +w[i-1][m-1]
                       +w[i+1][m-1] +_lambda*w[i][m-2])/mu
                  if abs(w[i][m-1]-z)>NORM:
                      NORM = abs(w[i][m-1]-z)
                  w[i][m-1] = z
             z = (-pow(h, 2)*(-q/K)+ 0 + 0
                   +w[n-2][m-1]+w[n-1][m-2])/mu
             if abs(w[n-1][m-1] - z) > NORM:
                  NORM = abs(w[n-1][m-1] - z)
             w[n-1][m-1] = z
             for j in range(m-2, 1, -1): # from m-2, ...., 2
                  z = (-pow(h, 2)*(-q/K)+ y[j]*(5-y[j]) +
                       _{1} = 1ambda*w[1][j+1] + _{1} = 1ambda*w[1][j-1]+w[2][j])/mu
                  if abs(w[1][j] - z) > NORM:
                      NORM = abs(w[1][j] - z)
                  w[1][j] = z
                  for i in range(2, n-1):
                      z = (-pow(h, 2)*(-q/K)+ w[i-1][j]
                           +_{\text{lambda}*w[i][j+1]} + w[i+1][j] + _{\text{lambda}*w[1][j-1]})/mu
                      if abs(w[i][j] - z) > NORM:
                          NORM = abs(w[i][j] - z)
                      w[i][j] = z
                  z = (-pow(h, 2)*(-q/K)+ 0 +w[n-2][j+1]
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if abs(w[n-1][j] - z) > NORM:
                     NORM = abs(w[n-1][j] - z)
                 w[n-1][j] = z
             z = (-pow(h, 2)*(-q/K)+ y[1]*(5-y[1])
                  + _lambda*x[1]*(5-x[1]) + _lambda*w[1][2] + w[2][1])/mu
             if abs(w[1][1] - z) > NORM:
                 NORM = abs(w[1][1] - z)
             w[1][1] = z
             for i in range(2, n-1):
                 z = (-pow(h, 2)*(-q/K)+ _lambda*x[i]*(5-x[i])
                      + w[i-1][1] + _lambda*w[i][2] + w[i+1][1])/mu
                 if abs(w[i][1] - z) > NORM:
                     NORM = abs(w[i][1] - z)
                 w[i][1] = z
             z = (-pow(h, 2)*(-q/K)+ 0 + _lambda*x[n-1]*(6-x[n-1])
                  + w[n-2][1] + _lambda*w[n-1][2])/mu
             if abs(w[n-1][1] - z) > NORM:
                 NORM = abs(w[i-1][1] - z)
             w[n-1][1] = z
             if NORM <= TOL:
                 for i in range(1, n):
                     for j in range(1, m):
                         print(x[i], y[j], w[i][j])
                 break
             1 = 1+1
0 0 0.3811346339371776
0 0 0.4873991662462554
0 1 2.3501207696656237
0 1 2.6115893277227316
0 1 2.734460684984241
0 2 3.674381451057718
0 2 3.8008478087250492
0 2 3.8175590707180502
0 3 3.8181205397425515
0 3 3.807094994812158
0 3 3.716044431758118
0 4 2.7712797840628323
0 4 2.596137058836237
0 4 2.2821936577936843
```

 $+ _{lambda*w[n-1][j+1]} + _{lambda*w[n-1][j-1])/mu$

- 0 0 0.7077551861547948
- 0 0 0.6322228180320693
- 0 1 1.5407313314897262
- 0 1 1.9203731525508625
- 0 1 2.0558877822165775
- 0 2 2.5225143657035254
- 0 2 2.706745518698706
- 0 2 2.7310125057107695
- 0 3 2.731605242342983
- 0 3 2.7166637595366048
- 0 3 2.6267438650160666
- 0 4 2.149889761889877
- 0 4 1.884145471313638
- 0 4 1.4400460964534967
- 1 0 1.1744711193143835
- 1 0 0.6605769537808189
- 1 1 1.142903236718828
- 1 1 1.5741978276742863
- 1 1 1.6962978066949792
- 1 2 1.951654455880046
- 1 2 2.1622575100564783
- 1 2 2.189960750135348
- 1 3 2.1907014143565724
- 1 3 2.176157034751235
- 1 3 2.1054273888842916
- 1 4 1.8355817910642558
- 1 4 1.5241863079311018
- 1 4 1.0261397057720798
- 1 0 1.447905854030328
- 1 0 0.6550438193406494
- 1 1 0.94683961872772
- 1 1 1.399854882049135
- 1 1 1.5073490617849692
- 1 2 1.668398831501582
- 1 2 1.8910156439769694
- 1 2 1.920304472520736
- 1 3 1.9213442206539328
- 1 3 1.9087015405863093
- 1 3 1.854889226896415
- 1 4 1.6764540066460383
