

# Data Science Cribsheet



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# Chapter 1

## Workflow

### 1.1 Preamble

A typical data science workflow can be framed as following these steps:

- Business: start with a business question, define the goal and measure of success
- Data: find, access and explore the data
- Features: extract, assess and evaluate, select and sort
- Models: find the right model for the problem at hand, compare, optimize, and fine tune
- Communication: Interpret and communicate the results
- Production: transform the code into production ready code, integrate into current ecosystem and deploy
- Maintain: adapt the models and features to the evolution of the environment

More succinctly, as per Hadley Wickham:

import -> tidy -> understand [ transform <-> visualize <-> model ] -> communicate

My combination of the two:

preparation -> import -> tidy -> understand [ transform <-> visualize <-> model ] -> [communicate + deploy + maintain]

Another note is that one way to structure projects is to write user stories a la software engineering.

What lies below is a succinct version of a workflow. Theoretical specifics can be found in other sections of this collection of cribsheets, and libraries or packages to use not included in the Stack can be found on this page.

### 1.2 Checklist

#### 1.2.1 Preparation

- Understand the business question, goals, and measures of success
- See if the data to answer the question exists, and if it is useful.
- Structure project as user stories

- Initialize report to track and summarise work and to do list.
- Remember to use atomic commit messages

### 1.2.2 Import

- Character Encoding Precedence: utf-8, iso-8859-1, utf-16
- Sampling from data if its too large

### 1.2.3 Tidy

- Follow tidy data principles.
- Figure out what you're trying to do with the data.
- See what the data looks like: types of variables, the first and last few observations, missing values or outliers.
- Outlier Detection: interquartile range, kernel density estimation, bonferroni test

### 1.2.4 Transform

- Look at missingness.
- Imputation. Options include the Mean, Mode, KNN, Random, and Regression.
- Use the Gower distance for categorical dissimilarity.
- Check for blank spaces and replace with NA. In R: `df[df==""] = NA`.
- Binned Stats

### 1.2.5 Visualize

- Quick Exploration Guide: S.O.C.S (Shape, Outlier, Center, Spread)
- Trendlines & Histograms
- Confidence intervals
- Compare the distributions of variables with overlayed density plots
- Scatterplots: Pairwise and color/size the dots by other variables to try to identify any confounding relationships.
- Dimensionality reduction (PCA, Kernel PCA, TSNE, Isomap) or hierarchical clustering for multivariate data to get a feel for high dimensional structure.

### 1.2.6 Model

- Stick to regression models for prescriptive analysis. Validate assumptions and tune appropriately. If using Python leverage statsmodels.
- Pre-processing: Use binning + chisquare / mutual information to see correlation between feature and target.
- Pipelines & Feature Unions

- Feature Selection: Variance Threshold, Univariate Feature Selection, Multivariate Feature Selection.
- Feature Engineering: Standardization, dimensionality reduction, dummifying. `sklearn.preprocessing.binarize`, `pandas.factorize`, and `featuretools` for automation in Python.
- Model Selection
- Model Explainability: SHAP
- Tuning: Do bayesian tuning instead of grid or random search. Also use `hyperopt-sklearn`, `sklearn-deap`, and `scikit-optimize`.
- Deal with potential class imbalance: Gradient boosting is one option.
- Create ensembles
- Ensembling: `mlxtend` in Python, and `caretEnsemble` in R.
- Look at learning curves: 1 | 2

### 1.2.7 Communicate

Reference this blog.

### 1.2.8 Deployment / Maintenance

Git Workflow

Write Tests.

Write helper functions, do testing:

1 | 2 | 3 | 4)

And validation:

1 | 2 | 3

A really useful feature is sharing environments so others can install all the packages used in your code, with the correct versions. You can save the packages to a YAML file with: `conda env export > environment.yaml`

The first part `conda env export` writes out all the packages in the environment, including the Python version. Above you can see the name of the environment and all the dependencies (along with versions) are listed. The second part of the export command, `> environment.yaml` writes the exported text to a YAML file `environment.yaml`. This file can now be shared and others will be able to create the same environment you used for the project. To create an environment from an environment file use: `conda env create -f environment.yaml`

This will create a new environment with the same name listed in `environment.yaml`.





## Chapter 2

# Import, Tidy, Transform & Visualize

## 2.1 Import

### 2.1.1 General

- A schema is a blueprint for storing data. For a table every row has same number of columns, and each column is of the same type.
- Make codebooks

### 2.1.2 SQL

- Maintain a query library
- Common Table Expressions
- cross apply = inner join | outer apply = full join
- SQL UNION stacks one dataset on top of the other. It only appends distinct values. More specifically, when you use UNION, the dataset is appended, and any rows in the appended table that are exactly identical to rows in the first table are dropped. If you'd like to append all the values from the second table, use UNION ALL.
- COUNT(DISTINCT month): returns count of non-null values like table in R
- The CASE statement is followed by at least one pair of WHEN and THEN statements: CASE WHEN year = 'SR' THEN 'yes' ELSE NULL END. You can also define a number of outcomes in a CASE statement by including as many WHEN/THEN statements as you'd like
- If you include two (or more) columns in a SELECT DISTINCT clause, your results will contain all of the unique pairs of those two columns

## 2.2 Tidy

- In tidy data: Each variable forms a column. Each observation forms a row. Each type of observational unit forms a table. There are three interrelated rules which make a dataset tidy.
- Each variable must have its own column.
- Each observation must have its own row.

- Each value must have its own cell.

## 2.3 Transform

### 2.3.1 General

- There is no one rule about when a number is not accurate enough to use, but as a rule of thumb, you should be cautious about using any number with a MOE (Margin-of-error) over 10%.

A good formula is: if your sample is picked uniformly at random and is of size at least:

$$\frac{-\log(\frac{\alpha}{2})}{2e^2}$$

then with probability at least 1-d your sample measured proportion q is no further away than e from the unknown true population proportion p (what you are trying to estimate). Need to estimate with 99% certainty the unknown true population rate to +/- 10% precision? That is d=0.01, e=0.1 and a sample of size 265 should be enough. A stricter precision of +/-0.05 causes the estimated sample size to increase to 1060, but increasing the certainty requirement to 99.5% only increases the estimated sample size to 300.

- Use spatial sign to transform data with outliers.
- Too many levels for a category:
  - limit number of categories through feature selection
  - <https://stats.stackexchange.com/questions/95212/improve-classification-with-many-categorical-variables>  
\* bucket groups by number of samples
- Long story short, if these outliers are really such (i.e. they appear with a very low frequency and very likely are bad/random/corrupted measurements) and they do not correspond to potential events/failures that your model should be aware of, you can safely remove them. In all other cases you should evaluate case by case what those outliers represent.
- Otherwise, assuming levels of the categorical variable are ordered, the polyserial correlation (here it is in R), which is a variant of the better known polychoric correlation. Note the latter is defined based on the correlation between the numerical variable and a continuous latent trait underlying the categorical variable.
- You should use a logarithmic scale when percent change, or change in orders of magnitude, is more important than changes in absolute units. You should also use a log scale to better visualize data that is heavily skewed. Taking the logarithm only works if the data is non-negative. There are other transforms, such as arcsinh or signed log, that you can use to decrease data range if you have zero or negative values.
- Normalizing by mean and standard deviation is most meaningful when the data distribution is roughly symmetric.
- Monetary amounts are often log- distributed—the log of the data is normally distributed. This leads us to the idea that taking the log of the data can restore symmetry to it.
- Dixon and Chi-squared tests for outlier detection plus LOF Algorithm.

### 2.3.2 Missingness & Imputation

- There are three types of missingness: 1) Completely at Random, 2) At Random, 3) Not at random
- Types of imputation

- Mean: Simple but can distort distribution, underestimate standard deviation, and distort variable relationships by dragging correlation to zero.
- Random: Can amplify outlier observation and induce bias.
- Regression: Use observed variables and relationships between these variables. Must make assumptions and can badly extrapolate. & multiple stochastic regression imputation
- The pros of imputation: 1) Helps retain a larger sample size of your data, 2) Does not sacrifice all the available information in an observation because of sparse missingness, 3) Can potentially avoid unwanted bias.
- The cons of imputation: 1) The standard errors of any estimates made during analyses following imputation can tend to be too small, 2) The methods are under the assumption that all measurements are actually “known,” when in fact some were imputed, 3) Can potentially induce unwanted bias.
- logging converts multiplicative relationships to additive relationships, and by the same token it converts exponential (compound growth) trends to linear trends. By taking logarithms of variables which are multiplicatively related and/or growing exponentially over time, we can often explain their behavior with linear models.

## 2.4 Visualize

- swarmplot | marimekko charts | radviz | Marey Chart



## Chapter 3

# Pre-processing, Feature Selection, and Feature Engineering

### 3.1 General

- sklearn log\_loss | brier score | cross entropy | youdens j
- hamming distance for categorical data. Available in sklearn DBSCAN.
- precision: how good were you at something being true when you said it was true. recall: how many of the true values did you catch. f1: harmonic mean of the two
- Brier score: Don't use for ordinal predictions. 0.25 if say .5 and .33 if randomly assign probs.
- R uses class encoded as 1 in classification to make predictions. Use levels() function on factor to determine what 1 is.
- 20 observations per feature is pretty good for making predictions.
- $y = b_0 + b_1x_1 + b_2x_2 + b_3x_1x_2$ . ( $b_1 + b_2x_2$ ) is the increase in y with a unit increase in  $x_1$ .
- Algorithms for Rec Systems: Linear/Logistic/Elastic Net Regression, Restricted Boltzmann Machines, Singular Value Decomposition, Markov Chains, Latent Dirichlet Allocation, Association Rules, Gradient Boosted Decision Trees, Random Forests, Affinity Propagation, K-Means, Matrix Factorization, Alternating Least Squares.
- For example, multilevel models themselves may be referred to as hierarchical linear models, random effects models, multilevel models, random intercept models, random slope models, or pooling models.
- Multi-Modal Classification: In the machine learning community, the term Multi-Modal is used to refer to multiple kinds of data. For example, consider a YouTube video. It can be thought to contain 3 different modalities: 1) The video frames (visual modality), 2) The audio clip of what's being spoken (audio modality), 3) Some videos also come with the transcription of the words spoken in the form of subtitles (textual modality)
- Less samples and more features increase the chance of overfitting.
- You can choose either of the following inference strategies: offline inference, meaning that you make all possible predictions in a batch, using a MapReduce or something similar. You then write the predictions to an SSTable or Bigtable, and then feed these to a cache/lookup table. online inference, meaning that you predict on demand, using a server.

- A static model is trained offline. That is, we train the model exactly once and then use that trained model for a while. A dynamic model is trained online. That is, data is continually entering the system and we're incorporating that data into the model through continuous updates.
- How would multiplying all of the predictions from a given model by 2.0 (for example, if the model predicts 0.4, we multiply by 2.0 to get a prediction of 0.8) change the model's performance as measured by AUC? No change. AUC only cares about relative prediction scores. Yes, AUC is based on the relative predictions, so any transformation of the predictions that preserves the relative ranking has no effect on AUC. This is clearly not the case for other metrics such as squared error, log loss, or prediction bias (discussed later).
- AUC is desirable for the following two reasons: AUC is scale-invariant. It measures how well predictions are ranked, rather than their absolute values. UC is classification-threshold-invariant. It measures the quality of the model's predictions irrespective of what classification threshold is chosen. However, both these reasons come with caveats, which may limit the usefulness of AUC in certain use cases: Scale invariance is not always desirable. For example, sometimes we really do need well calibrated probability outputs, and AUC won't tell us about that. Classification-threshold invariance is not always desirable. In cases where there are wide disparities in the cost of false negatives vs. false positives, it may be critical to minimize one type of classification error. For example, when doing email spam detection, you likely want to prioritize minimizing false positives (even if that results in a significant increase of false negatives). AUC isn't a useful metric for this type of optimization.
- Raising our classification threshold will cause the number of true positives to decrease or stay the same and will cause the number of false negatives to increase or stay the same. Thus, recall will either stay constant or decrease. In general, raising the classification threshold reduces false positives, thus raising precision.
- A feature cross is a synthetic feature formed by multiplying (crossing) two or more features. Crossing combinations of features can provide predictive abilities beyond what those features can provide individually.
- Bias: Error Introduced by approximating real-life problem by using a simple method
- Imagine a linear model with two strongly correlated features; that is, these two features are nearly identical copies of one another but one feature contains a small amount of random noise. If we train this model with L2 regularization, what will happen to the weights for these two features? L2 regularization will force the features towards roughly equivalent weights that are approximately half of what they would have been had only one of the two features been in the model.
- L2 regularization will encourage many of the non-informative weights to be nearly (but not exactly) 0.0.
- $F1\text{ Score} = TP / (TP + FP + FN)$ . Essentially how good you are at identifying the positive class.
- A variable that is completely useless by itself can provide a significant performance improvement when taken with others.
- Variance: The amount the model output will change if the model was trained using a different data
- Flexible Methods: higher variance, low bias, Example: KNN ( $k = 1$ ). \* Inflexible Methods: low variance, high bias, Example: Linear regression
- Set Random state by hand in sklearn.
- Generally need 3 rows of data per variable (to prevent model from seeing signal where there is only noise) [Nina Zumel]
- Domain knowledge for feature selection and random forest feature importance (5-10) best variables. [Nina Zumel]

- Because we have a couple thousand data points, even though salary can best be represented by a Poisson distribution, I'm going to use Gaussian distribution. (With bigger datasets, these two distribution start to become very similar).
- We can also tell that our input, `smart_1_normalized`, doesn't have a very strong relationship to our output because the standard error (0.009) is more than 1/10 of our estimate (0.02).
- The less complex an ML model, the more likely that a good empirical result is not just due to the peculiarities of the sample.

## 3.2 Pre-processing

## 3.3 Feature Engineering

- encode missingness as a feature
- Dealing with cyclical features: Hours of the day, days of the week, months in a year, and wind direction are all examples of features that are cyclical. Many new machine learning engineers don't think to convert these features into a representation that can preserve information such as hour 23 and hour 0 being close to each other and not far. Keeping with the hour example, the best way to handle this is to calculate the sin and cos component so that you represent your cyclical feature as (x,y) coordinates of a circle. In this representation hour, 23 and hour 0 are right next to each other numerically, just as they should be.

```
import numpy as np
df['hr_sin'] = np.sin(df.hr*(2.*np.pi/24))
df['hr_cos'] = np.cos(df.hr*(2.*np.pi/24))
df['mnth_sin'] = np.sin((df.mnth-1)*(2.*np.pi/12))
df['mnth_cos'] = np.cos((df.mnth-1)*(2.*np.pi/12))
```

- robust scaler python: median & quantiles

## 3.4 Feature Selection

- Variance Threshold: Use this to exclude features that don't meet a variance threshold.
- Univariate Feature Selection: For classification can use chi-squared and F-Test while F-Test for regression. Functions: `chi2`, `f_regression`, `f_classification` from `sklearn.feature_selection`.
- SelectKBest/SelectPercentile: Keep the k highest scoring features and keep a user-specified highest scoring percentage of features. Can use the univariate feature selection in these functions.
- `sklearn.feature_selection.RFE(CV)`
- To work around magic values, convert the feature into two features: One feature holds only quality ratings, never magic values. One feature holds a boolean value indicating whether or not a `quality_rating` was supplied. Give this boolean feature a name like `is_quality_rating_defined`.
- Handling extreme outliers: Given data with a very long tail, log scaling does a slightly better job, but there's still a significant tail of outlier values. Let's pick yet another approach. What if we simply "cap" or "clip" the maximum value at an arbitrary value, say 4.0? Clipping the feature value at 4.0 doesn't mean that we ignore all values greater than 4.0. Rather, it means that all values that were greater than 4.0 now become 4.0. This explains the funny hill at 4.0. Despite that hill, the scaled feature set is now more useful than the original data. Binning.

- Know your data. Follow these rules: 1) Keep in mind what you think your data should look like. 2) Verify that the data meets these expectations (or that you can explain why it doesn't). 3) Double-check that the training data agrees with other sources (for example, dashboards).

## 3.5 Other

### 3.5.1 Unbalanced Classes

Research on imbalanced classes often considers imbalanced to mean a minority class of 10% to 20%.

That said, here is a rough outline of useful approaches. These are listed approximately in order of effort:

- Do nothing. Sometimes you get lucky and nothing needs to be done. You can train on the so-called natural (or stratified) distribution and sometimes it works without need for modification.
- Balance the training set in some way: Oversample the minority class. Undersample the majority class. Synthesize new minority classes.

\*Throw away minority examples and switch to an anomaly detection framework.

- At the algorithm level, or after it: Adjust the class weight (misclassification costs). Adjust the decision threshold. Modify an existing algorithm to be more sensitive to rare classes.
- Construct an entirely new algorithm to perform well on imbalanced data.
- Use AUC, F1 Score, Cohen's Kappa, ROC curve, a precision-recall curve, a lift curve, or a profit (gain) curve for evaluation.
- Use probability estimates and not the default .5 threshold.
- Undersampling, oversampling, increase weight of minority class
- Decision trees often perform well on imbalanced datasets because their hierarchical structure allows them to learn signals from both classes.
- Sklearn Eg: `wclf = svm.SVC(kernel='linear', class_weight={1: 10})` & `svm.SVC(kernel='linear', class_weight='balanced')`

## 3.6 Model Selection

### 3.6.1 General

- Make sure that your test set meets the following two conditions: 1) Is large enough to yield statistically meaningful results, 2) Is representative of the data set as a whole. In other words, don't pick a test set with different characteristics than the training set.
- Linear SVM often outperforms logistic regression and is explainable as well.
- However, the problem with cross-validation is that it is rarely applicable to real world problems, for all the reasons described in the above sections. Cross-validation only works in the same cases where you can randomly shuffle your data to choose a validation set.
- If the performance of a classification model on the test set (out-of-sample) error is poor, you can't just re-calibrate your model parameters to achieve a better model. This is cheating.
- When the classes are well-separated, the parameter estimates for the logistic regression model are surprisingly unstable. Linear discriminant analysis does not suffer from this problem. If  $n$  is small



and the distribution of the predictors  $X$  is approximately normal in each of the classes, the linear discriminant model is again more stable than the logistic regression model.

- Roughly speaking, LDA tends to be a better bet than QDA if there are relatively few training observations and so reducing variance is crucial. In contrast, QDA is recommended if the training set is very large, so that the variance of the classifier is not a major concern, or if the assumption of a common covariance matrix for the  $K$  classes is clearly untenable.
- Two features interact if the effect on the prediction of one feature depends on the value of the other feature
- Warning `PolynomialFeatures(degree=d)` transforms an array containing  $n$  features into an array containing features, where  $n!$  is the factorial of  $n$ , equal to  $1 \times 2 \times 3 \times \dots \times n$ . Beware of the combinatorial explosion of the number of features!
- It appears that each feature has modestly improved our model. There are certainly more features that we could add to our model. For example, we could add the day of the week and the hour of the posting, we could determine if the article is a listicle by running a regex on the headline, or we could examine the sentiment of each article. This only begins to touch on the features that could be important to model virality. We would certainly need to go much further to continue reducing the error in our model.
- Suppose Fixitol reduces symptoms by 20% over a placebo, but the trial you're using to test it is too small to have adequate statistical power to detect this difference reliably. We know that small trials tend to have varying results; it's easy to get 10 lucky patients who have shorter colds than usual but much harder to get 10,000 who all do.
- As I mentioned earlier, one drawback of the Bonferroni correction is that it greatly decreases the statistical power of your experiments, making it more likely that you'll miss true effects. More sophisticated procedures than Bonferroni correction exist, ones with less of an impact on statistical power, but even these are not magic bullets. Worse, they don't spare you from the base rate fallacy. You can still be misled by your  $p$  threshold and falsely claim there's "only a 5% chance I'm wrong." Procedures like the Bonferroni correction only help you eliminate some false positives.
- In step 1, we find where missing values are located. The `md.pattern()` function from the `mice` package is a really useful function. It gives you a clear view of where missing values are located, helping you in decisions regarding exclusions or substitution. You can refer to the next recipe for missing value substitution.
- Another possible indication of collinearity in the inputs is seeing coefficients with an unexpected sign: for example, seeing that income is negatively correlated with years in the workforce.
- The overall model can still predict income quite well, even when the inputs are correlated; it just can't determine which variable deserves the credit for the prediction. Using regularization (especially ridge regression as found in `lm.ridge()` in the package `MASS`) is helpful in collinear situations (we prefer it to "x-alone" variable preprocessing, such as principal components analysis). If you want to use the coefficient values as advice as well as to make good predictions.
- The degrees of freedom is thought of as the number of training data rows you have after correcting for the number of coefficients you tried to solve for. You want the degrees of freedom to be large compared to the number of coefficients fit to avoid overfitting.
- The probable reason for nonconvergence is separation or quasi-separation: one of the model variables or some combination of the model variables predicts the outcome perfectly for at least a subset of the training data. You'd think this would be a good thing, but ironically logistic regression fails when the variables are too powerful.
- For categorical variables (male/female, or small/medium/large), you can define the distance as 0 if two points are in the same category, and 1 otherwise. If all the variables are categorical, then you can use Hamming distance, which counts the number of mismatches.

- Your next step is to select a performance measure. A typical performance measure for regression problems is the Root Mean Square Error (RMSE). It measures the standard deviation of the errors the system makes in its predictions.
- You should save every model you experiment with, so you can come back easily to any model you want. Make sure you save both the hyperparameters and the trained parameters, as well as the cross-validation scores and perhaps the actual predictions as well. This will allow you to easily compare scores across model types, and compare the types of errors they make. You can easily save Scikit-Learn models by using Python's pickle module, or using `sklearn.externals.joblib`, which is more efficient at serializing large NumPy arrays.
- If all classifiers are able to estimate class probabilities (i.e., they have a `predict_proba()` method), then you can tell Scikit-Learn to predict the class with the highest class probability, averaged over all the individual classifiers. This is called soft voting. It often achieves higher performance than hard voting because it gives more weight to highly confident votes. All you need to do is replace `voting="hard"` with `voting="soft"` and ensure that all classifiers can estimate class probabilities.
- The standard value for `k` in `k`-fold cross-validation is 10, which is typically a reasonable choice for most applications. However, if we are working with relatively small training sets, it can be useful to increase the number of folds. If we increase the value of `k`, more training data will be used in each iteration, which results in a lower bias towards estimating the generalization performance by averaging the individual model estimates. However, large values of `k` will also increase the runtime of the cross-validation algorithm and yield estimates with higher variance since the training folds will be more similar to each other. On the other hand, if we are working with large datasets, we can choose a smaller value for `k`.
- Distance Metrics: Hamming distance for categorical variables, Cosine distance for text data, Gower distance for categorical data
- AIC x BIC: Explanatory power x Parsimonious
- Bias is how far off on the average the model is from the truth. Variance is how much the estimate varies about its average. With low model complexity bias is high because predictions are more likely to stray from the truth, and variance is low because there are only few parameters being fit. With high model complexity bias is low because the model can adapt to more subtleties in the data, and variance is high because we have more parameters to estimate from the same amount of data.
- The mean of highly correlated quantities has higher variance than the mean of uncorrelated quantities. The smaller the number of folds, the more biased the error estimates (they will be biased to be conservative indicating higher error than there is in reality) but the less variable they will be. On the extreme end you can have one fold for each data point which is known as Leave-One-Out-Cross-Validation. In this case, your error estimate is essentially unbiased but it could potentially have high variance.
- LDA vs Logistic Regression: When the classes are well-separated parameters of logistic regression are unstable and LDA doesn't have this problem. If the distribution of `X` is approximately normal then LDA is more stable again. LDA doesn't need to fit multiple models for multiclass classification.
- SVM vs Logistic Regression: SVM is likely to overfit the data and can dominate LR on the training set. Kernel method makes SVM more flexible.
- Decision Tree vs Linear Model: Tree has non-linear boundary, selects important features, easier to interpret but unstable especially for small data.
- Naive Bayes vs LDA: Both use Bayes theorem, both assume gaussian distribution, but LDA takes care of the correlations. LDA might out-perform Naive Bayes when the features are highly correlated.
- KNN vs Other Classification Methods: KNN is completely non-parametric, doesn't tell which features are important. Dominates LDA and Logistic Regression when the decision boundary is highly non-linear.

