

Algorithms HW5

1. ~~A, E, F, B, D~~, A, F, C, B, D

2. A, 0

F, 1

C, 1

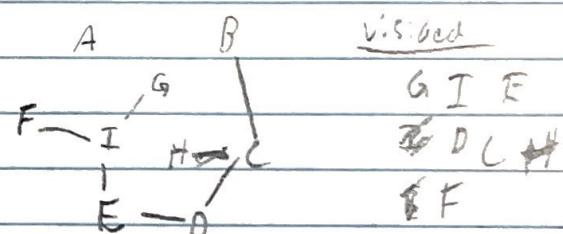
B, 1

D, 2

	In-Degree	Outdegree
A	2	3
B	1	2
C	5	0
D	2	2
E	1	2
F	1	2
G	1	2

Edge	Weight
G I	3
I E	5
E D	3
D C	5
C H	3
I F	7
C B	9
B A	5

TOTAL WEIGHT: 40



visited

G I E

D C #

F

5. Starting from F

V	F	C	E	B	D	A
F	0_F	7_F	15_F	6_F	00_F	00_F
B	0_F	7_F	15_F	6_F	00_F	5_B
A	0_F	7_F	15_F	6_F	9_A	5_B
✓ D	0_F	7_F	15_F	6_F	9_A	5_B

Paths: $s \rightarrow b \rightarrow d \rightarrow t$

✓ $s \rightarrow b \rightarrow d \rightarrow e \rightarrow t$

✗ $s \rightarrow b \rightarrow c \rightarrow e \rightarrow t$

$s \rightarrow b \rightarrow c \rightarrow t$

✗ $s \rightarrow a \rightarrow c \rightarrow e \rightarrow t$

$s \rightarrow a \rightarrow c \rightarrow d \rightarrow e \rightarrow t$

✓ $s \rightarrow a \rightarrow e \rightarrow t$

✗ $s \rightarrow c \rightarrow e \rightarrow t$

✗ $s \rightarrow c \rightarrow d \rightarrow e \rightarrow t$

✗ $s \rightarrow c \rightarrow d \rightarrow t$

✓ ~~Path~~ $s \rightarrow c \rightarrow t$ ★ shortest path!

Total Flow

7

3

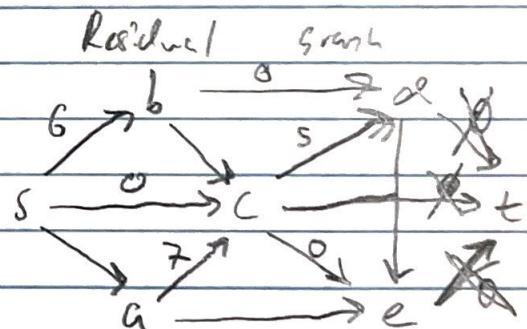
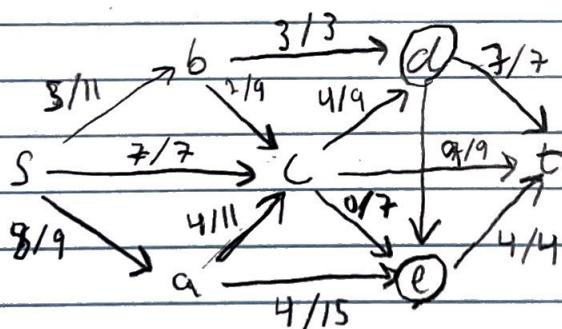
4

2

+ 4

20

Residual Graph



(a) Max Flow: 20

CUTS: dt

ct

et

(b) Capacity after min. cut: 20

(c) $s: s, b, a, c, d, e;$ $t: t$

(a) Edges with non-zero flow:	s_b	5
	s_L	7
	s_g	8
	b_d	3
	b_L	2
	c_d	4
	l_t	9
	a_L	4
	a_e	4
	e_t	4
	d_t	7