- 1 4 1.3425492585196313
- 1 4 0.8221793030078859
- 2 0 1.711237220416363
- 2 0 0.6433122161982506
- 2 1 0.8497348961469537
- 2 1 1.3113572307134753
- 2 1 1.4084080749027912
- 2 2 1.5273216099637033

- 2 2 1.7553500568387426
- 2 2 1.7853833609125114
- 2 3 1.7867681294472795
- 2 3 1.7760919017981658
- 2 3 1.7335756631691308
- 2 4 1.5954937872852588
- 2 4 1.250786503530057
- 2 4 0.7212688057195532
- 2 0 1.821889298855372
- 2 0 0.6330909207247506
- 2 1 0.8010028537242849
- 2 1 1.2655248331114064
- 2 1 1.3560726311926494
- 2 2 1.4560623331750462
- 2 2 1.6863876907782829
- 2 2 1.7167650184549568
- 2 3 1.7184561175384834
- 2 3 1.709315304857858
- 2 3 1.673549871239177
- 2 4 1.5533978790041445
- 2 4 1.203859018271084
- 2 4 0.6708078122519631
- 2 0 1.8552510847597572
- 2 0 0.625345355040458
- 2 1 0.7754662027539213
- 2 1 1.2401484107550267
- 2 1 1.3268215873757352
- 2 2 1.4181130449379449
- 2 2 1.6490943291280826
- 2 2 1.6795945320452372
- 2 3 1.6815121021664854
- 2 3 1.6734208831710504
- 2 3 1.641496463030132
- 2 4 1.5295825667124237
- 2 4 1.1785316987707726
- 2 4 0.6446372363781754
- 3 0 1.8347834826900964
- 3 0 0.6189722491714172
- 3 1 0.7601286320759343
- 3 1 1.2229508136661318
- 3 1 1.307180078884681
- 3 2 1.3940902295019384
- 3 2 1.624500603033163
- 3 2 1.6549466579990946
- 3 3 1.65699431935129
- 3 3 1.649554551487705
- 3 3 1.6198089545230197
- 3 4 1.5121823985232012

- 3 4 1.1620719874555863
- 3 4 0.6293222152790174
- 3 0 1.7478381828555625
- 3 0 0.6121455621348955
- 3 1 0.7474773602887302
- 3 1 1.2055611095904404
- 3 1 1.2878408164852004
- 3 2 1.3718509249952682
- 3 2 1.6000872307027934
- 3 2 1.6302430755008086
- 3 3 1.632307355946509
- 3 3 1.6252095475373822
- 3 3 1.5967529894486414
- 3 4 1.492179034210105
- 3 4 1.1459130980163927
- 3 4 0.6172364190269497
- 4 0 1.5375190915932695
- 4 0 0.6023027271827252
- 4 1 0.7318156208242206
- 4 1 1.1794250343584998
- 4 1 1.259404151195835
- 4 2 1.3404025733680176
- 4 2 1.5634533972440745
- 4 2 1.5928840276844956
- 4 2 1.3920040270044930
- 4 3 1.5948079998133113
- 4 3 1.5877674970683628
- 4 3 1.5600874050918057
- 4 4 1.458760456142005
- 4 4 1.121164094890083
- 4 4 0.602851585381341
- 4 0 1.3851628669465679
- 4 0 0.5853489651638107
- 4 1 0.7068345482244157
- 4 1 1.1316072122586296
- 4 1 1.2078715997575158
- 4 2 1.2845598313105782
- 4 2 1.4960664294366242
- 4 2 1.5238721594136788
- 4 3 1.5253959050549706
- 4 3 1.5180450178518197
- 4 3 1.4906333715237612 4 4 1.3935353181197916
- 4 4 1.073567280621303
- 4 4 0.5804773234632014
- 1 1 0.000111020100201
- 4 0 1.191886276743342
- 4 0 0.5539377908361237
- 4 1 0.6634774874237643
- 4 1 1.0384078044388407

- 4 1 1.1077435912971494
- 4 2 1.1777864641141933
- 4 2 1.3639462871186152
- 4 2 1.3882035042193437
- 4 3 1.3888489713480903
- 4 3 1.3805727869914532
- 4 3 1.3524303042556856
- 4 4 1.260552317960623
- 4 4 0.9749027133392175
- 4 4 0.5427515183254769
- 5 0 0.8338404566903422
- 5 0 0.4940231819845685
- 5 1 0.5876943958671704
- 5 1 0.8536425246849618
- 5 1 0.9092653961369347
- 5 2 0.9699409249439533
- 5 2 1.100612185753549
- 5 2 1.1171661732568563
- 5 3 1.1160159353378436
- 5 3 1.1057017318067512
- 5 3 1.0745129392354074
- 5 4 0.9868462873883771
- 5 4 0.7653508910229487
- 5 4 0.48025062640925437
- 5 0 0.7218932882319861
- 5 0 0.3777442572441023
- 5 1 0.45846461971338837
- 5 1 0.48581351770226566
- 5 1 0.513279412850431
- 5 2 0.5644847539225153
- 5 2 0.5737548664941671
- 5 2 0.573595289260867
- 5 3 0.5688578114928393
- 5 3 0.5545230316569106
- 5 3 0.5152737889936676
- 5 4 0.42336390879476976
- 5 4 0.31511742373037216
- 5 4 0.38478260589717866