- When building, testing, and validating a suite of models, the optimal model (i.e., the optimal point in the ROC curve) is the spot where the overall accuracy of the model is essentially unchanged as we make small adjustments in the choice of model. That is to say, the change (from one model to the next) in the model's precision (specificity) is exactly offset by the change in the model's recall (sensitivity). Consequently, allowing for some imperfection, where the false positive rate and the false negative rate are in proper balance (so that neither one has too great of an impact on the overall accuracy and effectiveness of the model), is good fruit from your big data labors. The metric I used to guide my cross-validation is the F-score. This is a good metric when we have a lot more samples from one category than from the other categories.
- The cost of the holdout method comes in the amount of data that is removed from the model training process. For instance, in the illustrative example here, we removed 30% of our data. This means that our model is trained on a smaller data set and its error is likely to be higher than if we trained it on the full data set. The standard procedure in this case is to report your error using the holdout set, and then train a final model using all your data.
- A metric that minimizes false positives, by rarely flagging players and teams that fail to achieve the desired outcome, is specific. A metric that minimizes false negatives, by rarely failing to flag players and teams that achieve the desired outcome, is sensitive.
- Sometimes it may be more useful to report the coefficient of determination ( $R^2$ ), which can be understood as a standardized version of the MSE, for better interpretability of the model performance. In other words,  $R^2$  is the fraction of response variance that is captured by the model. The value is defined as follows: Here, SSE is the sum of squared errors and SST is the total sum of squares, or in other words, it is simply the variance of the response.
- Most people start working with data from exactly the wrong end. They begin with a data set, then apply their favorite tools and techniques to it. The result is narrow questions and shallow arguments. Starting with data, without first doing a lot of thinking, without having any structure, is a short road to simple questions and unsurprising results. We don't want unsurprising - we want knowledge.
- Remember that the positive class in scikit-learn is the class that is labeled as class 1. If we want to specify a different positive label, we can construct our own scorer via the `make_scorer` function, which we can then directly provide as an argument to the scoring parameter in `GridSearchCV`.
- While the weighted macro-average is the default for multiclass problems in scikit-learn, we can specify the averaging method via the `average` parameter inside the different scoring functions that we import from the `sklearn.metrics` module, for example, the `precision_score` or `make_scorer` functions.
- Transforming words into feature vectors To construct a bag-of-words model based on the word counts in the respective documents, we can use the `CountVectorizer` class implemented in scikit-learn. As we will see in the following code section, the `CountVectorizer` class takes an array of text data, which can be documents or just sentences, and constructs the bag-of-words model for us:
- Naive Bayes is a linear classifier, while KNN is not. The curse of dimensionality and large feature sets are a problem for KNN, while Naive Bayes performs well. KNN requires no training (just load in the dataset), whereas Naive Bayes does.
- The McNemar test, introduced by Quinn McNemar in 1947 (McNemar 1947), is a non-parametric statistical test for paired comparisons that can be applied to compare the performance of two machine learning classifiers. Cochran's Q Test or F Test for  $>2$ .
- Model Comparison

### 3.6.2 Clustering

- Comparison
- Rules



# Chapter 4

## Model

General format: INtro, Assumptions, Evaluation, Interpretation, Pros/Cons, Notes

### 4.1 Supervised

#### 4.1.1 Linear Regression

Discuss Ridge, Lasso, and Elastic here.

The standard least squares coefficient estimates are scale equivariant: if we multiply a predictor variable by a constant, the corresponding least squares coefficient estimate will be scaled down by the same constant. Used when you're predicting a continuous value. In regression, it is often recommended to center the variables so that the predictors have mean 0. This makes it so the intercept term is interpreted as the expected value of  $Y_i$  when the predictor values are set to their means. Otherwise, the intercept is interpreted as the expected value of  $Y_i$  when the predictors are set to 0, which may not be a realistic or interpretable situation. When  $p > n$ , we can no longer calculate a unique least square coefficient estimate, the variances become infinite, so OLS cannot be used at all.

- In presence of few variables with medium / large sized effect, use lasso regression. In presence of many variables with small / medium sized effect, use ridge regression.
- The fitted regression line using a sample of data gives imperfect predictions for future observations due to sampling variability and randomness in  $Y$  that is not related to  $X$ .
- Linear Correlation  $\Rightarrow$  Causation if covariates respect: linearity normality indep homoscedasticity + all confounders in model
- In summary, “pooling” your data and fitting one combined regression function allows you to easily and efficiently answer research questions concerning the binary predictor variable.
- If two independent variables are measured in exactly the same units, we can assess their relative importance in their effect on  $y$  quite simply: the larger the coefficient, the stronger the effect.
- Okay, so many of the features are strongly correlated. We can make use of this in our model by including polynomial features (e.g. `PolynomialFeatures(degree=2)` from `scikit-learn`). Adding these brings our validation loss down to 0.69256 (-0.05% from baseline).
- We prefer natural logs (that is, logarithms base  $e$ ) because, as described above, coefficients on the natural-log scale are directly interpretable as approximate proportional differences: with a coefficient of 0.06, a difference of 1 in  $x$  corresponds to an approximate 6% difference in  $y$ , and so forth.

The regression assumption that is generally least important is that the errors are normally distributed. In fact, for the purpose of estimating the regression line (as compared to predicting individual data points), the assumption of normality is barely important at all. Thus, in contrast to many regression textbooks, we do not recommend diagnostics of the normality of regression residuals. [Gelman]

Linear regression errors are not autocorrelated. The Durbin-Watson statistic detects this; if it is close to 2, there is no autocorrelation.

A linear regression model is only as good as the validity of its assumptions, which can be summarized as:  $y = b_0 + b_1x + \epsilon$ ,  $\epsilon$  is i.i.d from  $N(0, \sigma)$ . More verbosely:

- **Linearity:** This is a linear relationship between the predictor and the response variables. If this relationship is not clearly present, transformations (log, polynomial, exponent and so on) of the X or Y may solve the problem. Check with a scatterplot.
- **Normality:** The error terms are drawn from an identical Gaussian distribution, i.e a normal distribution of the dependent variable for each value of the independent variable. Inspect the quantile-quantile plot of the residuals. Also Shapiro-Wilk Test for Normality.
- **Non-correlation or independence of errors:** A common problem in the time series and panel data where  $\epsilon_t = \beta\epsilon_{t-1}$ ; if the errors are correlated, you run the risk of creating a poorly specified model. The residual value for an arbitrary observation is not predictable from knowledge of another observation's residual value; they are uncorrelated. Inspect the residual plot after fitting the regression. Ideally, there would be no clear pattern in the fluctuation of the error terms.
- **Homoscedasticity (constant variance):** Normally the distributed and constant variance of errors, which means that the variance of the errors is constant across the different values of inputs. Violations of this assumption can create biased coefficient estimates, leading to statistical tests for significance that can be either too high or too low. This, in turn, leads to the wrong conclusion. This violation is referred to as heteroscedasticity. The error terms have the same variance. Check the residual plot which is a scatterplot of the residuals vs the fitted values.
- **No multi-collinearity:** No linear relationship between two predictor variables, which is to say that there should be no correlation between the features. This, again, can lead to biased estimates. If not coefficient estimates could be unstable, introduce redundancies within predictors, and make it more difficult to make inferences. Could inflate standard errors, decrease power and reliability of regression coefficients, and create need for a larger sample size. Check the variance inflation factors. Tells the factor by which the estimated variance of a variable is larger in comparison to it if it were completely uncorrelated with other variables in the model. If the VIF is more than five then the variable is a candidate to remove from the model. Its information is contained in the other variables. Variance Inflation Factor: Measures how the model factors influence the uncertainty of coefficient estimates.  $\geq 5$  is bad.
- **Minimal outliers:** Outliers can severely skew the estimation and, ideally, must be removed prior to fitting a model using linear regression; this again can lead to a biased estimate.

A practical summary using R.

```
# general check
plot(rgr_lr_st1)

# linearity check
avPlots(rgr_lr_st1)

# repeat of outlier analysis
#influencePlot(rgr_lr_st1)

# multi-collinearity
vif(model) %>% data.frame() %>% mutate(VIF = `GVIF..1..2.Df..`, VIF = VIF^2)
```

```
# Test for Autocorrelated Errors
durbinWatsonTest(rgr_lr_st1)

data = rnorm(100) # Generating data from a standard normal distribution.
shapiro.test(data) # P-value insignificant; retain H0, conclude data is normally distributed.

# Inspect this same data using the QQ-plots (For normal data, the QQ-plot produces a straight-line rela
qqnorm(normal.data) + qqline(normal.data)
#Breusch-Pagan (BP) test lmtest package: is used to test for heteroskedasticity in a linear regression
```

Outliers are observations that have high residual values. Leverage points are observations that have unusually small or large independent variable values. Cook's distance helps to measure the effect of deleting an observation from the #dataset and rerunning the regression. Observations that have large residual values and also high leverage tend to pose threats to the accuracy of the regression line and thus need to be further investigated. Look at influence plot. Confidence and prediction intervals. For avplot distinct patterns are indications of good contributions. Influence plot to look at hat values (lower is better). Use F-test to compare models. F-test & partial f-test for simple and multiple linear regression.

```
statsmodels.stats.outliers_influence.variance_inflation_factor
```

Fixing assumptions:

Transformations: Can remedy assumption violations and strengthen linear relationships between variables, but can lead to overfitting and less interpretability. square root correction: Take square root of x variable(s). log transformation: Take log of y. General rule of thumb: powers > 1 for skewed left data, powers < 1 for data skewed right.

Box-Cox: Iterates along values of lambda by maximum likelihood so as to maximize the fit of the transformed variable to a normal distribution. Does not guarantee normality since it minimizes standard deviation. Can only be used on positive values. Use on negative values by shifting by a constant value. Use Box-Cox transformations when predictions are skewed.

### 4.1.2 Selection

- Forward and Backward Stepwise Selection.
- For simple linear regression, the principal hypothesis test is as follows:  $H_0 : \beta_1 = 0$ ,  $H_A : \beta_1 \neq 0$ . If  $H_0$  is true then the population mean of Y would be  $\beta_0$  no matter what the value of X. (X has no effect on Y.)
- F-Test:  $H_0$  says that all/some coefficients are zero versus  $H_A$  which says that there is at least one non-zero coefficient. If  $H_0$  fail to reject then F value close to 1, else F value greater than 1.
- A.I.C and B.I.C: Smaller values are better. Can be used to compare multiple models at the same time. They reward goodness of fit and penalizes complexity. Favor A.I.C for prediction and B.I.C for descriptive power (penalty term more stringent and favors a parsimonious model)
- R-squared increases whenever a predictor is added, and it doesn't take model complexity into consideration which makes it prone to overfitting. Use adjusted R-squared instead. Additional predictors only make this increase if they are statistically significant. It's easy to show that given no other data for a set of numbers, the predictor that minimises the MAE is the median, while the predictor that minimises the MSE is the mean.
- Compare RSME to sd of data for sense of how good it is. (If RSME < sd then good.)

### 4.1.3 Pros/Cons

#### Pros

- Very fast (runs in constant time)
- Easy to understand the model
- Less prone to overfitting

#### Cons

- Unable to model complex relationships
- Unable to capture nonlinear relationships without first transforming the inputs

### 4.1.4 Other

- <https://twitter.com/alexpghayes/status/1033824995905077250>
- Quantile regression is an alternative for quantiles.
- Type 1 Error: Accept  $H_0$  when  $H_0$  is true.
- RSS is The sum of the squared error terms for each observation in our dataset. RSE is The standard deviation of the residuals about the regression surface and is an estimate of  $\sigma$ . TSS is a measure of the total squared deviation of our response variable from its mean value.  $R^2 = 1 - \text{RSS}/\text{TSS}$ .
- Increasing  $x_1$  by 1 means you are increasing the underlying  $X_1$  by 1 standard deviation  $x_1 + 1 = (X_1 + \sigma - \mu)/\sigma$ . Therefore you can say that  $b_1$  is the effect on  $y$  of increasing  $X_1$  by 1 sigma.
- If there is an ascending or descending order to your dependent variable, ordinal regression is more appropriate as it has more power than multinomial logistic regression.
- leaps lm package r is a greedy way to find the best predictors by cycling through all the combinations.
- Linear Regression by Year

```
library(purrr)
pga %>%
  select(name, year, driveavg, drivepct, score.avg) %>%
  split(.$year) %>%
  map(~lm(score.avg ~ driveavg + drivepct, data=.$)) %>%
  map(summary)
```

## 4.2 Ridge/Lasso

### 4.2.1 Intro

Minimizes RSS but also has shrinkage penalty (L2 penalty). A small  $\lambda$  penalizes the RSS more than the shrinkage penalty. A large  $\lambda$  penalizes the shrinkage penalty more than the RSS. By shrinking the coefficient estimates towards 0 by increasing  $\lambda$ , the bias increases slightly but remains relatively small, the variance reduces substantially, and the mean squared error of the predictions drops. Not scale invariant due to the shrinkage penalty. To avoid the issue of overvaluing or undervaluing certain predictor variables simply based on their magnitudes, we must standardize the variables prior to performing ridge regression. The main disadvantage of ridge regression is that, while parameter estimates are shrunk, they only asymptotically approach 0 as we increase the value of  $\lambda$ .



Standardize for ridge/lasso alpha makes them not scale invariant

Minimizes RSS but also has L1 penalty (norm). This necessarily forces some coefficient estimates to be exactly 0 (when lambda is sufficiently large). It has the added advantage of essentially performing variable selection, yielding models that are both accurate and parsimonious. Restricting ourselves to simpler models by including a Lasso penalty will generally decrease the variance of the fits at the cost of higher bias.

Note: In both ridge and lasso regression, is important to select an appropriate value of lambda by means of cross-validation.

## 4.3 Logistic Regression

### 4.3.1 Intro

logistic is the same as probit

wilkinson rogers logistic regression

weighted logistic regression

The right-hand predictor side of the equation must be linear with the left-hand outcome side of the equation. You must test for linearity in the logit (in logistic regression the logit is the outcome side). This is commonly done with the Box-Tidwell Transformation (Test): Add to the logistic model interaction terms which are the crossproduct of each independent times its natural logarithm  $[(X)\ln(X)]$ . If these terms are significant, then there is nonlinearity in the logit. This method is not sensitive to small nonlinearities.

Logistic regression assumes that  $\text{logit}(y)$  is linear in the values of  $x$ . Like linear regression, logistic regression will find the best coefficients to predict  $y$ , including finding advantageous combinations and cancellations when the inputs are correlated. In other words, you can think of logistic regression as a linear regression that finds the log-odds of the probability that you're interested in. Logistic Regression can also be used with kernel methods.

Logistic: When you're predicting which category your observation is in. (Is this is a cat or a dog?)

The link function is the logit function. Logit is the inverse of the sigmoid and gives the log odds, i.e  $p/(1-p)$ .

Easy to incorporate prior knowledge, number of features are small, training is fast, precision not critical.

No closed form expression to maximize coefficients with maximum likelihood estimation, so one uses gradient descent or stochastic gradient descent. The second one is faster.

For logistic regression value of  $c$  penalizes features. Low  $c$  penalizes a lot and vice versa. A large  $c$  decreases the effect of the regularization term (the l2 penalization).

Makes a linear boundary between classes.

For multiclass classification it will build multiple models. Given 3 classes 0,1, and 2, there will be models 0 and not 0, 1 and not 1, and 2 and not 2.

Standardization isn't required for logistic regression. The main goal of standardizing features is to help convergence of the technique used for optimization. For example, if you use Newton-Raphson to maximize the likelihood, standardizing the features makes the convergence faster. Otherwise, you can run your logistic regression without any standardization treatment on the features.

### 4.3.2 Assumptions

- The linear regression analysis requires all variables to be multivariate normal. This assumption can best be checked with a histogram or a Q-Q-Plot.

- Requires the dependent variable to be binary and ordinal logistic regression requires the dependent variable to be ordinal.
- The observations to be independent of each other. In other words, the observations should not come from repeated measurements or matched data.
- There to be little or no multicollinearity among the independent variables.
- Assumes linearity of independent variables and logit of the probabilities ( $\text{logit}(p) = \log(p/(1-p))$ ). Check in R.
- There is no influential values (extreme values or outliers) in the continuous predictors

Notice the points fall along a line in the middle of the graph, but curve off in the extremities. Normal Q-Q plots that exhibit this behavior usually mean your data have more extreme values than would be expected if they truly came from a Normal distribution.

The Durbin-Watson test is used to test the null hypothesis that linear regression residuals are uncorrelated, against the alternative that autocorrelation exists

<https://data.library.virginia.edu/diagnostic-plots/>

### No Multicollinearity

`multicol` shows which columns could be removed for multi-collinearity. (The `vif` is not working because of multicollinearity.)

```
# vif(clf_lr$finalModel)
# multicol <- alias(clf_lr$finalModel)$Complete
# multicol
```

### Linear With The Logit Of Predictions

```
# box tidwell doesn't work since features have negative values.

# min_max_scaler <- function(x) (x - min(x))/(max(x) - min(x))
#
# df_num_selected <- df2 %>%
#   select(
#     OverallMap,
#     StrandMap,
#     lesson_length,
#     g_avg_overall_map,
#     g_avg_strand_map,
#     g_avg_score,
#     g_num_students,
#     cohort_avg_overall_map,
#     cohort_avg_strand_map
#   ) %>%
#   map(min_max_scaler) %>%
#   data.frame() %>%
#
# formula_all_num_features <- as.formula(glue('pass ~ {paste(df_num_selected %>% names, collapse = " +
# car::boxTidwell(formula_all_num_features, data = df_num_selected )

# Visual test too many features to work well

# lin_test <- df2 %>%
#   dplyr::select_if(is.numeric)
#
```

```
# predictors <- colnames(lin_test)
#
# lin_test <- lin_test %>%
#   mutate(logit = log(clf_lr_final$fitted.values/(1-clf_lr_final$fitted.values))) %>%
#   gather(key = "predictors", value = "predictor.value", -logit)
#
# ggplot(lin_test, aes(logit, predictor.value))+
#   geom_point(size = 0.5, alpha = 0.5) +
#   geom_smooth(method = "loess") +
#   theme_bw() +
#   facet_wrap(~predictors, scales = "free_y")
```

### 4.3.3 Evaluation

- Wald Test:  $h_0: b = 0$  and  $h_a: b \neq 0$ .  $h_0$  means the log odds are unaffected by  $x$  and so  $x$  has no bearing on the prediction of success.
- Deviance  $G^2$  and Goodness of Fit: The deviance associated with a given logistic regression model  $M$  is based on comparing the maximum log-likelihood of model  $M$  against the saturated model  $S$ . The smaller the deviance the better. For goodness of fit  $h_0$  says the model is appropriate while  $H_a$  says the opposite.
- McFadden's Pseudo  $R^2$ .
- A.I.C / B.I.C
- Absolute scale odds instead of relative

### 4.3.4 Pros/Cons

#### Pros

- Highly interpretably
- Model training and prediction are fast
- No tuning outside of regularization required
- Features don't need scaling
- Can perform with a small number of observations
- Outputs well-calibrated predicted probabilities
- low variance

#### Cons

- Presumes a linear relationship between the features and the log-odds of the response.
- Performance is generally not competitive with the best supervised learning methods
- Can't automatically learn feature interactions
- Breaks down when classes are perfectly separable.
- High bias

### 4.3.5 Code Example

```
import statsmodels.api as sm
X = sm.add_constant(X)
clf_lr = sm.Logit(Y, X).fit(dispatch=False)
print(results.summary())
```

## 4.4 Poisson Regression

### 4.4.1 Intro

Poisson: When you're predicting a count value. (How many dogs will I see in the park?)

Poisson Regression: The Poisson distribution is used to model variation in count data (that is, data that can equal 0,1,2,...).

Remember that you must specify `family = poisson` or `family = quasipoisson` when using `glm()` to fit a count model.

### 4.4.2 Assumptions

One of the assumptions of Poisson regression to predict counts is that the event you are counting is Poisson distributed: the average count per unit time is the same as the variance of the count. In practice, "the same" means that the mean and the variance should be of a similar order of magnitude.

When the variance is much larger than the mean, the Poisson assumption doesn't apply, and one solution is to use quasipoisson regression, which does not assume that  $\text{variance} = \text{mean}$ .

### 4.4.3 Evaluation

### 4.4.4 Pros/Cons

**Pros**

**Cons**

## 4.5 Generalized Additive Models

### 4.5.1 Intro

`mgcv::gam`: More complex than `lm`, more likely to overfit, best used on larger data sets. use `s(var)` to denote non-linear relationship. Don't use `s()` with categorical variable. Use `type = terms` for y values of plots to get predictions `type = response`.

Also remember that `gam()` from the package `mgcv` has the calling interface

`gam(formula, family, data)` For standard regression, use `family = gaussian` (the default).

For GAM models, the `predict()` method returns a matrix, so use `as.numeric()` to convert the matrix to a vector.

### 4.5.2 Assumptions

### 4.5.3 Evaluation

### 4.5.4 Pros/Cons

**Pros**

**Cons**

## 4.6 K-Means Clustering [US]

### 4.6.1 Intro

K-Means clustering method considers two assumptions regarding the clusters – first that the clusters are spherical and second that the clusters are of similar size.

k-means assumes the variance of the distribution of each attribute (variable) is spherical; all variables have the same variance;

the prior probability for all k clusters is the same, i.e., each cluster has roughly equal number of observations;

Must choose k for clusters. Initialize cluster centres randomly, assign each point to its closest cluster by a distance metric. Recalculate centroids. Halt when cluster assignments no longer change. Clusters will be distinct and non-overlapping.

Goal to minimize within-cluster variation. The within-cluster variation for the kth cluster is the sum of all of the pairwise squared Euclidean distances between the observations in the kth cluster divided by the total number of observations in the kth cluster. Limitation is that it depends on initialization of centroids. Guaranteed convergence but only to a local minima. Run the algorithm several times and pick the solution that yields the smallest within-cluster variance. Increasing k will decrease variance and increase bias and vice versa. K-means: Jaccard coefficient.

Note: Not enough to use within-cluster variance as this decreases as one increases k. Use elbow method or scree plot to choose optimal k where the variance no longer decreases dramatically. To choose how many groups to use, I ran a k-means analysis for each possible number of groups from 5 to 35 and found that 20 was right about the spot that the amount of variance stopped decreasing consistently. This is called the elbow test and while the results weren't totally definitive, they fit in well with the general rule of thumb for determining # of groups which is the square root of the # of observations/2.

One way to assess whether a cluster represents true structure is to see if the cluster holds up under plausible variations in the dataset. The fpc package has a function called clusterboot() that uses bootstrap resampling to evaluate how stable a given cluster is.[3] clusterboot() is an integrated function that both performs the clustering and evaluates the final produced clusters. It has interfaces to a number of R clustering algorithms, including both hclust and kmeans.

In K-means, we assume that each cluster fits a Gaussian distribution (normal distribution)

We can set K to optimally cluster the data by starting with a small number of clusters, and then iteratively splitting them until all clusters fit a normal distribution.

Davies–Bouldin index: This is an internal evaluation scheme, where the validation of how well the clustering has been done is made using quantities and features inherent to the dataset. This has a drawback that a good value reported by this method does not imply the best information retrieval.

**Pros**

Uses simple principle which can be explained in non-statistical terms. It is efficient.

**Cons**

Less sophisticated, random choices of centers, and requires guess for centers.

**4.7 Hierarchical Clustering**

Generates dendrograms. The lower down a fusion occurs the more similar the group of observations and vice versa. Begin with  $n$  observations and a distance measure of all pairwise dissimilarities. Evaluate pairwise intercluster dissimilarities among the clusters and fuse pair of clusters that are least dissimilar. Repeat process for remaining clusters. Continue for  $i=n$  to  $i=2$ . Need to pick a dissimilarity measure and a linkage method. Complete linkage: maximal inter-cluster dissimilarity, single linkage: minimal inter-cluster dissimilarity, average linkage: mean inter-cluster dissimilarity. Complete is sensitive to outliers but tends to produce compact clusters. Distance between groups: complete, average, and ward. Single not as sensitive to outliers but susceptible to chaining effect where clusters can often not represent intuitive groups. Average strikes a balance between the two. Usually standardize data before clustering. Sklearn.metrics has pairwise distances.

K-Means vs Hierarchical Clustering: K-means clustering needs the number of clusters to be specified. Hierarchical clustering doesn't need the number of clusters to be specified. K-means clustering is usually more efficient run-time wise.

**4.7.1 Assumptions****4.7.2 Characteristics****4.7.3 Evaluation****4.7.4 Pros/Cons****4.8 PCA****4.8.1 Intro****4.8.2 Assumptions****4.8.3 Characteristics****4.8.4 Evaluation****4.8.5 Pros/Cons**

- Center and scale data. The eigenvectors yield orthogonal directions of greatest variability (principal components). The eigenvalues correspond to the magnitude of variance along the principal components. Interpretability is a negative. PCA is completely nonparametric: any data set can be plugged in and an answer comes out, requiring no parameters to tweak and no regard for how the data was recorded. From one perspective, the fact that PCA is non-parametric (or plug-and-play) can be considered a positive feature because the answer is unique and independent of the user. From another perspective the fact that PCA is agnostic to the source of the data is also a weakness. When using dimensional reduction we restrict ourselves to simpler models. Thus, we expect bias to increase and variance to decrease. Getting latent components. Visualize high dimensional data. Reduce noise. Preprocessing. scale and center

data before doing. Needs regularization. Too many principal components F1 score starts to drop after increase. Best F1 is 1. set number of components. Use `fit_transforms`, use `explained_variance_ratio_` to see how much of the variance is explained by each component. Choose features that explain most of the variances, then use a `inverse_transform` to reconstruct your `x`. Minimum number of principal components is  $\min(n, p)$ .

- `pca`: It accounts for as much of the variability in the data as possible by considering highly correlated features. Each succeeding component in turn has the highest variance using the features that are less correlated with the first principal component and that are orthogonal to the preceding component.

