

Linear Algebra from Scratch: Introduction

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"It does not matter how slowly you go as long as you do not stop." - Confucius

Udemy Open Course



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Matrices are not Digital Constructions of the Environment

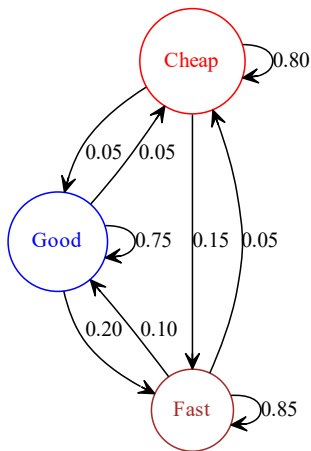


A Matrix is a collection of elements

① $a_1 \sim \text{Cheap}$

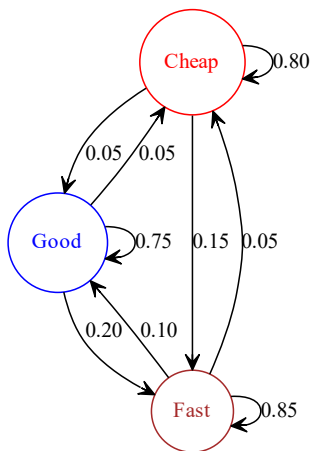
② $a_2 \sim \text{Good}$

③ $a_3 \sim \text{Fast}$



A Matrix is a collection of elements

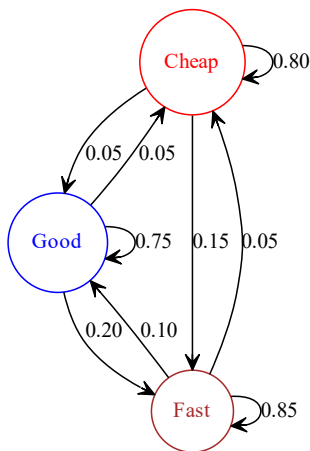
- 1 $a_1 \sim \text{Cheap}$
- 2 $a_2 \sim \text{Good}$
- 3 $a_3 \sim \text{Fast}$
- 4 The probability of changing to the i_{th} state to the j_{th} state can be expressed as:



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- 4 The probability of changing to the i_{th} state to the j_{th} state can be expressed as:

$$A' = \begin{bmatrix} 0.80 & 0.05 & 0.10 \\ 0.05 & 0.75 & 0.05 \\ 0.15 & 0.20 & 0.85 \end{bmatrix}$$



A Matrix is a rectangular array of elements

Overview.

- ①: Systems of Linear Equations
- ②: Row Echelon Form



Determinants can be calculated for square matrices.

Overview.

- ①: Determinant of a matrix
- ②: Properties of determinants



Vector Spaces preserve linearity

Overview.

- ①: Definitions and Examples
 - ②: Subspaces
 - ③: Linear Independence
 - ④: Basis and Dimension
 - ⑤: Change of Basis
- ⑥: Row and Column Spaces



A Linear Transformation is a mapping

Overview.

- ①: Definitions and Examples
- ②: The Matrix representation of a linear transformation
- ③: Similarity between Matrices



Orthogonality is the geometric generalization of perpendicular

Overview.

- ①: Inner Product
- ②: Orthogonal Subspaces
- ③: Least Squares
- ④: Inner Product Spaces
- ⑤: Gram-Schmidt Orthogonalization



Solving the eigenvalue problem is useful to many applications

Overview.

- ①: Eigenvalues and Eigenvectors
- ②: Diagonalization
- ③: Singular Value Decomposition



Coding as an additional exercise for ambitious scholars

Overview.

The Matlab, Python, and other relevant course related content can be found at: **GitHub Link**



References I

- [1] David Harville. *Matrix Algebra From a Statistician's Perspective*. New York: Springer-Verlag, 1997.
- [2] Leon Stephen. *Linear Algebra with Applications (9th Edition)* (*Featured Titles for Linear Algebra*). London, England: Pearson, 2014.