

# Algorithms HW5

1. ~~A, F, C, B, D~~ A, F, C, B, D

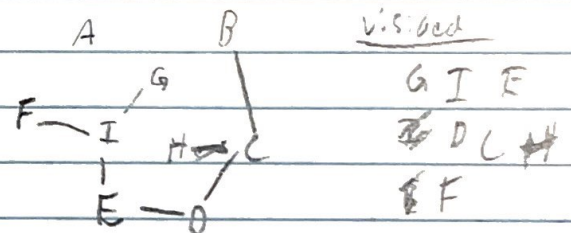
2. A, 0  
F, 1  
C, 1  
B, 1  
D, 2

3.

	In-Degree	Outdegree
A	2	3
B	1	2
C	5	0
D	2	2
E	1	2
F	1	2
G	1	2

4.

Edge	Weight
GI	3
IE	5
ED	3
DC	5
CH	3
IF	7
CB	9
BA	5



visited  
G I E  
~~D~~ C H  
F

TOTAL WEIGHT: 40

5. ~~Starting~~ Starting from F

V	F	C	E	B	D	A
F	0 <sub>F</sub>	7 <sub>F</sub>	15 <sub>F</sub>	6 <sub>F</sub>	∞ <sub>F</sub>	∞ <sub>F</sub>
B	0 <sub>F</sub>	7 <sub>F</sub>	15 <sub>F</sub>	6 <sub>F</sub>	∞ <sub>F</sub>	5 <sub>B</sub>
A	0 <sub>F</sub>	7 <sub>F</sub>	15 <sub>F</sub>	6 <sub>F</sub>	9 <sub>A</sub>	5 <sub>B</sub>
✓ D	0 <sub>F</sub>	7 <sub>F</sub>	15 <sub>F</sub>	6 <sub>F</sub>	9 <sub>A</sub>	5 <sub>B</sub>

~~Paths:~~ ✓ Paths:  $s \rightarrow b \rightarrow d \rightarrow t$

6. x  $s \rightarrow b \rightarrow d \rightarrow e \rightarrow t$

x  $s \rightarrow b \rightarrow c \rightarrow e \rightarrow t$

$s \rightarrow b \rightarrow c \rightarrow t$

x  $s \rightarrow a \rightarrow c \rightarrow e \rightarrow t$

$s \rightarrow a \rightarrow c \rightarrow d \rightarrow t$

✓  $s \rightarrow a \rightarrow e \rightarrow t$

x  $s \rightarrow c \rightarrow e \rightarrow t$

x  $s \rightarrow c \rightarrow d \rightarrow e \rightarrow t$

x  $s \rightarrow c \rightarrow d \rightarrow t$

✓ ~~★~~  $s \rightarrow c \rightarrow t$  ★★ shortest path!

Total Flow

7

3

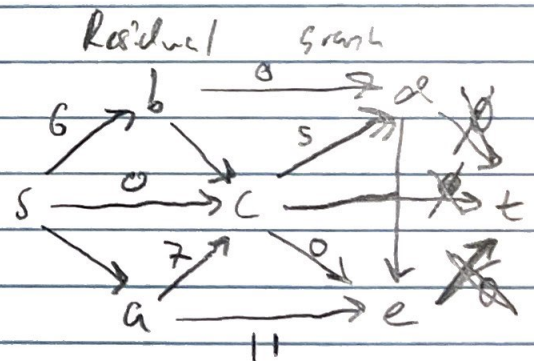
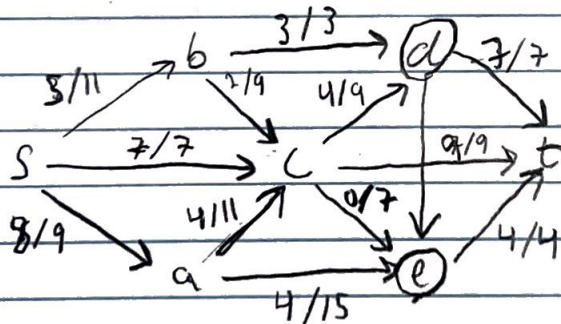
4

2

+ 4

20

~~Residual graph~~



(a) Max Flow: 20

Cuts:  $d \rightarrow t$

$c \rightarrow t$

$e \rightarrow t$

(b) Capacity after min. Cut: 29

(c)  $s$ :  $s, b, a, c, d, e$ ;  $t$ :  $t$



(d)	Edges with non-zero flow:	sb	5
		sc	7
		sa	8
		bd	3
		bc	2
		cd	4
		ct	9
		ac	4
		ae	4
		et	4
		dt	7