#### 4.8.6 Other

- 1) look at variance: `apply(USArrests, 2, var)` | 2) `pca` & scale: `pca = prcomp(USArrests, scale = TRUE)` | 3) plot: `biplot(pca, scale = 0)`
- `pca$rotation` contains the principal component loadings matrix which explains proportion of each variable along each principal component.
- Kaiser-Harris criterion suggests retaining PCs with eigenvalues  $> 1$ ; PCs with eigenvalues  $< 1$  explain less variance than contained in a single variable. Cattell Scree test visually inspects the elbow graph for diminishing return; retain PCs before a drastic drop-off.

PC columns contain loadings; correlations of the observed variables with the PCs. `h2` column displays the component communalities; amount of variance explained by the components.

Note: Look at `factorplot`. Shows pot of relationship between variables and principal components.

It is also possible to decompress the reduced dataset back to 784 dimensions by applying the inverse transformation of the PCA projection. Of course this won't give you back the original data, since the projection lost a bit of information (within the 5% variance that was dropped), but it will likely be quite close to the original data. The mean squared distance between the original data and the reconstructed data (compressed and then decompressed) is called the reconstruction error.

It turns out that many things behave very differently in high-dimensional space. For example, if you pick a random point in a unit square (a  $1 \times 1$  square), it will have only about a 0.4% chance of being located less than 0.001 from a border (in other words, it is very unlikely that a random point will be "extreme" along any dimension). But in a 10,000-dimensional unit hypercube (a  $1 \times 1 \times \dots \times 1$  cube, with ten thousand 1s), this probability is greater than 99.999999%. Most points in a high-dimensional hypercube are very close to the border.

Before looking at the PCA algorithm for dimensionality reduction in more detail, let's summarize the approach in a few simple steps: Standardize the  $d$ -dimensional dataset.

Construct the covariance matrix. Decompose the covariance matrix into its eigenvectors and eigenvalues. Select eigenvectors that correspond to the largest eigenvalues, where  $k$  is the dimensionality of the new feature subspace ( $k$ ).

Construct a projection matrix from the "top"  $k$  eigenvectors.

Transform the  $d$ -dimensional input dataset using the projection matrix to obtain the new  $k$ -dimensional feature subspace.

Probabilistic PCA introduces the Gaussian distribution to the PCA modeling framework.

Kernel PCA must project data into a higher dimensional space than that of the original data.

## 4.9 KNN

### 4.9.1 Intro

Calculate distance between each observation and all the others. Determine the  $k$  nearest observations to the observation. Classify the observation as the most frequent class of the  $k$  nearest observations. Small  $k$ 's are not robust to outliers, highlight local variations and induce unstable decision boundaries. Large  $k$ 's are robust to outliers, highlight global variations and induce stable decision boundaries. Good value to choose is  $k = \sqrt{n}$ . Can use maximum prior probability to decide ties. Use Euclidean distance for numerical data and Hamming distance for categorical data. Latter treats dimensions equally and is symmetric. Low  $k$  is low bias, high variance and high  $k$  is high bias low variance. 1NN can't adapt to outliers and has no notion of class frequencies. Can use weighted KNN. Easy in sklearn.

curse of dimensionality, overfitting, correlated features, cost to update, sensitivity of distance metrics

smaller  $k$  means smaller training error, ut larger  $k$  is more stable.

### 4.9.2 Assumptions

### 4.9.3 Characteristics

### 4.9.4 Evaluation

### 4.9.5 Pros/Cons

#### Pros

Only assumption is proximity. Non-parametric.

The only assumption we are making about our data is related to proximity (i. e., observations that are close by in the feature space are similar to each other in respect to the target value). We do not have to fit a model to the data since this is a non-parametric approach.

- Powerful
- No training involved ("lazy")
- Naturally handles multiclass classification and regression

What is a common drawback of 3NN classifiers? Prediction on large data sets is slow.

#### Cons

Have to decide  $k$  and distance metric. Can be sensitive to outliers or irrelevant attributes. Computationally expensive.

knn is terrible with high dimensions. Bad with categorical data.

Expensive and slow to predict new instances - Must define a meaningful distance function - Performs poorly on high-dimensionality datasets

We have to decide on  $K$  and a distance metric.

Can be sensitive to outliers or irrelevant attributes because they add noise.

Computationally expensive; as the number of observations, dimensions, and  $K$  increases, the time it takes for the algorithm to run and the space it takes to store the computations increases dramatically.



## 4.10 SVM

### 4.10.1 Intro

Selection of margin in SVM is a convex optimization problem. What is the objective of the maximum margin approach? To ensure small prediction error when the underlying distribution is not known

The LinearSVC class regularizes the bias term, so you should center the training set first by subtracting its mean. This is automatic if you scale the data using the StandardScaler. Moreover, make sure you set the loss hyperparameter to “hinge”, as it is not the default value. Finally, for better performance you should set the dual hyperparameter to False, unless there are more features than training instances (we will discuss duality later in the chapter).

With so many kernels to choose from, how can you decide which one to use? As a rule of thumb, you should always try the linear kernel first (remember that LinearSVC is much faster than SVC(kernel=“linear”)), especially if the training set is very large or if it has plenty of features. If the training set is not too large, you should try the Gaussian RBF kernel as well; it works well in most cases. Then if you have spare time and computing power, you can also experiment with a few other kernels using cross-validation and grid search, especially if there are kernels specialized for your training set’s data structure.

Here mostly talking about a maximal margin classifier. A separating hyperline of data of two classes. Maximizes distance to the nearest point in either class, i.e, the margin. Points which delineate the boundary are called support vectors. Correct classification first and then maximizing the margin. SVM only really works well with linear hyperplanes. The c hyperparameter deals with the tradeoff between a smooth decision boundary and correct classification. The larger the c the more points classified correctly as it increases the penalty for wrong classification. A smaller c gives more room for initial error which helps improve accuracy for not easily separable data. Work well in complicated domains with clear line of separation. Not so well in for large datasets because of training and not when there is a lot of noise. Can solve nonlinear decision boundaries by using polynomial terms. Kernel trick that draws boundaries by looking into higher dimensions.

Extracting the coefficients from the hyperplane equation (not including the intercept) yields what is called a normal vector. This vector points in a direction orthogonal to the surface of the hyperplane and essentially defines its orientation.

Big data set and lot of features SVM might be slow and prone to overfitting. SVM slower than naïve bayes. A kernel is a function that quantifies the similarity of two observations. The beauty of the “kernel trick” is that, even if there is an infinite-dimensional basis, we need only look at the  $n^2$  inner products between training data points. SVM not scale invariant. Check if library normalizes by default. RBF kernel is a good default. Try exponential sequences for parameters.

Extension of above info about relaxing margin. Doesn’t perfectly separate classes but is more robust to outliers. Helps better classify observations. Take a penalty by potentially misclassifying some observations. Have better predictive power. Called a soft margin. The C parameter is the budget for the slack variables which tell where observations are relative to the margin and hyperplane. Only observations that either fall on the margin or violate the margin affect the solution to the optimization problem. More robust than SVM.

When the support vector classifier is combined with a non-linear kernel, the resulting classifier is called a support vector machine.

Note: Important to make sure the normal vector is of unit length. For the radial kernel, suppose we have a test observation. If it is far from a training observation, the Euclidean distance will be large, but the value of the radial kernel will be small. Using kernels is much more computationally efficient because we only need to compute the kernel for distinct pairs of observations in our dataset. Furthermore, we need not actually work in the enlarged feature space. Intuitively, the gamma parameter defines how far the influence of a single training example reaches, with low values meaning ‘far’ and high values meaning ‘close’. The gamma parameters can be seen as the inverse of the radius of influence of samples selected by the model as support vectors.

## Multiclass

1v1: Construct a support vector machine for each pair of categories. For each classifier, record the prediction for each observation. Have the classifiers vote on the prediction for each observation.

1vAll: Construct a support vector machine for each individual category against all other categories combined. Assign the observation to the classifier with the largest function value.

### 4.10.2 Assumptions

### 4.10.3 Characteristics

### 4.10.4 Evaluation

### 4.10.5 Pros/Cons

#### Pros

- Performs similarly to logistic regression when linear separation
- Performs well with non-linear boundary depending on the kernel used
- Handle high dimensional data well
- Can model complex, nonlinear relationships
- Robust to noise (because they maximize margins)

#### Cons

- Susceptible to overfitting/training issues depending on kernel
- Need to select a good kernel function
- Model parameters are difficult to interpret
- Sometimes numerical stability problems
- Requires significant memory and processing power

## 4.11 Decision Tree

### 4.11.1 Intro

So should you use Gini impurity or entropy? The truth is, most of the time it does not make a big difference: they lead to similar trees. Gini impurity is slightly faster to compute, so it is a good default. However, when they differ, Gini impurity tends to isolate the most frequent class in its own branch of the tree, while entropy tends to produce slightly more balanced trees.

Decision Trees make very few assumptions about the training data (as opposed to linear models, which obviously assume that the data is linear, for example). Such a model is often called a nonparametric model, not because it does not have any parameters (it often has a lot) but because the number of parameters is not determined prior to training, so the model structure is free to stick closely to the data.

More generally, the main issue with Decision Trees is that they are very sensitive to small variations in the training data. For example, if you just remove the widest Iris-Versicolor from the iris training set (the one with petals 4.8 cm long and 1.8 cm wide) and train a new Decision Tree, you may get the model represented in Figure 6-8. As you can see, it looks very different from the previous Decision Tree (Figure 6-2). Actually,

since the training algorithm used by Scikit-Learn is stochastic<sup>6</sup> you may get very different models even on the same training data (unless you set the `random_state` hyperparameter).

Construct solutions that stratify the feature space into relatively easy to describe regions. Partition predictor space into rectangular or box-like regions. For regression predict the mean of the response variables in each region for the training observations in that space. Top down and greedy approach called recursive binary splitting to find best solution. Greedy because splits based on best result. The recursive binary splitting process depends on the greatest reduction in the RSS. Entropy very important. Decides where tree splits. Measure of impurity in examples. Entropy between 0 and 1. 0 means no impurity. Maximal is 1 when there is an even split between options. Key term: information gain. Decision tree maximizes this. Easy to interpret, prone to overfitting. Where each data point has its own node, the variance is high and the training error is 0. Deciding on the number of splits prior to building a tree isn't the best strategy. The best subtree will be the one that yields the lowest test error rate. Given a subtree, we can estimate the test error by implementing the crossvalidation process, but this is too cumbersome because the large number of possible subtrees. The tuning parameter  $\alpha$  helps balance the tradeoff between the overall complexity of the tree and its fit to the training data. Small values of  $\alpha$  yield trees that are quite extensive (have many terminal nodes). Large values of  $\alpha$  yield trees that are quite limited (have few terminal nodes). Similar to ridge/lasso regression. Ultimately, the subtree that is used for prediction is built using all of the available data with the determined optimal value of  $\alpha$ .

Regression: Use cost complexity pruning to build set of subtrees as a function of  $\lambda$ . Classification: Use Gini index, measures total variance among classes.

Note: Duplicate splits happen when they increase node purity. While pruning reduces the variance of the overall tree model upon repeated builds with different datasets, we induce bias because the trees are much simpler.

### 4.11.2 Assumptions

### 4.11.3 Characteristics

### 4.11.4 Evaluation

### 4.11.5 Pros/Cons

#### Pros

- Fast
- Robust to noise and missing values
- Accurate

#### Cons

- Weak predictive accuracy and prone to overfitting.
- Complex trees are hard to interpret
- Duplication within the same sub-tree is possible

## 4.12 Bagging

### 4.12.1 Intro

used to decrease variance in decision trees

How it works: train multiple trees using bootstrapped datasets, regression trees: average the predictions from all the trees, classification: take a majority vote of the predictions, majority vote: the class which occurs most frequently, Out of bag (OOB) error, Only a portion of the data is used to train each tree, The remaining data which wasn't selected can be used to assess the tree's performance, (the response for each observation is predicted using only the trees that were not fit using that observation)

Bagging involves randomly generating Bootstrap samples from the dataset and trains the models individually. Predictions are then made by aggregating or averaging all the response variables. For example, consider a dataset  $(X_i, Y_i)$ , where  $i=1 \dots n$ , contains  $n$  data points. Now, randomly select  $B$  samples with replacements from the original dataset using Bootstrap technique. Next, train the  $B$  samples with regression/classification models independently. Then, predictions are made on the test set by averaging the responses from all the  $B$  models generated in the case of regression. Alternatively, the most often occurring class among  $B$  samples is generated in the case of classification.

Bagging stabilizes decision trees and improves accuracy by reducing variance.

Bagging reduces generalization error.

Take repeated samples of the same size from the single overall training dataset. Treat these different sets of data as pseudo-training sets. Fitting separate, independent decision trees to each of the bootstrapped training data sets. We can then average all predictions (or take the majority vote) to obtain the bagged estimate. Instead of pruning back our trees, create very large trees in the first place. These large trees will tend to have low bias, but high variance. Retain the low bias, but get rid of the high variance by averaging. Con is that the trees are correlated. train multiple trees using bootstrapped data to reduce variance and prevent overfitting

### 4.12.2 Assumptions

### 4.12.3 Characteristics

### 4.12.4 Evaluation

### 4.12.5 Pros/Cons

#### Pros

- reduces variance in comparison to regular decision trees
- Can provide variable importance measures: classification: Gini index + regression: RSS
- Can easily handle qualitative (categorical) features
- Out of bag (OOB) estimates can be used for model validation

#### Cons

- Not as easy to visually interpret
- Does not reduce variance if the features are correlated

## 4.13 Random Forest

### 4.13.1 Intro

Build a number of decision trees using bootstrapped samples

At each split in the tree only a portion of the features are considered

a feature is selected from a subset of features not the whole feature space

the subset is usually  $\sqrt{n \cdot \text{features}}$

This allows trees to be built without some of the strong features decorrelates the trees, unlike bagging

Random forests are improvised supervised algorithms than bootstrap aggregation or bagging methods, though they are built on a similar approach. Unlike selecting all the variables in all the B samples generated using the Bootstrap technique in bagging, we select only a few predictor variables randomly from the total variables for each of the B samples. Then, these samples are trained with the models. Predictions are made by averaging the result of each model. The number of predictors in each sample is decided using the formula  $m = \sqrt{p}$ , where p is the total variable count in the original dataset. Here are some key notes: This approach removes the condition of dependency of strong predictors in the dataset as we intentionally select fewer variables.

Draw a random bootstrap sample of size n (randomly choose n samples from the training set with replacement). Grow a decision tree from the bootstrap sample. At each node: Randomly select d features without replacement. Split the node using the feature that provides the best split according to the objective function, for instance, by maximizing the information gain. Repeat the steps 1 to 2 k times. Aggregate the prediction by each tree to assign the class label by majority vote. Majority voting will be discussed in more detail in Chapter 7, Combining Different Models for Ensemble Learning.

Random forests further improve decision tree performance by de-correlating the individual trees in the bagging ensemble.

Random forests decorrelate tree it generates and thus results in a reduction in variance. Similar to bagging, we first build various decision trees on bootstrapped training samples, but we split internal nodes in a special way. Each time a split is considered within the construction of a decision tree, only a random subset of the overall predictors are allowed to be candidates. At every split, a new subset of predictors is randomly selected. The random forest procedure forces the decision tree building process to use different predictors to split at different times. Should a good predictor be left out of consideration for some splits, it still has many chances to be considered in the construction of other splits. We can't overfit by adding more trees. The variance just ends up decreasing. Out of bag score is a good estimate of the test score and is the non-bootstrapped data. Need to turn on this scoring method. Error Rate: Depends on correlation between trees (higher is worse), strength of single trees (higher is better). Increasing number of features for each split increases correlation and strength of single trees.

### 4.13.2 Assumptions

### 4.13.3 Characteristics

### 4.13.4 Evaluation

### 4.13.5 Pros/Cons

#### Pros

Decorrelates trees (relative to boosted trees)

important when dealing with multiple features which may be correlated

reduced variance (relative to regular trees)

All purpose model that performs well on most problems. Automatically chooses the best features. High accuracy.

#### Cons

Hard to interpret and needs a lot of work to tune parameters.

Not as easy to visually interpret

## 4.14 Boosting

### 4.14.1 Intro

Unlike boosting and random forests, can overfit if number of trees is too large

Similar to bagging, but trees are grown sequentially. Each tree is created using information from previously grown trees

Each tree is generated using information from previously grown trees; the addition of a new tree improves upon the performance of the previous trees. The trees are now dependent upon one another. Boosting approach tends to slowly learn our data. Given a current decision tree model, we fit a new decision tree to the residuals of the current decision tree. The new decision tree (based on the residuals) is then added to the current decision tree, and the residuals are updated. We limit the number of terminal nodes in order to sequentially fit small trees. By fitting small trees to the residuals, we slowly improve the overall model in areas where it does not perform well.

Note: Unlike in bagging and random forests, boosting can overfit if  $\alpha$  is large (although very slowly). Use cross-validation to select number of trees.  $\alpha$  controls the rate at which boosting learns and is usually between 0.01 to 0.001. A small  $\alpha$  usually goes with a large number of trees. Can also choose the number of splits. Typically using stumps (single splits  $d = 1$ ) is sufficient and results in an additive model.

Note on Variable Importance: For regression trees, we can use the reduction in the RSS. For classification trees, we can use the reduction in the Gini index. A relatively large value indicates a notable drop in the RSS or Gini index, and thus a better fit to the data; corresponding variables are relatively important predictors.

Similar to bagging, but learns sequentially and builds off previous trees

### 4.14.2 Assumptions

### 4.14.3 Characteristics

### 4.14.4 Evaluation

### 4.14.5 Pros/Cons

#### Pros

Somewhat more interpretable than boosted trees/random forest as the user can define the size of each tree resulting in a collection of stumps (1 level) which can be viewed as an additive model

Can easily handle qualitative (categorical) features

#### Cons

## 4.15 Association Rule Mining

### 4.15.1 Intro

- Used in Genetics, Fraud, and Market Basket Analysis, etc. A typical rule might be: if someone buys peanut butter and jelly, then that person is likely to buy bread as well.
- Tutorial: <http://pbpython.com/market-basket-analysis.html>
- Incredibly big feature space ( $2^k - 1$ ).
- The Apriori algorithm employs a simple a priori belief as a guideline for reducing the association rule space.
- Support: the fraction of which each item appears within the dataset as a whole.  $\text{Support}(\text{item}) = \text{count}(\text{item})/N$ . Higher support is better.
- Confidence: the likelihood that a constructed rule is correct given the items on the left hand side of the transaction. A higher level of confidence implies a higher likelihood that Y appears alongside transactions in which X appears.
- Lift: the ratio by which the confidence of a rule exceeds the expected outcome. When  $\text{lift} > 1$ , the presence of X seems to have increased the probability of Y occurring in the transaction. When  $\text{lift} < 1$ , the presence of X seems to have decreased the probability of Y occurring in the transaction. When  $\text{lift} = 1$ , X and Y are independent.
- $\text{min\_support}$  thresholds for support and confidence and then the algorithm goes from all 1-combinations to 2-combinations and up. Those subset below the threshold don't make it to the higher iterations.

### 4.15.2 Assumptions

### 4.15.3 Characteristics

### 4.15.4 Evaluation

### 4.15.5 Pros/Cons

#### Pros

- Ideally suited for working with very large amounts of transactional data.
- The results are rules that are generally easy to understand and have a high amount of interpretability.
- The process is useful for data mining and uncovering unexpected knowledge within a dataset.

#### Cons

- The outcome is usually not interesting when applied to smaller datasets.
- It is difficult to separate actual insights from common sense notions.
- The analyst might be compelled to draw spurious conclusions—remember that correlation doesn't imply causation!

## 4.16 Naïve Bayes

### 4.16.1 Intro

Practitioners do use Naive Bayes regularly for ranking, where the actual values of the probabilities are not relevant—only the relative values for examples in the different classes. Another advantage of Naive Bayes is that it is naturally an “incremental learner.” An incremental learner is an induction technique that can update its model one training example at a time. It does not need to reprocess all past training examples when new training data become available.

Document/spam classification is one use. Assumptions are that all the features are equally likely and are all important. Would be computationally expensive without these assumptions with having to track all the joint probabilities. Gaussian for continuous variables, Bernoulli for binary input, and Multinomial for binary and more input. Use MLE to estimate parameters for Gaussian. Bernoulli/Multinomial used for spam classification. The Laplace Estimator (usually chosen to be 1) is a corrective measure that adds a small amount of error to each of the counts in the frequency table of words. The addition of error ensures that each resulting probability of each event will necessarily be nonzero, even if the event did not appear in the training data.

Note: In addition, we can use function “partial\_fit” to fit on a batch of samples incrementally while we are using. MultinomialNB and Bernoulli NB also support sample weighting.

### 4.16.2 Assumptions

### 4.16.3 Characteristics

### 4.16.4 Evaluation

### 4.16.5 Pros/Cons

#### Pros

- It is relatively simple to understand. Training the classifier does not require many observations, and the method also works well with large amounts of data. It is easy to obtain the estimated probability for a classification prediction.
- Computationally fast
- Simple to implement
- Works well with high dimensions

#### Cons

- Relies on independence assumption and will perform badly if this assumption is not met
- While easily attainable, the estimated probabilities are often less reliable than the predicted class labels themselves.

## 4.17 LDA

### 4.17.1 Intro

Before we take a look into the inner workings of LDA in the following subsections, let’s summarize the key steps of the LDA approach:



Standardize the  $d$ -dimensional dataset ( $d$  is the number of features).

For each class, compute the  $d$ -dimensional mean vector.

Construct the between-class scatter matrix and the within-class scatter matrix  $S_B$  and  $S_W$ .

Compute the eigenvectors and corresponding eigenvalues of the matrix  $S_W^{-1} S_B$ .

Choose the eigenvectors that correspond to the largest eigenvalues to construct a  $d'$ -dimensional transformation matrix  $T$ ; the eigenvectors are the columns of this matrix.

Project the samples onto the new feature subspace using the transformation matrix  $T$ .

LDA similar to Naive Bayes but doesn't assume variables are independent, assumes that  $p(x|y)$  is a multivariate normal distribution, and assumes gaussian distributions for each class share the same covariance matrix. If they don't share the same covariance matrix, then we use Quadratic Discriminant Analysis which assumes each class has its own.

### 4.17.2 Assumptions

### 4.17.3 Characteristics

### 4.17.4 Evaluation

### 4.17.5 Pros/Cons

## 4.18 QDA

### 4.18.1 Intro

TBD

### 4.18.2 Assumptions

### 4.18.3 Characteristics

### 4.18.4 Evaluation

### 4.18.5 Pros/Cons

## 4.19 DataCamp: Nonlinear Modeling in R with GAMs

Wiggliness affected by smoothing factor ( $sp$ ) and number of basis functions ( $k$ )

```
gam(y ~ s(x, k = 3), data = df, sp = .1) gam(y ~ s(x, k = 3), data = df, method = "REML")
```

Categorical features must be included as factors.

```
gam(hw.mpg ~ s(weight) + fuel, data = mpg, method = "REML")
```

A factor smooth interaction fits different models for different categorical vars.

```
gam(hw.mpg ~ s(weight, by = fuel) + fuel, data = mpg, method = "REML")
```

Summary:

edf=1 is a straight line

Visualize:

```
plot(mod, select = 1, seWithMean = TRUE, shift = coef(mod)[1])
```

Model Evaluation:

gam.check: Bad if model hasn't converged. Likely due to too many features. Small p-values indicate residuals not randomly distributed which is often due to not enough basis functions.

first do concurvity(mod, full = T) then do concurvity(mod, full = F). check co-linearity. worst case is bad over 0.8.

```
interaction b/w x & y: mod2d <- gam(cadmium ~ s(x, y), data = meuse, method = "REML")
```

vis.gam for visualization

```
vis.gam(mod2d, view = c("x", "y"), plot.type = "persp", se = 2, theta = 135)
```

```
vis.gam(mod2d, view = c("x", "y"), plot.type = "contour", too.far = 0.05)
```

```
vis.gam(mod2d, view = c("x", "y"), plot.type = "contour", too.far = .1)
```

```
Make plot with 25% extrapolation vis.gam(mod2d, view = c("x", "y"), plot.type = "contour", too.far = .25)
```

Overlay data points(meuse)

Nonlinear Modeling in R with GAMs:

```
Fit a model with a factor-smooth interaction: mod_fs <- gam(copper ~ s(dist, landuse, bs = "fs"), data = meuse, method = "REML")
```

```
Plot both models making 3D perspective plots: vis.gam(mod_sep, view = c("dist", "landuse"), plot.type = "persp")
```

2-way interactions: 2d interaction smooths, categorical-continuous interaction, tensor smooths: allow to model on different scales (space & time)

```
tensor_mod <- gam(cadmium ~ te(x, y, elev), data = meuse, method = "REML")
```

Single-variable smooths use s(). Smooths in which multiple variables interact on the same scale also use s(). Smooths that have only interactions, but have multiple lambda terms or scales, use ti().

te() must be used along. if you include s() switch to ti()

classification:

outputs on the log odds scale

```
#Plot with intercept uncertainty
plot(log_mod2, pages = 1, trans = plogis, shift = coef(log_mod2)[1], seWithMean = TRUE)

#log odds scale
predict(mdl, type = "link")

#probability scale
predict(mdl, type = "response")

#construct se.fit on log odds scale than transform to probs with plogis
predict(mdl, type = "link", se.fit = T)

#granular for each record on log odds scale
predict(mdl, type = "terms")
```

```
# Calculate predictions and errors
predictions <- predict(log_mod2, newdata = new_credit_data,
                        type = "link", se.fit = TRUE)

# Calculate high and low predictions intervals
high_pred <- predictions$fit + 2*predictions$se.fit
low_pred <- predictions$fit - 2*predictions$se.fit

# Convert intervals to probability scale
high_prob <- plogis(high_pred)
low_prob <- plogis(low_pred)
```

gams work with broom and caret.



