

Practice Mode

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## Qualification Round 2016

A. Counting Sheep

B. Revenge of the Pancakes

C. Coin Jam

D. Fractiles

## **Contest Analysis**

## **Questions** asked



### Submissions

### Counting Sheep

7pt Not attempted 26558/29356 users correct (90%)

8pt Not attempted 25729/26216 users correct (98%)

### Revenge of the Pancakes

10pt Not attempted 22527/23686 users correct (95%)

10pt Not attempted 21383/22147 users correct (97%)

### Coin Jam

10pt | Not attempted 13361/15342 users correct (87%)

20pt Not attempted 6297/9111 users correct (69%)

## Fractiles

10pt Not attempted 8250/9708 users correct (85%) 25pt Not attempted 2356/4955 users correct (48%)

#### Top Scores Lewin 100 100 Endagorion xiaowuc1 100 xyz111 100 HellKitsune123 100 seanwentzel 100 ivan.popelyshev 100 burunduk3 100 Nicolas 16 100 ctunoku

# **Contest Analysis**

Overview | Problem A | Problem B | Problem C | Problem D

# **Counting Sheep: Analysis**

The most natural approach to this problem is to simulate the process: keep track of which digits Bleatrix has seen so far, and then keep generating and checking the numbers she names until she has seen all of the digits 0-9. But are there other cases like **N** = 0 that go on forever or take an unacceptably long time?

One way to answer this question for the purposes of the problem to just check all possible cases between 0 and  $10^6$  before downloading the Large dataset. With a well-written program on a reasonably fast machine, this should take only a few seconds.

More generally, it can be proven that for any N > 0, the sheep doesn't have to keep naming numbers for very long:

- Regarding the digit 0: The tenth number that Bleatrix names is 10 times N, and is therefore guaranteed to end in 0.
- Regarding digits 1-9: Consider the smallest power of 10 greater than N; call it P. Once the process reaches a number at least as large as P, then the leftmost digit will take on every possible value from 1-9 as the number increases up to (or past) 9P. No digit can be skipped, because that would require the step between successive numbers (which equals N) to be larger than P... but we know that N is less than P because of how we chose P.

Since, by definition of P,  $10N \ge P$ , we will reach a number larger than P after naming at most 10 numbers, and we will reach a number greater than 9P after naming at most 90 numbers. So, after checking for the special case of N = 0, we can run our simulation without fear of running forever, running for long enough to run out of time, or overflowing even a 32-bit integer. Within the limits of the Small and Large datasets, the worst cases turn out to be 125 followed by any number of zeroes. In those cases, Bleatrix will name 72 numbers before falling asleep.

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