## Chapter 5

# Hierarchical Models

“Across counties, as the average mother’s age increases the birth rate decreases while correcting for state-level impacts”  $\text{BirthRate} \sim \text{AverageAgeofMother} + (1 \mid \text{State})$

`lmerTest`

Analysis of Variance, or ANOVA, can be used to compare two different lmer models and test if one model explains more variability than the other model. We can use this to compare two lmer models. For example, if we wanted to see if Year is important for predicting Crime in Maryland, we can build a null model with only County as a random-effect and a year model that includes Year.

- One far out suggestion in one of the links is to do PCA and then regress the original variables against the new axis.
- Account for longitudinal data: random selection of one event from each student, partition cross validation by dates, pca finds major trends hidden within the data



## Chapter 6

# Communicate, Deploy, Maintain

### 6.1 Communicate

Summarize the motivation and goals of the project. It should either be an executive summary or a technical abstract.

State results with details as needed. For an end user presentation show how the model fits into and improves the user's workflow, and how to use it.

Discuss recommendations, outstanding issues, and possible future work.

Introduction | Motivation | Summary | Results | Conclusion

### 6.2 Deploy

### 6.3 Maintain





# Chapter 7

## Time Series

### 7.1 Notes

A stationary time series is one whose properties do not depend on the time at which the series is observed.

### 7.2 Packages

<https://robjhyndman.com/seminars/user-fable/>    <https://github.com/robjhyndman/forecast>    [https://facebook.github.io/prophet/docs/quick\\_start.html](https://facebook.github.io/prophet/docs/quick_start.html)    <https://keras.rstudio.com/articles/examples/index.html>  
<http://www.business-science.io/code-tools/2017/05/02/timekit-0-2-0.html>    <https://www.rdocumentation.org/packages/bsts/versions/0.8.0>

### 7.3 Data Conversion

<https://robjhyndman.com/hyndsight/seasonal-periods/>

```
dt = as.Date(StockData$Date, format="%m/%d/%Y") > Stockdataz = zoo(x=cbind(StockData$Volume, StockData$Adj),
ts: frequency = 5 means that data is at daily level business days
ts(completed_example_data$Wind, start = c(1973, 5, 1), frequency = 365.25)

x = xts(df[, -1], order.by = as.Date(df[, 1], "%m/%d/%Y"))
```

### 7.4 Models

Exponential smoothing and ARIMA models are the two most widely used approaches to time series forecasting, and provide complementary approaches to the problem. While exponential smoothing models are based on a description of the trend and seasonality in the data, ARIMA models aim to describe the autocorrelations in the data.

Benchmark models: Mean, naive, seasonal naive

0. Mean

1. Naive: Set all forecasts to be the value of the last observation. This method works remarkably well for many economic and financial time series. Because a naive forecast is optimal when data follow a random walk, these are also called random walk forecasts. `naive()`
2. Seasonal Naive: Assumes magnitude of the seasonal pattern is constant. `snaive()`

#### Linear

10. regression: `tslm()`: trend and season are not objects in the R workspace; they are created automatically by `tslm()` when specified in this way: `tslm(beer2 ~ trend + season)`. It is not recommended that quadratic or higher order trends be used in forecasting. When they are extrapolated, the resulting forecasts are often unrealistic.
11. harmonic regression: An alternative to using seasonal dummy variables, especially for long seasonal periods, is to use Fourier terms.  $i$ th Fourier terms, we often need fewer predictors than with dummy variables, especially when  $m$  is large. This makes them useful for weekly data, for example, where  $m = 52$ . For short seasonal periods (e.g., quarterly data), there is little advantage in using Fourier terms over seasonal dummy variables. `fourier()` - `tslm(beer2 ~ trend + fourier(beer2, K=2))`
12. Dynamic Regression

The R function `Arima()` will fit a regression model with ARIMA errors if the argument `xreg` is used. The order argument specifies the order of the ARIMA error model. If differencing is specified, then the differencing is applied to all variables in the regression model before the model is estimated.

```
Arima(y, xreg=x, order=c(1,1,0)) auto.arima(uschange[, "Consumption"], xreg=uschange[, "Income"])
```

There are two different ways of modelling a linear trend: deterministic and stochastic.

```
deterministic: fit1 <- auto.arima(austa, d=0, xreg=trend)
```

```
stochastic: fit2 <- auto.arima(austa, d=1)
```

There is an implicit assumption with deterministic trends that the slope of the trend is not going to change over time. On the other hand, stochastic trends can change, and the estimated growth is only assumed to be the average growth over the historical period, not necessarily the rate of growth that will be observed into the future. Consequently, it is safer to forecast with stochastic trends, especially for longer forecast horizons, as the prediction intervals allow for greater uncertainty in future growth.

When there are long seasonal periods, a dynamic regression with Fourier terms is often better than other models we have considered in this book.

Seasonal differencing of high order does not make a lot of sense — for daily data it involves comparing what happened today with what happened exactly a year ago and there is no constraint that the seasonal pattern is smooth.

So for such time series, we prefer a harmonic regression approach where the seasonal pattern is modelled using Fourier terms with short-term time series dynamics handled by an ARMA error.

```
fit <- auto.arima(caffe04, xreg = fourier(caffe04, K = i), seasonal = FALSE, lambda = 0)
```

#### ETS (Error-Trend-Seasonality) Models

This label can also be thought of as Exponential Smoothing. The possibilities for each component are: Error = {a,m}, Trend = {n,a,a\_d}, and Seasonal = {n,a,m}. Therefore, for each component in the ETS system, we can assign None, Multiplicative, or Additive (or N, M, A) for each of the three components in our time series.

Three of the combinations of (Error, Trend, Seasonal) can lead to numerical difficulties. Specifically, the models that can cause such instabilities are ETS(A,N,M), ETS(A,A,M), and ETS(A,A d ,M), due to division by values potentially close to zero in the state equations. We normally do not consider these particular combinations when selecting a model.

Models with multiplicative errors are useful when the data are strictly positive, but are not numerically stable when the data contain zeros or negative values. Therefore, multiplicative error models will not be considered if the time series is not strictly positive. In that case, only the six fully additive models will be applied.

The `ets()` function does not produce forecasts. Rather, it estimates the model parameters and returns information about the fitted model. By default it uses the AICc to select an appropriate model

ETS point forecasts are equal to the medians of the forecast distributions. For models with only additive components, the forecast distributions are normal, so the medians and means are equal. For ETS models with multiplicative errors, or with multiplicative seasonality, the point forecasts will not be equal to the means of the forecast distributions.

1. Simple Exponential Smoothing Method: Time series does not have a trend line and does not have seasonality component. We would use a Simple Exponential Smoothing model.  
ETS(A,N,N): simple exponential smoothing with additive errors | ETS(M,N,N): simple exponential smoothing with multiplicative errors
2. Holt's Linear Trend Method: Damped Holt's method is best whether you compare MAE or MSE values. So we will proceed with using the damped Holt's method and apply it to the whole data set to get forecasts for future years. Forecasts account for trend & continue at the same trend indefinitely into the future: `holt(damped = T)`. A damped trend makes it level off after time: `holt(damped = F)` ( $\phi = 1$  is Holt's method).

`holt()` | ETS(A,A,N): Holt's linear method with additive errors | ETS(M,A,N): Holt's linear method with multiplicative errors | (a,a) Additive Holt-Winters' method | (a,m) Multiplicative Holt-Winters' method | (a\_d,m) Holt-Winters' damped method | (a,n) Holt's linear method | (a\_d,n) Additive damped trend method

8. Holt-Winters Seasonal Method: `hw(aust,seasonal="additive")`. Accounts for trend and seasonality. In the additive version the seasonality averages to 0 but this changes to 1 in the multiplicative version

ARIMA(p,d,q): non-seasonal: White noise: ARIMA(0,0,0) Random walk: ARIMA(0,1,0) with no constant Random walk with drift: ARIMA(0,1,0) with a constant Autoregression: ARIMA(p,0,0) Moving average: ARIMA(0,0,q)

Seasonal ARIMA(p,d,q)(P,D,Q)\_m

`auto.arima()` does an auto fit.

When fitting an ARIMA model to a set of (non-seasonal) time series data, the following procedure provides a useful general approach.

Plot the data and identify any unusual observations.

If necessary, transform the data (using a Box-Cox transformation) to stabilize the variance.

If the data are non-stationary, take first differences of the data until the data are stationary.

Examine the ACF/PACF: Is an ARIMA(p,d,0) or ARIMA(0,d,q) model appropriate?

Try your chosen model(s), and use the AICc to search for a better model.

Check the residuals from your chosen model by plotting the ACF of the residuals, and doing a portmanteau test of the residuals. If they do not look like white noise, try a modified model.

Once the residuals look like white noise, calculate forecasts.

`auto.arima` only does steps 3-5.

`arima()`

`ggAcf()` | `ggPacf()`

If the data are from an  $\text{ARIMA}(p,d,0)$  or  $\text{ARIMA}(0,d,q)$  model, then the ACF and PACF plots can be helpful in determining the value of  $p/q$ . If  $p$  and  $q$  are both positive, then the plots do not help in finding suitable values of  $p$  and  $q$ .

The data may follow an  $\text{ARIMA}(p,d,0)$  model if the ACF and PACF plots of the differenced data show the following patterns:

the ACF is exponentially decaying or sinusoidal; there is a significant spike at lag  $p$  in the PACF, but none beyond lag  $p$ .

The data may follow an  $\text{ARIMA}(0,d,q)$  model if the ACF and PACF plots of the differenced data show the following patterns:

the PACF is exponentially decaying or sinusoidal; there is a significant spike at lag  $q$  in the ACF, but none beyond lag  $q$ .

seasnal arima: `arima(p,d,q) (P,Q,D)_m`,  $m$  = num of observations per year

The seasonal part of an AR or MA model will be seen in the seasonal lags of the PACF and ACF. For example, an  $\text{ARIMA}(0,0,0)(0,0,1)_{12}$  model will show:

a spike at lag 12 in the ACF but no other significant spikes; exponential decay in the seasonal lags of the PACF (i.e., at lags 12, 24, 36, ...).

`Arima(euroretail, order=c(0,1,3), seasonal=c(0,1,1))`

`auto.arima(euroretail, stepwise=FALSE, approximation=FALSE)`

comparing information criteria is only valid for ARIMA models of the same orders of differencing.

Other

1. `ma`
2. `wma`
3. X11 method: `seasonal::seas(x11 = ")`. from this output `seasonal()` will extract the seasonal component, `trendcycle()` will extract the trend-cycle component, `remainder()` will extract the remainder component, and `seasadj()` will compute the seasonally adjusted time series.
4. SEATS: `seasonal::seas()`
5. STL: best so far but only uses additive decomposition. `stl(t.window=13, s.window="periodic", robust=TRUE)`. automate picking of first 2 params with `mstl()`. A short-cut approach is to use the `stlf()` function. The following code will decompose the time series using STL, forecast the seasonally adjusted series, and return reseasonalize the forecasts: `stlf(elecequip, method='naive')`

`msts | mstsl | tbats | bld.mbb.bootstrap`

Auto Model:

`forecast()`: You can use this directly if you have no idea which model to use, or use it to produce forecasts after fitting a model.

Hierarchical:

`gts() | hts() | aggts()`

- Feature Engineering

<https://github.com/robjhyndman/tsfeatures>

There are several useful predictors that occur frequently when using regression for time series data:

- 1) A trend variable can be specified in the `tslm()` function using the trend predictor.

- 2) dummy variables for time like day of week. The `tslm()` function will automatically handle this situation if you specify the predictor season.
- 3) interventions, eg. competitor activity
- 4) trading days: `bizdays()`
- 5) distributed lags
- 6) `easter()`

Use lagged values of predictors

A log-log functional form is specified as  $\log(y) = \text{beta\_0} + \text{beta\_1} * \log(x) + \text{epsilon}$

scaling by `monthday()` by population or by inflation for money

Logarithms are useful because they are interpretable: changes in a log value are relative (or percentage) changes on the original scale. So if log base 10 is used, then an increase of 1 on the log scale corresponds to a multiplication of 10 on the original scale. Another useful feature of log transformations is that they constrain the forecasts to stay positive on the original scale. A log transformation can address heteroskedasticity.

`boxCox()/boxCox.lambda()`, power transforms,

bias adjustments: mean of forecast distribution instead of median for back-transformed forecast. Bias adjustment is not done by default in the forecast package. If you want your forecasts to be means rather than medians, use the argument `biasadj=TRUE` when you select your Box-Cox transformation parameter.

- Model Evaluation

train-test split: `window()` / `subset()`

`accuracy()`

`tsCV()`

A great advantage of the ETS statistical framework is that information criteria can be used for model selection - AIC, AIC\_c, and BIC

leave-one-out cross-validation statistic : `CV(fit.consMR)` for model selection

we recommend that one of the AICc, AIC, or CV statistics be used, each of which has forecasting as their objective.

When comparing forecast methods applied to a single time series, or to several time series with the same units, the MAE is popular as it is easy to both understand and compute. A forecast method that minimizes the MAE will lead to forecasts of the median, while minimizing the RMSE will lead to forecasts of the mean. Consequently, the RMSE is also widely used, despite being more difficult to interpret. Percentage errors have the advantage of being unit-free, and so are frequently used to compare forecast performances between data sets. The most commonly used measure is Mean Absolute Percentage Error (MAPE) or symmetric MAPE. forecast errors are different from residuals in two ways. First, residuals are calculated on the training set while forecast errors are calculated on the test set. Second, residuals are based on one-step forecasts while forecast errors can involve multi-step forecasts.

A good forecasting method will yield residuals with the following properties:

- 1) The residuals are uncorrelated. If there are correlations between residuals, then there is information left in the residuals which should be used in computing forecasts.
- 2) The residuals have zero mean. If the residuals have a mean other than zero, then the forecasts are biased. (Adjusting for bias is easy: if the residuals have mean  $m$  then add  $m$  to all forecasts and the bias problem is solved.)
- 3) It is useful (but not necessary) for the residuals to also have the following two properties: the residuals have constant variance and are normally distributed.

use the Box-Ljung test to test for autocorrelations: `h_0`: no autocorrelation, `h_a`: autocorrelation.

`checkresiduals()` which will produce a time plot, ACF plot and histogram of the residuals (with an overlaid normal distribution for comparison), and do a Ljung-Box test with the correct degrees of freedom.

#### -Notes

Fourier terms in `lm` good for intraday data.

Methods with multiplicative trend produce poor forecasts.

For stock market prices and indexes, the best forecasting method is often the naïve method. Use also dynamic regression.

Create time series with `ts(mydata[-1], start = c(1981, 1), frequency = 4)`

Time series that show no auto-correlation are called white noise. For white noise series, we expect each auto-correlation to be close to zero. For a white noise series, we expect 95% of the spikes in the ACF to lie within  $\pm 2 * \sqrt{T}$  where  $T$  is the length of the time series.

The possible time series (TS) scenarios can be recognized by asking the following questions: 1) TS has a trend? If yes, is the trend increasing linearly or exponentially? 2) TS has seasonality? If yes, do the seasonal components increase in magnitude over time?

Additive model for linear trend and multiplicative model for exponential trend. Additive for trend and Multiplicative and Additive for seasonal components. For trends that are exponential, we would need to use a multiplicative model. For increasing seasonality components, we would need to use a multiplicative model as well.

Therefore we can generalize all of these models using a naming system for ETS:

Error is the error line we saw in the time series decomposition part earlier in the course. If the error is increasing similar to an increasing seasonal components, we would need to consider a multiplicative design for the exponential model.

A time series model that has a constant error, linear trend, and increasing seasonal components means we would need to use an ETS model of `ETS(N,A,M)`

A time series model that has increasing error, exponential trend, and no seasonality means we would need to use an ETS model of:

non-stationary: This plot shows an upward trend and seasonality.

stationary: This plot revolves around a constant mean of 0 and shows contained variance.

#### -Metrics

Percentage errors, like MAPE, are useful because they are scale independent, so they can be used to compare forecasts between different data series, unlike scale dependent errors. The disadvantage is that it cannot be used if the series has zero values.

Mean Absolute Percentage Error (MAPE) is also often useful for purposes of reporting, because it is expressed in generic percentage terms it will make sense even to someone who has no idea what constitutes a “big” error in terms of dollars spent or widgets sold.

Mean Absolute Scaled Error (MASE) is another relative measure of error that is applicable only to time series data. It is defined as the mean absolute error of the model divided by the the mean absolute value of the first difference of the series. Thus, it measures the relative reduction in error compared to a naïve model. Ideally its value will be significantly less than 1 but is relative to comparison across other models for the same series. Since this error measurement is relative and can be applied across models, it is accepted as one of the best metrics for error measurement.

`AIC_c` for model selection.

**7.4.1 Intro****7.4.2 Assumptions****7.4.3 Characteristics****7.4.4 Evaluation****7.4.5 Pros/Cons****Pros****Cons**

- Seasonal Decomposition; Use additive model when the magnitude of the seasonal fluctuations surrounding the general trend doesn't vary over time. Use the multiplicative model when the magnitude of the seasonal fluctuations surrounding the general trend appear to change in a proportional manner over time. Go from additive to multiplicative with a log transformation.
- White noise: Describes the assumption that each element in the time series is a random draw from  $N(0, \text{constant variance})$ . Also called a stationary series. Time series with trends or seasonality are not stationary.

**ARIMA(p,d,q) (Auto-Regressive Integrated Moving Average) Models**

- AR(p): auto-regressive component for lags on the stationary series. The AR models say that the value of a variable at a specific time is related to the value of the variable at previous times.
- I(d): Integrated component for a series that needs to be differenced.
- MA(q): Moving average component for lag of the forecast errors. In a moving average model of order q, each value in a time series is predicted from the linear combination of the previous q errors. The value of a variable at a specific time is related to the residuals of prediction at previous times.
- In an auto-regressive model of order p, each value in a time series is predicted from a linear combination of the previous p values.
- Procedure: Make stationary if necessary by differencing. Determine possible values of p and q. Assess model fit and try other values of p and q to overfit. Make forecasts with the final model.
- Augmented Dicky-Fuller Test: This tests whether or not a time series is stationary.  $H_0$ : series is not stationary,  $H_a$ : the series is stationary.
- Determine p and q: Look at autocorrelation (AC) and partial correlation (PAC) functions. AC measures the way observations relate to each other. PAC measure the way observations relate to each other after accounting for all other intervening observations. Plot of the autocorrelation function (ACF) displays correlation of the series with itself at different lags. A plot of the PAC displays the amount of autocorrelation not explained by lower order correlations. Spikes in the PACF will choose for AR(p). Spikes in the ACF will choose MA(q).

**Assess Model Fit**

- Appropriate model should resemble white noise. Check scatterplot of residuals vs fit to check constant variance and qqplot to check normality. Autocorrelations should be zero to check for violation of independent errors.
- Box-Ljung Test: Check if all autocorrelations are zero, i.e the series is of white noise.  $H_0$ : autocorrelations are all 0.  $H_a$ : At least one is nonzero.
- Overfit model with extra AR/MA terms and compare using AIC/BIC.

- Interpretation: AR coefficient closer to 1 means series returns to mean slowly, vice versa for closer to 0.
- MA(1) coefficient indicates how much the shock of the previous time period is retained in the current time period. MA(2) refers to the previous two time periods.

## 7.5 DSP

FFT: time x amplitude to frequency x strength of signal domain

$y(t) = \text{Amplitude} * \sin(2\pi \text{freqtime} + \text{phase\_shift})$

The reduction of a continuous time signal to a discrete time signal is known as sampling

wavelets: continuous (time frequency analysis) vs discrete (data compression & noise reduction).

pipeline: signal -> wavelet transform -> pca -> features to classifier

## 7.6 Forecasting: Principles & Practice

### 7.6.1 C1-3

library(forecast) | ts | autoplot / autolayer | ggseasonplot | ggsubseriesplot | ggagplot | window | meanf | s/naive | residuals | gghistogram | ggAcf |

counterfactual plot

`myts <- ts(mydata[-1], start = c(1981, 1), frequency = 4)`

Time series that show no autocorrelation are called white noise.

For white noise series, we expect each autocorrelation to be close to zero. Of course, they will not be exactly equal to zero as there is some random variation. For a white noise series, we expect 95% of the spikes in the ACF to lie within

$\pm 2 * \sqrt{T}$  where T is the length of the time series.

For naïve forecasts, we simply set all forecasts to be the value of the last observation. This method works remarkably well for many economic and financial time series. Because a naïve forecast is optimal when data follow a random walk (see Section 8.1), these are also called random walk forecasts.

mean, naïve, and seasonal naïve are benchmarks.

feature engineering: scaling by monthday(), by population, inflation for money, log, boxCox()/boxCox.lambda(), power transforms, bias adjustments: mean of forecast distribution instead of median for back-transformed forecast,

Bias adjustment is not done by default in the forecast package. If you want your forecasts to be means rather than medians, use the argument `biasadj=TRUE` when you select your Box-Cox transformation parameter.

Logarithms are useful because they are interpretable: changes in a log value are relative (or percentage) changes on the original scale. So if log base 10 is used, then an increase of 1 on the log scale corresponds to a multiplication of 10 on the original scale. Another useful feature of log transformations is that they constrain the forecasts to stay positive on the original scale.

A good forecasting method will yield residuals with the following properties:

The residuals are uncorrelated. If there are correlations between residuals, then there is information left in the residuals which should be used in computing forecasts.



The residuals have zero mean. If the residuals have a mean other than zero, then the forecasts are biased.

Adjusting for bias is easy: if the residuals have mean  $m$  then add  $m$  to all forecasts and the bias problem is solved.

It is useful (but not necessary) for the residuals to also have the following two properties: the residuals have constant variance and are normally distributed.

For stock market prices and indexes, the best forecasting method is often the naïve method.

Recall that  $r_k$  is the autocorrelation for lag  $k$ . When we look at the ACF plot to see whether each spike is within the required limits, we are implicitly carrying out multiple hypothesis tests, each one with a small probability of giving a false positive. When enough of these tests are done, it is likely that at least one will give a false positive, and so we may conclude that the residuals have some remaining autocorrelation, when in fact they do not. In order to overcome this problem, we test whether the first  $h$  autocorrelations are significantly different from what would be expected from a white noise process. A test for a group of autocorrelations is called a portmanteau test, from a French word describing a suitcase containing a number of items. Use Box-Pierce/Ljung-Box test.

Large values of suggest that the autocorrelations do not come from a white noise series.

All of these methods for checking residuals are conveniently packaged into one R function `checkresiduals()`, which will produce a time plot, ACF plot and histogram of the residuals (with an overlaid normal distribution for comparison), and do a Ljung-Box test with the correct degrees of freedom.

train-test split: `window()/subset()`

forecast errors are different from residuals in two ways. First, residuals are calculated on the training set while forecast errors are calculated on the test set. Second, residuals are based on one-step forecasts while forecast errors can involve multi-step forecasts.

When comparing forecast methods applied to a single time series, or to several time series with the same units, the MAE is popular as it is easy to both understand and compute. A forecast method that minimizes the MAE will lead to forecasts of the median, while minimizing the RMSE will lead to forecasts of the mean. Consequently, the RMSE is also widely used, despite being more difficult to interpret. Percentage errors have the advantage of being unit-free, and so are frequently used to compare forecast performances between data sets. The most commonly used measure is Mean Absolute Percentage Error (MAPE) or symmetric MAPE.

`accuracy()`

With time series forecasting, one-step forecasts may not be as relevant as multi-step forecasts. In this case, the cross-validation procedure based on a rolling forecasting origin can be modified to allow multi-step errors to be used.

`tsCV()`

a prediction interval gives an interval within which we expect  $y_t$  to lie with a specified probability.

When forecasting one step ahead, the standard deviation of the forecast distribution is almost the same as the standard deviation of the residuals.

`forecast()`: You can use this directly if you have no idea which model to use, or use it to produce forecasts after fitting a model.

`checkresiduals()`

### 7.6.2 C4

There are three general settings in which judgmental forecasting is used: (i) there are no available data, so that statistical methods are not applicable and judgmental forecasting is the only feasible approach; (ii) data

are available, statistical forecasts are generated, and these are then adjusted using judgement; and (iii) data are available and statistical and judgmental forecasts are generated independently and then combined.

### 7.6.3 C5

`tslm()`

Another useful test of autocorrelation in the residuals designed to take account for the regression model is the Breusch-Godfrey test, also referred to as the LM (Lagrange Multiplier) test for serial correlation. It is used to test the joint hypothesis that there is no autocorrelation in the residuals up to a certain specified order. A small p-value indicates there is significant autocorrelation remaining in the residuals. The Breusch-Godfrey test is similar to the Ljung-Box test, but it is specifically designed for use with regression models.

More often than not, time series data are “non-stationary”; that is, the values of the time series do not fluctuate around a constant mean or with a constant variance.

There are several useful predictors that occur frequently when using regression for time series data:

- A trend variable can be specified in the `tslm()` function using the trend predictor.
- dummy variables for time like day of week. The `tslm()` function will automatically handle this situation if you specify the predictor season.

trend and season are not objects in the R workspace; they are created automatically by `tslm()` when specified in this way: `tslm(beer2 ~ trend + season)`

- interventions, eg. competitor activity
- trading days: `bizdays()`
- distributed lags
- `easter()`
- An alternative to using seasonal dummy variables, especially for long seasonal periods, is to use Fourier terms. With Fourier terms, we often need fewer predictors than with dummy variables, especially when  $m$  is large. This makes them useful for weekly data, for example, where  $m = 52$ . For short seasonal periods (e.g., quarterly data), there is little advantage in using Fourier terms over seasonal dummy variables. `fourier()` - `tslm(beer2 ~ trend + fourier(beer2, K=2))`

A regression model containing Fourier terms is often called a harmonic regression because the successive Fourier terms represent harmonics of the first two Fourier terms.

leave-one-out cross-validation statistic : `CV(fit.consMR)` for model selection

we recommend that one of the AICc, AIC, or CV statistics be used, each of which has forecasting as their objective.

Ex-ante forecasts are those that are made using only the information that is available in advance. Ex-post forecasts are those that are made using later information on the predictors. These are not genuine forecasts, but are useful for studying the behavior of forecasting models.

Use lagged values of predictors

A log-log functional form is specified as  $\log(y) = \beta_0 + \beta_1 \log(x) + \epsilon$

In this model, the slope can be interpreted as an elasticity, and is the average percentage change in  $y$  resulting from a 1% increase in  $x$ . Other useful forms can also be specified. The log-linear form is specified by only transforming the forecast variable and the linear-log form is obtained by transforming the predictor.

It is not recommended that quadratic or higher order trends be used in forecasting. When they are extrapolated, the resulting forecasts are often unrealistic.

```
fit.exp <- tslm(marathon ~ trend, lambda = 0)
splinef(lambda=0)
```

A log transformation can address heteroskedasticity.

#### 7.6.4 C6

Thus we think of a time series as comprising three components: a trend-cycle component, a seasonal component, and a remainder component (containing anything else in the time series).

$y = s + t + r$  or  $y = str$ .  $s$  is seasonal,  $t$  is trend,  $r$  is the remainder

The additive decomposition is the most appropriate if the magnitude of the seasonal fluctuations, or the variation around the trend-cycle, does not vary with the level of the time series. When the variation in the seasonal pattern, or the variation around the trend-cycle, appears to be proportional to the level of the time series, then a multiplicative decomposition is more appropriate. Multiplicative decompositions are common with economic time series.

An alternative to using a multiplicative decomposition is to first transform the data until the variation in the series appears to be stable over time, then use an additive decomposition. When a log transformation has been used, this is equivalent to using a multiplicative decomposition

Remove seasonality to make data seasonally adjusted. Remove when not needed.

simple moving average of order  $m$ : `ma(electsales, 5)`.  $m$  is usually odd so the sma is symmetric. It is possible to apply a moving average to a moving average. One reason for doing this is to make an even-order moving average symmetric. The notation “2x4-MA” in the last column means a 4-MA followed by a 2-MA. Called a centered MA of order 4.

The most common use of centered moving averages is for estimating the trend-cycle from seasonal data.

In general, a  $2xm$ -MA is equivalent to a weighted moving average of order  $m+1$  where all observations take the weight  $1/m$  except for the first and last terms which take weights  $1/2m$ .

wma

additive/multiplicative decomposition (`decompose(type=“multiplicative”)`) not used now because there are better methods.

Another popular method for decomposing quarterly and monthly data is the X11 method: `seasonal::seas(x11 = ”)`. from this output `seasonal()` will extract the seasonal component, `trendcycle()` will extract the trend-cycle component, `remainder()` will extract the remainder component, and `seasadj()` will compute the seasonally adjusted time series.

SEATS: `seasonal::seas()`

STL: best so far but only uses additive decomposition. `stl(t.window=13, s.window=“periodic”, robust=TRUE)`. automate picking of first 2 params with `mstl()`

A time series decomposition can be used to measure the strength of trend and seasonality in a time series. A series with seasonal strength close to 0 exhibits almost no seasonality, while a series with strong seasonality will have close to 1

While decomposition is primarily useful for studying time series data, and exploring historical changes over time, it can also be used in forecasting.

To forecast a decomposed time series, we forecast the seasonal component and the seasonally adjusted component separately. It is usually assumed that the seasonal component is unchanging, or changing extremely slowly, so it is forecast by simply taking the last year of the estimated component. In other words, a seasonal naïve method is used for the seasonal component.

To forecast the seasonally adjusted component, any non-seasonal forecasting method may be used. For example, a random walk with drift model, or Holt's method (discussed in the next chapter), or a non-seasonal ARIMA model.

A short-cut approach is to use the `stlf()` function. The following code will decompose the time series using STL, forecast the seasonally adjusted series, and return reseasonalized forecasts: `stlf(elecequip, method='naive')`

### 7.6.5 C7

simple exponential smoothing: For example, it may be sensible to attach larger weights to more recent observations than to observations from the distant past. This is exactly the concept behind simple exponential smoothing. It has the weighted average form, component form,

exponential smoothing has a “flat” forecast function. That is, all forecasts take the same value, equal to the last level component. Remember that these forecasts will only be suitable if the time series has no trend or seasonal component.

The application of every exponential smoothing method requires the smoothing parameters and the initial values to be chosen. This is a nonlinear optimization.

holt linear trend: `holt()`. Damped Holt's method is best whether you compare MAE or MSE values. So we will proceed with using the damped Holt's method and apply it to the whole data set to get forecasts for future years.

holt-winters seasonal method: `hw(aust,seasonal="additive")`

A method that often provides accurate and robust forecasts for seasonal data is the Holt-Winters method with a damped trend and multiplicative seasonality: `hw(y, damped=TRUE, seasonal="multiplicative")`

Each method is labelled by a pair of letters (T,S) defining the type of ‘Trend’ and ‘Seasonal’ components. For example, (A,M) is the method with an additive trend and multiplicative seasonality; (A\_d, N) is the method with damped trend and no seasonality, and so on.

short_hand	method
(n,n)	Simple exponential smoothing
(a,n)	Holt's linear method
(a_d,n)	Additive damped trend method
(a,a)	Additive Holt-Winters' method
(a,m)	Multiplicative Holt-Winters' method
(a_d,m)	Holt-Winters' damped method

Each model consists of a measurement equation that describes the observed data, and some state equations that describe how the unobserved components or states (level, trend, seasonal) change over time. Hence, these are referred to as state space models. For each method there exist two models: one with additive errors and one with multiplicative errors. The point forecasts produced by the models are identical if they use the same smoothing parameter values. They will, however, generate different prediction intervals.

To distinguish between a model with additive errors and one with multiplicative errors (and also to distinguish the models from the methods), we add a third letter to the classification of the table above. We label each state space model as ETS (Error, Trend, Seasonal). This label can also be thought of as Exponential Smoothing. The possibilities for each component are: Error = {a,m}, Trend = {n,a,a\_d}, and Seasonal = {n,a,m}.

ETS(A,N,N): simple exponential smoothing with additive errors

ETS(M,N,N): simple exponential smoothing with multiplicative errors

ETS(A,A,N): Holt's linear method with additive errors

ETS(M,A,N): Holt's linear method with multiplicative errors

An alternative to estimating the parameters by minimizing the sum of squared errors is to maximize the “likelihood”. The likelihood is the probability of the data arising from the specified model. Thus, a large likelihood is associated with a good model. For an additive error model, maximizing the likelihood gives the same results as minimizing the sum of squared errors. However, different results will be obtained for multiplicative error models.

Model Selection: A great advantage of the ETS statistical framework is that information criteria can be used for model selection - AIC, AIC<sub>c</sub>, and BIC

Three of the combinations of (Error, Trend, Seasonal) can lead to numerical difficulties. Specifically, the models that can cause such instabilities are ETS(A,N,M), ETS(A,A,M), and ETS(A,A d,M), due to division by values potentially close to zero in the state equations. We normally do not consider these particular combinations when selecting a model.

Models with multiplicative errors are useful when the data are strictly positive, but are not numerically stable when the data contain zeros or negative values. Therefore, multiplicative error models will not be considered if the time series is not strictly positive. In that case, only the six fully additive models will be applied.

The `ets()` function does not produce forecasts. Rather, it estimates the model parameters and returns information about the fitted model. By default it uses the AIC<sub>c</sub> to select an appropriate model

```
ets(y, model="ZZZ", damped=NULL, alpha=NULL, beta=NULL, gamma=NULL, phi=NULL,
lambda=NULL, biasadj=FALSE, additive.only=FALSE, restrict=TRUE, allow.multiplicative.trend=FALSE)
```

Point forecasts are obtained from the models by iterating the equations for  $t = T+1 \rightarrow T + h$  and setting all  $e_t = 0$  for  $t > T$ . These forecasts are identical to the forecasts from Holt's linear method, and also to those from model ETS(A,A,N). Thus, the point forecasts obtained from the method and from the two models that underlie the method are identical (assuming that the same parameter values are used).

ETS point forecasts are equal to the medians of the forecast distributions. For models with only additive components, the forecast distributions are normal, so the medians and means are equal. For ETS models with multiplicative errors, or with multiplicative seasonality, the point forecasts will not be equal to the means of the forecast distributions.

```
forecast: ets_fit %>% forecast(h=8)
```

### 7.6.6 C8: arima

Exponential smoothing and ARIMA models are the two most widely used approaches to time series forecasting, and provide complementary approaches to the problem. While exponential smoothing models are based on a description of the trend and seasonality in the data, ARIMA models aim to describe the autocorrelations in the data.

A stationary time series is one whose properties do not depend on the time at which the series is observed.<sup>14</sup> Thus, time series with trends, or with seasonality, are not stationary — the trend and seasonality will affect the value of the time series at different times. On the other hand, a white noise series is stationary — it does not matter when you observe it, it should look much the same at any point in time.

Some cases can be confusing — a time series with cyclic behaviour (but with no trend or seasonality) is stationary. This is because the cycles are not of a fixed length, so before we observe the series we cannot be sure where the peaks and troughs of the cycles will be.

In general, a stationary time series will have no predictable patterns in the long-term. Time plots will show the series to be roughly horizontal (although some cyclic behavior is possible), with constant variance.

note that the Google stock price was non-stationary in panel (a), but the daily changes were stationary in panel (b). This shows one way to make a non-stationary time series stationary — compute the differences between consecutive observations. This is known as differencing.

The ACF of the differenced Google stock price looks just like that of a white noise series. There are no autocorrelations lying outside the 95% limits, and the Ljung-Box statistic has a p-value of 0.355 (for  $h=10$ ). This suggests that the daily change in the Google stock price is essentially a random amount which is uncorrelated with that of previous days.

The differenced series is the change between consecutive observations in the original series, and can be written as:  $y_t^* = y_t - y_{t-1}$

When the differenced series is white noise, the model for the original series can be written as  $y_t - y_{t-1} = e_t$  (white noise)

Random walk models are widely used for non-stationary data, particularly financial and economic data. Random walks typically have: long periods of apparent trends up or down, sudden and unpredictable changes in direction.

In practice, it is almost never necessary to go beyond second-order differences.

A seasonal difference is the difference between an observation and the previous observation from the same season.

If seasonally differenced data appear to be white noise, then an appropriate model for the original data is  $y_t = y_{t-m} + e_t$ . Forecasts from this model are equal to the last observation from the relevant season. That is, this model gives seasonal naïve forecasts.

Sometimes it is necessary to take both a seasonal difference and a first difference to obtain stationary data

When both seasonal and first differences are applied, it makes no difference which is done first—the result will be the same. However, if the data have a strong seasonal pattern, we recommend that seasonal differencing be done first, because the resulting series will sometimes be stationary and there will be no need for a further first difference. If first differencing is done first, there will still be seasonality present.

One way to determine more objectively whether differencing is required is to use a unit root test. These are statistical hypothesis tests of stationarity that are designed for determining whether differencing is required.

A number of unit root tests are available, which are based on different assumptions and may lead to conflicting answers. In our analysis, we use the Kwiatkowski-Phillips-Schmidt-Shin (KPSS) test. In this test, the null hypothesis is that the data are stationary, and we look for evidence that the null hypothesis is false. Consequently, small p-values (e.g., less than 0.05) suggest that differencing is required. The test can be computed using the `ur.kpss()` function from the `urca` package.

This process of using a sequence of KPSS tests to determine the appropriate number of first differences is carried out by the function `ndiffs()`

A similar function for determining whether seasonal differencing is required is `nsdiffs()`, which uses the measure of seasonal strength

The backward shift operator  $B$  is a useful notational device when working with time series lags. The backward shift operator is convenient for describing the process of differencing. A first difference can be written as:

$$y_t' = y_t - y_{t-1} = y_t - by_t = (1-b)y_t$$

In general, a  $d$  th-order difference can be written as:  $(y_t)^d = (1-b)^d y_t$

In a multiple regression model, we forecast the variable of interest using a linear combination of predictors. In an auto-regression model, we forecast the variable of interest using a linear combination of past values of the variable. We refer to this as an  $AR(p)$  model, an autoregressive model of order  $p$ .

for  $ar(1)$  model,  $y_t$  is white noise when  $\beta_1$  is 0, a random walk when  $\beta_1$  is 1 and  $\beta_0$  is 0, a random walk with drift when  $\beta_1$  is 1 and  $\beta_0$  is not zero, and  $y_t$  oscillates if  $\beta_1$  is negative.

We normally restrict autoregressive models to stationary data, in which case some constraints on the values of the parameters are required.

Rather than using past values of the forecast variable in a regression, a moving average model uses past forecast errors in a regression-like model. We refer to this as an MA( $q$ ) model, a moving average model of order  $q$ .

If we combine differencing with autoregression and a moving average model, we obtain a non-seasonal ARIMA model. ARIMA is an acronym for AutoRegressive Integrated Moving Average

The “predictors” include both lagged values of  $y_t$  and lagged errors. We call this an ARIMA( $p,d,q$ ) model, where  $p$  is the order of the autoregressive part;  $d$  is the degree of first differencing involved, and  $q$  is the order of the moving average part.

The same stationarity and invertibility conditions that are used for autoregressive and moving average models also apply to an ARIMA model.

White noise: ARIMA(0,0,0) Random walk: ARIMA(0,1,0) with no constant Random walk with drift: ARIMA(0,1,0) with a constant Autoregression: ARIMA( $p,0,0$ ) Moving average: ARIMA(0,0, $q$ )

`auto.arima()` does an auto fit.

The constant  $c$  has an important effect on the long-term forecasts obtained from these models.

If  $c=0$  and  $d=0$ , the long-term forecasts will go to zero. If  $c=0$  and  $d=1$ , the long-term forecasts will go to a non-zero constant. If  $c=0$  and  $d=2$ , the long-term forecasts will follow a straight line. If  $c \neq 0$  and  $d=0$ , the long-term forecasts will go to the mean of the data. If  $c \neq 0$  and  $d=1$ , the long-term forecasts will follow a straight line. If  $c \neq 0$  and  $d=2$ , the long-term forecasts will follow a quadratic trend.

The value of  $d$  also has an effect on the prediction intervals — the higher the value of  $d$ , the more rapidly the prediction intervals increase in size. For

$d=0$ , the long-term forecast standard deviation will go to the standard deviation of the historical data, so the prediction intervals will all be essentially the same.

partial autocorrelations. These measure the relationship between  $y_t$  and  $y_{t-k}$  after removing the effects of lags 1,2,3,...

It is sometimes possible to use the ACF plot, and the closely related PACF plot, to determine appropriate values for  $p$  &  $q$ .

`ggAcf()` | `ggPacf()`

If the data are from an ARIMA( $p,d,0$ ) or ARIMA(0, $d,q$ ) model, then the ACF and PACF plots can be helpful in determining the value of  $p/q$ . If  $p$  and  $q$  are both positive, then the plots do not help in finding suitable values of  $p$  and  $q$ .

The data may follow an ARIMA( $p,d,0$ ) model if the ACF and PACF plots of the differenced data show the following patterns:

the ACF is exponentially decaying or sinusoidal; there is a significant spike at lag  $p$  in the PACF, but none beyond lag  $p$ .

The data may follow an ARIMA(0, $d,q$ ) model if the ACF and PACF plots of the differenced data show the following patterns:

the PACF is exponentially decaying or sinusoidal; there is a significant spike at lag  $q$  in the ACF, but none beyond lag  $q$ .

`Arima()`

When fitting an ARIMA model to a set of (non-seasonal) time series data, the following procedure provides a useful general approach.

1. Plot the data and identify any unusual observations.

2. If necessary, transform the data (using a Box-Cox transformation) to stabilize the variance.
3. If the data are non-stationary, take first differences of the data until the data are stationary.
4. Examine the ACF/PACF: Is an ARIMA(p,d,0) or ARIMA(0,d,q) model appropriate?
5. Try your chosen model(s), and use the AICc to search for a better model.
6. Check the residuals from your chosen model by plotting the ACF of the residuals, and doing a port-manteau test of the residuals. If they do not look like white noise, try a modified model.
7. Once the residuals look like white noise, calculate forecasts.

auto.arima only does steps 3-5.

```
eeadj %>% diff() %>% ggtsdisplay(main="")
```

The inclusion of a constant in a non-stationary ARIMA model is equivalent to inducing a polynomial trend of order d in the forecast function.

```
seasnal arima: arima(p,d,q) (P,Q,D)_m, m = num of observations per year
```

The seasonal part of an AR or MA model will be seen in the seasonal lags of the PACF and ACF. For example, an ARIMA(0,0,0)(0,0,1)<sub>12</sub> model will show:

a spike at lag 12 in the ACF but no other significant spikes; exponential decay in the seasonal lags of the PACF (i.e., at lags 12, 24, 36, ...).

```
Arima(eurotail, order=c(0,1,3), seasonal=c(0,1,1))
```

```
auto.arima(eurotail, stepwise=FALSE, approximation=FALSE)
```

comparing information criteria is only valid for ARIMA models of the same orders of differencing.

### 7.6.7 C9

The time series models in the previous two chapters allow for the inclusion of information from past observations of a series, but not for the inclusion of other information that may also be relevant. For example, the effects of holidays, competitor activity, changes in the law, the wider economy, or other external variables, may explain some of the historical variation and may lead to more accurate forecasts. On the other hand, the regression models in Chapter 5 allow for the inclusion of a lot of relevant information from predictor variables, but do not allow for the subtle time series dynamics that can be handled with ARIMA models. In this chapter, we consider how to extend ARIMA models in order to allow other information to be included in the models.

The R function Arima() will fit a regression model with ARIMA errors if the argument xreg is used. The order argument specifies the order of the ARIMA error model. If differencing is specified, then the differencing is applied to all variables in the regression model before the model is estimated.

```
Arima(y, xreg=x, order=c(1,1,0)) auto.arima(uschange[,“Consumption”], xreg=uschange[,“Income”])
```

```
cbind(“Regression Errors” = residuals(fit, type=“regression”), “ARIMA errors” = residuals(fit, type=“innovation”)) %>% autoplot(facets=TRUE)
```

## 9.4

There are two different ways of modelling a linear trend: deterministic and stochastic.

```
deterministic: fit1 <- auto.arima(austa, d=0, xreg=trend)
```

```
stochastic: fit2 <- auto.arima(austa, d=1)
```

There is an implicit assumption with deterministic trends that the slope of the trend is not going to change over time. On the other hand, stochastic trends can change, and the estimated growth is only assumed to be



the average growth over the historical period, not necessarily the rate of growth that will be observed into the future. Consequently, it is safer to forecast with stochastic trends, especially for longer forecast horizons, as the prediction intervals allow for greater uncertainty in future growth.

## 9.5

When there are long seasonal periods, a dynamic regression with Fourier terms is often better than other models we have considered in this book.

Seasonal differencing of high order does not make a lot of sense — for daily data it involves comparing what happened today with what happened exactly a year ago and there is no constraint that the seasonal pattern is smooth.

So for such time series, we prefer a harmonic regression approach where the seasonal pattern is modelled using Fourier terms with short-term time series dynamics handled by an ARMA error.

```
fit <- auto.arima(caf04, xreg = fourier(caf04, K = i), seasonal = FALSE, lambda = 0)
```

## 7.6.8 C10

### 10.2

```
gts() | hts() | aggts()
```

### 10.3

```
hts::
```

## 7.6.9 C11

So far, we have considered relatively simple seasonal patterns such as quarterly and monthly data. However, higher frequency time series often exhibit more complicated seasonal patterns. For example, daily data may have a weekly pattern as well as an annual pattern. Hourly data usually has three types of seasonality: a daily pattern, a weekly pattern, and an annual pattern

```
msts | mstsl | tbats |
```

```
bld.mbb.bootstrap
```

## 7.6.10 C12

```
stlf
```

The best way to deal with moving holiday effects is to use dummy variables. However, neither STL, ETS nor TBATS models allow for covariates. Amongst the models discussed in this book (and implemented in the forecast package for R), the only choice is a dynamic regression model, where the predictors include any dummy holiday effects (and possibly also the seasonality using Fourier terms).

To impose a positivity constraint, simply work on the log scale, by specifying the Box-Cox parameter  $\lambda = 0$ .

we can transform the data using a scaled logit transform which maps  $y$  to the whole real line:  $y = \log((x-a)/(b-x))$

Most time series models do not work well for very long time series. The problem is that real data do not come from the models we use. When the number of observations is not large (say up to about 200) the models often work well as an approximation to whatever process generated the data. But eventually we will have enough data that the difference between the true process and the model starts to become more obvious.

An additional problem is that the optimization of the parameters becomes more time consuming because of the number of observations involved.

## 7.7 Forecasting Datacamp

annual data can't be seasonal. seasonal has fixed lengths, cyclical doesn't.

When data are either seasonal or cyclic, the ACF will peak around the seasonal lags or at the average cycle length.

white noise is iid data. 95% of autocorrelations should be within blue lines of acf plot.

There is a well-known result in economics called the “Efficient Market Hypothesis” that states that asset prices reflect all available information. A consequence of this is that the daily changes in stock prices should behave like white noise (ignoring dividends, interest rates and transaction costs). The consequence for forecasters is that the best forecast of the future price is the current price.

`diff()` for daily changes

Time series forecasting is typically discussed where only a one-step prediction is required.

What about when you need to predict multiple time steps into the future?

Predicting multiple time steps into the future is called multi-step time series forecasting. There are four main strategies that you can use for multi-step forecasting.

Generally, time series forecasting describes predicting the observation at the next time step. This is called a one-step forecast, as only one time step is to be predicted. There are some time series problems where multiple time steps must be predicted. Contrasted to the one-step forecast, these are called multiple-step or multi-step time series forecasting problems.

A good model forecasts well (so has low RMSE on the test set) and uses all available information in the training data (so has white noise residuals).

`subset.ts()` | `meanf` | `mape` allows for cross model comparison

simple exponential smoothing: large alpha puts more weight on recent values and the weights decay quickly. `ses()`. Has the same value for all forecasts.

Let's review the process:

First, import and load your data. Determine how much of your data you want to allocate to training, and how much to testing; the sets should not overlap.

Subset the data to create a training set, which you will use as an argument in your forecasting function(s). Optionally, you can also create a test set to use later.

Compute forecasts of the training set using whichever forecasting function(s) you choose, and set `h` equal to the number of values you want to forecast, which is also the length of the test set.

To view the results, use the `accuracy()` function with the forecast as the first argument and original data (or test set) as the second.

Pick a measure in the output, such as RMSE or MAE, to evaluate the forecast(s); a smaller error indicates higher accuracy.

Holt's Linear Trend: Forecasts account for trend & continue at the same trend indefinitely into the future: `holt(damped = T)`. A damped trend makes it level off after time: `holt(damped = F)` (`phi = 1` is Holt's method).

Holt-Winters Method: Accounts for trend and seasonality. In the additive version the seasonality averages to 0 but this changes to 1 in the multiplicative version: `hw(df, seasonal = 'additive')`

Methods with multiplicative trend produce poor forecasts.

Innovation State Space Models

trends = {n, a, a\_d} {none, additive, damped}

seasons = {n, a, m} {none, additive, multiplicative}

So there are 9 possible exponential smoothing methods. Add:

error = {a,m}

And there are 18 possible state space models. Known as ets models. Estimated using likelihood. Choose model by minimizing AIC\_c (biased correct AIC). Roughly the same as time series CV but is much faster: ets()

transforms: square root, cube root, log, inverse (increasing strength of transformation from left to right). Equal to  $\lambda = 1/2$ ,  $L = 1/3$ ,  $L = 0$ ,  $L = -1$  for Box-Cox. ( $L=0$  is no transformation.)

Not common to use box-cox with ets since ets can handle seasons & trends. Use box-cox with arima models when there is increasing variation.

BoxCox.lambda()

Differencing is a way of making a time series stationary; this means that you remove any systematic patterns such as trend and seasonality from the data. A white noise series is considered a special case of a stationary time series. With non-seasonal data, you use lag-1 differences to model changes between observations rather than the observations directly. You have done this before by using the diff() function.

With seasonal data, differences are often taken between observations in the same season of consecutive years, rather than in consecutive periods. For example, with quarterly data, one would take the difference between Q1 in one year and Q1 in the previous year. This is called seasonal differencing. Sometimes you need to apply both seasonal differences and lag-1 differences to the same series, thus, calculating the differences in the differences.

auto.arima()

Don't compare an arima AIC\_c with one from an ets. Comparisons only work within models of the same type.

The Arima() function can be used to select a specific ARIMA model. Its first argument, order, is set to a vector that specifies the values of p, d and q. The second argument, include.constant, is a boolean that determines if the constant c, or drift, should be included.

```
# Set up forecast functions for ETS and ARIMA models
fets <- function(x, h) {
  forecast(ets(x), h = h)
}
farima <- function(x, h) {
  forecast(____, ____)
```

The AICc statistic is useful for selecting between models in the same class. For example, you can use it to select an ETS model or to select an ARIMA model. However, you cannot use it to compare ETS and ARIMA models because they are in different model classes. Instead, you can use time series cross-validation to compare an ARIMA model and an ETS model on the austa data. Because tsCV() requires functions that return forecast objects, you will set up some simple functions that fit the models and return the forecasts.

seasonal arima: arima (p,d,q) (P,D,Q)\_m. Coefficients are hard to interpret for original data.

```
austa %>% Arima(order = c(2,1,3), include.constant = T) %>% forecast() %>% autoplot()
```

To make `auto.arima()` work harder to find a good model, add the optional argument `stepwise = FALSE` to look at a much larger collection of models.

What happens when you want to create training and test sets for data that is more frequent than yearly? If needed, you can use a vector in form `c(year, period)` for the start and/or end keywords in the `window()` function. You must also ensure that you're using the appropriate values of `h` in forecasting functions. Recall that `h` should be equal to the length of the data that makes up your test

In dynamic regression the error term is an arima process.

`autoplot(advert, facets = TRUE)` #2nd param scales vars to be comparable coefficients(fit)[3]

dynamic harmonic regression uses Fourier series: `e_t` is non-seasonal since Fourier handles that. Assumes seasonality doesn't change. Only need to select `k` for complexity. Start from `k=1` and choose model with lowest `aic_c`. `k <= m/2` where `m` is the seasonal period. Good when the seasonality is very large, weekly, daily, sub-daily, etc. The higher the order (`K`), the more "wiggly" the seasonal pattern is allowed to be. With `K=1`, it is a simple sine curve.

```
# Set up harmonic regressors of order 13
harmonics <- fourier(gasoline, K = 13)
# Fit regression model with ARIMA errors
fit <- auto.arima(gasoline, xreg = harmonics, seasonal = FALSE)
# Forecasts next 3 years
fc <- forecast(fit, xreg = fourier(gasoline, K = 13, h = 156))
# Plot forecasts fc
autoplot(fc)
```

Harmonic regressions are also useful when time series have multiple seasonal patterns.

```
tslm()
# Fit a harmonic regression using order 10 for each type of seasonality
fit <- tslm(taylor ~ fourier(taylor, K = c(10, 10)))
# Forecast 20 working days ahead
fc <- forecast(fit, newdata = data.frame(fourier(taylor, K = c(10, 10), h = 960)))
# Plot the forecasts
autoplot(fc)
# Check the residuals of fit
checkresiduals(fit)
```

Another time series with multiple seasonal periods is `calls`, which contains 20 consecutive days of 5-minute call volume data for a large North American bank. There are 169 5-minute periods in a working day, and so the weekly seasonal frequency is  $5 \times 169 = 845$ . The weekly seasonality is relatively weak, so here you will just model daily seasonality.

The residuals in this case still fail the white noise tests, but their autocorrelations are tiny, even though they are significant. This is because the series is so long. It is often unrealistic to have residuals that pass the tests for such long series. The effect of the remaining correlations on the forecasts will be negligible.

`tbats` model: automates everything. `tbats()`, Good for data with large and multiple seasonal periods.

Let's break down elements of a TBATS model in `TBATS(1, {0,0}, -, {<51.18,14>})`, one of the graph titles from the video (Component: Meaning):

1: Box-Cox transformation parameter

{0,0}: ARMA error

-:Damping parameter

{<51.18,14>}: Seasonal period, Fourier terms

# Chapter 8

## Stats

### 8.1 General

ecdf: 1 | 2

<http://www.stat.umn.edu/geyer/old/5101/rlook.html>

<https://stats.idre.ucla.edu/other/mult-pkg/whatstat/>

categorical    dissimilarity    <https://www.rdocumentation.org/packages/StatMatch/versions/1.2.5/topics/gower.dist>

<http://frog.oerc.ox.ac.uk:8080/stato-app/>

Pearson's Coefficient of Skewness | Bayes factor | Correction methods for non representative samples | Numeric-Categorical Correlation    <https://www.rdocumentation.org/packages/lrm/versions/1.1-1/topics/biserial.cor>

Outliers in small samples: <https://stats.stackexchange.com/questions/78609/outlier-detection-in-very-small-sets/78617#78617>

Since all outcomes are 0 or 1, and drawn with the same (unknown) probability, we know that the number of ones and zeros follows a binomial distribution. This means that the confidence interval of a “k out of n” scenario is a Beta distribution.

Another common measure of effect size is d, sometimes known as Cohen's d (as you might have guessed by now, Cohen was quite influential in the field of effect sizes). This can be used when comparing two means, as when you might do a t-test, and is simply the difference in the two groups' means divided by the average of their standard deviations\*. This means that if we see a d of 1, we know that the two groups' means differ by one standard deviation; a d of .5 tells us that the two groups' means differ by half a standard deviation; and so on. Cohen suggested that d=0.2 be considered a 'small' effect size, 0.5 represents a 'medium' effect size and 0.8 a 'large' effect size. This means that if two groups' means don't differ by 0.2 standard deviations or more, the difference is trivial, even if it is statistically significant.

Beta Distribution: The larger the alpha parameter is the closer the resulting distribution is to 1.0 and the larger the beta the closer it is to 0.

Fisher's Exact Test: Test for proportions

cohen's f<sup>2</sup> | <https://stats.stackexchange.com/questions/266003/interpretation-of-cohens-f2-for-effect-size-in-multiple-regression> | [https://www.researchgate.net/post/How\\_to\\_calculate\\_the\\_effect\\_size\\_in\\_multiple\\_linear\\_regression\\_analysis](https://www.researchgate.net/post/How_to_calculate_the_effect_size_in_multiple_linear_regression_analysis)

Bayes Rule: Posterior = Likelihood \* Prior / Marginal Likelihood

<https://www.rdocumentation.org/packages/effsize/versions/0.7.1/topics/cohen.d>

Likelihood  $P(\text{Data}|\theta)$ : Probability of the data could be generated by a model with the given parameter(s)

Prior  $P(\theta)$ : Probability of parameter value

Posterior  $P(\theta|D)$ : Credibility of the parameter value with the data taken into account.

Marginal Likelihood (Evidence): Probability of evidence

Variance: Spread of the data | Distance from the mean

Standard Deviation: Square root of the variance | Same units as the data

Mean: Average/Expected Value

Covariance: Measure of how two random values change together. Negative - variables show opposite behavior (As A increases B decreases). Positive - variables show similar behavior (As A increases B increases)

Pearson Correlation: Normalized version of covariance

Median: Number at the halfway point of the dataset, found through sorting data into ascending order and selecting middle point

Mode: Most frequent value in dataset

Note about Populations and Samples: Populations have parameters. Samples have statistics.

Distributions:

Normal/Gaussian: Parameters are mean and standard deviation. Bell shaped. z-score: indicates how many standard deviations an element is from the mean

Student t: used to estimate the mean of a normally distributed population where the sample size is small and the standard deviation is unknown

A t test (t.test in R) is a special case of an ANOVA and a paired t test (parameter paired = T) is a special case of a repeated measures ANOVA.

Sample size: A good formula is: if your sample is picked uniformly at random and is of size at least:

$$\frac{-\log(\frac{\delta}{2})}{2e^2}$$

then with probability at least  $1-d$  your sample measured proportion  $q$  is no further away than  $e$  from the unknown true population proportion  $p$  (what you are trying to estimate). Need to estimate with 99% certainty the unknown true population rate to  $\pm 10\%$  precision? That is  $d=0.01$ ,  $e=0.1$  and a sample of size 265 should be enough. A stricter precision of  $\pm 0.05$  causes the estimated sample size to increase to 1060, but increasing the certainty requirement to 99.5% only increases the estimated sample size to 300.

- Type I Error: Saying there is an effect when there isn't one. Type II error: concluding there is no effect when, in fact, there is one.
- The MWW RankSum test is a useful test to determine if two distributions are significantly different or not. Unlike the t-test, the RankSum test does not assume that the data are normally distributed, potentially providing a more accurate assessment of the data sets.
- Probably the most useful types of statistics for skewed probability distributions are quantiles.
- Hypothesis testing requires an inferential-statistical approach. Crucial are meaningful distributions of test statistics, on which p-values for hypothesis tests can be based. It is not trivial to construct such "meaningful distributions" for complete network data!
- Random sampling & random assignment: generalizable & causal
- Get 95% ci around p-value

- There is no one rule about when a number is not accurate enough to use, but as a rule of thumb, you should be cautious about using any number with a MOE (Margin-of-error) over 10%.
- Probability is calibrated if it is empirically correct, i.e. the empirical probability matches the theoretical one.
- Effect size
- `jarque.bera.test`: Tests the null of normality for the series using the Jarque-Bera test statistics
- `box.test`: Compute the Box-Pierce or Ljung-Box test statistics for examining the null of independence in a given series
- `shapiro.test`: Test for normality
- Sum of normally distributed random variables: sum of means & sum of variances
- Zero correlation doesn't mean independent variables. Covariance only determines linear relationships.
- test heteroscedasticity: `breusch-pagan` or `ncv` test
- Test Normality: Shapiro-Wilk test is a test of normality
- Bypass inferential stats if features at least 1/10 of data points.
- The probability (p-value) of observing results at least as extreme as what is present in your data sample. P-value less than .05 retain `h_0` else reject `h_0`.
- One Sample T-test: To examine the average difference between a sample and the known value of the population mean. Assumes the population from which the sample is drawn is normally distributed and the sample observations are randomly drawn and independent.
- Two Sample T-test: To examine the average difference between two samples drawn from two different populations. Assumes the populations from which the samples are drawn are normally dist, the standard deviations of the two populations are equal, and sample observations are randomly drawn and independent.
- One-Way ANOVA: To assess the equality of means of two or more groups. Assumes the populations from which the samples are drawn are normally dist, the standard deviations of the populations are equal, and sample observations are randomly drawn and independent.
- Chi-Squared Test of Independence: To test whether two categorical variables are independent. Assumes the sample observations are randomly drawn and independent.
- F-Test: To assess whether the variances of two different populations are equal. Assumes the population from which the sample is drawn is normally distributed and the sample observations are randomly drawn and independent.
- Barlett Test: F-Test for more than two populations.
- If we take a larger and larger sample from a population, its distribution will tend to become normal no matter what it is initially. It won't. The Central Limit Theorem, the misreading of which is the cause of this mistake, refers to the distribution of standardized sums of random variables as their number grow, not to the distribution of a collection of random variables.
- Frequentists: Probability is a measure of the the frequency of repeated events. The parameters are fixed (but unknown) and data are random.
- Bayesians: Probability is a measure of the degree of certainty about values, so the interpretation is that rameters are random and data are fixed.
- Independent rvs are uncorrelated. That is  $\text{Cor}(X,Y)=0$
- Don't sum sd's, sum variances.

- One Sample T-Test? To examine the average difference between a sample and the known value of the population mean. Assumptions: The population from which the sample is drawn is normally distributed. Sample observations are randomly drawn and independent.
- When do we use the Two Sample T-Test? To examine the average difference between two samples drawn from two different populations. Assumptions: The populations from which the samples are drawn are normally dist. The standard deviations of the two populations are equal. Sample observations are randomly drawn and independent.
- When do we use the F-Test? To assess whether the variances of two different populations are equal. Assumptions: The populations from which the samples are drawn are normally dist. Sample observations are randomly drawn and independent.
- When do we use One-Way ANOVA? To assess the equality of means of two or more groups. NB: When there are exactly two groups, this is equivalent to a Two Sample T-Test. Assumptions: The populations from which the samples are drawn are normally dist. The standard deviations of the populations are equal. Sample observations are randomly drawn and independent.
- When do we use the chisq2 Test of Independence? To test whether two categorical variables are independent. Assumptions: Sample observations are randomly drawn and independent.
- To perform the one-way ANOVA, we can use the `f_oneway()` function of the SciPy package.
- The degrees of freedom is the number of data rows minus the number of coefficients fit.
- Hypothesis tests aim to describe the plausibility of a parameter taking on a specific value. Confidence intervals aim to describe a range of plausible values a parameter can take on. If the value of the parameter specified by  $H_0$  is contained within the 95% confidence interval, then  $H_0$  cannot be rejected at the 0.05 p-value threshold. If the value of the parameter specified by  $H_0$  is not contained within the 95% confidence interval, then  $H_0$  can be rejected at the 0.05 p-value threshold.

## Introduction to Data

There is no random sampling since the subjects of the study were volunteers, so the results cannot be generalized to all people. However, due to random assignment, we are able to infer a causal link between the belief information is stored and the ability to recall that same information.

Explanatory variables are conditions you can impose on the experimental units, while blocking variables are characteristics that the experimental units come with that you would like to control for.

In random sampling, you use stratifying to control for a variable. In random assignment, you use blocking to achieve the same goal.

Control: compare treatment of interest to a control group

Randomize: randomly assign subjects to treatments

Replicate: collect a sufficiently large sample within a study, or replicate the entire study

Block: account for the potential effect of confounding variables

Group subjects into blocks based on these variations, and randomize within each block to treatment groups

Random Sampling + Random Assignment: Causal + generalizable

No Random Sampling + Random Assignment: Causal + not generalizable

Random Sampling + No Random Assignment: Not causal + generalizable

No Random Sampling + No Random Assignment: Not causal + not generalizable



### 8.1.1 Statistical Tests

The appropriate sample size depends on many things, chiefly the complexity of the analysis and the expected effect size. The “30” rule comes from one of the simplest cases: Whether to use a z-test or t-test for comparing two means.

- 1) for large  $n$  (sample size), many distributions can be approximated to normal. [ courtesy : Central Limit Theorems ]
- 2) The approximation becomes better with larger  $n$ , given other things remaining the same.

However if you are wondering why 30 ? why not 25 or 40 or something else ? Note that actual answer will depend:

- 1) how much error are you going to tolerate
- 2) size of the effect
- 3) exact distribution family (like  $t$  vs chi-square vs gamma)

The power of any test of statistical significance is defined as the probability that it will reject a false null hypothesis. Statistical power is inversely related to beta or the probability of making a Type II error. In short,  $\text{power} = 1 - \beta$ . In plain English, statistical power is the likelihood that a study will detect an effect when there is an effect there to be detected. If statistical power is high, the probability of making a Type II error, or concluding there is no effect when, in fact, there is one, goes down. Statistical power is affected chiefly by the size of the effect and the size of the sample used to detect it. Bigger effects are easier to detect than smaller effects, while large samples offer greater test sensitivity than small samples.

The following four quantities have an intimate relationship:

- sample size
- effect size
- significance level =  $P(\text{Type I error})$  = probability of finding an effect that is not there
- power =  $1 - P(\text{Type II error})$  = probability of finding an effect that is there

Given any three, we can determine the fourth.

#### Other

- The power of any test of statistical significance is defined as the probability that it will reject a false null hypothesis. Statistical power is inversely related to beta or the probability of making a Type II error. In short,  $\text{power} = 1 - \beta$ .
- For quantitative explanatory variables, effect sizes always have the unit of the response variable divided by the unit of the explanatory variable.
- Power Analysis Calculator

### 8.1.2 Stats For Hackers

- Methods: Simulation, Bootstrapping (with replacement, not good with ranks), Shuffling (Works when assumption is that the data are the same, representative samples, non-longitudinal data), & Cross Validation.
- Assumes iid.

### 8.1.3 Think Stats

- Is it possible that the apparent effect is due to selection bias or some other error in the experimental setup? If so, then we might conclude that the effect is an artifact; that is, something we created (by accident) rather than found.
- The sampling distribution is the distribution of the samples mean.
- The CDF is the function that maps values to their percentile rank in a distribution.
- I'll start with the exponential distribution because it is easy to work with. In the real world, exponential distributions come up when we look at a series of events and measure the times between events, which are called interarrival times. If the events are equally likely to occur at any time, the distribution of inter-arrival times tends to look like an exponential distribution.
- CLT: More specifically, if the distribution of the values has mean and standard deviation and  $n$ , the distribution of the sum is approximately  $N(n\mu, n\sigma^2)$ .
- Another option is to report just the Bayes Factor or likelihood ratio,  $P(E | H_A) / P(E | H_0)$ , rather than the posterior probability.
- Statistical power is the probability that the test will be positive if the null hypothesis is false. In general, the power of a test depends on the sample size, the magnitude of the effect, and the threshold  $\alpha$ .
- If there are no outliers, the sample mean minimizes the mean squared error
- An estimator is unbiased if the expected total (or mean) error, after many iterations of the estimation game, is 0.
- A challenge in measuring correlation is that the variables we want to compare might not be expressed in the same units. For example, height might be in centimeters and weight in kilograms. And even if they are in the same units, they come from different distributions. There are two common solutions to these problems:
  1. Transform all values to standard scores. This leads to the Pearson coefficient of correlation.
  2. Transform all values to their percentile ranks. This leads to the Spearman coefficient.

### 8.1.4 AB Testing Overview

Guide: Choose metric (CTR), review stats (Hypothesis Testing), design, analyse

Need to have clear control and thing to test. Also need time. Frequency of customer interaction is important. shopping and searching not independent events.

Point estimate of CTR (users who clicked)/users. Need margin of error for estimate. Approximate binomial by normal if  $Np \geq 5$  &  $N(1-p) \geq 5$ .

margin of error =  $Z \cdot (\text{standard error})$

$se = \sqrt{p(1-p)/n}$

Z for 95% is 1.96 and 2.58 for 99%.

for Two samples calculate a pooled CTR point estimate and standard error.

Need to be substantive (a worthy difference) in addition to being statistically significant. Some changes might not be useful due to the resources one might want to allocate.

Results are repeatable (stat sig) bar should be lower than business interesting (practically sig)

Stat Power: How many page view necessary to get a stat sig result.

Size v Power: The smaller the effect or increased confidence you want to detect/have (greater power of experiment), the larger the sample you need to use.

$\alpha = P(\text{reject null when true})$   $\beta = P(\text{accept null when false})$

small sample: low  $\alpha$ , high  $\beta$  larger sample: low  $\alpha$ , low  $\beta$

$1 - \alpha = \text{confidence level}$   $1 - \beta = \text{sensitivity (often 80\%)}$

practical significance: 2%,  $\alpha = 0.05$ ,  $\beta = 0.2$

sample size dp\_to ctr (increase in se), confidence level, sensitivity sample size invp\_to practical sig (larger changes easier to detect)

above is design of experiment. below is analysis:

estimate diff: experimental prop - control prop margin of error =  $z \cdot se$

conf int: estimated diff +/- margin of error

### Policy & Ethics

In the study, what risk is the participant undertaking? The main threshold is whether the risk exceeds that of “minimal risk”.

Next, what benefits might result from the study? Even if the risk is minimal, how might the results help?

Third, what other choices do participants have? For example, if you are testing out changes to a search engine, participants always have the choice to use another search engine.

Finally, what data is being collected, and what is the expectation of privacy and confidentiality? This last question is quite nuanced, encompassing numerous questions: Do participants understand what data is being collected about them? What harm would befall them should that data be made public? Would they expect that data to be considered private and confidential?

Our recommendation is that there should be internal reviews of all proposed studies by experts regarding the questions:

Are participants facing more than minimal risk? Do participants understand what data is being gathered? Is that data identifiable? How is the data handled?

Internal process recommendations Finally, regarding internal process of data handling, we recommend that:

Every employee who might be involved in A/B test be educated about the ethics and the protection of the participants. Clearly there are other areas of ethics beyond what we’ve covered that discuss integrity, competence, and responsibility, but those generally are broader than protecting participants of A/B tests (cite ACM code of ethics).

All data, identified or not, be stored securely, with access limited to those who need it to complete their job. Access should be time limited. There should be clear policies of what data usages are acceptable and not acceptable. Moreover, all usage of the data should be logged and audited regularly for violations. You create a clear escalation path for how to handle cases where there is even possibly more than minimal risk or data sensitivity issues.

rate better for usability test than prob

### Choosing & Characterizing Metrics

#### Define

Make sure to granularize funnel

#### Intuition

NA

### Characterize

Focus groups, UER (user experience study), survey, experiments, retrospective analysis, external data  
temporal effects across hours, days, weeks are important

different browsers screw with the CTR depending on how they deal with JS

Can use cookies to track users

Metric definitions

Def #1 (Cookie probability): For each , number of cookies that click divided by number of cookies

Def #2 (Pageview probability): Number of pageviews with a click within divided by number of pageviews

Def #3 (Rate): Number of clicks divided by number of pageviews

CTR vs CTP: The first can be  $>1$ .

Take into consideration mean and median. Median is robust but might not be useful so look at percentiles.

Measuring sensitivity and robustness: 1) Running experiments to see if metrics move as predicted. A vs A experiments: Measure people who saw the same thing to see if there is a difference between them according to the metric or its too sensitive. Look at previous experiments. 2) Retrospective analysis of logs to see how the metrics responded in the past.

Metric For Loading Vid: Look at distribution of load times for vid. Want a robust metric that doesn't really change for comparable vids. But what a metric that is sensitive to a change that you care about like resolution.

How to compare experiment vs control: difference or relative change. Relative change allows you to keep same significance boundary.

Check that practical sig level is good for metric. Need to have handle on variability for confidence interval.

sign test: Good for looking to implement a change, but doesn't give effect size.

empirical vs analytic: underlying distribution could be weird so do empirical. Analytical for simple metrics. If empirical and analytical don't agree then run AvA test.

A vs A test: Std proportional to square root of number of samples. Diminishing returns for many tests. Can use bootstrap if don't have enough traffic for a big A v A test.

### Designing An Experiment

#### Choose Subject

Unit of Diversion: How to identify a person. Cookie (could clear so change), userid, deviceid, and address (changes all the time).

Intra-user vs inter-user experiment.

#### Choose Population

Size

Duration

Cohort: People who enter the experiment at the same time.

Cohort > Population: Learning effects, user retention

Can reduce sample if just targeting english speaking traffic

When going to run experiment: holiday or not? How many people to put through experiment and control?

**Analyzing Results**

Sanity Checks:

Pass all before move on

Good invariants: # of events, video load time (user has no control over it). Want these to be about the same for experiment and control.

Single Metric:

sign test

Multiple Metrics:

More metrics increase false positive chance. Use Bonferroni assumption: makes no independence assumption and is conservative.

margin of error smaller than observed diff so the confidence interval won't include 0.

Different strategies: family-wise error rate, false discovery rate,

Gotchas:

Simpson's Paradox

Usually A/B testing works for testing changes in elements in the web page. A/B testing framework is following sequence:

Design a research question.

Choose test statistics method or metrics to evaluate experiment.

Designing the control group and experiment group.

Analyzing results, and draw valid conclusions.

**8.2 DataCamp: Experimental Design**

Randomized Complete Block Design (RCBD) experiment

Power usually @ 80%. power effect size & sample size all inter-related (with 2 can calculate 3rd).

power: prob that test correctly rejects null hypo when alt hypo is true

effect size: standardized measure of the difference you're trying to detect

sample size: how many experimental units needed to survey to detect the desired diff at the desired power

`pwr::pwr.anova.test()` [exactly one of n, d, power, and sig.level must be NULL]

`aov = lm + anova aov + tukey hsd`

Another assumption of ANOVA and linear modeling is homogeneity of variance. Homogeneity means "same", and here that would mean that the variance of `int_rate` is the same for each level of grade. We can test for homogeneity of variances using `bartlett.test()`, which takes a formula and a dataset as inputs.

One non-parametric alternative to ANOVA is the Kruskal-Wallis rank sum test. For those with some statistics knowledge, it is an extension of the Mann-Whitney U test for when there are more than two groups, such as with our grade variable.

Use the correct function from `pwr` to find the sample size (d is the effect size) `pwr::pwr.t.test(n = NULL, d = .2, power = .8, sig.level = .05, alternative = "two.sided")`

multivariable experiment:

```
lendingclub_multi <- lm(loan_amnt ~ Group + grade + verification_status, lendingclub_ab)
tidy(lendingclub_multi)
```

The sampling package's `cluster()` creates cluster samples. It takes in a dataset name, the variable in the set to be used as the cluster variable, passed as a vector with the name as a string, e.g. `c("variable")`, a number of clusters to select, and a method

#### Randomized Complete Block Designs

the purpose of blocking an experiment is to make the experimental groups more like one another.

A rule of thumb in experimental design is often “block what you can, randomize what you cannot”, which means you should aim to block the effects you can control for (e.g. sex) randomize on those you cannot (e.g. smoking status). Variability inside a block is expected to be fairly small, but variability between blocks will be larger.

## Chapter 9

# Deep Learning

### 9.1 General

- resnet, attention > RNN / LSTM
- “Training with large minibatches is bad for your health. More importantly, it’s bad for your test error. Friends dont let friends use minibatches larger than 32.” - Yann Le Cun
- DL Cheatsheet
- By reducing learning rate (for example, to 0.001), Test loss drops to a value much closer to Training loss. In most runs, increasing Batch size does not influence Training loss or Test loss significantly. However, in a small percentage of runs, increasing Batch size to 20 or greater causes Test loss to drop slightly below Training loss.
- Reducing the ratio of training to test data from 50% to 10% dramatically lowers the number of data points in the training set. With so little data, high batch size and high learning rate cause the training model to jump around chaotically (jumping repeatedly over the minimum point).
- There are several activation functions you may encounter in practice:
  - Sigmoid: Takes a real-valued input and squashes it to range between 0 and 1 ( $\sigma(x) = 1/(1+\exp(-x))$ )
  - Softmax: Same end result as sigmoid, but different function.
  - tanh: Takes a real-valued input and squashes it to the range  $[-1, 1]$  ( $\tanh(x) = 2\sigma(2x) - 1$ )
- ReLU: The rectified linear activation function (called ReLU) has been shown to lead to very high-performance networks. This function takes a single number as an input, returning 0 if the input is negative, and the input if the input is positive.  $f(x) = \max(0, x)$
- softmax doesn’t like multi-label classification
- Embeddings vs One-Hot Encoding: Embeddings are better than One-Hot Encodings because it allows for relationships to be shown between days.
- Advised to scale features
- Rule of 30: A change that affects at least 30 data points in your validation set is usually significant and not just noise.
- Gradient descent takes about 3 times longer than the loss function. Stochastic gradient descent works off an estimate of the loss function from a sample of the training set. Scales better than normal gradient descent.

- Momentum and learning rate decay are good for knowing which way to go in gradient descent.
- Always try to lower your learning rate for improvement.
- ADAGRAD is another optimization option that takes care of some of the hyperparameters for you.
- $n$  inputs and  $k$  outputs gives you  $(n + 1) * k$  parameters.
- Back propagation takes about twice the memory as forward propagation.
- Stop model from overoptimizing on training set: early termination (stop as soon as performance on validation set drops) and regularization which applies artificial constraints to reduce the number of free parameters while making it difficult to optimize. Uses l2 regularization or dropout. Dropout works by randomly setting activations from one layer to the next to 0 repeatedly. Forces the network to learn redundant representations, and takes average consensus for final prediction. Makes things more robust and prevents overfitting. Scale the non-zero activations by 2 to get the right average. If it doesn't work, go deeper.
- Two ways are to average the yellow, blue, and green channels or to use YUV representation. If position on the screen doesn't matter then use translation invariance. Use weight sharing if this occurs in text.
- Things that don't change across time, space, etc are called statistical invariants.
- RNN's use shared parameters over time to extract patterns. Uses a recurrent connection to provide a summary of the past and pass this info to the classifier.
- Backpropagation occurs throw time to the beginning. All derivative applied to same parameters, so very correlated. Bad for stochastic gradient descent and makes math very unstable. Gradients are either zero (doesn't remember the past well) or infinity. The latter is fixed by gradient clipping and the former by LSTM (long-short term memory). LSTM replaced the rectified linear units by continuous functions. You can use dropout or L2 regularization with an LSTM.
- Generally dealing with images, Convolutional Neural Network is used mostly because of its better accuracy results.
- Model capacity: Same as underfitting and overfitting in bias-variance. Less nodes and hidden layers corresponds to simpler model and vice versa.
- The perceptron is the simplest neural network. The perceptron is an iterative classification method. The perceptron starts with a random hyperplane then adjust its weights to separate the data.
- BackProp Algorithm: Initially all the edge weights are randomly assigned. For every input in the training dataset, the ANN is activated and its output is observed. This output is compared with the desired output that we already know, and the error is "propagated" back to the previous layer. This error is noted and the weights are "adjusted" accordingly. This process is repeated until the output error is below a predetermined threshold.
- The last layer of a neural network captures the most complex interactions.
- When plotting the mean-squared error loss function against predictions, the slope is  $2x(y - xb)$ , or  $2input_dataerror$ .
- $weights\_updated = weights - slope * learning\_rate$
- This is exactly what's happening in the vanishing gradient problem – the gradients of the network's output with respect to the parameters in the early layers become extremely small. That's a fancy way of saying that even a large change in the value of parameters for the early layers doesn't have a big effect on the output.
- Batch: Subset of the data used to calculate slopes during back propagation. Different batches are used to calculate different updates.
- Epoch: One full pass through all the batches in the training data.



- Stochastic gradient descent calculates slopes one batch at a time.
- This network again uses the ReLU activation function, so the slope of the activation function is 1 for any node receiving a positive value as input.
- Few people use kfold cv in deep learning because of the large datasets in play.
- Dying neuron + vanishing gradient: Change activation function

## 9.2 LSTMS

Long Short Term Memory networks – usually just called “LSTMs” – are a special kind of RNN, capable of learning long-term dependencies. LSTMs are essentially the same thing as the RNN we will develop in this tutorial, they just have a different way of computing the hidden state.

The default activation function for LSTMs is the hyperbolic tangent (tanh), which outputs values between -1 and 1. This is the preferred range for the time series data: `MinMaxScaler(feature_range=(-1, 1))`.

Keras LSTM expects the input as well as the target data to be in a specific shape. The input has to be a 3-d array of size `num_samples, num_timesteps, num_features`.

The way we can do this, with Keras, is by wiring the LSTM hidden states to sets of consecutive outputs of the same length. Thus, if we want to produce predictions for 12 months, our LSTM should have a hidden state length of 12.

Keras - stateful vs stateless LSTMs

One major issue with `layer_simple_rnn` is that although it should theoretically be able to retain at time  $t$  information about inputs seen many time steps before, in practice, such long-term dependencies are impossible to learn. This is due to the vanishing gradient problem, an effect that is similar to what is observed with non-recurrent networks (feed forward networks) that are many layers deep: as you keep adding layers to a network, the network eventually becomes un-trainable.

A loss function is used to optimize a machine learning algorithm. An accuracy metric is used to measure the algorithm’s performance (accuracy) in an interpretable way.

```
network <- keras_model_sequential() %>% layer_dense(units = 512, activation = "relu", input_shape = c(
network %>% compile( optimizer = "rmsprop", loss = "categorical_crossentropy", metrics = c("accuracy")
network %>% fit(train_images, train_labels, epochs = 5, batch_size = 128)
metrics <- network %>% evaluate(test_images, test_labels)
```

## 9.3 DL.AI: Intro

ng thinks dl easier of matrix is  $n \times m$  instead of  $m \times n$  so target is a row vector instead of a column vector

Loss function applies to a single training example while the cost function applies to many. The loss function computes the error for a single training example; the cost function is the average of the loss functions of the entire training set.

A trick when you want to flatten a matrix  $X$  of shape  $(a,b,c,d)$  to a matrix  $X\_flatten$  of shape  $(b \times c \times d, a)$  is to use:

```
X_flatten = X.reshape(X.shape[0], -1).T
```

One common preprocessing step in machine learning is to center and standardize your dataset, meaning that you subtract the mean of the whole numpy array from each example, and then divide each example by the standard deviation of the whole numpy array. But for picture datasets, it is simpler and more convenient and works almost as well to just divide every row of the dataset by 255 (the maximum value of a pixel channel).

Scale images: `train_set_x = train_set_x_flatten/255.`

Common steps for pre-processing a new dataset are:

- Figure out the dimensions and shapes of the problem (`m_train`, `m_test`, `num_px`, ...)
- Reshape the datasets such that each example is now a vector of size (`num_px * num_px * 3, 1`)
- “Standardize” the data

Preprocessing the dataset is important.

You implemented each function separately: `initialize()`, `propagate()`, `optimize()`. Then you built a `model()`.

Tuning the learning rate (which is an example of a “hyperparameter”) can make a big difference to the algorithm. You will see more examples of this later in this course!

The tanh activation usually works better than sigmoid activation function for hidden units because the mean of its output is closer to zero, and so it centers the data better for the next layer.

Initialize weights randomly but set bias to zero.

You have built a network using the tanh activation for all the hidden units. You initialize the weights to relative large values, using `np.random.randn(...)*1000`. What will happen? This will cause the inputs of the tanh to also be very large, thus causing gradients to be close to zero. The optimization algorithm will thus become slow.

a42: 4th neuron of the 2nd layer for the 12th training example.

No. Sigmoid outputs a value between 0 and 1 which makes it a very good choice for binary classification. You can classify as 0 if the output is less than 0.5 and classify as 1 if the output is more than 0.5. It can be done with tanh as well but it is less convenient as the output is between -1 and 1.

random initialization of weights for logreg

What is the “cache” used for in our implementation of forward propagation and backward propagation? We use it to pass variables computed during forward propagation to the corresponding backward propagation step. It contains useful values for backward propagation to compute derivatives.

The deeper layers of a neural network are typically computing more complex features of the input than the earlier layers.

During backpropagation, the corresponding backward function also needs to know what is the activation function for layer `l`, since the gradient depends on it.

- To compute the function using a shallow network circuit, you will need a large network (where we measure size by the number of logic gates in the network), but
- To compute it using a deep network circuit, you need only an exponentially smaller network.

gradient checking

vanishing/exploding gradients

data augmentation for images: rotate and crop

ng doesn't like dropout bc it couples optimization with regularization

early stopping

dropout is a regularization technique to prevent over-fitting.

## 9.4 DL.AI: Improving Deep Neural Network

If you have 10,000,000 examples, how would you split the train/dev/test set? 98% train . 1% dev . 1% test  
The dev and test set should: Come from the same distribution

If your Neural Network model seems to have high variance, what of the following would be promising things to try? Add regularization & Get more training data. For high bias, make a bigger and deeper network.

What is weight decay? A regularization technique (such as L2 regularization) that results in gradient descent shrinking the weights on every iteration. As a rule of thumb, the more training examples you have, the weaker this term should be. The more parameters you have the higher this term should be.

With the inverted dropout technique, at test time: You do not apply dropout (do not randomly eliminate units) and do not keep the  $1/\text{keep\_prob}$  factor in the calculations used in training.

With the inverted dropout technique, at test time: You do not apply dropout (do not randomly eliminate units) and do not keep the  $1/\text{keep\_prob}$  factor in the calculations used in training

Increasing the parameter `keep_prob` from (say) 0.5 to 0.6 will likely cause the following: Reducing the regularization effect & Causing the neural network to end up with a lower training set error

Normalization makes the cost function faster to optimize

Which of these techniques are useful for reducing variance (reducing overfitting)? Dropout, L2 regularization  
Data augmentation

Different initializations lead to different results

Random initialization is used to break symmetry and make sure different hidden units can learn different things

Don't initialize to values that are too large

He initialization works well for networks with ReLU activations.

### Fast.AI

Do a loss vs learning rate plot to pick a good one. It's the key thing to set.

learning rate annealing: decrease learning rate as you reach the minimum.

If you try training for more epochs, you'll notice that we start to overfit, which means that our model is learning to recognize the specific images in the training set, rather than generalizing such that we also get good results on the validation set. One way to fix this is to effectively create more data, through data augmentation. This refers to randomly changing the images in ways that shouldn't impact their interpretation, such as horizontal flipping, zooming, and rotating.

mse: loss function for regression

Cross-entropy: loss function for classification

Gradient descent: a generic method that can optimize any differentiable loss function

Analytical solution for linear models and MSE effective when: Small number of features

There is an analytical solution for linear regression parameters and MSE loss, but we usually prefer gradient descent optimization over it. What are the reasons?

- Gradient descent doesn't require to invert a matrix
- Gradient descent is more scalable and can be applied for problems with high number of features

Number of params in logistic regression:  $k \cdot d$  where  $k$  is the number of classes and  $d$  is the size of the dimensional space.

Large model weights can indicate that model is overfitted

Weight penalty drives model parameters closer to zero and prevents the model from being too sensitive to small changes in features

disadvantages do model validation on holdout sample can give biased quality estimates for small samples

Stochastic gradient descent: Noisy but eventually converge to minimum. Needs only one example at each step. Can be used online. Choose the learning rate carefully.

mini-batch gradient descent

Gradient descent extensions: adagrad, rms prop, adam

The best nonlinearity functions to use in a Multilayer perceptron are step functions as they allow to reconstruct the decision boundary with better precision? No. Step function gradient with respect to its input is zero almost everywhere - thus the resulting network can't be trained via backpropagation.

A dense layer applies a linear transformation to its input

For an MLP to work, the nonlinearity function must have a finite upper bound? No, widely used ReLU has no upper bound.

How many dimensions will a derivative of a 1-D vector by a 2-D matrix have? 3. The rule of thumb is that the final derivative will consist of derivatives of each component of the output by each component of input. So, for each element of the output vector there will be a 2-D matrix of derivatives, 3 dimensions in total.

Sigmoid neurons can lead to vanishing gradients at its extremes. ReLU better. Leaky ReLU best to avoid non-activation.

Dropout is a regularization technique.

Convolutions and pooling layers are invariant to translation of images.

We have reviewed the activation function, weights initializations, and a bunch of new techniques that help to train better networks. What are the takeaways? First, always use ReLU activation because it doesn't saturate and it converges faster. Use He et al initialization which is square root of two divided by square root of number of inputs. Try to add batch normalization or dropout, maybe it will converge better. Try to augment your training data.

Transfer learning

You should use dropout (randomly eliminate nodes) only in training.

Apply dropout both during forward and backward propagation.

During training time, divide each dropout layer by keep\_prob to keep the same expected value for the activations. For example, if keep\_prob is 0.5, then we will on average shut down half the nodes, so the output will be scaled by 0.5 since only the remaining half are contributing to the solution. Dividing by 0.5 is equivalent to multiplying by 2. Hence, the output now has the same expected value. You can check that this works even when keep\_prob is other values than 0.5.

inverted dropout

Gradient checking verifies closeness between the gradients from backpropagation and the numerical approximation of the gradient (computed using forward propagation).

Gradient checking is slow, so we don't run it in every iteration of training. You would usually run it only to make sure your code is correct, then turn it off and use backprop for the actual learning process.

### 9.4.1 Optimization Algorithms

In batch GD the cost should be monotone decreasing. In mini-batch it doesn't have to be since it's like training on a different training set every time. It should still be trending downwards.

For small training set use (  $< 2000$  ) use batch GD. Use batches of 64, 128, 256, 512 otherwise which should speed up training. Make sure it fits in meemory. MIni-batch size is another hyperparameter.

RMS PProp

ADAM: Adam combines the advantages of RMSProp and momentum, We usually use “default” values for the hyperparameters, The learning rate hyperparameter in Adam usually needs to be tuned.

Learning rate decay

epoch: one pass through the training set

If batch gradient descent in a deep network is taking excessively long to find a value of the parameters that achieves a small value for the cost function: Try mini-batch gradient descent, Try better random initialization for the weights, Try Adam, Try tuning the learning rate.

A variant of this is Stochastic Gradient Descent (SGD), which is equivalent to mini-batch gradient descent where each mini-batch has just 1 example. When the training set is large, SGD can be faster. But the parameters will “oscillate” toward the minimum rather than converge smoothly.

In practice, you’ll often get faster results if you do not use neither the whole training set, nor only one training example, to perform each update. Mini-batch gradient descent uses an intermediate number of examples for each step. With mini-batch gradient descent, you loop over the mini-batches instead of looping over individual training examples.

The difference between gradient descent, mini-batch gradient descent and stochastic gradient descent is the number of examples you use to perform one update step. You have to tune a learning rate hyperparameter alpha. With a well-turned mini-batch size, usually it outperforms either gradient descent or stochastic gradient descent (particularly when the training set is large).

Shuffling and Partitioning are the two steps required to build mini-batches. Powers of two are often chosen to be the mini-batch size, e.g., 16, 32, 64, 128.

Momentum takes into account the past gradients to smooth out the update

Momentum takes past gradients into account to smooth out the steps of gradient descent. It can be applied with batch gradient descent, mini-batch gradient descent or stochastic gradient descent. You have to tune a momentum hyperparameter beta and a learning rate alpha.

Mini-batch Gradient descent, Mini-batch Gradient descent with momentum, mini-batch with Adam. Adam usually performs best. Some advantages of Adam include: Relatively low memory requirements (though higher than gradient descent and gradient descent with momentum), usually works well even with little tuning of hyperparameters (except alpha).

### 9.4.2 Hyperparameter Tuning

Use random values.

batch normalization

softmax regression

During hyperparameter search, whether you try to babysit one model (“Panda” strategy) or train a lot of models in parallel (“Caviar”) is largely determined by computational power

Which of the following statements about and in Batch Norm are true? They can be learned using Adam, Gradient descent with momentum, or RMSprop, not just with gradient descent. They set the mean and variance of the linear variable  $z[l]$  of a given layer.

After training a neural network with Batch Norm, at test time, to evaluate the neural network on a new example you should: Perform the needed normalizations, use and 2 estimated using an exponentially weighted average across mini-batches seen during training

tf: To summarize, remember to initialize your variables, create a session and run the operations inside the session.

When you code in tensorflow you have to take the following steps:

- Create a graph containing Tensors (Variables, Placeholders ...) and Operations (tf.matmul, tf.add, ...)
- Create a session
- Initialize the session
- Run the session to execute the graph

## Chapter 10

# Probabilistic Programming

<https://towardsdatascience.com/introduction-to-bayesian-linear-regression-e66e60791ea7>

Bayes Rule:

$\text{old\_prob} [P(h)/p(\sim h)] * \text{strength\_of\_evidence} [p(e|h)/p(e|\sim h)] = \text{new\_prob} [p(h|e)/p(\sim h|e)]$

- Models have a lot of parameters classical methods that use simple point estimates of the parameters don't adequately capture uncertainty so we turn to Bayesian methods because Bayesian inference is one way of finding a large model with metadata.
- The second reason we use Bayesian inference is for combining information you might have experimental data on the drug under one condition and aggregate data under another condition we can combine polls and election forecast of public opinion data from multiple poles and environmental statistics we have measurements of different quality Bayesian methods are particularly adapted to combining information.
- The third appeal of Bayesian methods and the sort of applications that I work on is that the inferences can map directly to decisions based on inferences express not its estimates and standard errors but rather as probability distributions we can take these probability distributions and pipe them directly into decision analysis for these reasons.
- An advantage of recognizing that the prior distribution is a testable part of a Bayesian model is that it clarifies the role of the prior inference, and where it comes from.
- Approximate Bayesian Computation
- Laplace approximation: Approximate the posterior of a non-conjugate model
- When one uses likelihood to get point estimates of model parameters, it's called maximum-likelihood estimation, or MLE. If one also takes the prior into account, then it's maximum a posteriori estimation (MAP). MLE and MAP are the same if the prior is uniform.
- Beta conjugacy: Beta for prior & binomial for likelihood implies beta for posterior. Update:  $\text{beta}(\alpha + \text{successes}, \beta + \text{failures})$ . Mean:  $\alpha / (\alpha + \beta)$
- Small alpha and beta means the prior is less informative
- Empirical Bayes is an approximation to more exact Bayesian methods. With a lot of data it is a very good approximation.

```
from numpy.random import beta as beta_dist
import numpy as np
N_samp = 10000 #number of samples to draw
clicks_A = 450
views_A = 56000
```

```

clicks_B = 345
views_B = 49000
alpha = 1.1
beta = 14.2
A_samples = beta_dist(clicks_A + alpha, views_A - clicks_A + beta, N_samp)
B_samples = beta_dist(clicks_B + alpha, views_B - clicks_B + beta, N_samp)

```

Posterior prob that CTR\_A > CTR\_B given data is `np.mean(A_samples > B_samples)`. Prob that lift of A relative to B is  $\geq 3\%$ : `np.mean(100*(A_samples-B_samples)/B_samples > 3)`

## 10.1 Doing Bayesian DA

In general, Bayesian analysis of data follows these steps:

1. Identify the data relevant to the research questions. What are the measurement scales of the data? Which data variables are to be predicted, and which data variables are supposed to act as predictors?
2. Define a descriptive model for the relevant data. The mathematical form and its parameters should be meaningful and appropriate to the theoretical purposes of the analysis.
3. Specify a prior distribution on the parameters. The prior must pass muster with the audience of the analysis, such as skeptical scientists.
4. Use Bayesian inference to re-allocate credibility across parameter values. Interpret the posterior distribution with respect to theoretically meaningful issues (assuming that the model is a reasonable description of the data; see next step).
5. Check that the posterior predictions mimic the data with reasonable accuracy (i.e., conduct a “posterior predictive check”). If not, then consider a different descriptive model.

## 10.2 Statistical Rethinking

bayesian: 1) likelihood: binomial 2) parameters of the likelihood 3) prior for each param

Data are measured and known; parameters are unknown and must be estimated from data.

Compared to MCMC, variational inference tends to be faster and easier to scale to large data

To combat under/overfitting use a regularizing prior or a scoring device like information criteria.

As you’ll see once you start using AIC and related measures, it is true that predictor variables that do improve prediction are not always statistically significant. It is also possible for variables that are statistically significant to do nothing useful for prediction.

But the prior on  $\beta$  is narrower and is meant to regularize. The prior  $\beta \sim \text{Normal}(0,1)$  says that, before seeing the data, the machine should be very skeptical of values above 2 and below  $-2$ , as a Gaussian prior with a standard deviation of 1 assigns only 5% plausibility to values above and below 2 standard deviations. Because the predictor variable  $x$  is standardized, you can interpret this as meaning that a change of 1 standard deviation in  $x$  is very unlikely to produce 2 units of change in the outcome.

metrics: dic, waic

Sampling from the posterior now and plotting the model’s predictions would help immensely with interpretation. And that’s the course I want to encourage and provide code for. In general, it’s not safe to interpret interactions without plotting them.



bayesian model: generative model (binomial number of success) + prior (eg. sample of probabilities of success from uniform)

bayesian inference: bayesian model + data

bayesian inference is conditioning on the data to learn the parameter values.

The reason that we call it posterior is because it represents the uncertainty after (that is, posterior to) having included the information in the data.

Bayesian Inference Methods: Sampling, Grid Approximation



# Chapter 11

## Notes

measurement theory / decision science, semi-supervised, unsupervised, online, & weak learning

set the seed always

Shapiro-Wilk Test for Normality:  $H_0$  says the data is normally distributed while  $H_a$  says it is not. To run this test in R, the syntax is quite simple:

```
import statsmodels.api as sm
X = sm.add_constant(X)
rgr_lr = sm.OLS(Y, X).fit(dis=False)
print(results.summary())
```

### 11.1 Other

#### 11.1.1 Vanderplas Jupyter

- create helper functions and units tests as R/py for Rmd/ipynb
- pytest/hypothesis for testing
- use makefile to run cmd commands
- Write file with date: `df.to_csv('{ }_model.csv'.format(str(datetime.datetime.now()).split(' ')[0]))`
- Make package for workflow with data (**init.py**) and use this formation for function docs:
- `def fun(a): return(a) #Role Parameters Returns`

#### 11.1.2 Sample R Pipeline

Source:

IO: `odbc readxl httr` EDA: `DataExplorer` Prep: `tidyverse` Sampling: `rsample` modelr Feature Engineering: `recipes` Modeling: `glmnet h2o FFTrees` Evaluation: `broom yardstick` Deployment: `sqlrutils AzureML opencpu` Monitoring: `flexdashboard` Docs: `rmarkdown`

natural log goes from unit change to percentage change

generalized low rank models

conditional random field

linear probability model

<http://r-pkgs.had.co.nz/tests.html>

<https://cartesianfaith.com/2013/03/10/better-logging-in-r-aka-futile-logger-1-3-0-released/>

<http://www.markvanderloo.eu/yaRb/2016/03/25/easy-data-validation-with-the-validate-package/>

<https://cran.r-project.org/web/packages/assertr/vignettes/assertr.html>

Power-Of-Test: <https://rpsychologist.com/d3/NHST/> <https://juliasilge.shinyapps.io/power-app/>  
<https://www.statmethods.net/stats/power.html> <https://www.graphpad.com/quickcalcs/binomial1.cfm>  
<https://stat.ethz.ch/R-manual/R-devel/library/stats/html/power.prop.test.html> <https://stat.ethz.ch/R-manual/R-devel/library/stats/html/prop.test.html>

confint conjoint analysis Incremental PCA fe: Permutation Measure meta learning | Rasch Model | Learning\_to\_rank

ff | bigmemory | biganalytics | bigtabulate | purrrlyr: dplyr purrr | furrr: parallelized purrr

foreach + doMC | parallel | doParallel

ts: Vector autoregression, quantile regression forests

Out-of-Core: pandas chunksize Semantic Style Transfer symbolic regression

Quantile Regression models the median while Linear Regression models the mean

Linear Regression - BLUE: Best Linear Unbiased (average amount wrong by is error) Estimator

- With large data we can to the train x dev x test split of 98 x 1 x 1.

Bayes optimal error: Aim for this. The difference b/w training error and BOE is the avoidable bias.

end to end deep learning: an end-to-end approach as it maps directly the input (x) to the output (y).  
 end-to-end learning works better in practice than multi-task learning, but requires a large amount of data.

new data degrades your model. what should you do? Use the data you have to define a new evaluation metric (using a new dev/test set) taking into account the new species, and use that to drive further progress for your team.

because even though you have higher overall accuracy, you have more false negatives (failing to raise an alarm when a bird is in the air). What should you do? Rethink the appropriate metric for this task, and ask your team to tune to the new metric.

If you overfit to the dev set, get a bigger one.

Spend a few days training a basic model and see what mistakes it makes.

softmax not used for multi-classification

- But map allows us to bypass the function function. Using a tilde (~) in place of function and a dot (.) in place of x, we can do this: `map(dat, ~mean(.$Open))`
- Cohen's H | Cohen's D | Multiple comparisons Problem | Importance sampling | Bayes Error Rate
- **The Coefficient of Unalikeability:** Unalikeability is defined as how often observations differ from one another. It varies from 0 to 1. The higher the value, the more unlike the data are.

Consequently, practical decision-tree learning algorithms are based on heuristics such as the greedy algorithm where locally optimal decisions are made at each node. Such algorithms cannot guarantee to return the globally optimal decision tree. To reduce the greedy effect of local optimality, some methods such as the dual information distance (DID) tree were proposed

Laplace smoothing/estimator in Naive Bayes: To see why consider the worst case where none of the words in the training sample appear in the test sentence. In this case, under your model we would conclude that the sentence is impossible but it clearly exists creating a contradiction.

Zero correlation doesn't imply independence

- Active Learning: Finding the optimal data to manually label
- Simulated Annealing: Gradient descent extension
- “No Free Lunch” theorem: no single classifier works best across all possible scenarios
- So, if your problem involves kind of searching a needle in the haystack when for ex: the positive class samples are very rare compared to the negative classes, use a precision recall curve. Otherwise use a ROC curve because a ROC curve remains the same regardless of the baseline prior probability of your positive class (the important rare class).
- Sequence mining Algorithms: spade, gsp, freespan; hmmlearn
- Network models: graphical lasso, ising model, granger causality test, network hypothesis testing, bayesian networks
- Parametric: Model has a function shape and form, Model is trained/fit using training data to determine parameter values, reduces the problem of training a model down to training a set of parameter values, Examples: linear regression. Non-Parametric: No assumption about model form is made, Example: KNN
- The ML Fine Print: Three basic assumptions: 1) We draw examples independently and identically (i.i.d.) at random from the distribution, 2) The distribution is stationary: It doesn't change over time, 3) We always pull from the same distribution: Including training, validation, and test sets. In practice, we sometimes violate these assumptions. For example: 1) Consider a model that chooses ads to display. The i.i.d. assumption would be violated if the model bases its choice of ads, in part, on what ads the user has previously seen. 2) Consider a data set that contains retail sales information for a year. User's purchases change seasonally, which would violate stationarity. When we know that any of the preceding three basic assumptions are violated, we must pay careful attention to metrics.
- empirical risk minimization: In supervised learning, a machine learning algorithm builds a model by examining many examples and attempting to find a model that minimizes loss.
- Loss is the penalty for a bad prediction. That is, loss is a number indicating how bad the model's prediction was on a single example. If the model's prediction is perfect, the loss is zero; otherwise, the loss is greater.
- If a model suffers from overfitting, we also say that the model has a high variance, which can be caused by having too many parameters that lead to a model that is too complex given the underlying data. Similarly, our model can also suffer from underfitting (high bias), which means that our model is not complex enough to capture the pattern in the training data well and therefore also suffers from low performance on unseen data.
- “Product classification is an example of multicategory or multinomial classification. Most classification problems and most classification algorithms are specialized for two-category, or binomial, classification. There are tricks to using binary classifiers to solve multicategory problems (for example, building one classifier for each category, called a “one versus rest” classifier). But in most cases it's worth the effort to find a suitable multiple-category implementation, as they tend to work better than multiple binary classifiers (for example, using the package `mlogit` instead of the base method `glm()` for logistic regression).”



## Chapter 12

# Code Snippets

### 12.1 Albon

<http://chrisalbon.com/>

### 12.2 Sampling File

```
pip install subsample
gzcat ginormous.csv.gz | subsample -n 100000 > sampled.csv.gz
```

### 12.3 Hold

SELECT 'Dummy Column Text' as DUMMYCOL FROM tbl

Temporary pandas Columns

- `ggplot(df, aes(fitted_probability, binary_class_indicator)) + geom_smooth()`: a quick way of visualizing model calibration without having to manually bin any observations
- Rule of thumb for bins in histogram: `ggplot() + geom_histogram(aes(x), binwidth = diff(range(x)) / (2 * IQR(x) / length(x)^(1/3)))`.
- Optimal Bins For Histogram

<http://blog.rtwilson.com/how-to-rescue-lost-code-from-a-jupyteripython-notebook/>





## Chapter 13

# Frameworks

### 13.1 PySpark

A [cheatsheet](<https://www.qubole.com/resources/pyspark-cheatsheet/>).

Setup

```
import findspark
findspark.init()
import pyspark
from pyspark.sql import SparkSession
sc = pyspark.SparkContext()
spark = SparkSession.builder.appName('example').getOrCreate()
import findspark
findspark.init()
import pyspark
import random
sc = pyspark.SparkContext(appName="Pi")
num_samples = 100000000
def inside(p):
    x, y = random.random(), random.random()
    return x*x + y*y < 1
count = sc.parallelize(range(0, num_samples)).filter(inside).count()
pi = 4 * count / num_samples
print(pi)
sc.stop()
```

Libs

```
from pyspark.ml.feature import StringIndexer, OneHotEncoder, VectorAssembler
from pyspark.ml import Pipeline
from pyspark.ml.classification import LogisticRegression
import pyspark.ml.evaluation as evals
import pyspark.ml.tuning as tune
import numpy as np
df = spark.read.csv('data.csv', header = True)
df.show(5)
df.columns
```

Preprocessing

```

df = df.withColumn("label", df["target"].cast('integer'))
scf_indexer = StringIndexer(inputCol = "some_cat_feature", outputCol = "some_cat_feature_index")
scf_encoder = OneHotEncoder(inputCol = "some_cat_feature_index", outputCol = "some_cat_feature_fact")
feature_cols = ["some list of column names"]
vec_assembler = VectorAssembler(inputCols = feature_cols,
                                outputCol = "features")

pipe = Pipeline(stages = [scf_indexer, scf_encoder, vec_assembler])
piped_data = pipe.fit(df).transform(df)
training, test = piped_data.randomSplit([.8, .2])

```

Model

```

clf_lr = LogisticRegression()
evaluator = evals.BinaryClassificationEvaluator(metricName = "areaUnderROC")
grid = tune.ParamGridBuilder()
grid = grid.addGrid(clf_lr.regParam, np.arange(0, .1, .01))
grid = grid.addGrid(clf_lr.elasticNetParam, [0, 1])
grid = grid.build()
clf_lr_cv = tune.CrossValidator(
    estimator = clf_lr,
    estimatorParamMaps = grid,
    evaluator = evaluator,
    numFolds = 5
)
best_clf_lr = clf_lr_cv.fit(training).bestModel
results = best_clf_lr.transform(training)
print(evaluator.evaluate(results))
#stop
sc.stop()

```

Quick Test:

```

import findspark
findspark.init()
import pyspark
import random
sc = pyspark.SparkContext(appName="Pi")
num_samples = 100000000
def inside(p):
    x, y = random.random(), random.random()
    return x*x + y*y < 1
count = sc.parallelize(range(0, num_samples)).filter(inside).count()
pi = 4 * count / num_samples
print(pi)
sc.stop()

```

First have to create a SparkSession object from your SparkContext. The SparkContext is the connection to the cluster and the SparkSession as your interface with that connection.

```

import pyspark
from pyspark.sql import SparkSession
sc = pyspark.SparkContext()
spark = SparkSession.builder.getOrCreate() # SparkSession.builder.appName('chosenName').getOrCreate()

```

The rest of my notes:

```

## List tables
spark.catalog.listTables()
## Access and display data
query = "FROM flights SELECT * LIMIT 10"
flights10 = spark.sql(query)
flights10.show()
## Cast
df['g'] = df['g'].astype(str)
## Read from csv
df = spark.read.csv(file_path, header = True)
df = spark.read.csv('fileNameWithPath', mode="DROPMALFORMED", inferSchema=True, header = True)
df = spark.read.format("csv").option("header", "true").option("inferSchema", "true").load("john_doe.csv")
## Spark df to pandas and vice versa
toPandas()
spark_temp = spark.createDataFrame(pd_temp)
## Add to the catalog
spark_temp.createOrReplaceTempView("temp")
## Mutate
df = df.withColumn("newCol", df.oldCol + 1)
model_data = model_data.withColumn("arr_delay", model_data.arr_delay.cast('integer'))
model_data = model_data.withColumn("plane_age", model_data.year - model_data.plane_year)
## Create the DataFrame flights
flights = spark.table('flights')
## Get column names
spark_df.schema.names
spark_df.printSchema()
## Filter: takes either a Spark Column of boolean (True/False) values or the WHERE clause of a SQL expr
long_flights1 = flights.filter('distance > 1000')
long_flights2 = flights.filter(flights.distance > 1000)
model_data = model_data.filter("arr_delay is not NULL and dep_delay is not NULL and air_time is not NULL")
## Groupby examples
flights.filter(flights.origin == "PDX").groupBy().min("distance").show()
flights.filter(flights.carrier=="DL").filter(flights.origin=="SEA").groupBy().avg('air_time').show()
flights.withColumn("duration_hrs", flights.air_time/60).groupBy().sum('duration_hrs').show()
## Spark functions
import pyspark.sql.functions as F
by_month_dest.agg(F.stddev('dep_delay')).show()

## Drop column
final_test_data.drop('State')
## Dummying
#The first step to encoding your categorical feature is to create a StringIndexer. Members of this class
#The second step is to encode this numeric column as a one-hot vector using a OneHotEncoder. This works
## Create a StringIndexer
carr_indexer = StringIndexer(inputCol="carrier", outputCol="carrier_index")
## Create a OneHotEncoder
carr_encoder = OneHotEncoder(inputCol="carrier_index", outputCol="carrier_fact")
## Make a VectorAssembler
vec_assembler = VectorAssembler(inputCols=["month", "air_time", "carrier_fact", "dest_fact", "plane_age"])
## Import & Make Pipeline
from pyspark.ml import Pipeline
flights_pipe = Pipeline(stages=[dest_indexer, dest_encoder, carr_indexer, carr_encoder, vec_assembler])
## Fit and transform the data
piped_data = flights_pipe.fit(model_data).transform(model_data)

```

```

## Train-test split
training, test = piped_data.randomSplit([.6, .4])
## Tuning & Selection
## Import LogisticRegression
from pyspark.ml.classification import LogisticRegression
## Create a LogisticRegression Estimator
lr = LogisticRegression()
## Import the evaluation submodule
import pyspark.ml.evaluation as evals
## Create a BinaryClassificationEvaluator
evaluator = evals.BinaryClassificationEvaluator(metricName="areaUnderROC")
## Import the tuning submodule
import pyspark.ml.tuning as tune
## Create the parameter grid
grid = tune.ParamGridBuilder()
## Add the hyperparameter
grid = grid.addGrid(lr.regParam, np.arange(0, .1, .01))
grid = grid.addGrid(lr.elasticNetParam, [0, 1])
## Build the grid
grid = grid.build()
## Create the CrossValidator
cv = tune.CrossValidator(
    estimator=lr,
    estimatorParamMaps=grid,
    evaluator=evaluator
)
## Fit cross validation models
models = cv.fit(training)
## Extract the best model
best_lr = models.bestModel
## Use the model to predict the test set
test_results = best_lr.transform(test)
## Evaluate the predictions
print(evaluator.evaluate(test_results))

```

- Spark’s assumes the target is called ‘label’ in ML. Everything else is a feature.
- `alias()` method to rename a column you’re selecting.
- `cast()` method: nominative determinism on columns
- `withColumn()`: create new column
- `pyspark.ml.feature`
- At the core of the `pyspark.ml` module are the Transformer and Estimator classes. Transformer classes are used for pre-processing and have a `.transform()` method. eg. PCA
- You can create what are called ‘one-hot vectors’ to represent the carrier and the destination of each flight. A one-hot vector is a way of representing a categorical feature where every observation has a vector in which all elements are zero except for at most one element, which has a value of one (1).
- Estimator classes are for modeling and all implement a `.fit()` method. eg. `StringIndexerModel` for including categorical data saved as strings in your models
- `selectExpr()` takes SQL expressions as a string
- `show()` vs `collect()`

- Spark only handles numeric data
- In Spark it's important to make sure you split the data after all the transformations. This is because operations like StringIndexer don't always produce the same index even when given the same list of strings.

## 13.2 Sparklyr

```
library(sparklyr)

sc <- spark_connect(master="local")
config <- spark_config()
config$spark.executor.cores <- 8
config$spark.executor.memory <- "25G"

flights <- copy_to(sc, flights, "flights")
src_tbls(sc)

iris_tbl %>%
  spark_apply(
    function(e) summary(lm(Petal_Length ~ Petal_Width, e))$r.squared,
    names = "r.squared",
    group_by = "Species")

spark_disconnect(sc)

library(sparklyr)

## Connect to your Spark cluster
spark_conn <- spark_connect(master = "local")

## Print the version of Spark
spark_version(sc = spark_conn)

## Disconnect from Spark
spark_disconnect(sc = spark_conn)

## See tables
src_tbls(sc)

## Copy track_metadata to Spark
track_metadata_tbl <- copy_to(spark_conn, track_metadata)

## Print 5 rows, all columns
print(track_metadata_tbl, n = 5, width = Inf)

## Write and run SQL query
query <- "SELECT * FROM track_metadata WHERE year < 1935 AND duration > 300"
(results <- dbGetQuery(spark_conn, query))

## General transformation structure and example
a_tibble %>%
```

```

    ft_some_transformation("x", "y", some_other_args)

hotttnesss <- track_metadata_tbl %>%
  # Select artist_hotttnesss
  select(artist_hotttnesss) %>%
  # Binarize to is_hottt_or_nottt
  ft_binarizer('artist_hotttnesss', 'is_hottt_or_nottt', threshold = .5) %>%
  # Collect the result
  collect() %>%
  # Convert is_hottt_or_nottt to logical
  mutate(is_hottt_or_nottt = as.logical(is_hottt_or_nottt))

## Get and transform the schema

(schema <- sdf_schema(track_metadata_tbl))
schema %>%
  lapply(function(x) do.call(data_frame, x)) %>%
  bind_rows()

## Train-test split
partitioned <- track_metadata_tbl %>%
  sdf_partition(training = 0.7, testing = 0.3)

## List ml functions
ls("package:sparklyr", pattern = "^ml")

## GBT Example

gradient_boosted_trees_model <- track_data_to_model_tbl %>%
  # Run the gradient boosted trees model
  ml_gradient_boosted_trees('year', feature_colnames)

responses <- track_data_to_predict_tbl %>%
  # Select the year column
  select(year) %>%
  # Collect the results
  collect() %>%
  # Add in the predictions
  mutate(
    predicted_year = predict(
      gradient_boosted_trees_model,
      track_data_to_predict_tbl
    )
  )
)

```

### Parquet Aside

Parquet files are quicker to read and write. parquet files can be used with other tools in the Hadoop ecosystem, like Shark, Impala, Hive, and Pig.

```

## The parquet_dir has been pre-defined
parquet_dir

## List the files in the parquet dir
filenames <- dir(parquet_dir, full.names = TRUE)

```

```
## Show the filenames and their sizes
data_frame(
  filename = basename(filenames),
  size_bytes = file.size(filenames)
)

#Import the data into Spark

timbre_tbl <- spark_read_parquet(spark_conn, 'timbre', parquet_dir)
```

- To collect your data: that is, to move it from Spark to R, you call collect(). copy\_to() moves your data from R to Spark.
- Use compute() to compute the calculation, but store the results in a temporary data frame on Spark.
- If you want to delay returning the data, you can use dbSendQuery() to execute the query, then dbFetch() to return the results.
- feature transforms: ft\_, ml functions: ml\_, spark df functions: sdf\_
- ft\_tokenizer(): to lower and split into individual words, ft\_regex\_tokenizer, sdf\_sort

## 13.3 Caret

attributes(clf\_lr): results, finalModel

### 13.3.1 Preprocessing

```
# Apply median imputation: model
model <- train(
  x = breast_cancer_x,
  y = breast_cancer_y,
  method = 'glm',
  trControl = myControl,
  preProcess = c('medianImpute', "knnImpute", 'center', 'scale', 'pca')
)

dotplot(resamples, metric = "ROC")

min(model$results$RSME)

# Identify near zero variance predictors: remove_cols
remove_cols <- nearZeroVar(bloodbrain_x, names = TRUE,
                           freqCut = 2, uniqueCut = 20)

# Get all column names from bloodbrain_x: all_cols
all_cols = colnames(bloodbrain_x)

# Remove from data: bloodbrain_x_small
bloodbrain_x_small <- bloodbrain_x[, setdiff(all_cols, remove_cols)]
```

### 13.3.2 LM

```
# Set seed
set.seed(42)

# Fit lm model: model
model <- lm(price ~ ., data = diamonds)

# Predict on full data: p
p <- predict(model, diamonds)

# Compute errors: error
error <- p - diamonds$price

# Calculate RMSE
sqrt(mean(error^2))

# Fit lm model using 5 x 5-fold CV: model
model <- train(
  medv ~ .,
  Boston,
  method = "lm",
  trControl = trainControl(
    method = "cv", number = 5,
    repeats = 5, verboseIter = TRUE
  )
)
```

### 13.3.3 Lasso/Ridge

Alpha controls balance between lasso and ridge. Lambda controls penalty.

```
# Fit glmnet model: model
model <- train(
  y~., data = overfit,
  method = "glmnet",
  trControl = myControl
)

# Train glmnet with custom trainControl and tuning: model
model <- train(
  y~., overfit,
  tuneGrid = expand.grid(alpha = 0:1, lambda = seq(0.0001, 1, length = 20)),
  method = 'glmnet',
  trControl = myControl
)

# Print model to console
model

# Print maximum ROC statistic
max(model[["results"]][["ROC"]])
```



### 13.3.4 Logistic Regression

```
# Fit glm model
model = glm(Class ~ ., family = "binomial", train)

# Predict on test: p
p = predict(model, test, type = "response")

# Calculate class probabilities: p_class
p_class <- ifelse(p > 0.50, "M", "R")

# Create confusion matrix
confusionMatrix(p_class, test$Class)
```

### 13.3.5 Train-Test Split, Folds, & CV

```
# Shuffle row indices: rows
rows = sample(nrow(Sonar))

# Randomly order data: Sonar
Sonar = Sonar[rows,]

# Identify row to split on: split
split <- round(nrow(Sonar) * .6)

# Create train: 60%
train = Sonar[1:split,]

# Create test: 40%
test = Sonar[(split+1):nrow(Sonar),]

# Create custom indices: myFolds
myFolds <- createFolds(churn_y, k = 5)

# Create reusable trainControl object: myControl
myControl <- trainControl(
  summaryFunction = twoClassSummary, #default option is default summary
  classProbs = TRUE, # IMPORTANT!
  verboseIter = TRUE,
  savePredictions = TRUE,
  index = myFolds
)
```

### 13.3.6 Random Forest

```
# Fit random forest: model
model <- train(
  quality~.,
  tuneLength = 3,
  #tuneGrid = data.frame(mtry = c(2, 3, 7)),
```

```

data = wine,
method = 'ranger',
trControl = trainControl(method = "cv", number = 5, verboseIter = TRUE)
)

# Print model to console
model

# Plot model
plot(model)

```

### 13.3.7 SVM

```

clf_svm <- train(
  pass ~.,
  data = df3,
  method = "svmLinear",
  preProcess = c("center", "scale")
)

```

### 13.3.8 Model Selection

Now that you have fit two models to the churn dataset, it's time to compare their out-of-sample predictions and choose which one is the best model for your dataset.

You can compare models in caret using the `resamples()` function, provided they have the same training data and use the same `trainControl` object with preset cross-validation folds. `resamples()` takes as input a list of models and can be used to compare dozens of models at once (though in this case you are only comparing two models).

```

# Create model_list
model_list <- list(item1 = model_glmnet, item2 = model_rf)

# Pass model_list to resamples(): resamples
resamples = resamples(model_list)

# Summarize the results
summary(resamples)

# Create bwplot
bwplot(resamples, metric = 'ROC')

# Create xyplot
xyplot(resamples)

# Predict on test: p
p = predict(model, test, type = 'response')

# Make ROC curve
colAUC(p, test$Class, plotROC = TRUE)

```

- caret: finalModel of model object

### 13.3.9 Stacking

caretEnsemble provides the caretList() function for creating multiple caret models at once on the same dataset, using the same resampling folds. You can also create your own lists of caret models. Use the caretStack() function to make a stack of caret models, with the two sub-models (glmnet and ranger) feeding into another (hopefully more accurate!) caret model.

```
# Create ensemble model: stack
stack <- caretStack(model_list, method = 'glm')

# Look at summary
summary(stack)
```

& caretEnnsemble

## 13.4 Data Table

- Operations done by reference
- dt[i, j, by] : subset by i calculate by j grouped using by
- 1: numeric | 1L: integer
- NA\_integer\_: integer
- DT[N] : prints last row
- names(DT): colnames
- dim(DT): dimensions
- DT[, .(A, B)]: returns two columns
- DT[, c(A, B)]: returns a concatenated vector
- DT[, .(sum\_c = sum(C))]
- DT[, plot(A, C)]
- DT[, A:=NULL]: Remove column A
- DT[, .(sumB = sum(B)), by = .(Grp = A%%2)]
- DT[, .N, by = Sepal.Width]: .N is the count of each group
- DT[, lapply(.SD, median)]: .SD is a placeholder for all the columns
- dogs[, lapply(.SD, mean), .SDcols = 2:3]: Find mean of columns 2 & 3
- for (i in 1:5) set(DT, i, 3L, i+1): update first 5 rows of 3rd column
- setnames(DT, 'y', 'z'): changes colname from y to z
- setkey(DT, A, B)
- DT[('b')]
- DT[(c('b', 'c'))]
- DT[(c('b', 'c')), mult="first"]
- DT[c("b", "c"), .SD[c(1, .N)], by = .EACHI]: First and last row of the "b" and "c" groups
- DT[c("b", "c"), { print(.SD); .SD[c(1, .N)] }, by = .EACHI]

- roll=TRUE, 'nearest', -Inf, Inf | rollends=FALSE

## 13.5 Keras

Here's a Hello World and the general framework:

- declare: sequential
- add layers input-hidden-output
- compile
- fit

Keras only uses numpy arrays.

### 13.5.1 Regression

- loss = mean\_squared\_error
- metric: rmse
- activation\_function = relu

```
import keras
from keras.layers import Dense
from keras.models import Sequential
# Specify the model: Two hidden layers
model = Sequential()
## Input
n_cols = predictors.shape[1]
model.add(Dense(50, activation='relu', input_shape = (n_cols,)))
# Hidden
model.add(Dense(32, activation='relu'))
# Output
model.add(Dense(1))
# Compile the model
model.compile(optimizer = 'adam', loss = 'mean_squared_error')
# Fit the model
model.fit(predictors, target)
#Look at summary
model.summary()
# Calculate predictions: predictions
predictions = model.predict(pred_data)
```

### 13.5.2 Classification

- loss = categorical\_crossentropy
- metric = accuracy
- activation\_function = softmax
- output layer with stuff equal to number of categorical groups

```

import keras
from keras.layers import Dense
from keras.models import Sequential
# Specify the model: Two hidden layers
n_cols = predictors.shape[1]
model = Sequential()
## Input
model.add(Dense(50, activation='relu', input_shape = (n_cols,)))
# Hidden
model.add(Dense(32, activation='relu'))
# Output
model.add(Dense(2, activation = 'softmax'))
# Compile the model
model.compile(optimizer = 'sgd', loss = 'categorical_crossentropy', metrics = ['accuracy'])
# Fit the model
model.fit(predictors, target)
#Look at summary
model.summary()
#Calculate predictions: predictions
predictions = model.predict(pred_data)
#Calculate predicted probability of survival
predicted_prob_true = predictions[:, 1]

```

### 13.5.3 More

keras: declare model | compile with loss, optimizer, and scoring metric | fit | keras::to\_categorical

keras.callbacks.EarlyStopping: Stop training when validation score stop improving after a certain number of epochs (batches?)

```

# Import the SGD optimizer
from keras.optimizers import SGD
# Create list of learning rates: lr_to_test
lr_to_test = [.000001, 0.01, 1]
# Loop over learning rates
for lr in lr_to_test:
    print('Testing model with learning rate: ')

    # Build new model to test, unaffected by previous models
    model = get_new_model()

    # Create SGD optimizer with specified learning rate: my_optimizer
    my_optimizer = SGD(lr = lr)

    # Compile the model
    model.compile(optimizer = my_optimizer, loss = 'categorical_crossentropy')

    # Fit the model
    model.fit(predictors,
              target,
              validation_split = 0.3,
              epochs = 20,
              callbacks = [early_stopping_monitor],

```

```
verbose = False)
```